1-Vector Arithmetic

EE1030:Matrix Theory

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Question: 1.8.13

The distance between the points A(0,6) and B(0,-2) is **Solution:**

Vertex	Coordinates
A	$\begin{pmatrix} 0 \\ 6 \end{pmatrix}$
В	$\begin{pmatrix} 0 \\ -2 \end{pmatrix}$

Table 1.8.13.1 0: Vertex and its coordinates

Let the distance between **A** and **B** be **d**, then **d** is given by

$$\mathbf{d} = \|\mathbf{A} - \mathbf{B}\| \tag{0.1}$$

$$\mathbf{A} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} \tag{0.2}$$

$$\mathbf{B} = \begin{pmatrix} 0 \\ -2 \end{pmatrix} \tag{0.3}$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} - \begin{pmatrix} 0 \\ -2 \end{pmatrix} \tag{0.4}$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} 0 - 0 \\ 6 - (-2) \end{pmatrix} \tag{0.5}$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} 0 \\ 8 \end{pmatrix} \tag{0.6}$$

$$(\mathbf{A} - \mathbf{B})^{\mathsf{T}} = \begin{pmatrix} 0 & 8 \end{pmatrix} \tag{0.7}$$

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From equation 0.1, distance between \boldsymbol{A} and \boldsymbol{B} is

$$\mathbf{d} = \|\mathbf{A} - \mathbf{B}\| \tag{0.8}$$

$$\mathbf{d} = \sqrt{(\mathbf{A} - \mathbf{B})^{\mathsf{T}} (\mathbf{A} - \mathbf{B})} \tag{0.9}$$

$$\mathbf{d} = \sqrt{\begin{pmatrix} 0 & 8 \end{pmatrix} \begin{pmatrix} 0 \\ 8 \end{pmatrix}} \tag{0.10}$$

$$\mathbf{d} = \sqrt{(0)^2 + (8)^2} \tag{0.11}$$

$$= 8$$
 (0.12)

Therefore the distance between A and B is 8.

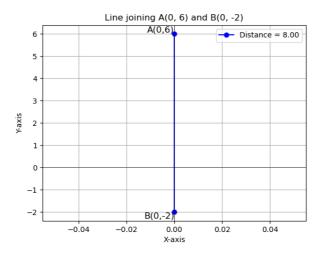


Fig. 0.1: Line joining A and B