

# 1-Vector Arithmetic

EE1030:Matrix Theory

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## Question:1.7.6

Find a relation between  $x$  and  $y$  if the points  $\mathbf{A}(x, y)$ ,  $\mathbf{B}(-4, 6)$ , and  $\mathbf{C}(-2, 3)$  are collinear. (10, 2019)

**Solution:**

Vertex	Coordinates
<b>A</b>	$\begin{pmatrix} x \\ y \end{pmatrix}$
<b>B</b>	$\begin{pmatrix} -4 \\ 6 \end{pmatrix}$
<b>C</b>	$\begin{pmatrix} -2 \\ 3 \end{pmatrix}$

Table 1.7.6.1 0: Vertex and its coordinates

Points  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$  are said to be collinear if

$$\text{rank}(\mathbf{B} - \mathbf{A} \quad \mathbf{C} - \mathbf{A}) = 1 \quad (0.1)$$

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} -4 \\ 6 \end{pmatrix} - \begin{pmatrix} x \\ y \end{pmatrix} \quad (0.2)$$

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} -4 - x \\ 6 - y \end{pmatrix} \quad (0.3)$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} -2 \\ 3 \end{pmatrix} - \begin{pmatrix} x \\ y \end{pmatrix} \quad (0.4)$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} -2 - x \\ 3 - y \end{pmatrix} \quad (0.5)$$

$$(\mathbf{B} - \mathbf{A} \quad \mathbf{C} - \mathbf{A}) = \begin{pmatrix} -4 - x & -2 - x \\ 6 - y & 3 - y \end{pmatrix} \quad (0.6)$$

$$\begin{pmatrix} -4 - x & -2 - x \\ -6 - y & 3 - y \end{pmatrix} \xrightarrow{R_2 \rightarrow R_1 + \frac{2}{3}R_2} \begin{pmatrix} -4 - x & -2 - x \\ -x - \frac{2}{3}y & -x - \frac{2}{3}y \end{pmatrix} \quad (0.7)$$

$$(0.8)$$

Given  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$  are collinear, so  $\text{rank}(\mathbf{B} - \mathbf{A} \quad \mathbf{C} - \mathbf{A}) = 1$  from equation 0.1

Therefore,

$$-x - \frac{2}{3}y = 0 \quad (0.9)$$

$$x = -\frac{2}{3}y \quad (0.10)$$

$$3x = -2y \quad (0.11)$$

$$3x + 2y = 0 \quad (0.12)$$

$$(0.13)$$

The relation between  $x$  and  $y$  is  $3x + 2y = 0$ .

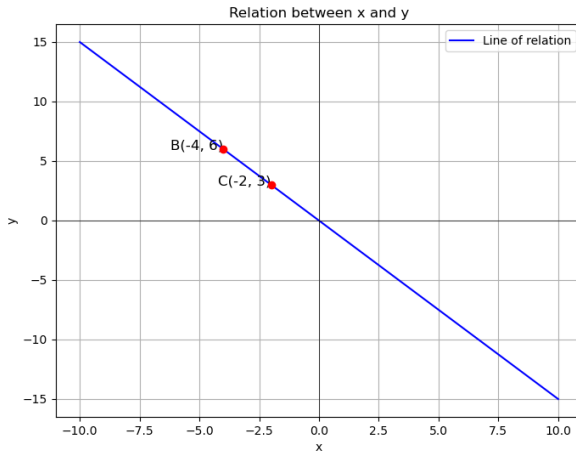


Fig. 0.1: Relation between  $x$  and  $y$ :  $3x + 2y = 0$