## 1-Vector Arithmetic

### EE1030:Matrix Theory

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### Question: 1.8.24

Find a relation between x and y such that the point (x, y) is equidistant from the points (7,1) and (3,5).

#### **Solution:**

Coordinates Given	Labeled as
$\begin{pmatrix} x \\ y \end{pmatrix}$	A
$\begin{pmatrix} 7 \\ 1 \end{pmatrix}$	В
$\binom{3}{5}$	C

Table 1.8.24.1 0: Labeling given coordinates as A, B, C

A is said to be equidistant from B and C if

$$\|\mathbf{B} - \mathbf{A}\| = \|\mathbf{C} - \mathbf{A}\| \tag{0.1}$$

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 7 \\ 1 \end{pmatrix} - \begin{pmatrix} x \\ y \end{pmatrix} \tag{0.2}$$

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 7 - x \\ 1 - y \end{pmatrix} \tag{0.3}$$

$$(\mathbf{B} - \mathbf{A})^{\mathsf{T}} = \begin{pmatrix} 7 - x & 1 - y \end{pmatrix} \tag{0.4}$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} 3 \\ 5 \end{pmatrix} - \begin{pmatrix} x \\ y \end{pmatrix} \tag{0.5}$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} 3 - x \\ 5 - y \end{pmatrix} \tag{0.6}$$

$$(\mathbf{C} - \mathbf{A})^{\mathsf{T}} = \begin{pmatrix} 3 - x & 5 - y \end{pmatrix} \tag{0.7}$$

Given A is equidistant from B and C, so  $\|B-A\|=\|C-A\|$  from equation 0.1 , Therefore

$$\sqrt{(\mathbf{B} - \mathbf{A})^{\mathsf{T}} (\mathbf{B} - \mathbf{A})} = \sqrt{(\mathbf{C} - \mathbf{A})^{\mathsf{T}} (\mathbf{C} - \mathbf{A})}$$
(0.8)

Squaring the equation 0.8 on both sides,

$$(\mathbf{B} - \mathbf{A})^{\mathsf{T}} (\mathbf{B} - \mathbf{A}) = (\mathbf{C} - \mathbf{A})^{\mathsf{T}} (\mathbf{C} - \mathbf{A})$$

$$(0.9)$$

$$(7 - x \quad 1 - y) \begin{pmatrix} 7 - x \\ 1 - y \end{pmatrix} = (3 - x \quad 5 - y) \begin{pmatrix} 3 - x \\ 5 - y \end{pmatrix}$$
 (0.10)

$$(7-x)^2 + (1-y)^2 = (3-x)^2 + (5-y)^2$$
(0.11)

$$49 + x^2 - 14x + 1 + y^2 - 2y = 9 + x^2 - 6x + 25 + y^2 - 10y$$
 (0.12)

$$8x - 8y - 16 = 0 \tag{0.13}$$

$$x - y - 2 = 0 \tag{0.14}$$

The relation between x and y is x - y - 2 = 0.

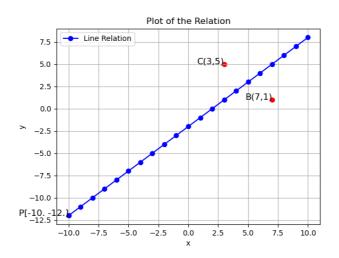


Fig. 0.1: Relation between x and y: x - y - 2 = 0