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# Cable Driven Parallel Robot Manipulator for Pick and Place Applications

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## Abstract

This report aims to describe the cable based parallel robots, which can help fill the gaps in larger autonomous warehouse managements. Inverse kinematics, quasi static analysis and gripping has been discussed in this report. All the theoretical work has been carried out and results are validated with the simulations. All the details about simulating this robot in gazebo software has been provided. Scope of this project is limited as of now, but it will surely help in building the real system.

**Key words:** Parallel robots, Cable based parallel robots, CDPR, Forward kinematic, Inverse kinematics, Velocity kinematics, Degree of Freedom(dof)

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# 1 Introduction and Motivation

With increasing demand of automation in warehouses and mass manufacturing facilities, more and more robots are being used to do several tasks in such environments. These tasks include moving big packages or heavy loads in metal industry. In metal or manufacturing industry, usually hand type serial manipulators are used on larger scale. Because of their smaller workspace, number of such robots have to be incorporated. For moving packages, serial manipulators are being used with automatic guided vehicles which again complicates the whole process.

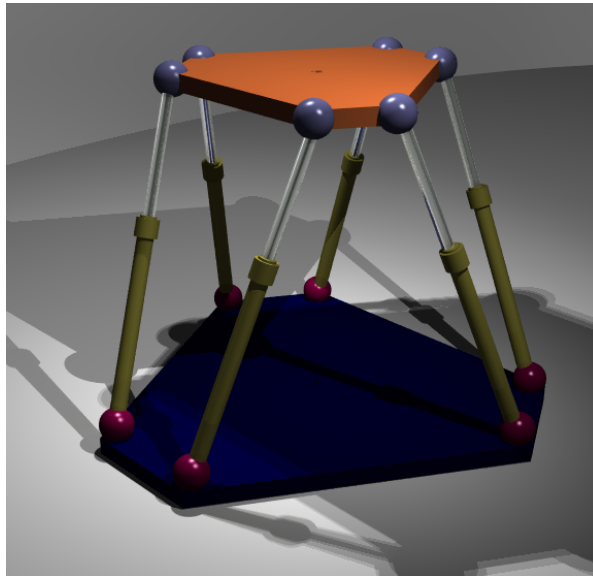


Figure 1.1: 6 DOF type Stewart-Gough platform

Parallel manipulators have some good advantages over serial manipulators because of their closed loop structures. Because of quick responses and good accuracy they are heavily used in medical robotics. They can carry high loads because of closed kinematic structures, which makes them a good candidate for industrial applications. 6 degree of freedom type Stewart gough platform, as shown in Figure 1.1, is the most common kind of parallel manipulator which can achieve six degrees of freedom. This platform is normally used in flight simulators or tire testing and their applications are not limited to only these tasks.

Cable based parallel manipulators are a modified version of parallel manipulators where prismatic joints are replaced with cables under tension. These cables give them an extra edge because of less complex structure which can be easily scaled. Though cables have their own disadvantages because they can pull but cannot push the end-effector, but this problem can be resolved with the inclusion of redundant joints.

## 2 Robot Description

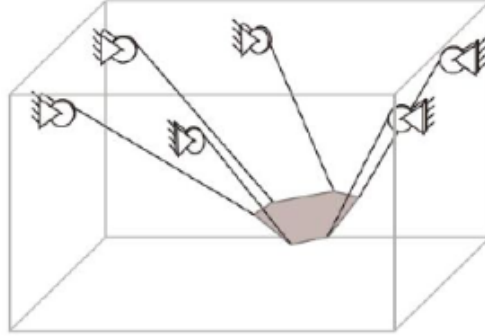


Figure 2.1: Robot

A cable driven parallel robot (CDPR) can be constructed with different architectures. Essentially an end effector should be connected with cables and other ends of cables should be connected to the actuator-which are usually servo motors. Cables pass through a fixed point which is a pulley in our case, over which cables bend and go to the servo motors. Joint between cables and end effector is usually taken as a ball joint. While the joint between a fixed point and cables is taken as universal joint, because of which pulley should have a degree of freedom and should be connected to a revolute joint rather than a fixed joint. Length of cables between this fixed point and end effector is changed in order to move the end effector in the workspace.

Figure 1 contains a simple 6 cable CDPR which can achieve 6 degrees of freedom, but it is not well suited for the task because of cables. Cables can only pull the object but cannot push, which will make end effector vibration prone and slow. To make the system more stable, two more cables are introduced, which will increase the efficacy of task performance.

We will use the architecture as shown in figure 3 as basis of this project. Workspace will be a square warehouse of size  $3.5m \times 3.5m \times 3.5m$ , each upper corner being the fix point for the joint. Because of square workspace each corner will lie on the same circle, and this symmetry will make the mathematics behind the problem somewhat easier to follow. End effector will be a square box of size  $0.6m \times 0.6m \times 0.6m$  and at all the corners of the box are considered as a ball joint which establish connections with cables.

### 2.1 Assumptions

It is an enormous task to build the entire robotic system and requires lots of small considerations. Some assumptions are required to be taken in order to achieve the goal of this project, which are mentioned below.

- The entire warehouse is assumed to be rigid.
- The robot utilizes its parallel gripper to grasp a metallic cubic object that is rigid in nature and cannot be deformed. Position of the object is known and no sensing elements is present which can sense the location of the object.
- All the cables are massless, rigid and no collision is taking place between cables and between cables and other environment object available.
- All the spherical and universal joints does not have any joint limitations and all the joints are massless and frictionless.
- Motors can generate any required amount torque to grip and move the object.
- The workspace is obstacle-free which excludes the task of path planning.

### 3 Robot Modelling

#### 3.1 Inverse Position Kinematics

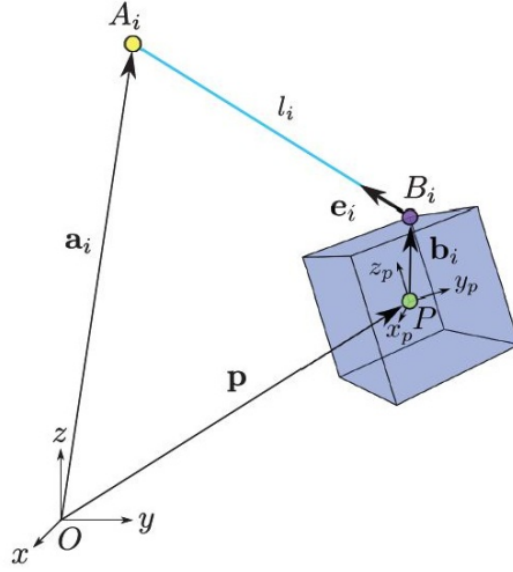


Figure 3.1: Geometric description of the robot

To move out end effector in the workspace and to position it at certain defined state, we change the length of cables and it is necessary to have an idea about what length should we keep to reach a particular state. World frame is assumed to be at the at the centre of the warehouse, but at the ground level. Let's assume that  $O_d$  is the new position of the end-effector in the world coordinate frame and  $\theta_x, \theta_y$  and  $\theta_z$  are the XYZ euler angles of the new position.  $A_i$ s are the coordinates of the outer frames from where cables pass through to get to motors. This joints will not move and distance between these joints and end-effector joints will actually give the length of the cable, which we are trying to compute.  $b_i$ s are the positions of joints in the end-effector frame, on the end-effector, where the cables are connected.  $B_i$ s are the positions of those spherical joints in world frame.

$$\vec{P} = \vec{O}_p^0 = [x_d \quad y_d \quad z_d]^T$$

$$R_d = R_n^0 = R_x(\theta_x) * R_y(\theta_y) * R_z(\theta_z)$$

The final rotation matrix will look like this,

$$R_d = \begin{bmatrix} \cos\theta_y \cos\theta_z & -\cos\theta_y \sin\theta_z & \sin\theta_y \\ \cos\theta_x \sin\theta_z + \sin\theta_x \sin\theta_y \cos\theta_z & \cos\theta_x \cos\theta_z - \sin\theta_x \sin\theta_y \sin\theta_z & -\sin\theta_x \cos\theta_y \\ \sin\theta_x \sin\theta_z - \cos\theta_x \sin\theta_y \cos\theta_z & \sin\theta_x \cos\theta_z + \cos\theta_x \sin\theta_y \sin\theta_z & \cos\theta_x \cos\theta_y \end{bmatrix}$$



A  $4 \times 4$  transformation matrix can be described as below. With these transformation matrix we can get the position and orientation (in the world frame) of the objects, whose position and orientation is known in end effector frame.

$$T_d = T_n^0 = \begin{bmatrix} R_d & \vec{P} \\ O_{1 \times 3} & 1 \end{bmatrix}$$

Length of each cable is our main goal and thus all the length vectors can be described as below,

$$\vec{q} = \vec{l} = [l_1 \quad l_2 \quad l_3 \quad l_4 \quad l_5 \quad l_6 \quad l_7 \quad l_8]^T$$

Length vectors can be calculated with the following formula,

$$\vec{l}_i = \vec{B}_i - \vec{A}_i$$

$$\vec{B}_i = [R_n^0] \vec{b}_i + \vec{P}$$

Python code written below, calculates the lengths and length vectors required.

```
#####
import numpy as np
from math import cos, sin, radians
from sympy import Symbol, cos, sin, Matrix, zeros
#####
frame = [[-3.5, -3.5, 3.5],
          [-3.5, -3.5, 3.5],
          [3.5, -3.5, 3.5],
          [3.5, -3.5, 3.5],
          [-3.5, 3.5, 3.5],
          [-3.5, 3.5, 3.5],
          [3.5, 3.5, 3.5],
          [3.5, 3.5, 3.5]]
platform = [[0.3, -0.3, -0.3],
            [-0.3, 0.3, 0.3],
            [-0.3, -0.3, 0.3],
            [0.3, 0.3, -0.3],
            [-0.3, -0.3, -0.3],
            [0.3, 0.3, 0.3],
            [0.3, -0.3, 0.3],
            [-0.3, 0.3, -0.3]]
platform = np.array(platform)
frames = np.array(frame)

def rotation(ax, ay, az):
    tx = radians(ax)
    ty = radians(ay)
```

```

tz = radians(az)
rx = np.array([[1,0,0],[0,cos(tx),-sin(tx)],[0,sin(tx),cos(tx)])
ry = np.array([[cos(ty),0,sin(ty)],[0,1,0],[-sin(ty),0,cos(ty)])
rz = np.array([[cos(tz),-sin(tz),0],[sin(tz),cos(tz),0],[0,0,1]])
return np.matmul(rx, np.matmul(ry, rz))

pose = [1,1,1,10,10,10] ### Position and euler angles (x, y, z, rx, ry, rz)

for i in range(8):
    ll = frames[i,:] - np.array(pose[:3]) +
    np.matmul(rotatio(pose[3], pose[4], pose[5])
    ,np.matrix.transpose(platform[i,:])) ##### Length vectors
    print(ll)

for i in range(8):
    ### Prints the lengths of cables
    print(np.sqrt(ll[i,0]**2 + ll[i,1]**2 +ll[i,2]**2))
#####

```

## 3.2 Quasi Static Analysis

Quasi static analysis gives us the forces with which each cable should be pulled to keep the end effector in at the desired position. This force can be used to calculate the torques required by the motor to achieve a static position. Tensions can be found with the help of virtual work method and for that we need to complete inverse velocity kinematics. Velocity jacobian can be computed with the equation given below.

$$\dot{L} = J\dot{x}$$

$$J^T = \begin{bmatrix} -d_1^T & (d_1 \times Rb_1)^T \\ -d_2^T & (d_2 \times Rb_2)^T \\ -d_3^T & (d_3 \times Rb_3)^T \\ -d_4^T & (d_4 \times Rb_4)^T \\ -d_5^T & (d_5 \times Rb_5)^T \\ -d_6^T & (d_6 \times Rb_6)^T \\ -d_7^T & (d_7 \times Rb_7)^T \\ -d_8^T & (d_8 \times Rb_8)^T \end{bmatrix}$$

$$d_i = \frac{l_i}{||l_i||}$$

Here  $d_i$ s are the unit vectors in the direction of the length of the cable.

From virtual work theorem, we can write,

$$\vec{q} = J(q)\vec{\epsilon}_d$$

Where  $\vec{q}$  is the applied wrench on end effector and  $\vec{\epsilon}_d$  is the cable tension matrix. Forces applied at the the spherical joints, due to the tensions in the cables, are in direction of the the length vector of the respective cable. Moments can be can be taken as the cross product of the force in the direction of length vectors and the position vector of a spherical joint in world frame. This forces and moments should be equal to the wrench provided on the end effector, in order to keep it stable at the desired pose.

So, tensions in cables can be computed with,

$$\vec{\epsilon}_d = J^{-1}(q)\vec{q}$$

Here  $J(q)$  is not a square matrix and thus we have to find the pseudo inverse of the matrix. Below is the python code which computes the tension values,

```
#####
import numpy as np
from math import cos, sin, radians
from sympy import Symbol, cos, sin, Matrix, zeros
#####

D = Matrix(11) ##### ll — length matrix calculated from inverse kinematics
for i in range(8):
    D[:, i] = D[:, i] / (L[:, i].norm()) ## Unit vector

J = zeros(8, 6)
for i in range(8):
    J[i, :3] = -D[:, i].transpose() ### Direction of negative length unit vector
    J[i, 3:] = (D[:, i].transpose()).cross(R*B[:, i]) ### Cross product

f = Matrix([0, 0, -150*9.8, 0, 0, 0]) ### External wrench

print(J.transpose().pinv()*f) ### Tension values
#####
```

### 3.3 Grasping

Grasping modelling determines the set of contact forces and torques exerted by the end-effector to resist the external wrench applied by the object to be held.

With the soft-finger contact model,

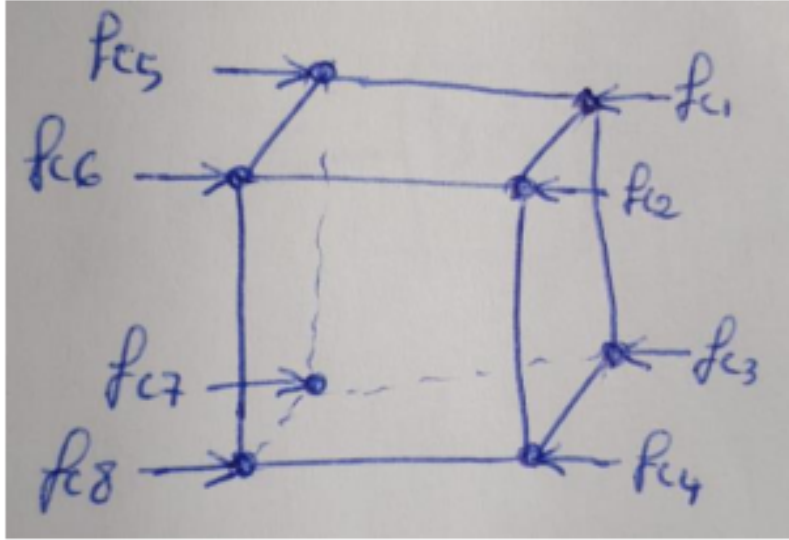


Figure 3.2: Grasp diagram of parallel gripper

$$\left\{ \begin{array}{l} \text{wrench basis} = B_{c_i} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\ \text{contact force} = \vec{f}_{c_i} = [f_{i_1} \ f_{i_2} \ f_{i_3} \ f_{i_4}]^T \in FC_{c_i}; \\ FC_{c_i} = \left\{ \vec{f} \in \mathbb{R}^4: \sqrt{f_1^2 + f_2^2} \leq \mu f_3, f_3 \geq 0, |f_4| \leq \gamma f_3 \right\} \end{array} \right.$$

where the static coefficient of friction  $\mu = 1$  and the coefficient of torsional friction  $\gamma = 1$ , contact map can be defined as,

The contact forces  $f_c$  can be alternatively computed by formulating the problem as a quadratic mathematical program as follows:

$$\begin{array}{ll} \min & \|\vec{f}_c\|^2 \\ \text{subject to} & \left\{ \begin{array}{l} \vec{F}_g = G \vec{f}_c \\ f_{i_3} \geq 0; \ 1 \leq i \leq 8 \end{array} \right. \end{array}$$

## 4 Validation

All the required mathematics to solve inverse kinematics, inverse velocity kinematics, quasi static analysis and grasping. But it is necessary to validate all those by comparing them with the actual robot's data or simulating the robot in the virtual world, which could be done with any simulation software. We have chosen ROS and Gazebo to validate our results.

### 4.1 ROS and Gazebo

Robotic operating system (ROS) is widely used middle ware to communicate between different modules of a robot. Gazebo is a physics engine software, which can simulate dynamics, contact and kinematics of robot, and which is quite reliable and gives results which are very close to the actual robot moving around in the real world.

### 4.2 Model Generation

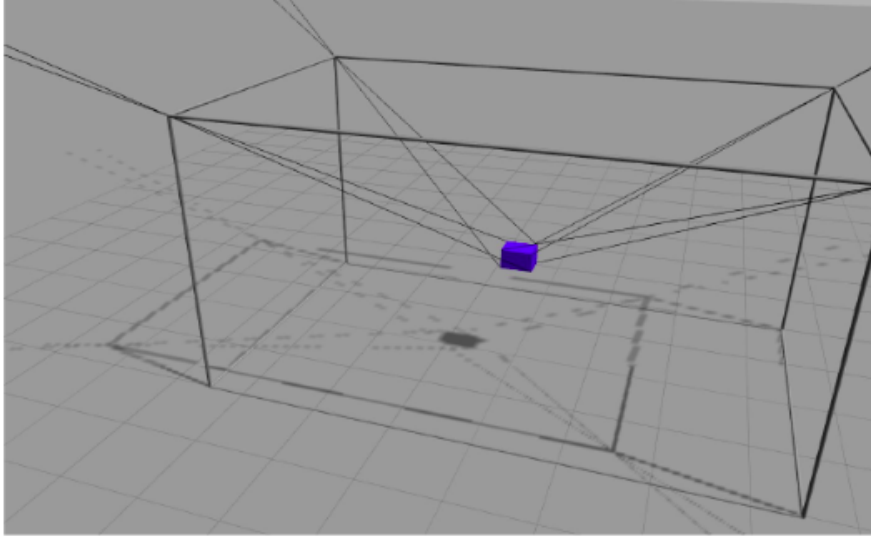


Figure 4.1: Model in gazebo

Assuming warehouse to be the outer frame of our model, we will create a virtual world with mesh files created with the Solidworks. Outer frame is assumed to be an empty square of dimension  $3.5m$ . Platform which moves in the entire workspace has been considered as a rigid square box of  $0.6m$ , which is shown as blue box in Figure 4.1. Gazebo doesn't allow to create massless and flexible links, so cables are taken as rods of mass  $10g$  and of  $10mmdiameter$ . Joints between rods and frame corners are taken as universal joints and joints between rods and platform are taken as spherical ball joints without any joint limitations. As shown in Figure 4.2 rods and universal joints are connected with prismatic joints which allows the movement.

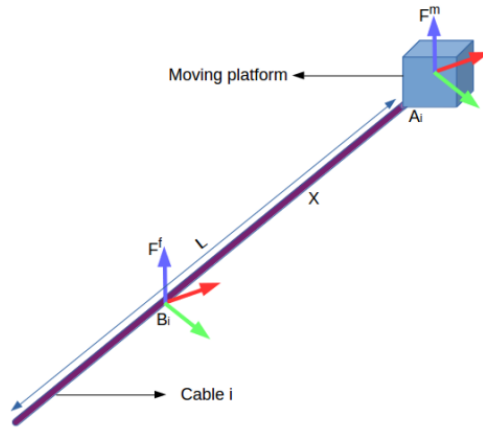


Figure 4.2: Platform and cables

#### 4.2.1 Movement in World

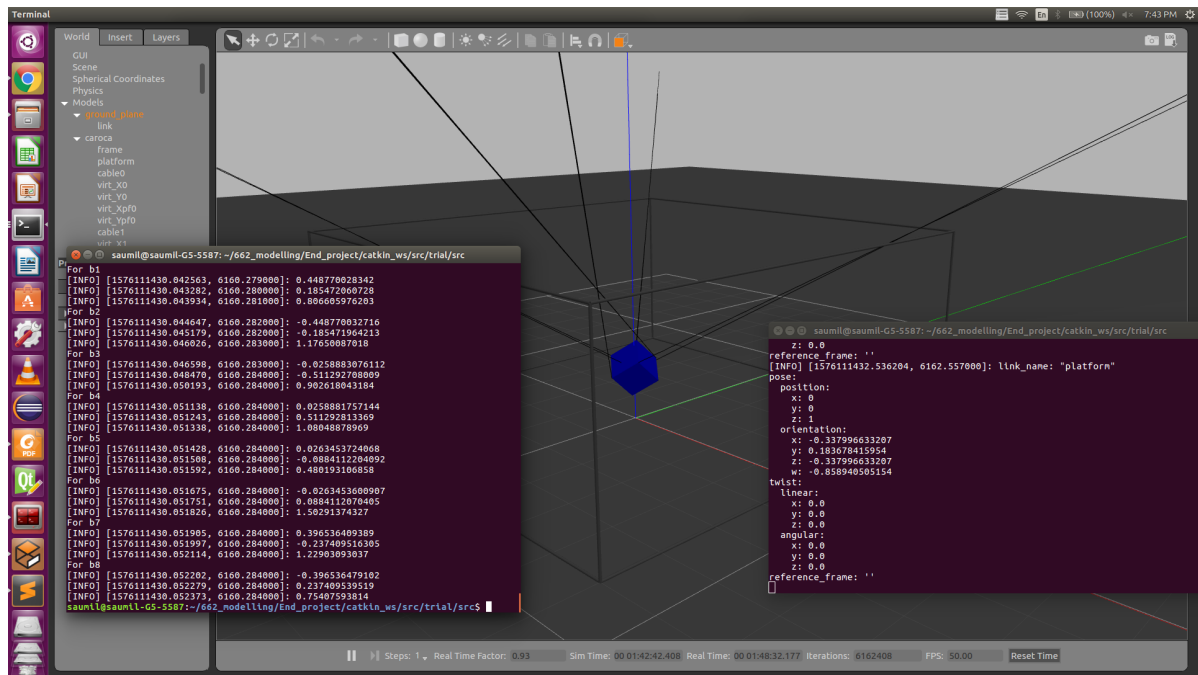


Figure 4.3: Service call to set platform at [0,0,1,10,10,10] pose

This gazebo model was connected with ROS and ros-services allow to change the platform position and orientations. With defining certain state of the platform we can use ros-services to get the positions of spherical joints in the world coordinate frame. As position of universal joints are fixed at the outer frame, we can get the lengths of every cables with this data. For different positions and orientations data points were taken and errors were computed. Computed errors for inverse kinematics are shown in Table 4.1.

Platform state $X, Y, Z, \theta_x, \theta_y, \theta_z$ (meters and degrees)	Lengths Theoretical (meters)	Lengths Simulation (meters)	Error Theoretical - practical ( % )
(0, 0, 1, 0, 0, 0)	5.43323	5.42123	0.221
	5.70263	5.72631	-0.415
	5.70263	5.61263	1.578
	5.43323	5.42311	0.186
	5.43323	5.33231	1.857
	5.70263	5.76310	-1.060
	5.70263	5.70310	-0.008
	5.43323	5.40829	0.459
(1, 1, 1, 0, 0, 0)	6.74685	6.85112	-1.545
	6.96563	6.92991	0.513
	5.97662	5.91190	1.083
	5.50636	5.51600	-0.175
	5.72014	5.71399	0.108
	5.77235	5.73479	0.651
	4.52990	4.54066	-0.238
	4.18569	4.15690	0.688
(1, 1, 1, 0, 0, 10)	6.67700	6.69782	-0.312
	7.03262	7.02169	0.155
	6.03582	6.02740	0.140
	5.44141	5.44068	0.013
	5.65442	5.64184	0.223
	5.83674	5.81942	0.297
	4.58704	4.59409	-0.154
	4.12299	4.12911	-0.148
(1, 1, 1, 0, 10, 10)	6.63673	6.64264	-0.089
	7.07063	7.06338	0.103
	6.08699	6.09858	-0.191
	5.38411	5.37066	0.250
	5.71015	5.71496	-0.084
	5.78223	5.78306	-0.014
	4.53163	4.51634	0.337
	4.18381	4.19130	-0.179
(0, 0, 1, 10, 10, 10)	5.31702	5.29223	0.466
	5.81113	5.82569	-0.250
	5.82018	5.82776	-0.130
	5.30712	5.31712	-0.188
	5.42455	5.44927	-0.456
	5.71089	5.70578	0.089
	5.72394	5.71640	0.132
	5.41078	5.39976	0.204

Table 4.1: Errors in lengths of cables

### 4.3 Quasi Static Analysis

It is not possible to directly measure the tensions in the cable, as we have assumed them to be rigid rod with prismatic joint. It is easy to measure the forces required to pull the rods while sliding over prismatic joint. Gazebo allows to include force sensors on joints and we can use those values to validate our model. Friction at all the joints is taken as zero in order to reduce any loss of energy. Figure 4.4 shows the output of sensor values with velocity and acceleration of platform at the instance. Simulation values and errors computed are included in Table 4.2.

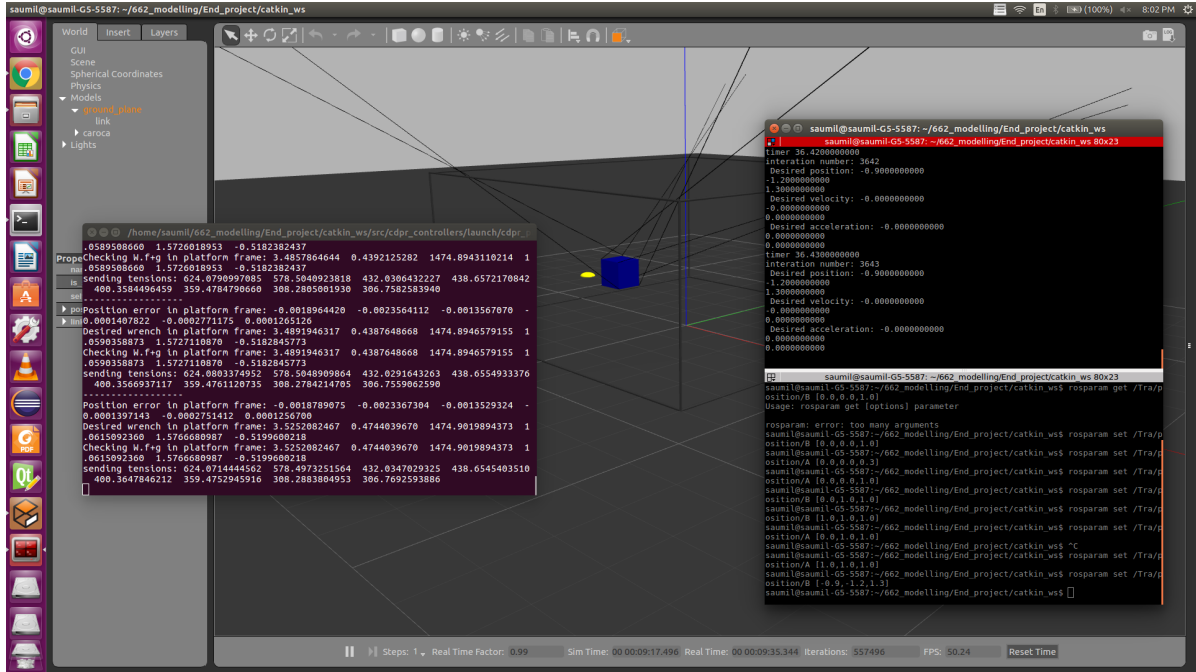


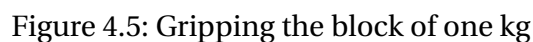
Figure 4.4: Forces at prismatic joint when platform at [0.9 , 1.2 , 1.3] pose



Platform state X, Y, Z, $\theta_x, \theta_y, \theta_z$ (Meters and Degrees)	Tensions Theoretical (Newtons)	Tensions Simulation (Newtons)	Error Theoretical - practical ( % )
(0, 0, 1, 0, 0, 0)	419.143	418.41	0.175
	399.342	398.606	0.185
	399.342	398.606	0.185
	419.143	418.41	0.175
	419.143	418.41	0.175
	399.342	398.606	0.185
	399.342	398.606	0.185
	419.143	418.41	0.175
(0, 1, 1, 0, 0, 0)	329.332	329.766	-0.132
	326.691	326.958	-0.082
	316.491	316.6973	-0.065
	339.066	339.465	-0.118
	483.029	483.254	-0.047
	462.082	462.497	-0.090
	454.394	454.726	-0.073
	490.169	490.36	-0.039
(1, 1, 1, 0, 0, 0)	278.742	280.269	-0.545
	275.457	276.355	-0.325
	353.357	353.167	0.054
	388.380	389.811	-0.367
	375.106	375.858	-0.200
	367.076	368.9	-0.494
	522.489	523.4	-0.174
	561.784	562.426	-0.114
(0.9, 1.2, 1.3, 0, 0, 0)	623.073	624.071	-0.160
	576.756	578.497	-0.301
	428.198	432.035	-0.888
	437.294	438.654	-0.310
	397.514	400.364	-0.712
	359.935	359.475	0.128
	306.773	308.288	-0.491
	303.968	306.769	-0.913

Table 4.2: Errors between theoretical and simulated results for tensions in cable

A simple parallel gripper with two plates of  $0.3m \times 0.6m \times 0.1m$  were attached to the moving platform with the prismatic joint. Surfaces of both the plates were rough and contains friction coefficient of  $\mu = 1$ . "ApplyJointEffort" service from ROS was used to apply force at the prismatic joint. A rigid rectangular block with mass  $1kg$  was introduced in the virtual world. As per calculations gripper would require  $5\text{ N}$  force to pick up the block. After applying  $5\text{ N}$  force to the prismatic joint, gripper was unable to grip the block while moving, because of acceleration of the end effector. With the application of  $6\text{ N}$  force it was able to pick up the block as shown in Figure 4.5.



## 5 Conclusion and Future Work

In this report, several important aspects of 8-cable driven parallel robot have been modeled, containing inverse kinematics, inverse velocity kinematics (though not included in the proposal), quasi static analysis and grasping. All those models were verified with the simulation using Gazebo and ROS. Simulation also proves that CDPR is faster in terms of pick and place task and be used for bigger warehouses.

The next step would be to model dynamic analysis of the robot and stiffness analysis of cables. These models will help to create suitable control system for the real time application. In the real world, robot must be able to avoid obstacles and shall contain the capabilities to generate and follow trajectories that avoids all the obstacles.

Entire code base, robot models, ROS and Gazebo files and videos can be found on the following link.

<https://github.com/SaumilShah66/CDPR-Robot-modelling-project>

## References

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