Presentation - Matgeo

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EE1030 - Matrix Theory

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Problem Statement

If the lines $2x - 3y = 5$ and $3x - 4y = 7$ are the diameters of a circle of area 154 square units, then obtain the equation of the circle.

Description of Variables used

Variables	Description
c	centre
r	radius
u	$-\mathbf{c}$
f	$\|\mathbf{u}\|^2 - r^2$
x	$\begin{pmatrix} x \\ y \end{pmatrix}$

Row Reduction: Finding **c**

The augmented matrix formed by the given equations of diameter is

$$\begin{pmatrix} 2 & -3 & 5 \\ 3 & -4 & 7 \end{pmatrix} \xrightarrow{R_2 \to 2R_2 - 3R_1} \begin{pmatrix} 2 & -3 & 5 \\ 0 & 1 & -1 \end{pmatrix} \tag{3.1}$$

$$\xrightarrow{R_1 \to R_1 + 3R_2} \begin{pmatrix} 2 & 0 & 2 \\ 0 & 1 & -1 \end{pmatrix} \tag{3.2}$$

$$\xrightarrow{R_1 \to \frac{R_1}{2}} \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & -1 \end{pmatrix} \tag{3.3}$$

Therefore from equation **??**

$$\mathbf{c} = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \tag{3.4}$$

Finding **u**, r and f

$$\mathbf{u} = \begin{pmatrix} -1 \\ 1 \end{pmatrix} \tag{3.5}$$

$$\mathbf{u}^{\mathsf{T}} = \begin{pmatrix} -1 & 1 \end{pmatrix} \tag{3.6}$$

$$\|\mathbf{u}\|^2 = \mathbf{u}^{\mathsf{T}}\mathbf{u} \tag{3.7}$$

$$\|\mathbf{u}\|^2 = 2 \tag{3.8}$$

Given area is 154 square units

$$\pi r^2 = 154 \tag{3.9}$$

$$r = 7 \tag{3.10}$$

$$f = 2 - 49 \tag{3.11}$$
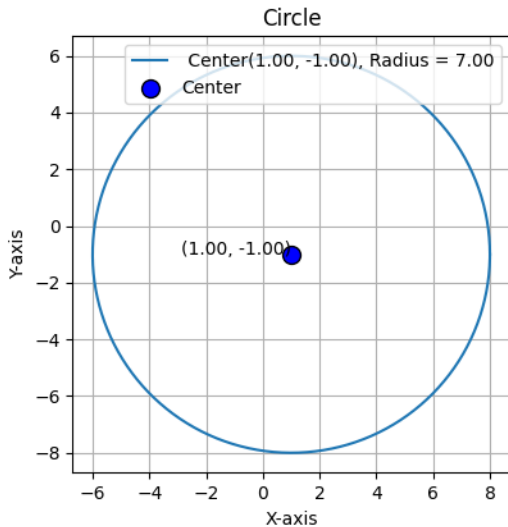
$$f = -47 \tag{3.12}$$

Equation of Circle

The equation of circle is given by

$$\|\mathbf{x}\|^2 + 2\mathbf{u}^\mathsf{T}\mathbf{x} + f = 0 \tag{3.13}$$

$$\mathbf{x}^\mathsf{T}\mathbf{x} + 2\begin{pmatrix} -1 & 1 \end{pmatrix}\mathbf{x} + (-47) = 0 \tag{3.14}$$

$$x^2 + y^2 - 2x + 2y - 47 = 0 \tag{3.15}$$

Plot

Codes

The equation of circle (**??**) can be found through

https://github.com/Satyanarayana−123456/EE1030/blob/49
c3368ff40b51aed83efa82383340d2fa51db7d/Presentation/matgeo/codes/main.c

The plot of the circle can be obtained by

https://github.com/Satyanarayana−123456/EE1030/blob/49
c3368ff40b51aed83efa82383340d2fa51db7d/Presentation/matgeo/codes/circle.py