**Highlights:**

* We present a spectral method to solve infinite-dimensional Kolmogorov equations associated with a particular family of SPDs
* We also establish theory to characterize the stability respect to initial conditions of the regarding the spectral method
* The numerical experiments illustrate our theory