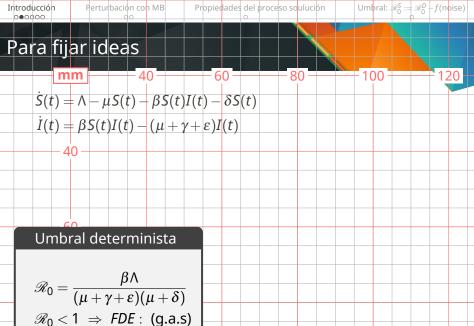


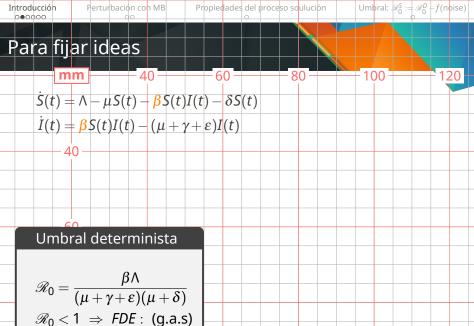
 $\mathcal{R}_0 > 1 \Rightarrow EE : (g.a.s)$



$$arepsilon)(\mu+\delta)$$

F: (a.a.s

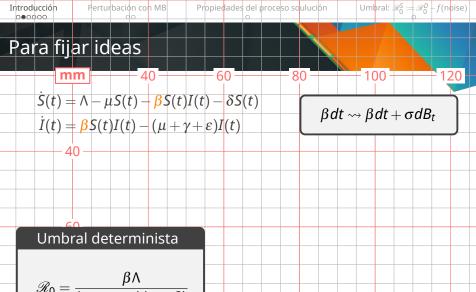
 $\mathcal{R}_0 > 1 \Rightarrow EE : (g.a.s)$



$$(+\delta)$$

 $\mathcal{R}_0 > 1 \Rightarrow EE : (g.a.s)$

$$+\delta$$
)



$$\mathscr{R}_0 = \frac{\beta \Lambda}{(\mu + \gamma + \varepsilon)(\mu + \delta)}$$

$$rac{eta \wedge}{\mu + \gamma + arepsilon)(\mu + \delta}$$

$$\frac{\gamma}{\gamma + \varepsilon}(\mu + \delta)$$

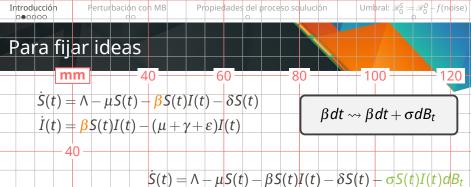
$$\mathcal{R}_0 < 1 \Rightarrow FDE : (g.a.s)$$

 $\mathcal{R}_0 > 1 \Rightarrow EE : (g.a.s)$









 $\mathcal{R}_0 > 1 \Rightarrow EE : (q.a.s)$

$$(\mu + \epsilon)$$

$$\mathscr{R}_0 = \frac{\beta \Lambda}{(\mu + \gamma + \varepsilon)(\mu + \delta)}$$

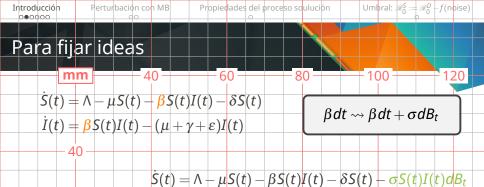
$$\mathcal{R}_0 = \frac{\rho \Lambda}{(\mu + \gamma + \varepsilon)(\mu + \delta)}$$

$$\mathcal{R}_0 < 1 \Rightarrow FDE : (g.a.s)$$





$$\dot{I}(t) = \beta S(t)I(t) - (\mu + \gamma + \varepsilon)I(t) + \sigma S(t)I(t)dB_t$$



Umbral determinista

$$I(t) = \beta S(t)I(t) - (\mu + \gamma + \varepsilon)I(t) + \sigma S(t)I(t)dB_t$$
nista

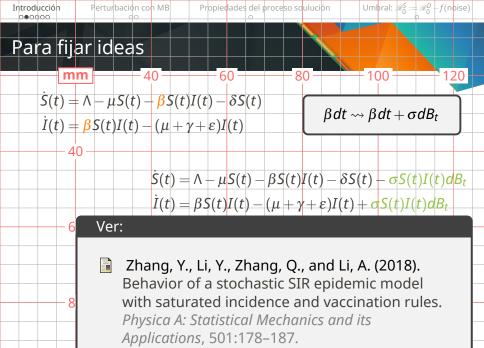
Umbral estocástico

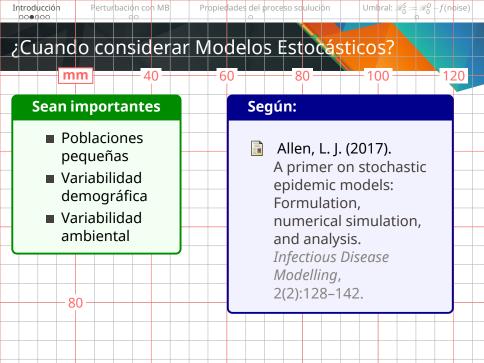
$$\mathscr{R}_0^{\mathsf{S}} = ?$$

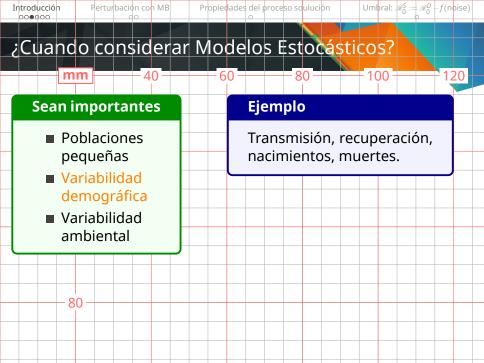
$$\mathcal{R}_0 = \frac{\beta \Lambda}{(\mu + \gamma + \varepsilon)(\mu + \delta)}$$
$$\mathcal{R}_0 < 1 \Rightarrow FDE : (g.a.s)$$

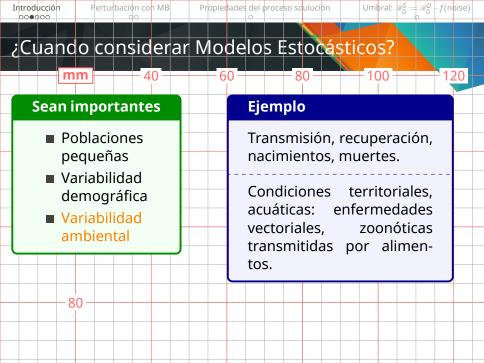
$$\mathcal{R}_0 < 1 \Rightarrow FDE : (g.a.s)$$

 $\mathcal{R}_0 > 1 \Rightarrow EE : (g.a.s)$
 $\mathcal{R}_0 > 1 \Rightarrow EE : (g.a.s)$









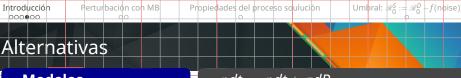
- parámetros
 - Procesos reversibles en media
 - $\beta_t^H H \in (0.5, 1)$
 - Random Diff. Eq.

Herramientas

- Gillespie
- Kloeden-Methods
- Hermite-PC

A primer on stochastic

epidemic models: Formulation, numerical simulation, and analysis. Infectious Disease Modelling, 2(2):128–142, may 2017.



- (D/C)–TMCs
- Perturbación de parámetros
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Gray, A., Greenhalgh, D., Hu, L., Mao, X., and Pan, J. (2011). A Stochastic Differential Equation SIS Epidemic Model. SIAM Journal on Applied Mathematics, 71(3):876–902.



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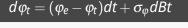
- Schurz, H. and Tosun, K. (2015).
- Stochastic Asymptotic Stability of SIR Model with Variable Diffusion Rates. Journal of Dynamics and
- Differential Equations,
- 27(1):69-82.

■ (D/C)-TMCs

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Allen, E. (2016). Environmental variability and

mean-reverting processes. Discrete and Continuous

Dynamical Systems - Series B, 21(7):2073-2089.

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Herramientas

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$d\varphi_t = (\varphi_e - \varphi_t)dt + \sigma_{\varphi}dBt$



(2017).

Mean-square dissipativity of numerical methods for a class

Ma, Y., Zhang, Q., and Ye, M.

of resource-competition models with fractional brownian motion. Systems Science & Control Engineering, 5(1):268–277.

Alternativas

Introducción

Modelos

- (D/C)-TMCs
- Perturbación de parámetros
 - Procesos reversibles en media
 - $\blacksquare \beta_t^H H \in (0.5, 1)$
 - Random Diff. Eq.

Herramientas

- Gillespie
- Kloeden-Methods
- Hermite-PC

parametros son v.a.



Chen-Charpentier, B.-M., Cortés, J.-C., Licea, J.-A., Romero, J.-V., Roselló, M.-D., Santonja, F.-J., and Villanueva, R.-J. (2015). Constructing adaptive

generalized polynomial chaos method to measure the uncertainty in continuous models: A computational approach.

Mathematics and Computers in Simulation, 109:113 – 129.



- (D/C)-TMCs
- Perturbación de parámetros
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Herramientas

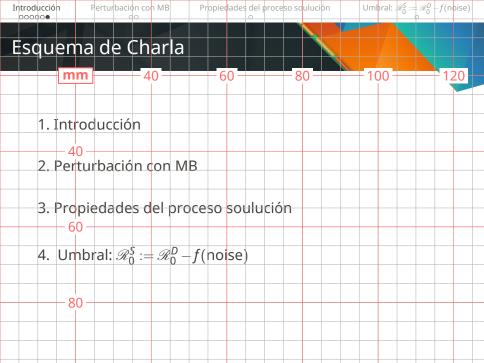
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| Introducción 000000 | Perturbación con M | B Propiedad | es del proceso sou | ılución | Jmbral: ℛ ^S := | $\mathcal{R}_0^D - f(\text{noise})$ |
|------------------------|--------------------|-------------|--------------------|---------|---------------------------|-------------------------------------|
| CDE | | | | | | |
| SDE | | | | | | |
| m | m 40 | 60 | 80 |) | 100 | 120 |
| | | | | | | |
| | | | | | | |
| 4 | 0 | | | | | |
| | | | | | | |
| | | | | | | |
| 6 | 0 | | | | | |
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| | | | | | | |
| | | | | | | |
| 8 | 0 | | | | | |
| | | | | | | |
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