(https://www.machinelearningplus.com/)

ARIMA Model – Complete Guide to Time Series Forecasting in Python

by <u>Selva Prabhakaran (https://www.machinelearningplus.com/author/selva86/)</u> | Posted on <u>February 18, 2019 (https://www.machinelearningplus.com/time-series/arima-model-time-series-forecasting-python/)</u>

Using ARIMA model, you can forecast a time series using the series past values. In this post, we build an optimal ARIMA model from scratch and extend it to Seasonal ARIMA (SARIMA) and SARIMAX models. You will also see how to build autoarima models in python



ARIMA Model - Time Series Forecasting. Photo by Cerquiera

Contents

[columnize]

- 1. Introduction to Time Series Forecasting
- 2. Introduction to ARIMA Models
- 3. What does the p, d and q in ARIMA model mean?
- 4. What are AR and MA models
- 5. How to find the order of differencing (d) in ARIMA model
- 6. How to find the order of the AR term (p)
- 7. How to find the order of the MA term (q)
- 8. How to handle if a time series is slightly under or over differenced
- 9. How to build the ARIMA Model
- 10. How to do find the optimal ARIMA model manually using Out-of-Time Cross validation
- 11. Accuracy Metrics for Time Series Forecast
- 12. How to do Auto Arima Forecast in Python
- 13. How to interpret the residual plots in ARIMA model
- 14. How to automatically build SARIMA model in python
- 15. How to build SARIMAX Model with exogenous variable
- 16. Practice Exercises
- 17. Conclusion

Search ...

Search

Recent Posts

<u>data.table in R – The Complete Beginners</u> <u>Guide</u>

(https://www.machinelearningplus.com/datamanipulation/datatable-in-r-complete-guide/)

<u>Augmented Dickey Fuller Test (ADF Test) – Must Read Guide</u>

(https://www.machinelearningplus.com/timeseries/augmented-dickey-fuller-test/)

KPSS Test for Stationarity

(https://www.machinelearningplus.com/timeseries/kpss-test-for-stationarity/)

101 R data.table Exercises

(https://www.machinelearningplus.com/datamanipulation/101-r-data-table-exercises/)

P-Value – Understanding from Scratch (https://www.machinelearningplus.com/statistics/p-value/)

101 Python datatable Exercises (pydatatable) (https://www.machinelearningplus.com/data-manipulation/101-python-datatable-exercises-pydatatable/)

<u>Vector Autoregression (VAR) –</u>
<u>Comprehensive Guide with Examples in Python</u>

(https://www.machinelearningplus.com/timeseries/vector-autoregression-examplespython/)

<u>Mahalonobis Distance – Understanding the</u> <u>math with examples (python)</u>

(https://www.machinelearningplus.com/statistics/makdistance/)

<u>datetime in Python – Simplified Guide with</u> <u>Clear Examples</u>

(https://www.machinelearningplus.com/python/datet
python-examples/)

<u>Principal Component Analysis (PCA) – Better Explained</u>

(https://www.machinelearningplus.com/machinelearning/principal-components-analysis-pcabetter-explained/)

Python Logging – Simplest Guide with Full

Code and Examples

(https://www.machinelearningplus.com/python/pythclogging-guide/).

Conclusion

1. Introduction to Time Series Forecasting

A time series is a sequence where a metric is recorded over regular time intervals.

Depending on the frequency, a time series can be of yearly (ex: annual budget), quarterly (ex: expenses), monthly (ex: air traffic), weekly (ex: sales qty), daily (ex: weather), hourly (ex: stocks price), minutes (ex: inbound calls in a call canter) and even seconds wise (ex: web traffic).

We have already seen the steps involved in a previous post on Time Series Analysis (https://www.machinelearningplus.com/time-series-analysis-python). If you haven't read it, I highly encourage you to do so.

Forecasting is the next step where you want to predict the future values the series is going to take.

But why forecast?

Because, forecasting a time series (like demand and sales) is often of tremendous commercial value.

In most manufacturing companies, it drives the fundamental business planning, procurement and production activities. Any errors in the forecasts will ripple down throughout the supply chain or any business context for that matter. So it's important to get the forecasts accurate in order to save on costs and is critical to success.

Not just in manufacturing, the techniques and concepts behind time series forecasting are applicable in any business.

Now forecasting a time series can be broadly divided into two types.

If you use only the previous values of the time series to predict its future values, it is called **Univariate Time Series Forecasting**.

And if you use predictors other than the series (a.k.a exogenous variables) to forecast it is called **Multi Variate Time Series Forecasting**.

This post focuses on a particular type of forecasting method called **ARIMA** modeling.

ARIMA, short for 'AutoRegressive Integrated Moving Average', is a forecasting algorithm based on the idea that the information in the past values of the time series can alone be used to predict the future values.

2. Introduction to ARIMA Models

So what exactly is an ARIMA model?

ARIMA, short for 'Auto Regressive Integrated Moving Average' is actually a class of models that 'explains' a given time series based on its own past values, that is, its own lags and the lagged forecast errors, so that equation can be used to forecast future values.

<u>Matplotlib Histogram – How to Visualize</u>

<u>Distributions in Python</u>

(https://www.machinelearningplus.com/plots/matplothistogram-python-examples/)

ARIMA Model – Complete Guide to Time Series Forecasting in Python (https://www.machinelearningplus.com/timeseries/arima-model-time-series-forecastingpython/).

<u>Time Series Analysis in Python – A</u>

<u>Comprehensive Guide with Examples</u>
(https://www.machinelearningplus.com/time-series/time-series-analysis-python/)

<u>Matplotlib Tutorial – A Complete Guide to</u> <u>Python Plot w/ Examples</u>

(https://www.machinelearningplus.com/plots/matplot tutorial-complete-guide-python-plotexamples/)

<u>Topic modeling visualization – How to present the results of LDA models?</u>
(https://www.machinelearningplus.com/nlp/topic-modeling-visualization-how-to-present-results-lda-models/).

<u>Top 50 matplotlib Visualizations – The Master Plots (with full python code)</u>
(https://www.machinelearningplus.com/plots/top-50-matplotlib-visualizations-the-master-plots-python/)

<u>List Comprehensions in Python – My Simplified Guide</u>

(https://www.machinelearningplus.com/python/list-comprehensions-in-python/)

Python @Property Explained – How to Use and When? (Full Examples)

(https://www.machinelearningplus.com/python/pythc property/)

How Naive Bayes Algorithm Works? (with example and full code)

(https://www.machinelearningplus.com/predictive-modeling/how-naive-bayes-algorithm-works-with-example-and-full-code/)

Tags

Bigrams (https://www.machinelearningplus.com/tag/bigrams/)

Classification

(https://www.machinelearningplus.com/tag/cla

<u>Corpus (https://www.machinelearningplus.com/tag/corpus/)</u>
<u>Cosine Similarity</u>

(https://www.machinelearningplus.com/tag/cosine-similarity/)
data.table

(https://www.machinelearningplus.com/tag/data-

table/) Data Manipulation

(https://www.machinelearningplus.com/tag manipulation/) Debugging

(https://www.machinelearningplus.com/tag/debugging/) Doc2Vec

(https://www.machinelearningplus.com/tag/doc2vec/)

Any 'non-seasonal' time series that exhibits patterns and is not a random white noise can be modeled with ARIMA models.

An ARIMA model is characterized by 3 terms: p, d, q

where,

p is the order of the AR term

q is the order of the MA term

d is the number of differencing required to make the time series stationary

If a time series, has seasonal patterns, then you need to add seasonal terms and it becomes SARIMA, short for 'Seasonal ARIMA'. More on that once we finish ARIMA.

So, what does the 'order of AR term' even mean? Before we go there, let's first look at the 'd' term.

3. What does the p, d and q in ARIMA model mean

The first step to build an ARIMA model is to make the time series stationary (https://www.machinelearningplus.com/stationary-time-series).

Why?

Because, term 'Auto Regressive' in ARIMA means it is a <u>linear regression model</u> (https://www.machinelearningplus.com/machine-learning/complete-introduction-linear-regression-r/) that uses its own lags as predictors. Linear regression models, as you know, work best when the predictors are not correlated and are independent of each other.

So how to make a series stationary?

The most common approach is to difference it. That is, subtract the previous value from the current value. Sometimes, depending on the complexity of the series, more than one differencing may be needed.

The value of d, therefore, is the minimum number of differencing needed to make the series stationary. And if the time series is already stationary, then d = 0.

Next, what are the 'p' and 'q' terms?

'p' is the order of the 'Auto Regressive' (AR) term. It refers to the number of lags of Y to be used as predictors. And 'q' is the order of the 'Moving Average' (MA) term. It refers to the number of lagged forecast errors that should go into the ARIMA Model.

4. What are AR and MA models

So what are AR and MA models? what is the actual mathematical formula for the AR and MA models?

Evaluation Metrics

(https://www.machinelearningplus.com/tag/evaluation-

metrics/) FastText

(https://www.machinelearningplus.com/tag/fasttext/)

Feature Selection

(https://www.machinelearningplus.com/tag/feature-selection/)

Gensim

(https://www.machinelearningplus.com/tag/gensim

<u>LDA</u>

(https://www.machinelearningplus.com/tag/lda/)

Lemmatization

(https://www.machinelearningplus.com/tag/lemmatization/) Linear

Regression (https://www.machinelearningplus.com/tag/linear-

regression/) Logistic

(https://www.machinelearningplus.com/tag/logistic/) LSI

 $\underline{(https://www.machinelearningplus.com/tag/lsi/)} \ \underline{Matplotlib}$

(https://www.machinelearningplus.com/tag/matplo

Multiprocessing

(https://www.machinelearningplus.com/tag/multiprocessing/)

NLP

(https://www.machinelearningplus.com/tag/nl

NLTK (https://www.machinelearningplus.com/tag/nltk/)

<u>Numpy</u>

(https://www.machinelearningplus.com/tag/numpy

P-Value

(https://www.machinelearningplus.com/tag/p-

value/) Pandas

 $\underline{(https://www.machinelearningplus.com/tag/pandas/)}\ \underline{Parallel}$

Processing (https://www.machinelearningplus.com/tag/parallel-

processing/) Phraser

(https://www.machinelearningplus.com/tag/phraser/) Practice

Exercise (https://www.machinelearningplus.com/tag/practice-

exercise/) Python

(https://www.machinelearni

<u>R</u>

(https://www.machinelearningplus.co

Regex (https://www.machinelearningplus.com/tag/regex/)

Regression

(https://www.machinelearningplus.com/tag/regression/)

Residual Analysis

(https://www.machinelearningplus.com/tag/residual-analysis/)

Scikit Learn (https://www.machinelearningplus.com/tag/scikit-

learn/) Significance Tests

(https://www.machinelearningplus.com/tag/signific

tests/) Soft Cosine Similarity

(https://www.machinelearningplus.com/tag/soft-

cosine-similarity/) spaCy

(https://www.machinelearningplus.com/tag/spacy/)

<u>Stationarity</u>

(https://www.machinelearningplus.com/tag/station

Summarization

(https://www.machinelearningplus.com/tag/summarization/)

<u>TaggedDocument</u>

(https://www.machinelearningplus.com/tag/taggeddocument/)

<u>TextBlob</u> (https://www.machinelearningplus.com/tag/textblob/)

TFIDF (https://www.machinelearningplus.com/tag/tfidf/) Time

<u>Series</u>

(https://www.machinelearningplus.com/tag

eedback

A pure **Auto Regressive (AR only) model** is one where Yt depends only on its own lags. That is, Yt is a function of the 'lags of Yt'.

<u>series/)</u> <u>Topic Modeling</u>
(https://www.machinelearningplus.com/tag/topic-modeling/) <u>Visualization</u>
(https://www.machinelearningplus.com/tag/visualiz

$$Y_t = \alpha + \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + ... + \beta_p Y_{t-p} + \epsilon_1$$

Word2Vec (https://www.machinelearningplus.com/tag/word2vec/)

(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/E/q/n/Equation-1-min.png)

where, $Y\{t-1\}$ is the lag1 of the series, λ \beta1\$ is the coefficient of lag1 that the model estimates and α is the intercept term, also estimated by the model.

Likewise a pure **Moving Average (MA only) model** is one where Yt depends only on the lagged forecast errors.

$$Y_t = \alpha + \epsilon_t + \phi_1 \epsilon_{t-1} + \phi_2 \epsilon_{t-2} + \dots + \phi_a \epsilon_{t-a}$$

(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/E/q/n/Equation-2-min.png)

where the error terms are the errors of the autoregressive models of the respective lags. The errors Et and E(t-1) are the errors from the following equations :

$$Y_t = \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + ... + \beta_0 Y_0 + \epsilon_t$$

$$Y_{t-1} = \beta_1 Y_{t-2} + \beta_2 Y_{t-3} + ... + \beta_0 Y_0 + \epsilon_{t-1}$$

(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/E/q/n/Equation-3-min.png)

[Error: The beta coefficients in the second equation above is incorrect.] That was AR and MA models respectively.

So what does the equation of an ARIMA model look like?

An ARIMA model is one where the time series was differenced at least once to make it stationary and you combine the AR and the MA terms. So the equation becomes:

$$Y_t = \alpha + \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + \ldots + \beta_p Y_{t-p} \varepsilon_t + \phi_1 \varepsilon_{t-1} + \phi_2 \varepsilon_{t-2} + \ldots + \phi_q \varepsilon_{t-q}$$

(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/E/q/n/Equation-4-min.png)

ARIMA model in words:

Predicted Yt = Constant + Linear combination Lags of Y (upto p lags) + Linear Combination of Lagged forecast errors (upto q lags)

The objective, therefore, is to identify the values of p, d and q. But how?

5. How to find the order of differencing (d) in ARIMA model

The purpose of differencing it to make the time series stationary.

But you need to be careful to not over-difference the series. Because, an over differenced series may still be stationary, which in turn will affect the model parameters.

So how to determine the right order of differencing?

The right order of differencing is the minimum differencing required to get a near-stationary series which roams around a defined mean and the ACF plot reaches to zero fairly quick.

If the autocorrelations are positive for many number of lags (10 or more), then the series needs further differencing. On the other hand, if the lag 1 autocorrelation itself is too negative, then the series is probably over-differenced.

In the event, you can't really decide between two orders of differencing, then go with the order that gives the least standard deviation in the differenced series.

Let's see how to do it with an example.

First, I am going to check if the series is stationary using the Augmented Dickey Fuller test (adfuller()), from the statsmodels package.

Why?

Because, you need differencing only if the series is non-stationary. Else, no differencing is needed, that is, d=0.

The null hypothesis of the ADF test is that the time series is non-stationary. So, if the p-value of the test is less than the significance level (0.05) then you reject the null hypothesis and infer that the time series is indeed stationary.

So, in our case, if P Value > 0.05 we go ahead with finding the order of differencing.

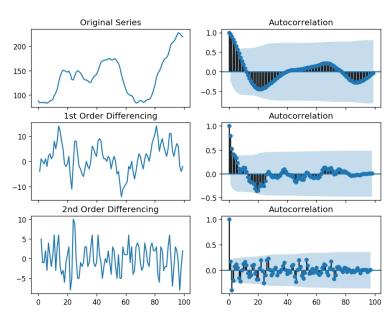
```
from statsmodels.tsa.stattools import adfuller
from numpy import log
result = adfuller(df.value.dropna())
print('ADF Statistic: %f' % result[0])
print('p-value: %f' % result[1])
```

ADF Statistic: -2.464240

p-value: 0.124419

Since P-value is greater than the significance level, let's difference the series and see how the autocorrelation plot looks like.

```
import numpy as np, pandas as pd
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
import matplotlib.pyplot as plt
plt.rcParams.update({'figure.figsize':(9,7), 'figure.dpi':120})
# Import data
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/wwwus
# Original Series
fig, axes = plt.subplots(3, 2, sharex=True)
axes[0, 0].plot(df.value); axes[0, 0].set_title('Original Series')
plot_acf(df.value, ax=axes[0, 1])
# 1st Differencing
axes[1, 0].plot(df.value.diff()); axes[1, 0].set_title('1st Order Differencing')
plot_acf(df.value.diff().dropna(), ax=axes[1, 1])
# 2nd Differencing
axes[2, 0].plot(df.value.diff().diff()); axes[2, 0].set_title('2nd Order Differencing')
plot_acf(df.value.diff().diff().dropna(), ax=axes[2, 1])
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_5_0-min.png)

Order of Differencing

For the above series, the time series reaches stationarity with two orders of differencing. But on looking at the autocorrelation plot for the 2nd differencing the lag goes into the far negative zone fairly quick, which indicates, the series might have been over differenced.

So, I am going to tentatively fix the order of differencing as 1 even though the series is not perfectly stationary (weak stationarity).

```
from pmdarima.arima.utils import ndiffs

df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/wwwus
y = df.value

## Adf Test
ndiffs(y, test='adf') # 2

# KPSS test
ndiffs(y, test='kpss') # 0

# PP test:
ndiffs(y, test='pp') # 2
```

2 0 2

6. How to find the order of the AR term (p)

The next step is to identify if the model needs any AR terms. You can find out the required number of AR terms by inspecting the Partial Autocorrelation (PACF) plot.

But what is PACF?

Partial autocorrelation can be imagined as the correlation between the series and its lag, after excluding the contributions from the intermediate lags. So, PACF sort of conveys the pure correlation between a lag and the series. That way, you will know if that lag is needed in the AR term or not.

So what is the formula for PACF mathematically?

Partial autocorrelation of lag (k) of a series is the coefficient of that lag in the autoregression equation of Y.

```
\$Yt = \lambda Ipha0 + \lambda Ipha1 Y\{t-1\} + \lambda Ipha2 Y\{t-2\} + \lambda Ipha3 Y\{t-3\}
```

That is, suppose, if Y_t is the current series and Y_{t-1} is the lag 1 of Y, then the partial autocorrelation of lag 3 (Y_{t-3}) is the coefficient α 3 of Y_{t-3} in the above equation.

Good. Now, how to find the number of AR terms?

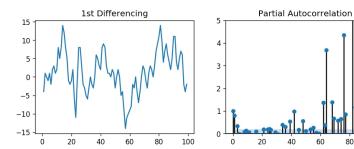
Any autocorrelation in a stationarized series can be rectified by adding enough AR terms. So, we initially take the order of AR term to be equal to as many lags that crosses the significance limit in the PACF plot.

```
# PACF plot of 1st differenced series
plt.rcParams.update({'figure.figsize':(9,3), 'figure.dpi':120})

fig, axes = plt.subplots(1, 2, sharex=True)
axes[0].plot(df.value.diff()); axes[0].set_title('1st Differencing')
axes[1].set(ylim=(0,5))
plot_pacf(df.value.diff().dropna(), ax=axes[1])

plt.show()
```

/Library/Frameworks/Python.framework/Versions/3.7/lib/python3.7/site-packages/statsmodels/regreeturn rho, np.sqrt(sigmasq)



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_9_1-min.png)

Order of AR Term

You can observe that the PACF lag 1 is quite significant since is well above the significance line. Lag 2 turns out to be significant as well, slightly managing to cross the significance limit (blue region). But I am going to be conservative and tentatively fix the p as 1.

7. How to find the order of the MA term (q)

Just like how we looked at the PACF plot for the number of AR terms, you can look at the ACF plot for the number of MA terms. An MA term is technically, the error of the lagged forecast.

The ACF tells how many MA terms are required to remove any autocorrelation in the stationarized series.

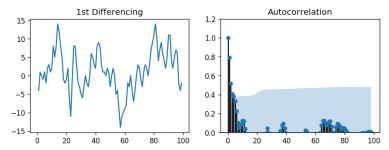
Let's see the autocorrelation plot of the differenced series.

```
import pandas as pd
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
import matplotlib.pyplot as plt
plt.rcParams.update({'figure.figsize':(9,3), 'figure.dpi':120})

# Import data
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/austa.c

fig, axes = plt.subplots(1, 2, sharex=True)
axes[0].plot(df.value.diff()); axes[0].set_title('1st Differencing')
axes[1].set(ylim=(0,1.2))
plot_acf(df.value.diff().dropna(), ax=axes[1])

plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_12_0-min.png)

Order of MA Term

Couple of lags are well above the significance line. So, let's tentatively fix q as 2. When in doubt, go with the simpler model that sufficiently explains the Y.

8. How to handle if a time series is slightly under or over differenced

It may so happen that your series is slightly under differenced, that differencing it one more time makes it slightly over-differenced.

How to handle this case?

If your series is slightly under differenced, adding one or more additional AR terms usually makes it up. Likewise, if it is slightly over-differenced, try adding an additional MA term.

9. How to build the ARIMA Model

Now that you've determined the values of p, d and q, you have everything needed to fit the ARIMA model. Let's use the ARIMA() implementation in statsmodels package.

```
from statsmodels.tsa.arima_model import ARIMA

# 1,1,2 ARIMA Model
model = ARIMA(df.value, order=(1,1,2))
model_fit = model.fit(disp=0)
print(model_fit.summary())
```

Dep. Variable	:	D.value	No. Obser	vations:	99		
Model:	ARI	MA(1, 1, 2)	Log Like	lihood	- 2	253.790	
Method:		css-mle	S.D. of i	nnovations		3.119	
Date:	Wed,	06 Feb 2019	AIC		9	517.579	
Time:		23:32:56	BIC		530.555		
Sample:		1	HQIC		5	522.829	
		std err			_		
const	1.1202	1.290					
ar.L1.D. value	0.6351	0.257	2.469	0.015	0.131 1.139		
na.L1.D. value	0.5287	0.355	1.489	0.140	-0.167 1.224		
na.L2.D. value	-0.0010	0.321	-0.003	0.998	-0.631	0.629	
			ots				
		Imagin					
AR.1	1.5746	+0.00	 00j	1.5746		0.0000	
MA.1	-1.8850	+0.00	00j	1.8850	6	5000	
MA.2	545.3515	+0.00	00j	545.3515	6	0.0000	

The model summary reveals a lot of information. The table in the middle is the coefficients table where the values under 'coef' are the weights of the respective terms.

Notice here the coefficient of the MA2 term is close to zero and the P-Value in P>|z|' column is highly insignificant. It should ideally be less than 0.05 for the respective X to be significant.

So, let's rebuild the model without the MA2 term.

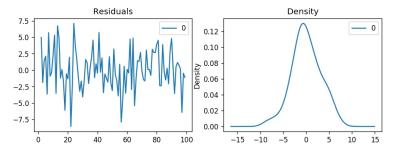
```
# 1,1,1 ARIMA Model
model = ARIMA(df.value, order=(1,1,1))
model_fit = model.fit(disp=0)
print(model_fit.summary())
```

ep. Variable:		D.value	No. Obser	vations:	99		
lodel:	ARI	MA(1, 1, 1)	Log Likel	.ihood	-2	53.790	
lethod:		css-mle	S.D. of i	nnovations.		3.119	
ate:	Sat,	09 Feb 2019	AIC		5	15.579	
ime:		12:16:06	BIC		5	25.960	
ample:		1	HQIC		5	19.779	
	coef	std err	z	P> z	[0.025		
onst				0.386		3.641	
r.L1.D. value	0.6344	0.087	7.317	0.000	0.464	0.804	
a.L1.D. value	0.5297	0.089	5.932	0.000	0.355	0.705	
			ots				
	Real	Real Imagin		ary Modulus		Frequency	
NR.1	1.5764					.0000	
IA.1	-1.8879	+0.000	00i	0j 1.8879		0.5000	

The model AIC has reduced, which is good. The P Values of the AR1 and MA1 terms have improved and are highly significant (<< 0.05).

Let's plot the residuals to ensure there are no patterns (that is, look for constant mean and variance).

```
# Plot residual errors
residuals = pd.DataFrame(model_fit.resid)
fig, ax = plt.subplots(1,2)
residuals.plot(title="Residuals", ax=ax[0])
residuals.plot(kind='kde', title='Density', ax=ax[1])
plt.show()
```

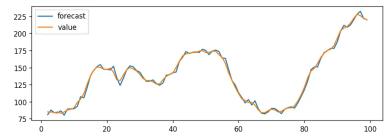


(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_20_0-min.png)

Residuals Density

The residual errors seem fine with near zero mean and uniform variance. Let's plot the actuals against the fitted values using plot_predict().

Actual vs Fitted
model_fit.plot_predict(dynamic=False)
plt.show()



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_22_0-min.png)

Actual vs Fitted

When you set dynamic=False the in-sample lagged values are used for prediction.

That is, the model gets trained up until the previous value to make the next prediction. This can make the fitted forecast and actuals look artificially good.

So, we seem to have a decent ARIMA model. But is that the best?

Can't say that at this point because we haven't actually forecasted into the future and compared the forecast with the actual performance.

So, the real validation you need now is the Out-of-Time cross-validation.

10. How to do find the optimal ARIMA model manually using Out-of-Time Cross validation

In Out-of-Time cross-validation, you take few steps back in time and forecast into the future to as many steps you took back. Then you compare the forecast against the actuals.

To do out-of-time cross-validation, you need to create the training and testing dataset by splitting the time series into 2 contiguous parts in approximately 75:25 ratio or a reasonable proportion based on time frequency of series.

Why am I not sampling the training data randomly you ask?

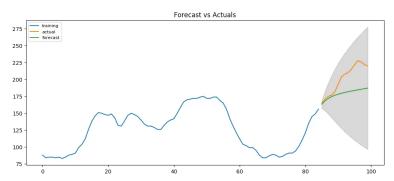
That's because the order sequence of the time series should be intact in order to use it for forecasting.

from statsmodels.tsa.stattools import acf

Create Training and Test
train = df.value[:85]
test = df.value[85:]

You can now build the ARIMA model on training dataset, forecast and plot it.

```
# Build Model
# model = ARIMA(train, order=(3,2,1))
model = ARIMA(train, order=(1, 1, 1))
fitted = model.fit(disp=-1)
# Forecast
fc, se, conf = fitted.forecast(15, alpha=0.05) # 95% conf
# Make as pandas series
fc_series = pd.Series(fc, index=test.index)
lower_series = pd.Series(conf[:, 0], index=test.index)
upper_series = pd.Series(conf[:, 1], index=test.index)
# PLot
plt.figure(figsize=(12,5), dpi=100)
plt.plot(train, label='training')
plt.plot(test, label='actual')
plt.plot(fc_series, label='forecast')
plt.fill_between(lower_series.index, lower_series, upper_series,
                color='k', alpha=.15)
plt.title('Forecast vs Actuals')
plt.legend(loc='upper left', fontsize=8)
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_28_0-min.png)

Forecast vs Actuals

From the chart, the ARIMA(1,1,1) model seems to give a directionally correct forecast. And the actual observed values lie within the 95% confidence band. That seems fine.

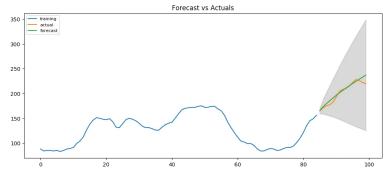
But each of the predicted forecasts is consistently below the actuals. That means, by adding a small constant to our forecast, the accuracy will certainly improve. So, there is definitely scope for improvement.

So, what I am going to do is to increase the order of differencing to two, that is set d=2 and iteratively increase p to up to 5 and then q up to 5 to see which model gives least AIC and also look for a chart that gives closer actuals and forecasts.

While doing this, I keep an eye on the P values of the AR and MA terms in the model summary. They should be as close to zero, ideally, less than 0.05.

```
# Build Model
model = ARIMA(train, order=(3, 2, 1))
fitted = model.fit(disp=-1)
print(fitted.summary())
# Forecast
fc, se, conf = fitted.forecast(15, alpha=0.05) # 95% conf
# Make as pandas series
fc_series = pd.Series(fc, index=test.index)
lower_series = pd.Series(conf[:, 0], index=test.index)
upper_series = pd.Series(conf[:, 1], index=test.index)
# Plot
plt.figure(figsize=(12,5), dpi=100)
plt.plot(train, label='training')
plt.plot(test, label='actual')
plt.plot(fc_series, label='forecast')
plt.fill_between(lower_series.index, lower_series, upper_series,
                color='k', alpha=.15)
plt.title('Forecast vs Actuals')
plt.legend(loc='upper left', fontsize=8)
plt.show()
```

			del Results				
ep. Variable:		D2.value No. Observations: 83					
del:	ARIM	A(3, 2, 1)	Log Likelihood		-21	4.248	
thod:		css-mle	S.D. of i	nnovations	3.153		
te:	Sat, 0	9 Feb 2019	AIC		440.497		
me:		12:49:01	BIC		45	5.010	
nple:		2	HQIC		44	6.327	
.======							
	coef	std err	z	P> z	[0.025		
nst				0.565		0.212	
.L1.D2.value	1.1386	0.109	10.399	0.000	0.924	1.353	
.L2.D2.value	-0.5923	0.155	-3.827	0.000	-0.896	-0.289	
.L3.D2.value	0.3079	0.111	2.778	0.007	0.091	0.525	
.L1.D2.value	-1.0000	0.035	-28.799	0.000	-1.068	-0.932	
			ots				
========				Modulus			
.1				1.1557			
.2	0.3839	-1.63	3				
.3	0.3839	+1.63			0.2132		
.1	1.0000	+0.00	00i	1.0000	0.	0000	



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_30_1-min.png)

Revised Forecast vs Actuals

The AIC has reduced to 440 from 515. Good. The P-values of the X terms are less the < 0.05, which is great.

So overall it's much better.

Ideally, you should go back multiple points in time, like, go back 1, 2, 3 and 4 quarters and see how your forecasts are performing at various points in the year.

Here's a great practice exercise: Try to go back 27, 30, 33, 36 data points and see how the forcasts performs. The forecast performance can be judged using various accuracy metrics discussed next.

11. Accuracy Metrics for Time Series Forecast

The commonly used accuracy metrics to judge forecasts are:

- 1. Mean Absolute Percentage Error (MAPE)
- 2. Mean Error (ME)
- 3. Mean Absolute Error (MAE)
- 4. Mean Percentage Error (MPE)
- 5. Root Mean Squared Error (RMSE)
- 6. Lag 1 Autocorrelation of Error (ACF1)
- 7. Correlation between the Actual and the Forecast (corr)
- 8. Min-Max Error (minmax)

Typically, if you are comparing forecasts of two different series, the MAPE, Correlation and Min-Max Error can be used.

Why not use the other metrics?

Because only the above three are percentage errors that vary between 0 and 1. That way, you can judge how good is the forecast irrespective of the scale of the series.

The other error metrics are quantities. That implies, an RMSE of 100 for a series whose mean is in 1000's is better than an RMSE of 5 for series in 10's. So, you can't really use them to compare the forecasts of two different scaled time series.

```
# Accuracy metrics
def forecast_accuracy(forecast, actual):
   mape = np.mean(np.abs(forecast - actual)/np.abs(actual)) # MAPE
   me = np.mean(forecast - actual)
   mae = np.mean(np.abs(forecast - actual)) # MAE
   mpe = np.mean((forecast - actual)/actual) # MPE
   rmse = np.mean((forecast - actual)**2)**.5 # RMSE
   corr = np.corrcoef(forecast, actual)[0,1] # corr
   mins = np.amin(np.hstack([forecast[:,None],
                             actual[:,None]]), axis=1)
   maxs = np.amax(np.hstack([forecast[:,None],
                             actual[:,None]]), axis=1)
   minmax = 1 - np.mean(mins/maxs)
   acf1 = acf(fc-test)[1]
                                               # ACF1
   return({'mape':mape, 'me':me, 'mae': mae,
            'mpe': mpe, 'rmse':rmse, 'acf1':acf1,
           'corr':corr, 'minmax':minmax})
forecast_accuracy(fc, test.values)
#> {'mape': 0.02250131357314834,
#> 'me': 3.230783108990054,
    'mae': 4.548322194530069,
    'mpe': 0.016421001932706705,
    'rmse': 6.373238534601827,
   'acf1': 0.5105506325288692,
   'corr': 0.9674576513924394,
   'minmax': 0.02163154777672227}
```

Around 2.2% MAPE implies the model is about 97.8% accurate in predicting the next 15 observations.

Now you know how to build an ARIMA model manually.

But in industrial situations, you will be given a lot of time series to be forecasted and the forecasting exercise be repeated regularly.

So we need a way to automate the best model selection process.

12. How to do Auto Arima Forecast in Python

Like R's popular auto.arima() function, the pmdarima package provides auto_arima() with similar functionality.

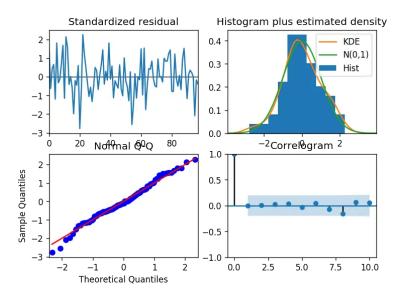
auto_arima() uses a stepwise approach to search multiple combinations of p,d,q parameters and chooses the best model that has the least AIC.

```
from statsmodels.tsa.arima_model import ARIMA
import pmdarima as pm
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/wwwus
model = pm.auto_arima(df.value, start_p=1, start_q=1,
                test='adf',
                            # use adftest to find optimal 'd'
                max_p=3, max_q=3, # maximum p and q
                m=1,
                             # frequency of series
                d=None,
                            # let model determine 'd'
                seasonal=False, # No Seasonality
                start P=0,
                D=0,
                trace=True.
                error action='ignore'.
                suppress warnings=True,
                stepwise=True)
print(model.summary())
#> Fit ARIMA: order=(1, 2, 1); AIC=525.586, BIC=535.926, Fit time=0.060 seconds
#> Fit ARIMA: order=(0, 2, 0); AIC=533.474, BIC=538.644, Fit time=0.005 seconds
#> Fit ARIMA: order=(1, 2, 0); AIC=532.437, BIC=540.192, Fit time=0.035 seconds
#> Fit ARIMA: order=(0, 2, 1); AIC=525.893, BIC=533.648, Fit time=0.040 seconds
#> Fit ARIMA: order=(2, 2, 1); AIC=515.248, BIC=528.173, Fit time=0.105 seconds
#> Fit ARIMA: order=(2, 2, 0); AIC=513.459, BIC=523.798, Fit time=0.063 seconds
#> Fit ARIMA: order=(3, 2, 1); AIC=512.552, BIC=528.062, Fit time=0.272 seconds
#> Fit ARIMA: order=(3, 2, 0); AIC=515.284, BIC=528.209, Fit time=0.042 seconds
#> Fit ARIMA: order=(3, 2, 2); AIC=514.514, BIC=532.609, Fit time=0.234 seconds
#> Total fit time: 0.865 seconds
#>
                       ARIMA Model Results
#> -----
#> Dep. Variable:
                          D2.y No. Observations:
#> Model:
                  ARIMA(3, 2, 1) Log Likelihood
                                                      -250.276
                                                       3.069
                       css-mle S.D. of innovations
#> Method:
                Sat, 09 Feb 2019 AIC
#> Date:
                                                       512.552
                      12:57:22 BIC
#> Time:
                                                       528.062
#> Sample:
                            2 HQIC
                                                        518.825
#>
coef std err
                                z
                                      P>|z| [0.025
                                                        0.9751
#> -----
#> const
            0.0234
                    0.058 0.404 0.687
                                               -0.090
                                                        0.137
                    0.097 11.965
#> ar.L1.D2.y 1.1586
                                      0.000
                                               0.969
                                                         1.348
#> ar.L2.D2.y -0.6640 0.136 -4.890 0.000
                                               -0.930
                                                      -0.398
#> ar.L3.D2.y
             0.3453
                      0.096
                              3.588
                                       0.001
                                                0.157
                                                         0.534
#> ma.L1.D2.y -1.0000
                      0.028 -36.302
                                       0.000
                                               -1.054
                                                        -0.946
                             Roots
#> -----
               Real
                         Imaginary
                                         Modulus
                                                     Frequency
#> -----
             1.1703
                                         1.1703
#> AR.1
                          -0.0000i
                                                      -0.0000
#> AR.2
             0.3763
                                         1.5731
                                                       -0.2116
                          -1.52741
#> AR.3
            0.3763
                          +1.5274j
                                        1.5731
                                                       0.2116
             1.0000
                           +0.0000i
#> MA.1
                                          1.0000
                                                       0.0000
#> ------
```

13. How to interpret the residual plots in ARIMA model

Let's review the residual plots using stepwise_fit.

```
model.plot_diagnostics(figsize=(7,5))
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_39_0-min.png)

Residuals Chart

So how to interpret the plot diagnostics?

Top left: The residual errors seem to fluctuate around a mean of zero and have a uniform variance.

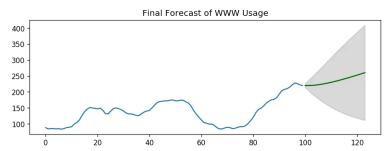
Top Right: The density plot suggest normal distribution with mean zero.

Bottom left: All the dots should fall perfectly in line with the red line. Any significant deviations would imply the distribution is skewed.

Bottom Right: The Correlogram, aka, ACF plot shows the residual errors are not autocorrelated. Any autocorrelation would imply that there is some pattern in the residual errors which are not explained in the model. So you will need to look for more X's (predictors) to the model.

Overall, it seems to be a good fit. Let's forecast.

```
# Forecast
n_{periods} = 24
fc, confint = model.predict(n_periods=n_periods, return_conf_int=True)
index_of_fc = np.arange(len(df.value), len(df.value)+n_periods)
# make series for plotting purpose
fc_series = pd.Series(fc, index=index_of_fc)
lower_series = pd.Series(confint[:, 0], index=index_of_fc)
upper series = pd.Series(confint[:, 1], index=index of fc)
# PLot
plt.plot(df.value)
plt.plot(fc_series, color='darkgreen')
plt.fill_between(lower_series.index,
                 lower_series,
                 upper_series,
                 color='k', alpha=.15)
plt.title("Final Forecast of WWW Usage")
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_41_0-min.png)

Final Forecast of WWW Usage

14. How to automatically build SARIMA model in python

The problem with plain ARIMA model is it does not support seasonality.

If your time series has defined seasonality, then, go for SARIMA which uses seasonal differencing.

Seasonal differencing is similar to regular differencing, but, instead of subtracting consecutive terms, you subtract the value from previous season.

So, the model will be represented as SARIMA(p,d,q)x(P,D,Q), where, P, D and Q are SAR, order of seasonal differencing and SMA terms respectively and 'x' is the frequency of the time series.

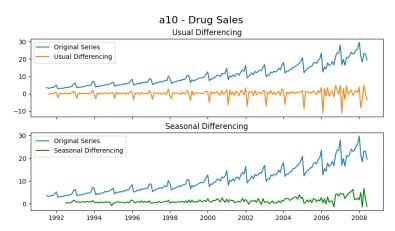
If your model has well defined seasonal patterns, then enforce D=1 for a given frequency 'x'.

Here's some practical advice on building SARIMA model:

As a general rule, set the model parameters such that D never exceeds one. And the total differencing 'd + D' never exceeds 2. Try to keep only either SAR or SMA terms if your model has seasonal components.

Let's build an SARIMA model on 'a10' - the drug sales dataset.

```
# Import
data = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/a10.d
# PLot
fig, axes = plt.subplots(2, 1, figsize=(10,5), dpi=100, sharex=True)
# Usual Differencing
axes[0].plot(data[:], label='Original Series')
axes[0].plot(data[:].diff(1), label='Usual Differencing')
axes[0].set_title('Usual Differencing')
axes[0].legend(loc='upper left', fontsize=10)
# Seasinal Dei
axes[1].plot(data[:], label='Original Series')
axes[1].plot(data[:].diff(12), label='Seasonal Differencing', color='green')
axes[1].set_title('Seasonal Differencing')
plt.legend(loc='upper left', fontsize=10)
plt.suptitle('a10 - Drug Sales', fontsize=16)
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_43_0-min.png)

Seasonal Differencing

As you can clearly see, the seasonal spikes is intact after applying usual differencing (lag 1). Whereas, it is rectified after seasonal differencing.

Let's build the SARIMA model using pmdarima's $auto_arima()$. To do that, you need to set seasonal=True, set the frequency m=12 for month wise series and enforce D=1.

```
Fit ARIMA: order=(1, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=534.818, BIC=551.105, Fit time=1.7 Fit ARIMA: order=(0, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=624.061, BIC=630.576, Fit time=0.0 Fit ARIMA: order=(1, 0, 0) seasonal_order=(1, 1, 0, 12); AIC=596.004, BIC=609.034, Fit time=0.6 Fit ARIMA: order=(0, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=611.475, BIC=624.505, Fit time=0.7 Fit ARIMA: order=(1, 0, 1) seasonal_order=(1, 1, 1, 12); AIC=557.501, BIC=577.046, Fit time=3.6 (...TRUNCATED...)

Fit ARIMA: order=(3, 0, 0) seasonal_order=(1, 1, 1, 12); AIC=554.570, BIC=577.372, Fit time=2.4 Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=554.094, BIC=570.381, Fit time=0.2 Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 2, 12); AIC=529.502, BIC=552.305, Fit time=2.1 Fit ARIMA: order=(3, 0, 0) seasonal_order=(1, 1, 2, 12); AIC=nan, BIC=nan, Fit time=nan seconds Total fit time: 31.613 seconds
```

Statespace Model Results

Dep. Variable:	у	No. Observations:	204
Model:	SARIMAX(3, 0, 0)x(0, 1, 1, 12)	Log Likelihood	-258.300
Date:	Sat, 09 Feb 2019	AIC	528.601
Time:	21:07:16	BIC	548.146
Sample:	0	HQIC	536.517
	- 204		

opg

	coef	std err	z	P> z	[0.025	0.975]
intercept	0.1649	0.097	1.705	0.088	-0.025	0.354
ar.L1	0.0949	0.043	2.205	0.027	0.011	0.179
ar.L2	0.4145	0.035	11.907	0.000	0.346	0.483
ar.L3	0.3531	0.053	6.601	0.000	0.248	0.458
ma.S.L12	-0.4635	0.058	-8.008	0.000	-0.577	-0.350
sigma2	0.8461	0.057	14.925	0.000	0.735	0.957

Covariance Type:

Ljung-Box (Q):	59.80	Jarque-Bera (JB):	124.59
Prob(Q):	0.02	Prob(JB):	0.00
Heteroskedasticity (H):	12.75	Skew:	0.29
Prob(H) (two-sided):	0.00	Kurtosis:	6.90

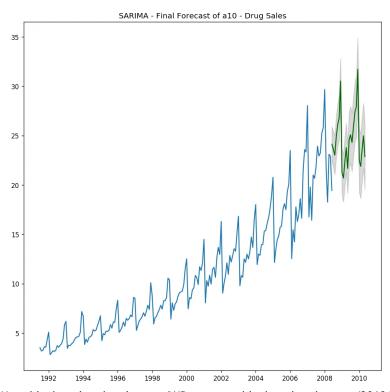
(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/M/o/n/Model-Summary-1-min.png)

The model has estimated the AIC and the P values of the coefficients look significant. Let's look at the residual diagnostics plot.

The best model SARIMAX(3, 0, 0)x(0, 1, 1, 12) has an AIC of 528.6 and the P Values are significant.

Let's forecast for the next 24 months.

```
# Forecast
n periods = 24
fitted, confint = smodel.predict(n_periods=n_periods, return_conf_int=True)
index_of_fc = pd.date_range(data.index[-1], periods = n_periods, freq='MS')
# make series for plotting purpose
fitted_series = pd.Series(fitted, index=index_of_fc)
lower_series = pd.Series(confint[:, 0], index=index_of_fc)
upper_series = pd.Series(confint[:, 1], index=index_of_fc)
# PLot
plt.plot(data)
plt.plot(fitted_series, color='darkgreen')
plt.fill_between(lower_series.index,
                lower_series,
                 upper_series,
                 color='k', alpha=.15)
plt.title("SARIMA - Final Forecast of a10 - Drug Sales")
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_48_0-min.png).

There you have a nice forecast that captures the expected seasonal demand pattern.

15. How to build SARIMAX Model with exogenous variable

The SARIMA model we built is good. I would stop here typically.

But for the sake of completeness, let's try and force an external predictor, also called, 'exogenous variable' into the model. This model is called the SARIMAX model.

The only requirement to use an exogenous variable is you need to know the value of the variable during the forecast period as well.

For the sake of demonstration, I am going to use the seasonal index from the classical seasonal decomposition (https://www.machinelearningplus.com/time-series/time-series-analysis-python/) on the latest 36 months of data.

Why the seasonal index? Isn't SARIMA already modeling the seasonality, you ask?

You are correct.

But also, I want to see how the model looks if we force the recent seasonality pattern into the training and forecast.

Secondly, this is a good variable for demo purpose. So you can use this as a template and plug in any of your variables into the code. The seasonal index is a good exogenous variable because it repeats every frequency cycle, 12 months in this case.

So, you will always know what values the seasonal index will hold for the future forecasts.

Import Data

data = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/a10.d

Let's compute the seasonal index so that it can be forced as a (exogenous) predictor to the SARIMAX model.

The exogenous variable (seasonal index) is ready. Let's build the SARIMAX model.

```
Fit ARIMA: order=(1, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=536.818, BIC=556.362, Fit time=2.6 Fit ARIMA: order=(0, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=626.061, BIC=635.834, Fit time=0.0 Fit ARIMA: order=(1, 0, 0) seasonal_order=(1, 1, 0, 12); AIC=598.004, BIC=614.292, Fit time=0.6 Fit ARIMA: order=(0, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=613.475, BIC=629.762, Fit time=0.5 Fit ARIMA: order=(1, 0, 1) seasonal_order=(1, 1, 1, 12); AIC=559.530, BIC=582.332, Fit time=3.1 (...Truncated...)
Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=556.094, BIC=575.639, Fit time=0.2 Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 2, 12); AIC=531.502, BIC=557.562, Fit time=2.3 Fit ARIMA: order=(3, 0, 0) seasonal_order=(1, 1, 2, 12); AIC=nan, BIC=nan, Fit time=nan seconds Total fit time: 30.781 seconds
```

Statespace Model Results

Dep. Va	ariable:				y No	. Observa	itions:	204
	Model: 9	SARIMAX(MAX(3, 0, 0)x(0, 1, 1, 12)				lihood -	258.300
	Date:		Sat, 09 Feb 2019				AIC	530.601
		2	0:57:50		BIC			
S	Sample:			(0		HQIC	539.836
				- 204	4			
Covarianc	е Туре:			op	g			
	coe	f std	err	z P>	· z	[0.025	0.975	I
intercept	0.164	9 0.0	097 1.7	0.0	88	-0.025	0.354	ı
x1	3.924e-0	7 2.43e-	-09 161.8	12 0.0	000 3	3.88e-07	3.97e-07	7
ar.L1	0.0949	9 0.0)43 2.2	0.0	027	0.011	0.179)
ar.L2	0.414	5 0.0	35 11.9	0.0	000	0.346	0.483	3
ar.L3	0.353	1 0.0	53 6.6	01 0.0	000	0.248	0.458	3
ma.S.L12	-0.463	5 0.0	58 -8.0	0.0	000	-0.577	-0.350)
sigma2	0.846	1 0.0	057 14.9	25 0.0	000	0.735	0.957	7
Ljung-Box (Q):		(Q): 59.8	BO Jarqu	e-Bera	(JB):	124.59		
	Prob((Q): 0.0	02	Prob	(JB):	0.00		
Heteroske	dasticity ((H): 12.	75	5	Skew:	0.29		
Prob(H)	Prob(H) (two-sided):		00	Kur	tosis:	6.90		

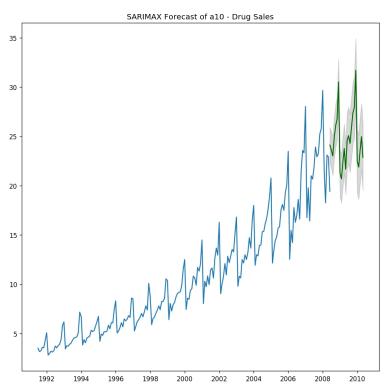
(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/M/o/n/Model-Summary-2-min.png)

So, we have the model with the exogenous term. But the coefficient is very small for x1, so the contribution from that variable will be negligible. Let's forecast it anyway.

We have effectively forced the latest seasonal effect of the latest 3 years into the model instead of the entire history.

Alright let's forecast into the next 24 months. For this, you need the value of the seasonal index for the next 24 months.

```
# Forecast
n_{periods} = 24
fitted, confint = sxmodel.predict(n_periods=n_periods,
                                  exogenous=np.tile(seasonal_index.value, 2).reshape(-1,1),
                                  return_conf_int=True)
index_of_fc = pd.date_range(data.index[-1], periods = n_periods, freq='MS')
# make series for plotting purpose
fitted_series = pd.Series(fitted, index=index_of_fc)
lower_series = pd.Series(confint[:, 0], index=index_of_fc)
upper_series = pd.Series(confint[:, 1], index=index_of_fc)
# PLot
plt.plot(data['value'])
plt.plot(fitted_series, color='darkgreen')
plt.fill_between(lower_series.index,
                 lower_series,
                 upper_series,
                 color='k', alpha=.15)
plt.title("SARIMAX Forecast of a10 - Drug Sales")
plt.show()
```



(https://machinelearningplus.sirv.com/WP_www.machinelearningplus.com/2019/02/o/u/n/output_59_0-min.png)

SARIMAX Forecast

16. Practice Exercises

In the AirPassengers dataset, go back 12 months in time and build the SARIMA forecast for the next 12 months.

- 1. Is the series stationary? If not what sort of differencing is required?
- 2. What is the order of your best model?
- 3. What is the AIC of your model?
- 4. What is the MAPE achieved in OOT cross-validation?
- 5. What is the order of the best model predicted by auto_arima() method?

17. Conclusion

Congrats if you reached this point. Give yourself a BIG hug if you were able to solve the practice exercises.

I really hope you found this useful?

We have covered a lot of concepts starting from the very basics of forecasting, AR, MA, ARIMA, SARIMA and finally the SARIMAX model. If you have any questions please write in the comments section. Meanwhile, I will work on the next article.

Happy Learning!

What do you think? 51 Responses Upvote Love Comments Community Privacy Policy Login Sort by Newest Join the discussion... LOG IN WITH OR SIGN UP WITH DISQUS ? Name Mike Heimlich • 9 days ago Did anyone else had the problem that in each of the (partial) autocorr and normal autocorrelation graphs only the first 20 values were used? ^ | ~ • Reply • Thushara De Silva • a month ago I follow the codes to fit a SARIMAX. However, I didn't get the 'x1' term in my model. I got the same SARIMA model. Any comments on this? ^ | * • Reply • Asad • 2 months ago plot_diagnostics function giving error: AttributeError: 'ARMAResults' object has no attribute 'plot_diagnostics'. I checked, I installed and imported

all the necessary libraries and modules.