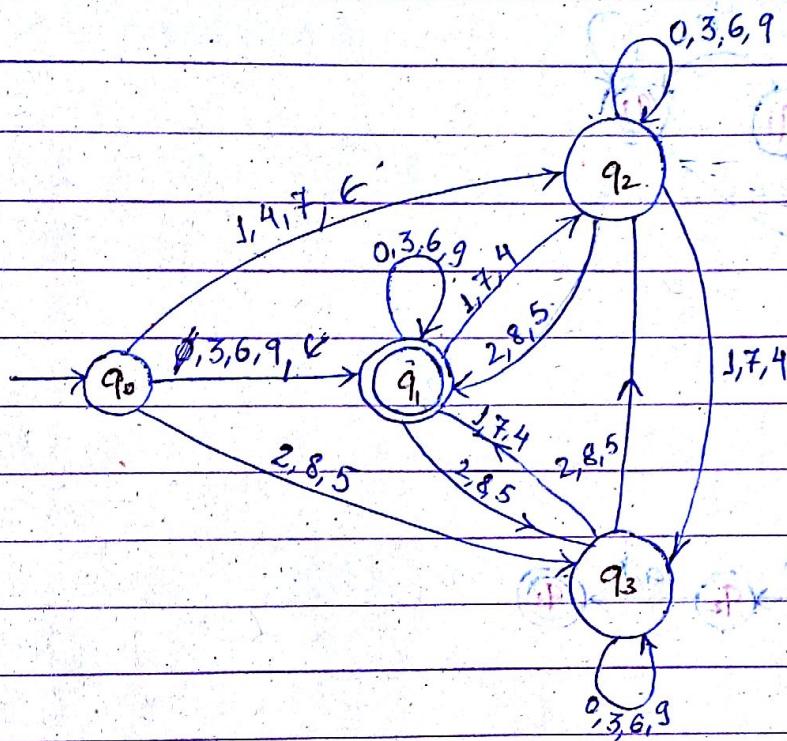
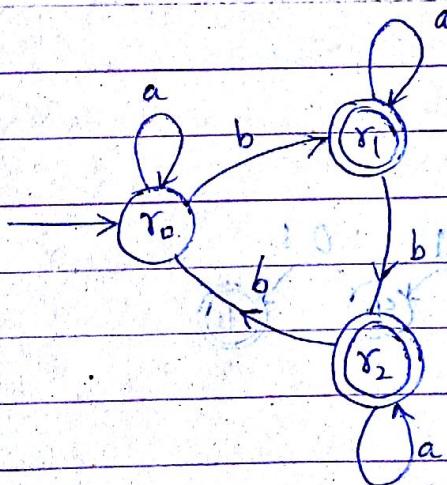


# ASSIGNMENT - 1

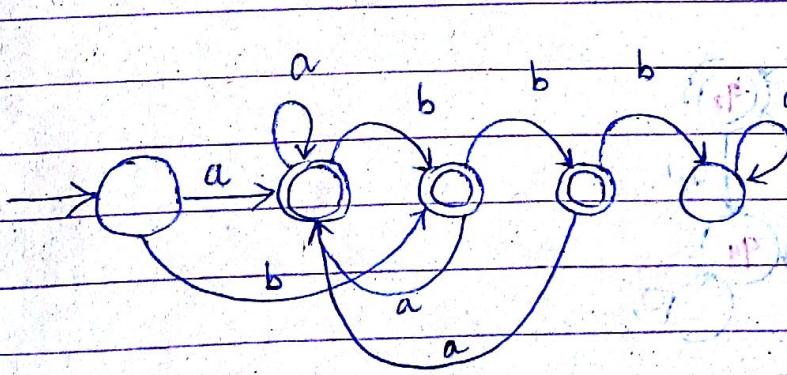
1.



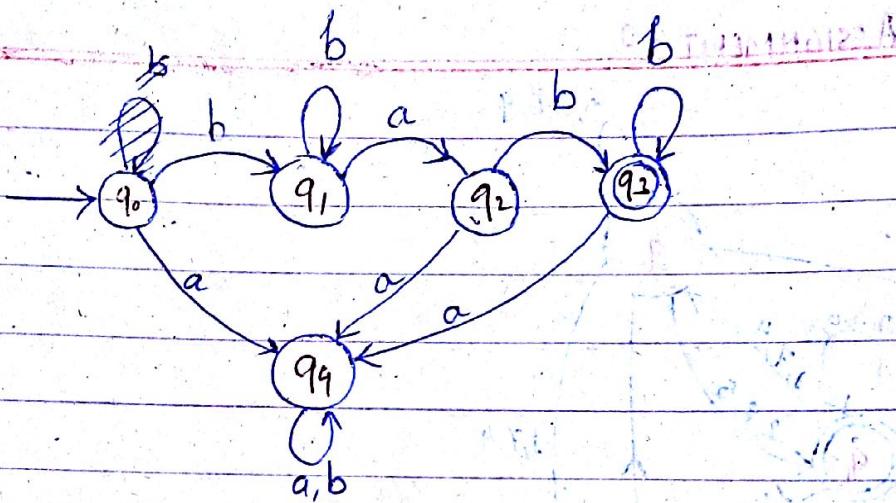
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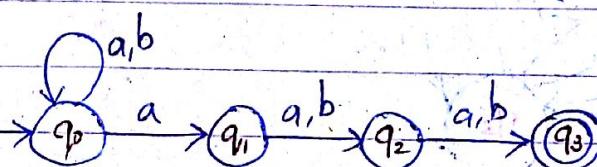
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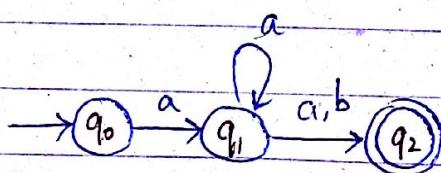
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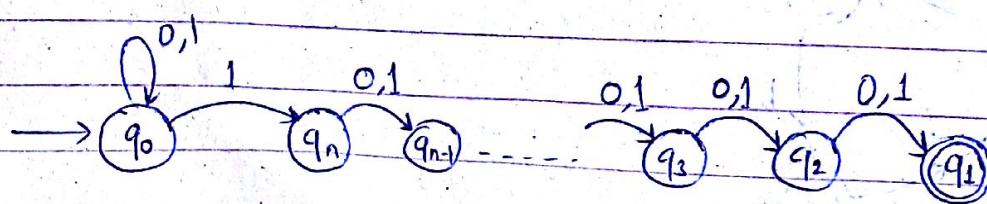
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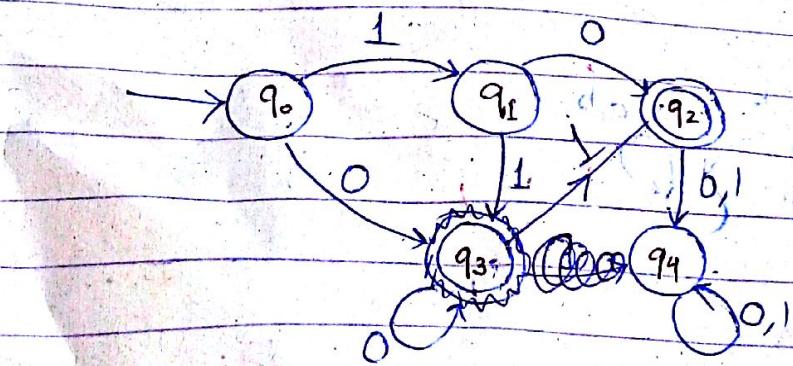
6.



7.



8.



9.  $S \rightarrow aAb \mid asb$

$A \rightarrow bAa \mid ba$

(10)

$A \rightarrow aAb \mid abAa \mid \text{[crossed out]}$

$A \rightarrow AA \mid \epsilon$

11.

$S \rightarrow asb \mid aAb$

$A \rightarrow bA \mid b$

(12)

$S \rightarrow ash \mid aab \mid ab \mid aA \mid bB$

$A \rightarrow aA \mid a$

$B \rightarrow bB \mid b$

Simplifying:  $T_a \rightarrow a$  Eliminating unit productions:

$T_b \rightarrow b$   $S \rightarrow asb \mid aAb \mid abB \mid aA \mid a \mid bB \mid b$

$A \rightarrow aA \mid a$

$B \rightarrow bB \mid b$

Normalizing:

$T_a \rightarrow a$

$T_b \rightarrow b$

$A \rightarrow TaA \mid a$

$B \rightarrow TbB \mid b$

$K_1 \rightarrow ST_b$

$K_2 \rightarrow AT_b$

$K_3 \rightarrow BT_b$

$S \rightarrow TaK_1 \mid TaK_2 \mid TaK_3 \mid TaA \mid TbB \mid a \mid b$ . (Ans.)

13.  $S \rightarrow 0|1S \mid 1S \mid A$   
 $A \rightarrow 0|A \mid \epsilon$

14. Assuming  $m, n \geq 0$

$$\begin{aligned} S &\rightarrow AC \mid B \\ A &\rightarrow aAb \mid \epsilon \\ C &\rightarrow CC \mid \epsilon \\ B &\rightarrow aB \mid D \\ D &\rightarrow bDc \mid \epsilon \end{aligned}$$

15.  $S \rightarrow aAbB$   
 $A \rightarrow aA \mid a$   
 $B \rightarrow bB \mid b$

Simplified already;

$$\begin{aligned} T_a &\rightarrow a \\ T_b &\rightarrow b \\ A &\rightarrow T_a A \mid a \\ B &\rightarrow T_b B \mid b \\ K_1 &\rightarrow T_b B \\ K_2 &\rightarrow AK_1 \\ S &\rightarrow T_a K_2 \end{aligned}$$

16.

NDFA (given)

16

state	a	b	
$\rightarrow q_0$	$q_1$	$q_0$	
$q_1$	$q_0$	$q_2$	
$q_2$	$q_3$	$q_1$	
* $q_3$	$q_3$	$q_0$	
$q_4$	$q_3$	$q_5$	
$q_5$	$q_4, q_6$	$q_2, \phi$	
$q_6$	$q_5$	-	
$q_7$	$q_6$	$q_3$	

Converting into DFA:

$\rightarrow [q_0]$	$[q_1]$	$[q_0]$
$[q_1]$	$[q_0]$	$[q_2]$
$[q_2]$	$[q_3]$	$[q_1]$
* $[q_3]$	$[q_3]$	$[q_0]$

No unused state found.

$$\pi_0 = \{ \underbrace{q_0, q_1, q_2}_{r_0}, q_3 \}$$

$$\pi_1 = \{ q_0, q_1, \underbrace{q_2}_{r_1}, q_3 \}$$

$$\pi_2 = \{ \underbrace{q_0, q_1}_{r_0, r_3}, \underbrace{q_2}_{r_1}, q_3 \}$$

State	a	b	
$\rightarrow r_0$	$r_3$	$r_0$	
$r_1$	$r_2$	$r_0$	
* $r_2$	$r_2$	$r_0$	
$r_3$	$r_3$	$r_1$	
	a	a	
	b	b	
	b	b	

17.

	0	1
$\rightarrow * q_0$	$q_1$	$q_3$
$q_1$	$q_4$	$q_2$
$* q_2$	$q_{15}$	-
$q_3$	$q_0$	$q_4$
$q_4$	$q_4$	$q_4$
$q_5$	-	$q_2 q_4$

Converting into DFA

State	0	1
$\rightarrow * [q_0]$	$[q_1]$	$[q_3]$
$[q_1]$	$[q_4]$	$[q_2]$
$* [q_2]$	$[q_{15}]$	$[\phi]$
$[q_3]$	$[q_0]$	$[q_4]$
$[q_4]$	$[q_4]$	$[q_4]$
$[q_{15}]$	$[q_4]$	$[q_2 q_4]$
$* [q_2 q_4]$	$[q_{15} q_4 q_5]$	$[q_4]$
$[q_{15} q_4 q_5]$	$[q_4]$	$[q_2 q_4]$
$[\phi]$	$[\phi]$	$[\phi]$

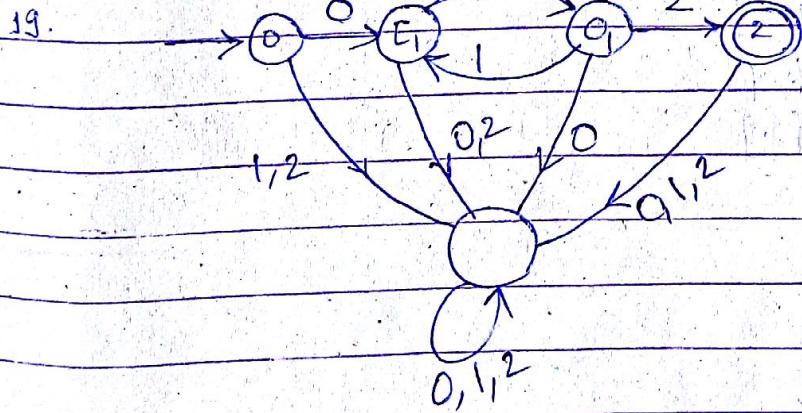
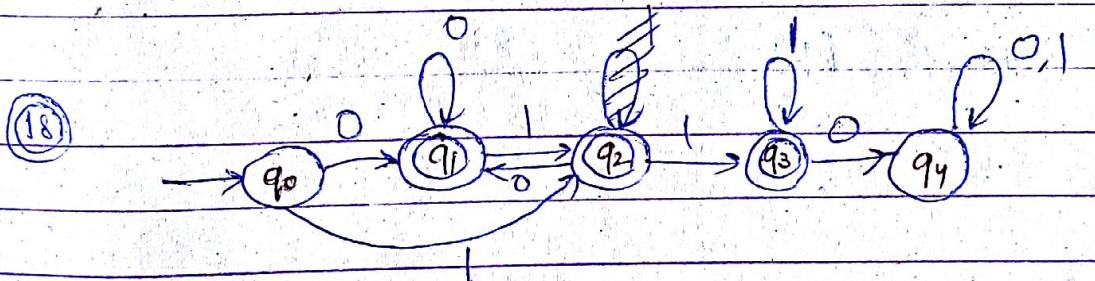
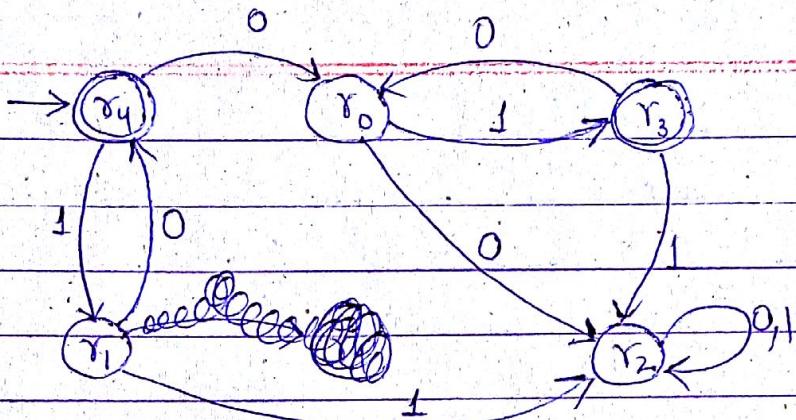
No useless state.

$$\pi_0 = \{ \underbrace{q_1, q_3, q_4, q_{15}, q_{15}, \phi}_{q_0, q_2, q_4} \}$$

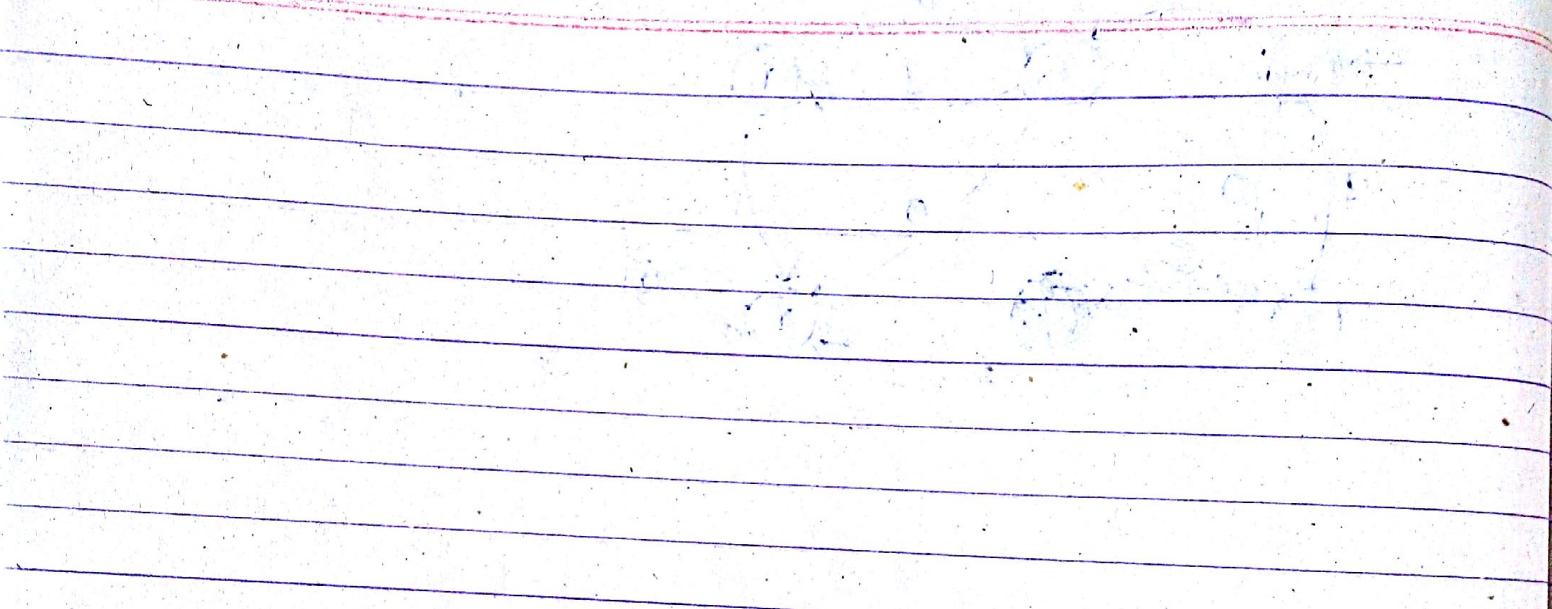
$$\{ \underbrace{q_1, q_{15}, q_{15}}_{r_0}, \underbrace{q_3}_{r_1}, \underbrace{q_4, \phi}_{r_2}, \underbrace{q_0}_{r_3}, \underbrace{q_2, q_4}_{r_4} \}$$

State	0	1
$\rightarrow * r_4$	$r_0$	$r_1$
$* r_3$	$r_0$	$r_2$
$r_2$	$r_2$	$r_2$
$r_1$	$r_4$	$r_2$
$r_0$	$r_2$	$r_3$

Mimized  
DFA



20.

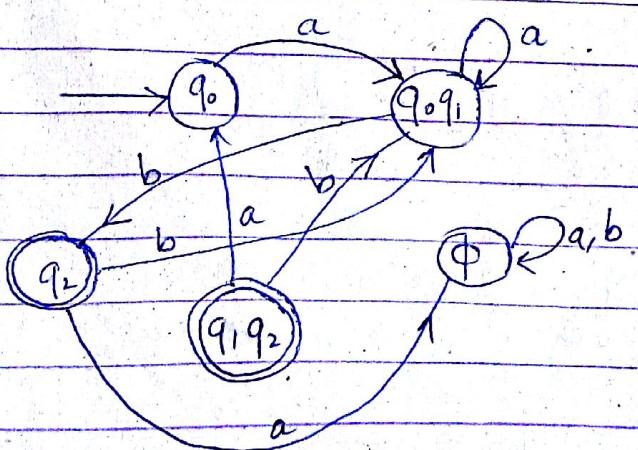


21. NDFA:

	a	b
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_2\}$
$q_1$	$q_0$	$q_1$
$* q_2$	$-$	$q_0, q_1$

DFA:

$\rightarrow [q_0]$	$[q_0 q_1]$	$[q_2]$
$* [q_2]$	$[\emptyset]$	$[q_0 q_1]$
$[q_0 q_1]$	$[q_0 q_1]$	$[q_1 q_2]$
$* [q_1 q_2]$	$[q_0]$	$[q_0, q_1]$
$[\emptyset]$	$[\emptyset]$	$[\emptyset]$



22.

	0	1
$\rightarrow q_0$	$q_1$	$q_3$
$q_1$	$q_2$	$q_4$
$q_2$	$q_1$	$q_4$
$q_3$	$q_2$	$q_4$
$* q_4$	$q_4$	$q_4$

No unused state

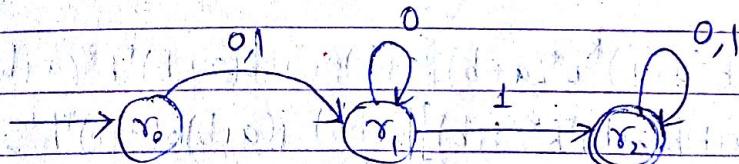
$$\pi_0 = \{ \underline{q_0}, \underline{q_1}, \underline{q_2}, \underline{q_3}, \underline{\underline{q_4}} \}$$

$$\pi_1 = \{ \underline{q_0}, \underline{\underline{q_1}}, \underline{\underline{q_2}}, \underline{\underline{q_3}}, \underline{\underline{q_4}} \}$$

$$\pi_2 = \{ \underline{\underline{q_0}}, \underline{\underline{\underline{q_1}}}, \underline{\underline{\underline{q_2}}}, \underline{\underline{\underline{q_3}}}, \underline{\underline{\underline{q_4}}} \}$$

state labels

$\rightarrow r_0$	$r_1$	$r_2$
$r_1$	$r_1$	$r_2$
$* r_2$	$r_2$	$r_2$



23.

$$q_1 = e$$

$$q_2 = q_1 a + q_2 b + q_3 a + q_3 b + q_4 a + q_4 b$$

$$* q_3 = q_2 a$$

$$q_4 = q_2 b$$

$$\begin{aligned} q_3 &\neq (q_1(a+b) + q_3(a+b) + q_4(a+b)) a \\ &= (a+b) + q_3(a+b) + \end{aligned}$$

$$q_4 = (q_1(a+b) + q_3(a+b) + q_4(a+b)) b$$

$$q_4 = (a+b)b + q_3(a+b)b + q_4(a+b)b$$

$$q_4 = ((e+q_3)(a+b)b)(a+b)^*b^*$$

$$q_3 = (a+b) + q_3(a+b) + ((e+q_3)(a+b)b)(a+b)^*b^*(a+b)$$

$$q_3 = (a+b) + q_3(a+b) + (a+b)b(a+b)^*b^*(a+b)$$

$$q_3 = (a+b)[e + b(a+b)^*b^*(a+b)] + q_3(a+b)(e + b(a+b)^*b^*(a+b))$$

$$\begin{aligned} q_3 &= (a+b)[e + b(a+b)^*b^*(a+b)][(a+b)(e + b(a+b)^*b^*(a+b))]^* \\ &= [(a+b) + (a+b)b(a+b)^*b^*(a+b)][(a+b) + (a+b)b(a+b)^*b^*(a+b)]^* \\ &= \{(a+b)[e + b(a+b)^*b^*(a+b)]\}^* \end{aligned}$$

$$= \{(a+b)[e + b(a+b)^*b^*(a+b)]\}^* \quad (\text{Ans})$$

$$q_2 = (a+b) + q_2 a(a+b) + q_2 b(a+b)$$

$$q_2 = (a+b)[(a+b)(a+b)]^*$$

$$q_3 = a(a+b)[(a+b)(a+b)]^* \quad (\text{Ans})$$

24.

$$q_3 = q_2a + q_4a$$

$$q_2 = q_1(a+b) \Rightarrow q_2 = (a+b)$$

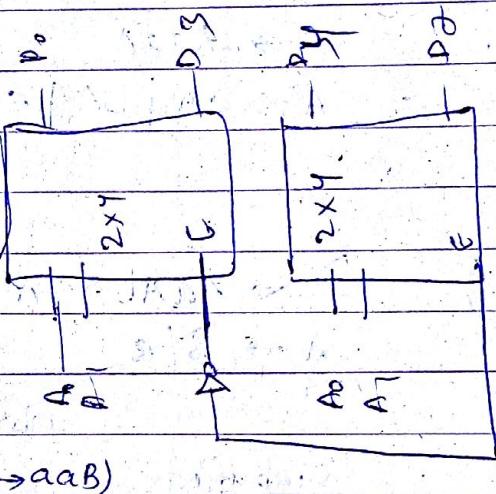
$$q_1 = \epsilon$$

$$q_4 = q_3(a+b)$$

$$q_3 = (a+b)a + q_3(a+b)a$$

$$q_3 = (a+b)a[(a+b)a]^*$$

$$q_3 = ((a+b)a)^* \text{ (Ans.)}$$



Q4 NFA

25.

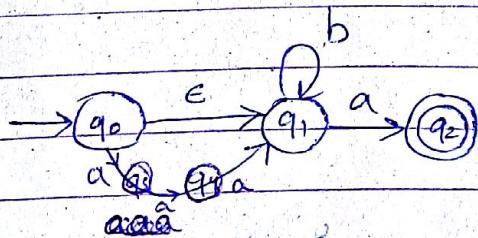
$$S \xrightarrow{*} a^* A | B$$

$$\rightarrow a(aaB) | B \quad (A \rightarrow aaB)$$

$$\xrightarrow{*} aaab^n B | b^n B \quad (n \text{ times})$$

$$\rightarrow aaab^n a | b^n a, n \geq 0 \quad (\text{terminating } B \text{ with } a)$$

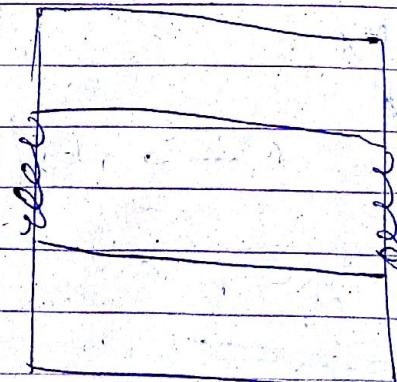
$$R.E. \Rightarrow a^* b^* a + b^* a$$



26.

$$S \xrightarrow{*} Aaa\bar{A}$$

$$A \xrightarrow{*} aA | bA | \epsilon$$



27.

$$S \xrightarrow{*} asa | bsb | b | a$$

$$S \xrightarrow{*} asc | A$$

$$A \xrightarrow{*} aAb | \epsilon$$

29. Assuming 'OR' is 'AND':

$$S \rightarrow a A b | b D B$$

$$A \rightarrow a A b | \epsilon$$

$$C \rightarrow C c | \epsilon$$

$$\begin{array}{l} D \rightarrow a D | \epsilon \\ B \rightarrow b B c | \epsilon \\ E \rightarrow c E | \epsilon \end{array}$$

~~$$B \rightarrow b B c | D B E | \epsilon$$~~

~~$$D \rightarrow a D | b B c$$~~

~~$$E \rightarrow c E | \epsilon$$~~

30.

$$S \rightarrow A a A$$

$$A \rightarrow a A | b A | \epsilon$$

$$S \rightarrow A a A a A$$

$$\rightarrow \textcircled{1} a \textcircled{2} a \textcircled{3} a \textcircled{4} a \textcircled{5} a \textcircled{6} a \textcircled{7} a \textcircled{8} a, b$$

$$\begin{array}{l} q_0 \xrightarrow{a} q_1 \xrightarrow{b} q_2 \xrightarrow{a} q_3 \\ q_0 \xrightarrow{b} q_1 \end{array}$$

31.

~~$$S \rightarrow A a A b A a A | A a A a A b A | A b A a A a A$$~~

~~$$A \rightarrow S | \epsilon$$~~

simplified :

~~$$S \rightarrow s a s b s a s | s a s a s b s | s b s a s a s | \epsilon$$~~

~~$$S \rightarrow a s b s a | a s a s b | b s a s a | s s | \epsilon$$~~

~~2b0q990~~

~~a<sup>n</sup>b<sup>m</sup>c<sup>n</sup>~~

~~$$S \rightarrow a b a | a a b$$~~

~~$$a^m b^n c^n$$~~

~~S → a<sup>n</sup>b<sup>m</sup>c<sup>n</sup>~~

~~$$a^m b^n c^n$$~~