

## *Process simulation*

### *Front End of Line Process Models*

*Ion Implantation, Diffusion*

*Epitaxy, Oxidation,*



## *Device simulation*

## *Equipment simulation*

### *Equipment Modeling, Transport Simulation*

*PVD (Monte Carlo, MD (\*))*

*Feature scale, Topography (line of sight))*

*Lithography*

*CMP*

*CVD (\*)*

*ECD*

*Etching (\*)*

*ALD*



CVD Chemical Vapour Deposition / Epitaxy

ALD Atomic Layer Deposition

**PVD Physical Vapour Deposition**

ECD Electro Chemical Deposition

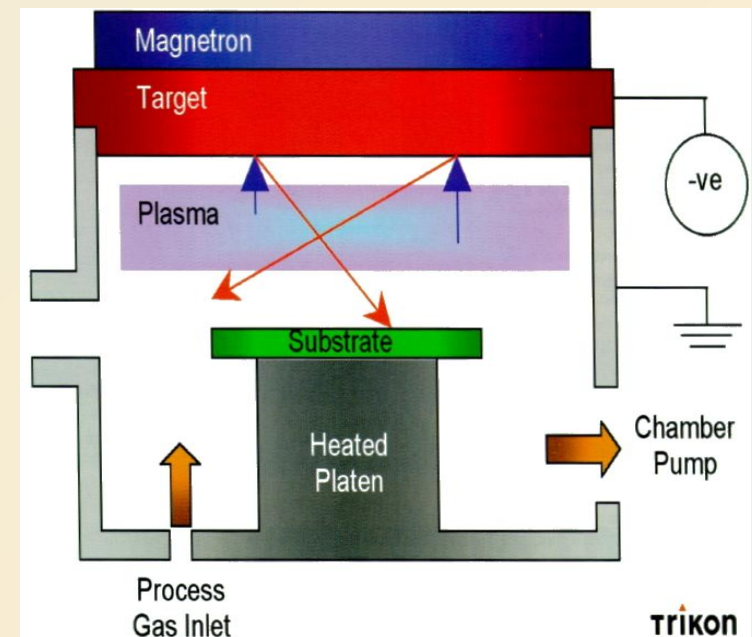
MBE Molecular beam epitaxy

spin on

...Modeling and Simulation

Transport Simulation

1. Particles to wafer



# Sputtering Process

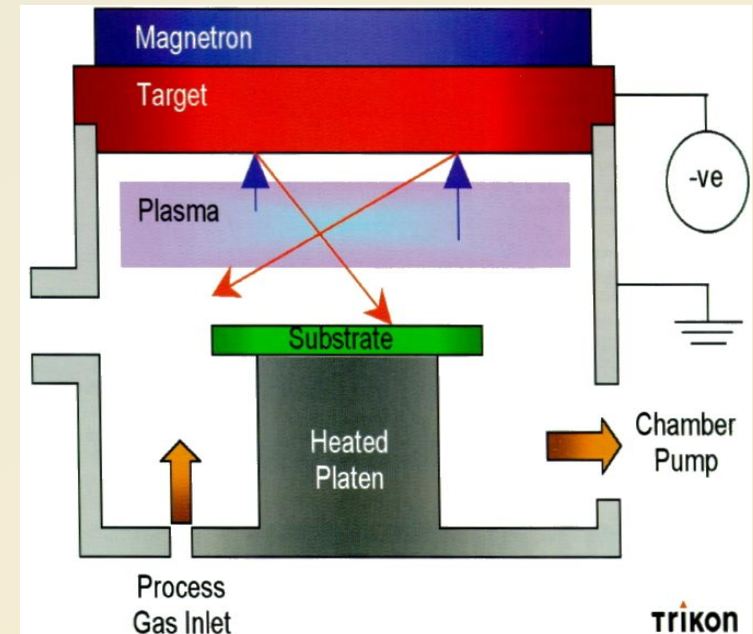
## Principle:

The target consists of the material, which should be deposited on the wafer.

- Area of ionization will not be separated from the area of deposition !
- The pressure will be defined by the plasma.
- Ballistic transport of the target atoms to the wafer (few collisions on the way to the substrate)
- Main field of application today in the microelectronic technology and technology of MEMS

reason: productivity and purity of the targets

e.g.: 99.9995 % **[5N5]**

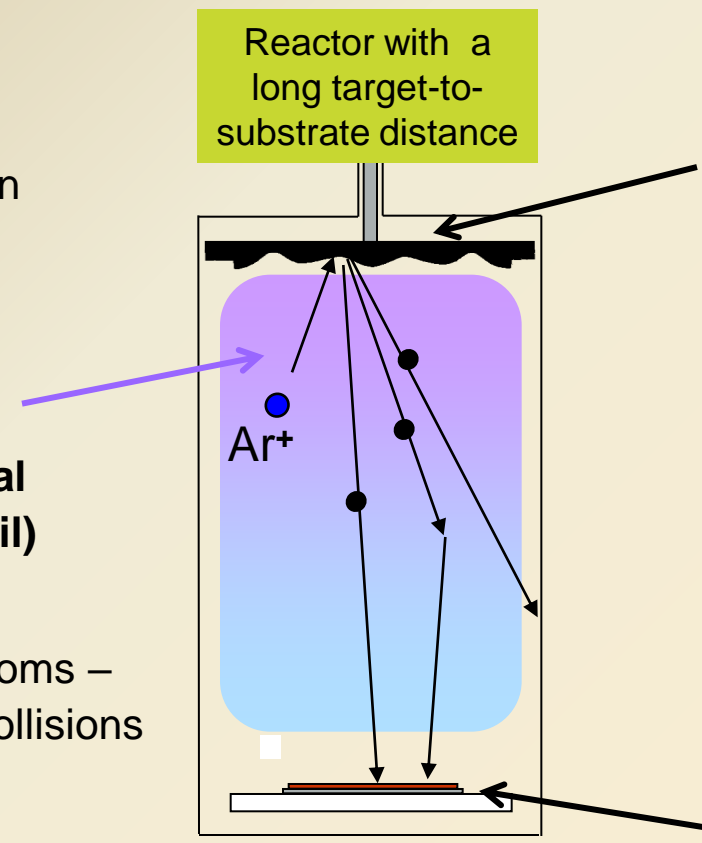


## ■ ...Modeling and Simulation

Transport Simulation on different length scales

- Reactor - Monte Carlo Transport Simulation
- Feature - Monte Carlo Surface Kinematics Simulation
- Surface - Molecular Dynamics Approach





Transport in the argon plasma (scattering simulation)

**IPVD: with additional ionization (e.g. a coil) → more metal ions**

Transport of metal atoms – low pressure – few collisions

**Monte Carlo Transport and Scattering**

Metal target, negative voltage (~ 500 V)

Sputtering of metal atoms by Ar<sup>+</sup> bombardment

Angular and energy distributions of sputtered metal atoms

**Molecular Dynamics**

Deposition of metal atoms on the substrate in the feature (topography simulation)

**PVD**

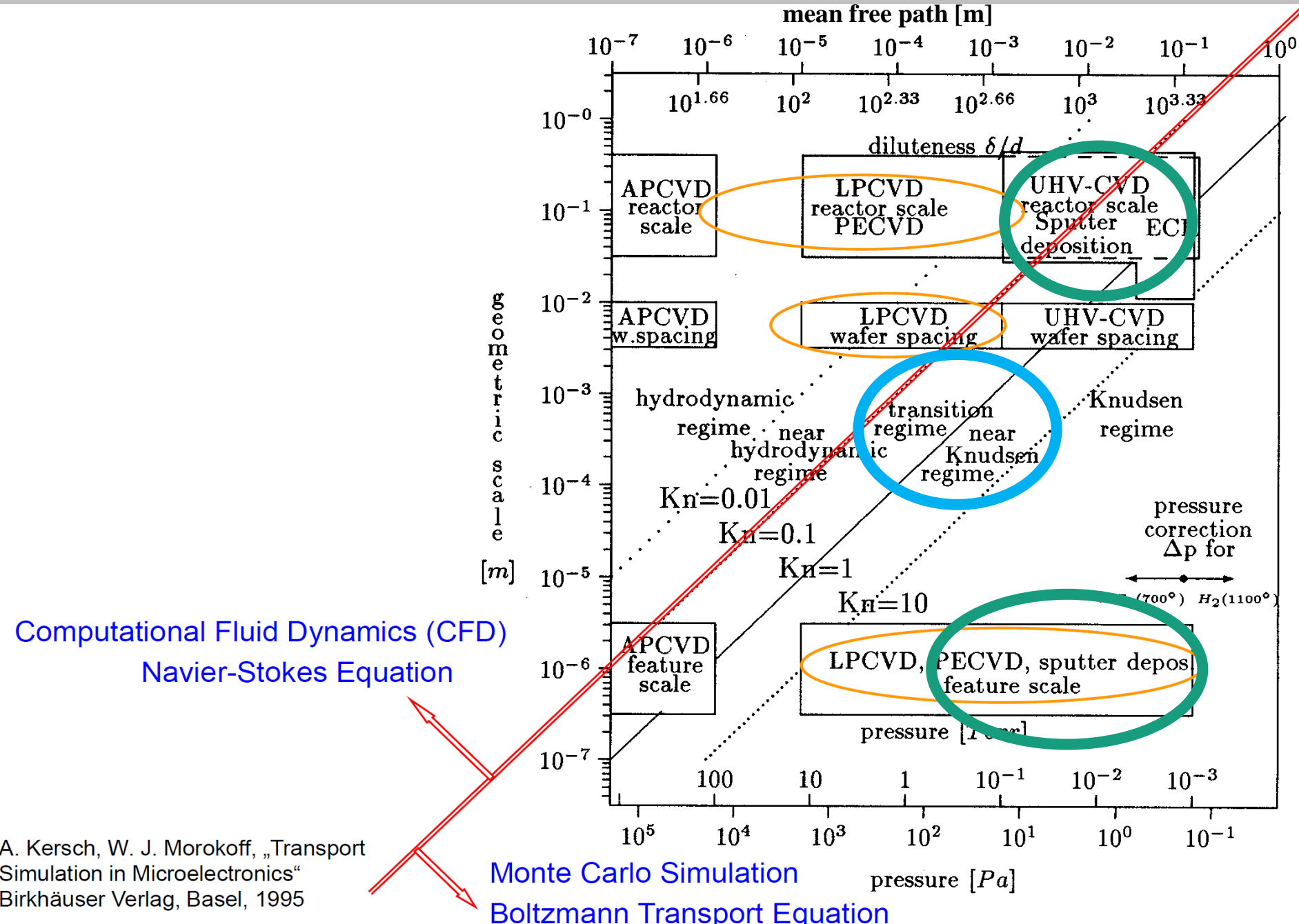
Each atom that has reached the substrate is adsorbed (sticking coefficient 100%)

**IPVD**

IPVD: Negative voltage on the substrate (~ 100 V)  
Increase of the normal component of velocity for charged particles: not 100% absorption, also reflection, and sputtering of film particles

→ Molecular Dynamics Calculation

# Transport Simulation in Relation to geometric Scale



A. Kersch, W. J. Morokoff, „Transport Simulation in Microelectronics“  
Birkhäuser Verlag, Basel, 1995

## Mathematical methods:

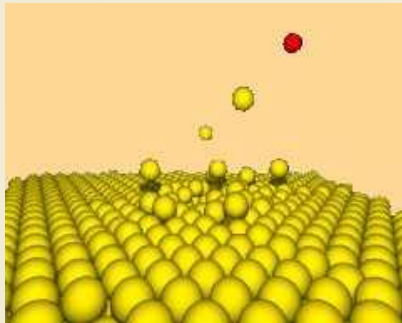
*numerical treatment of differential equations describing particle flow*

- simulation of continuum flow

**condition: Knudsen number  $Kn \ll 1$**

## Molecular-Dynamics (MD)

The MD-method emulates trajectories of particles and collision interactions accordingly given interaction potentials (particularly solids, liquids)



## Physical methods:

***Simulation of particle flow by tracking of particle trajectories and interactions of the particles among themselves and with interfaces***

***Each simulated particle represents a huge number of physical particles***

## Direct simulation Monte Carlo (DSMC)


No exact emulation of particle trajectories and interactions

Particle movement and interaction independent

Collisions not exact, but random

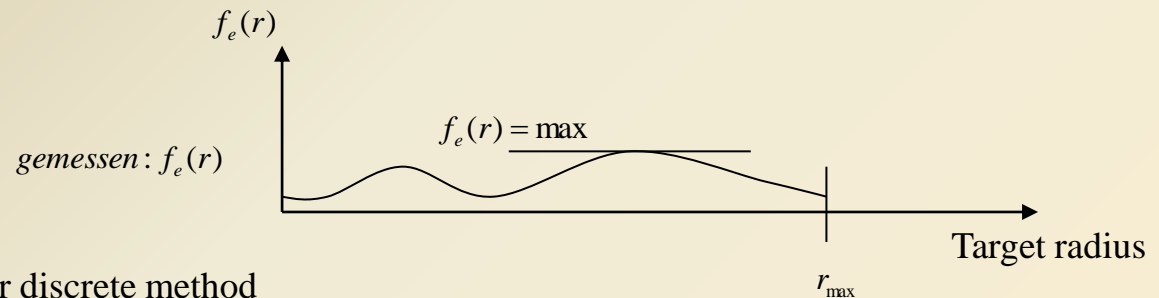


Calculation of  
energy distribution  
angular distribution  
of particles impinge at wafer surface

- 
1. Start particle at target (Modelling of target emission)
  2. Modelling of particle flight through from target to wafer taking collisions into consideration
  3. Store particle properties at wafer (position, species, energy, angle)
  4. Repeat (10 000 000 and more)



## 1. Emission position



e. g. acceptance-rejection or discrete method

## 1. Emission angle (polar, azimuthal)

$$f_{\text{polar}}(\Theta) = \sin(\Theta) \cos(\Theta)$$

Or measured distribution (Jones))

$$f_{\text{azimuthal}}(\varphi) = 2R\pi$$

## 2. Emission energy (Thompson)

$$f_{\text{Tho}}(E) = E \left( 1 - \frac{\sqrt{\frac{E_b - E}{\lambda E_i}}}{\left( \frac{E_b - E}{eV} \right)^3} \right)$$

$$\lambda = \frac{4m_i m_t}{(m_i + m_t)^2}$$

max. energy transfer

$E_b$  Surface binding energie

$E_i$  Av. kinetic ion energy

$mfp$  Mean free path

## 3. Mean free path

$$x = -mfp \ln(R)$$

If new collision position  
outside reaktor then goto **6.**

## 4. Collision

$$S = 0$$

for( $i = 0; i < \text{numberOfSpecies}; i++$ ) {

$S = S + \text{mole\_fraction}_i$

if ( $S > R$ ) break; //  $i$  is index of collision partner

}

## 5. Energy of collision partner

$$t = \sqrt{-2 \ln(R/2)}$$

(Maxwell distribution)

$$v = \sqrt{kT/m} \left( t - \frac{c_0 + c_1 t + c_1 t^2}{1 + d_1 t + d_2 t^2 + c_3 t^3} \right)$$

c, d empirical coefficients

## 5. Calculation of collision (model dependent)

result:            new direction  
                     new energy of collision partners  
                     dependent on collision parameters, particle mass, energies

...goto 3.

## 6. Calculation of surface interaction

rsc = 1 ... save particle (position, direction, energy)

or MD based calculation of adsorption/sputtering/reflexion probability  $f_{ads}$ ,  $f_{reflex}$ ,  $f_{sputt}$

$$f_{ads} + f_{reflex} + f_{sputt} = 1$$

if ( $f_{ads} > R$ ): Adsorption

if ( $f_{reflex} > R$ ): Reflexion

else Sputtering



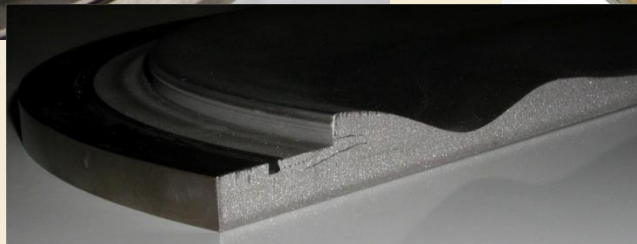
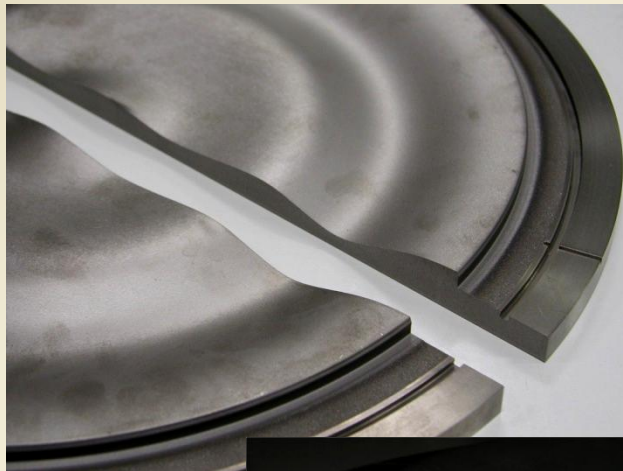
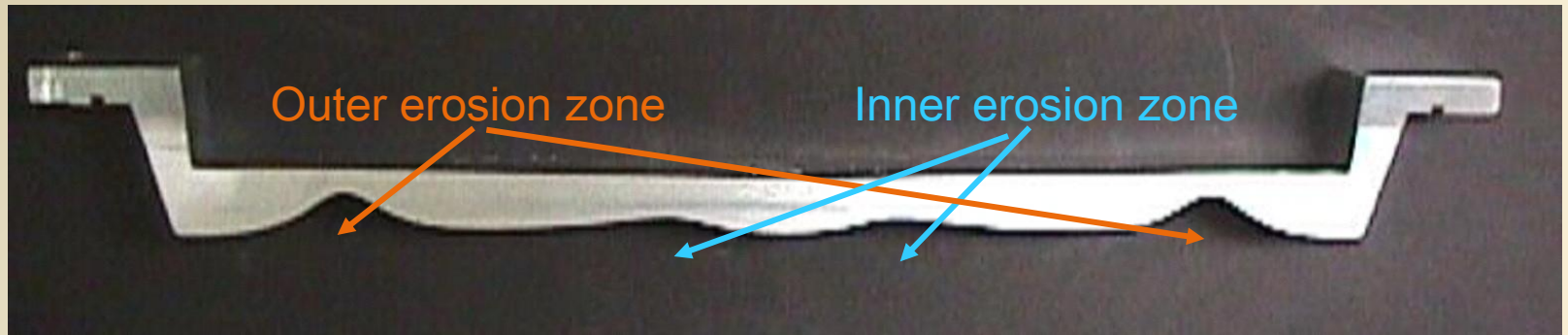
Sputtering rate, emission angle, energy of sputtered particles

rsc: reactive sticking coefficient

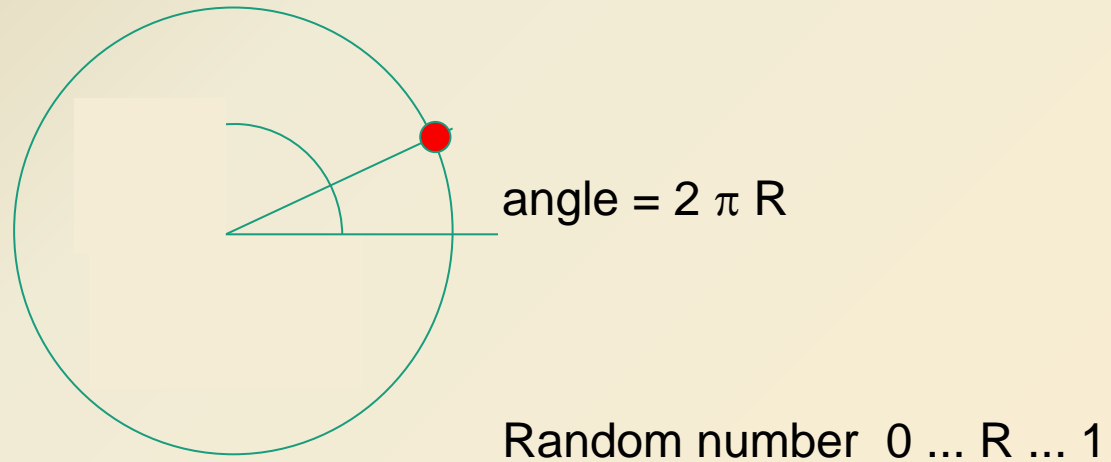
feature scale simulation

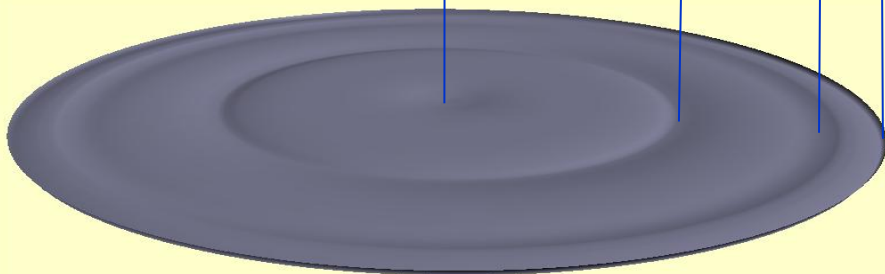
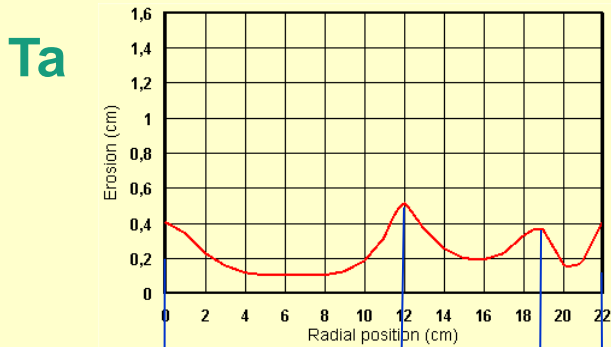
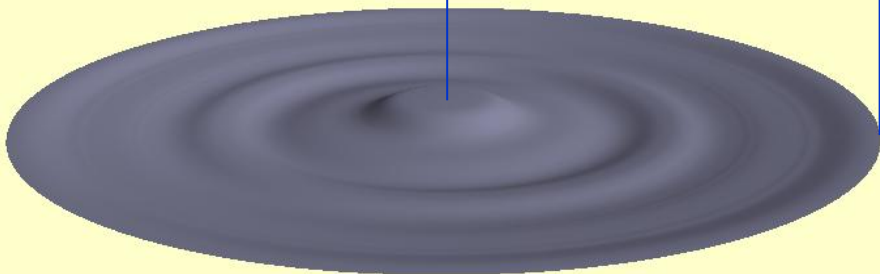
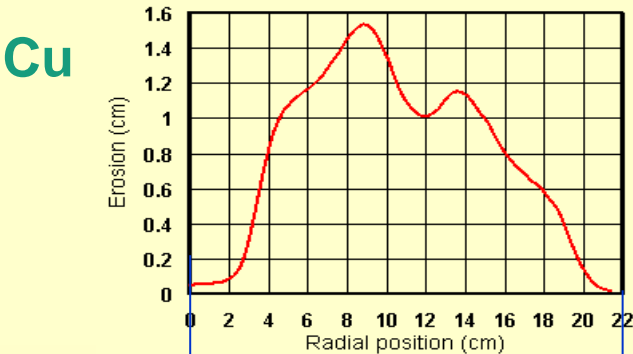
rsc ... reactive sticking coefficient

## Erosion trench on a magnetron target



**Target, diameter approx. 400 mm**





# Random Numbers, by Acceptance-Rejection Method

Random number, distributed with probability density  $f(x) = dW/dx$  by the acceptance-rejection method

## Step 1. Normalization

$$f_n(x) = \frac{f(x)}{f_{\max}}$$

## Step 2. R1

choose R1, uniformly distributed random numbers in interval  $(x_u, x_o)$

$$R1 = R * (x_o - x_u) + x_u, \quad 0 < R < 1$$

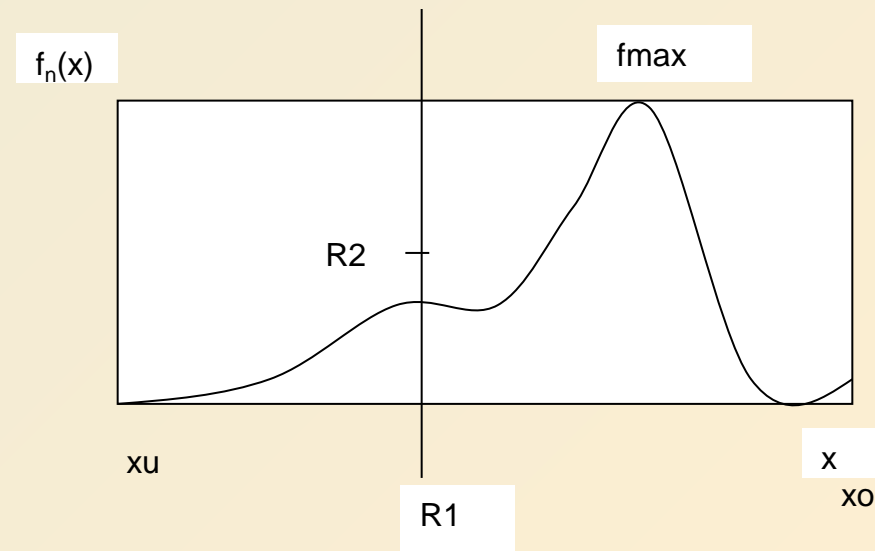
## Step 3. choose R2 = R \* fmax,

R1 is then randomly distributed if

$$R_2 < f_n(R_1)$$

(acceptance)

else rejection of R1, R2



# RN from Discrete Given or Numerically Integrable Probability Distribution

Given:  $f(x)$  as vector  $f[i]$  at  $x[i]$ ,  $i = 0 \dots n-1$

**Step 1.** Determination of the discrete probability mass function  $F[j]$  at  $x[i]$

$$f[j] = N \sum_{i=0}^j \frac{f(x[i+1]) + f(x[i])}{2} (x[i+1] - x[i])$$

**Step 2.** Normalization, e. g. trapezoidal rule

$$N = \frac{1}{\sum_{i=0}^{j-2} \frac{f(x[i+1]) + f(x[i])}{2} (x[i+1] - x[i])}$$

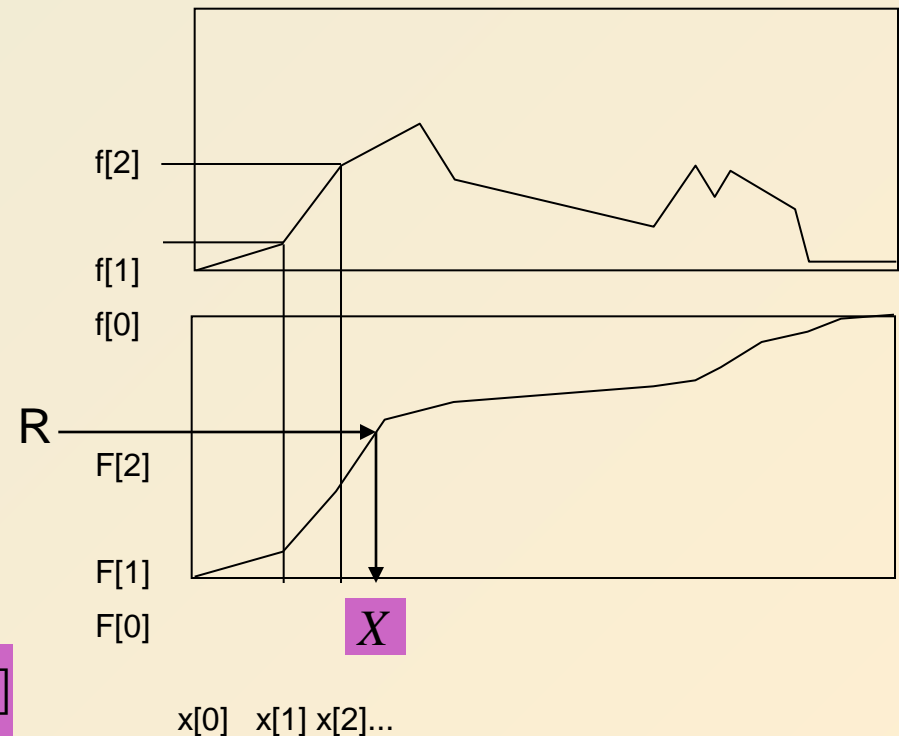
**Step 3.** Determination of R

Determination of interval

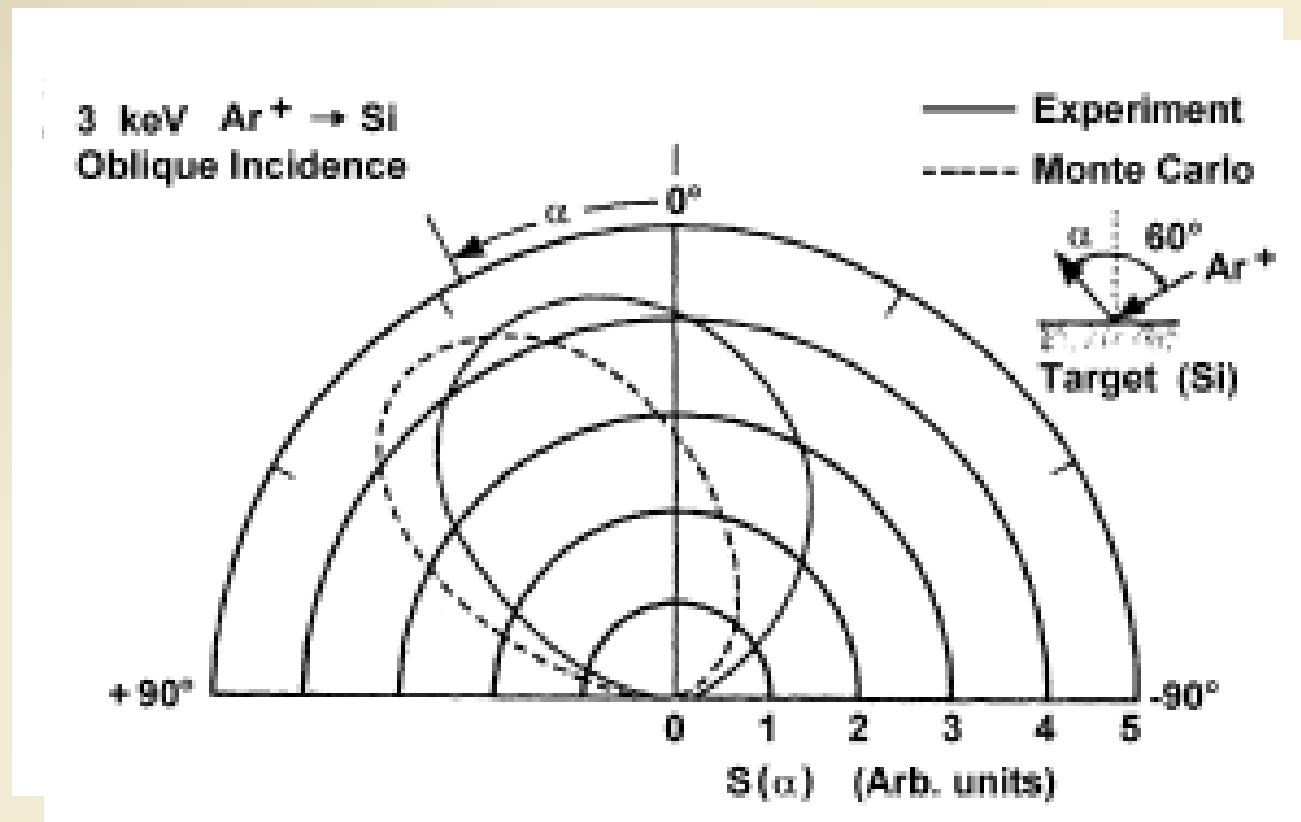
$$F[i] < R < F[i+1]$$

Interpolation

$$X = \frac{x[i+1] - x[i]}{F[i+1] - F[i]} (R - F[i]) + x[i]$$







Angular distributions of sputtered Si atoms for 3 keV,  $\text{Ar}^+$  ion bombardment at an incident angle of  $60^\circ$

## Example: Particle Emission from Target with Cosine Distribution

Angular dependence of the probability density of emission  $f(\varphi, \Theta)$

$$f(\varphi, \Theta) \propto \sin(\varphi) \cos(\varphi) \quad \sin(\varphi) \cos(\varphi) = 1/2 \sin(2x)$$

Step 1. Probability mass function

$$F(z) = N \int_0^z f(\varphi) d\varphi$$

Step 2. Normalization

$$F(z) = 1 = N \int_0^{\pi/2} f(\varphi) d\varphi \quad N = \frac{1}{\int_0^{\pi/2} \sin(\varphi) \cos(\varphi) d\varphi}$$

Step 3. Integration

$$R = F(z) = N \int_0^z \sin(\varphi) \cos(\varphi) d\varphi$$

$$R = F(z) = \left[ N \frac{1}{2} \sin^2(\varphi) \right]_0^z = N \frac{1}{2} \sin^2(z) = \frac{1}{\frac{1}{2} \sin^2(\pi/2)} \frac{1}{2} \sin^2(z)$$

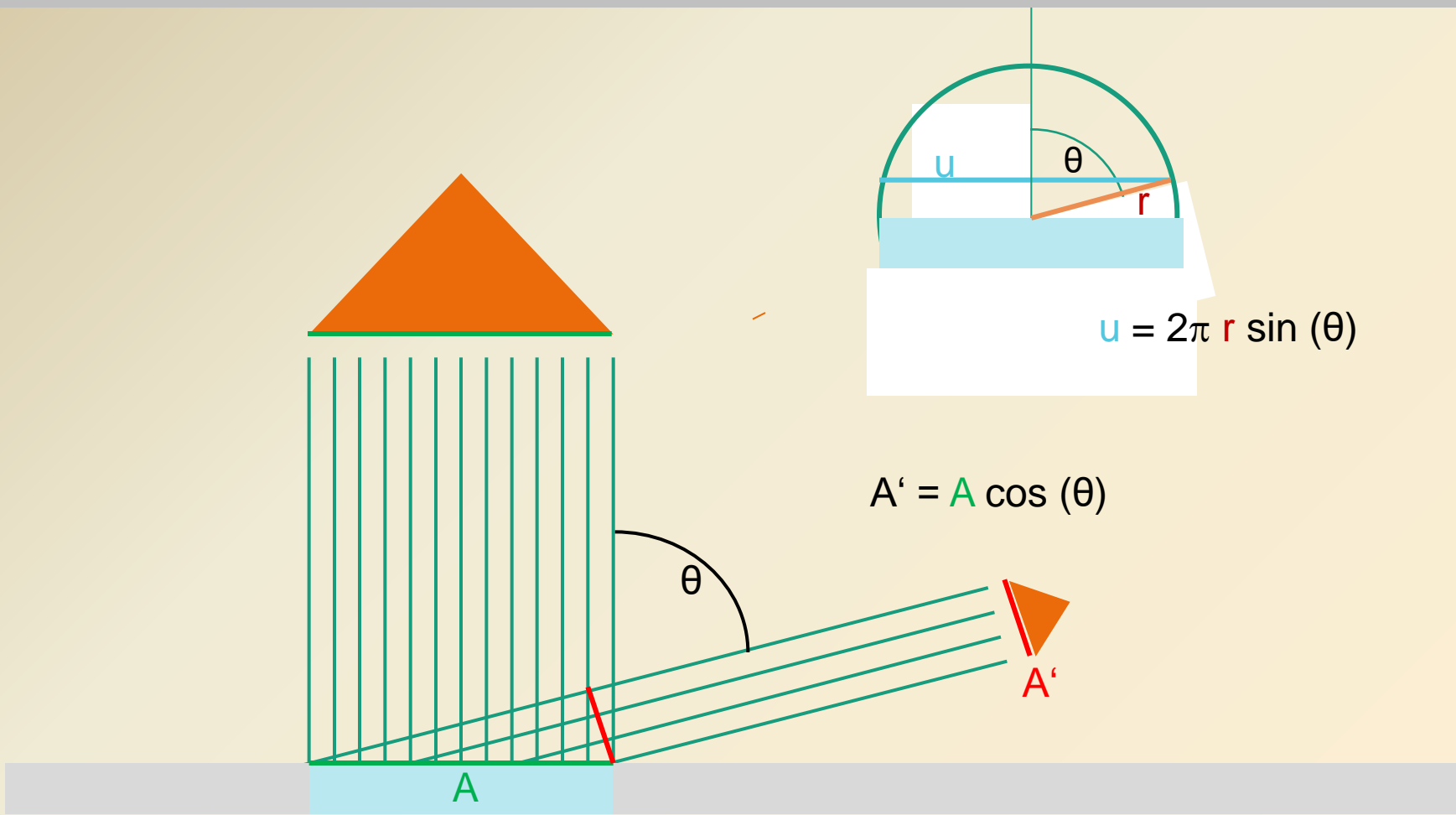
Step 4. Inverse

$$z = \arcsin(\sqrt{R})$$

$$R = \sin^2(z)$$



Example: Particle Emission from Target with Cosine Distribution

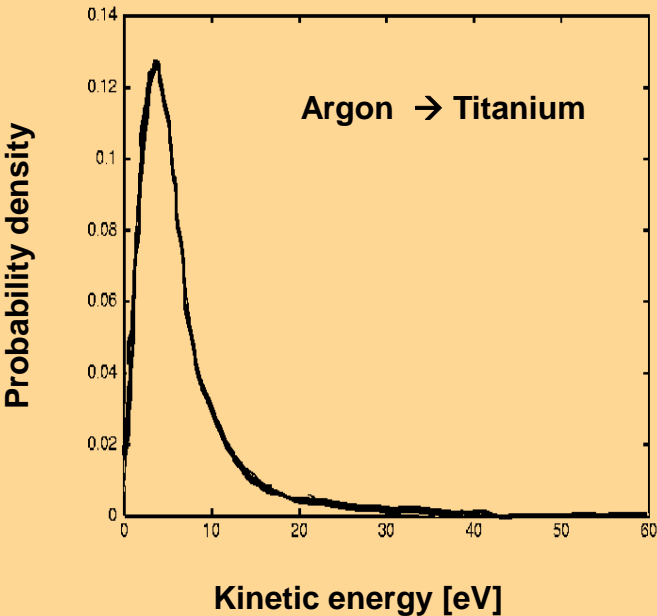


$E \propto u A' \propto \sin (\theta) \cos (\theta)$

Goal: Calculation of angular and energy distributions of sputtered metal atoms



A typical energy distribution of sputtered particles:



95% sputtered atoms:  $E_{\text{kin}} < 25 \text{ eV}$

despite of the fact that projectile energy is about 500 V

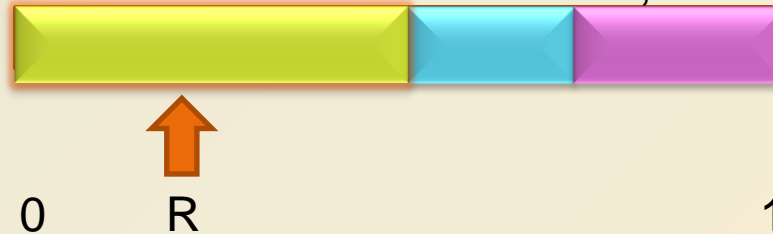
## 4. Collision

mole fraction

Species A 0,5

Species B 0,2

Species C 0,3



$S = 0$

*for*( $i = 0; i < numberOfSpecies; i++$ ){

$S = S + mole\_fraction_i$

*if* ( $S > R$ )*break*; //  $i$  is index of collision partner

}

# Simulation package T2

# PVD Module

## Plasma

Ionization cross sections  
Electron temperature

Simple Plasma Model

Electron density  
Ion fluxes

Bias  
(dc, rf)

Sheath Model

Angular and energy  
distribution of ions /  
particle ensemble

Radial film thickness profile  
Radial energy distribution

## Particle-surface interaction

TaN

Particle energy  
Impact direction  
Target composition

BCA Simulation Tools  
(SRIM, Tridyn-FZR)

Cu,Ta,Ti

Particle energy  
Impact direction  
T. crystal structure

MD Simulation Tool  
(Kalypso)

Tabulated results

Sputtering yields  
Adsorption probabilities  
Reflection probabilities

offline

Substrate  
topography

## Transport

Reactor & process characteristics  
Target erosion profile  
Sputtered material characteristics

Target Emission Model

MC based  
Equipment Simulation Tool

Angular and energy  
distribution of atoms /  
particle ensemble

MC based  
Topography Simulation Tool

Deposited film properties:  
Topography  
Energy deposition  
Composition

## Results

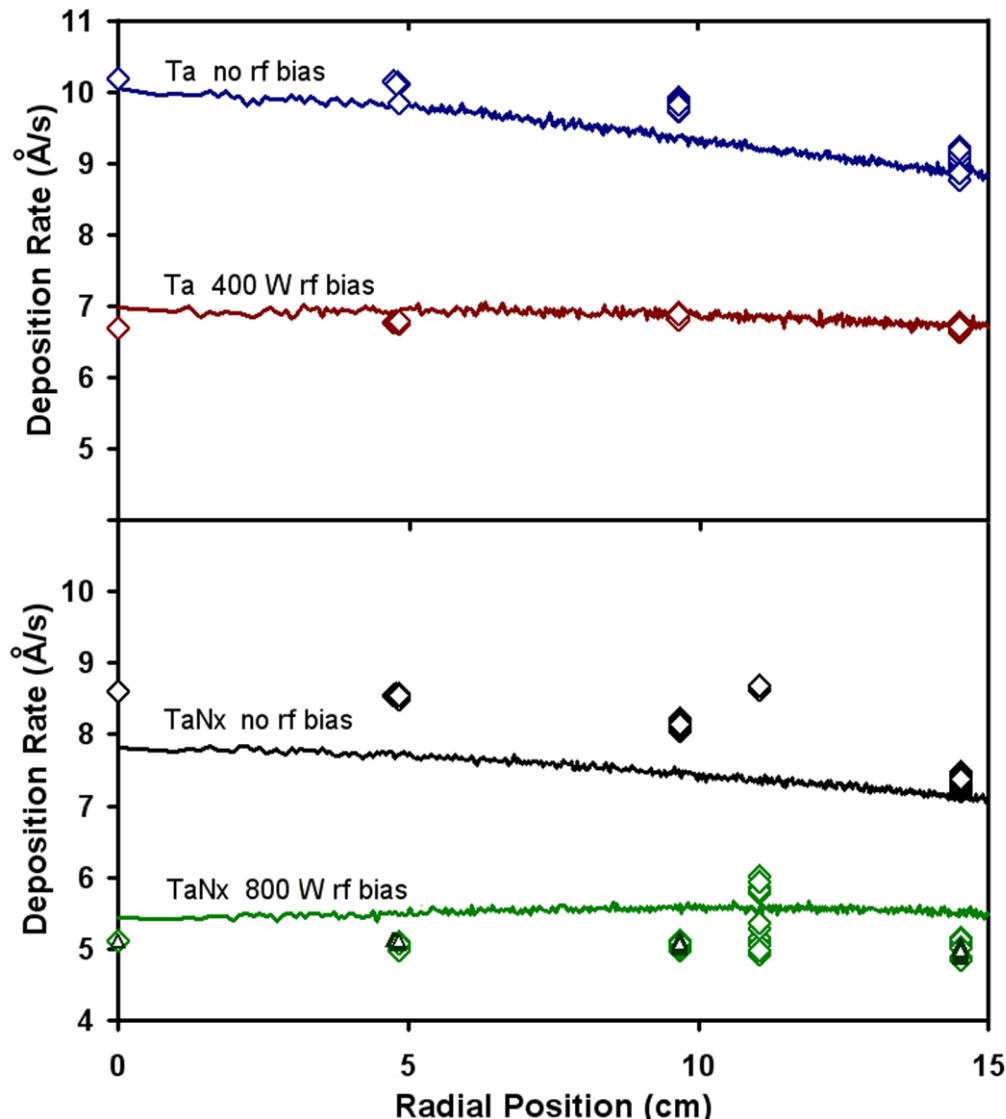
Transport Simulation on different length scales

- Reactor scale - Monte Carlo Transport Simulation
- Feature - Monte Carlo Surface Kinematics Simulation
- Surface - Molecular Dynamics Approach





# Radial dependence of deposition rates




Radial dependence of simulated (lines) and measured (symbols) deposition rates for the deposition of Ta (upper frame) and TaN<sub>x</sub> (lower frame) without and with rf bias applied to the wafer. Diamonds denote experimental deposition rates determined from thickness measurements by x-ray reflectometry and triangles designate deposition rates derived from measurements of the sheet resistance. The deposition rates at 11 cm are wafer-averaged values from different tools. The observed offset is presumably due to different target properties (age).

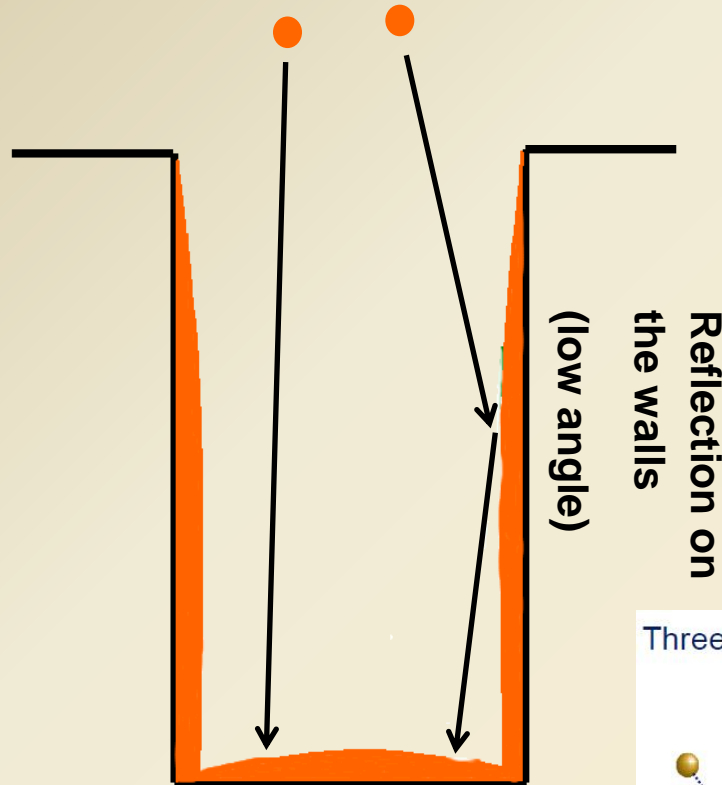
Calculation of

film growth

based on particle ensemble from  
reactor scale simulation

- 
1. Start particle at wafer surface from collection
  2. Modelling of particle flight near or in the feature (lattice based transport)
  3. Modelling surface interaction (reflection, sputtering, sticking)
  4. Repeat (10 000 000 and more)

## IPVD situation



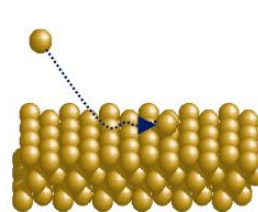
On the bottom  
mainly: Adsorption

Also some sputtering

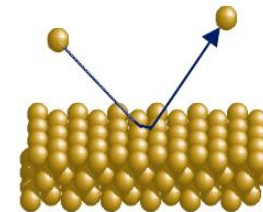
With **Molecular Dynamics** we determine:

- probabilities of adsorption, reflection, and sputtering
- reflection or sputtering: the energy and angular distributions of reflected / sputtered atoms and the quantity of sputtered atoms

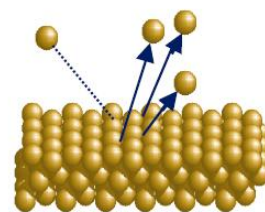
Three major types of surface reactions:



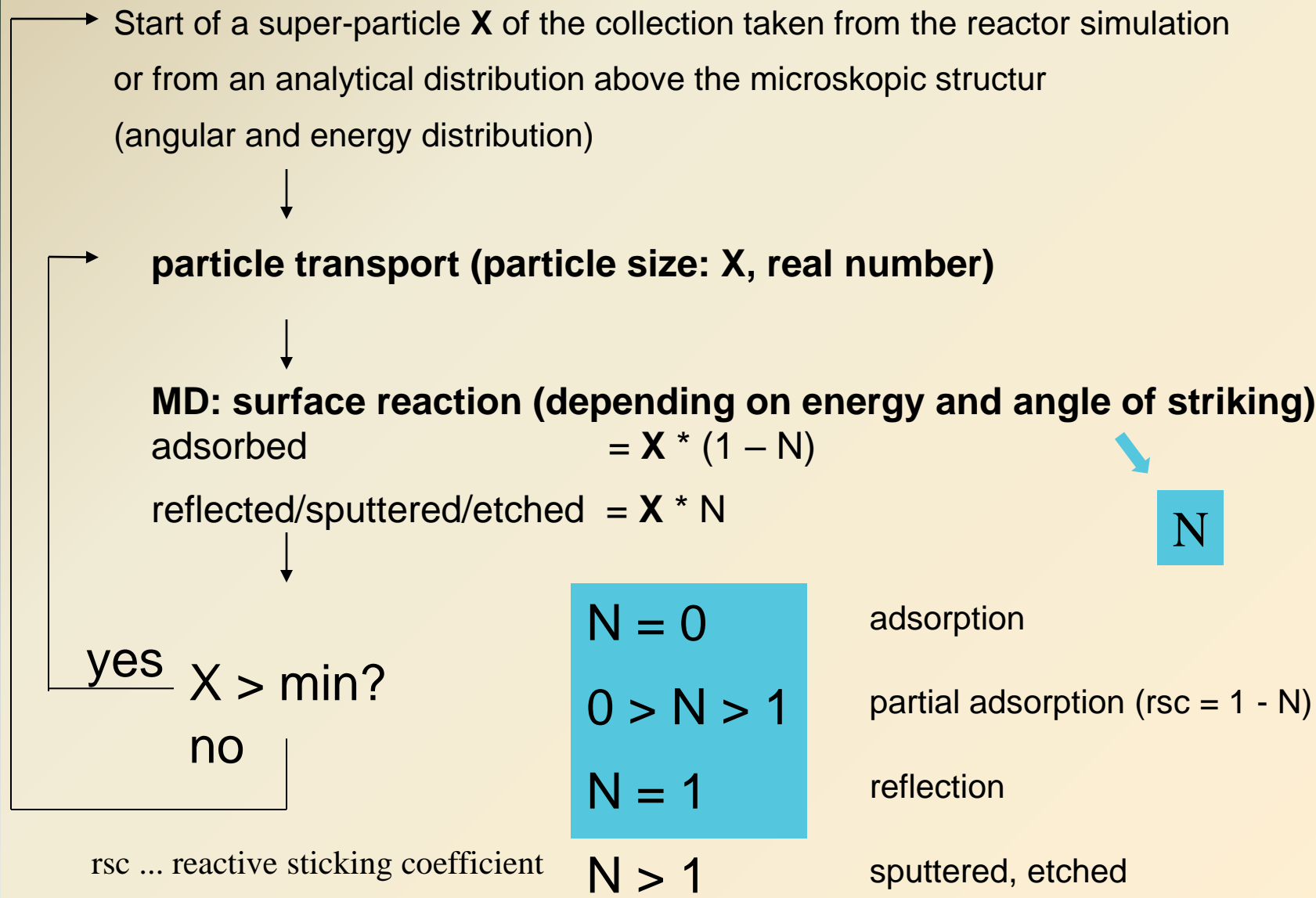
adsorption



reflection



etching / sputtering



## Molecular (classical) dynamics

Quantum mechanics  
(Schrödinger equation)

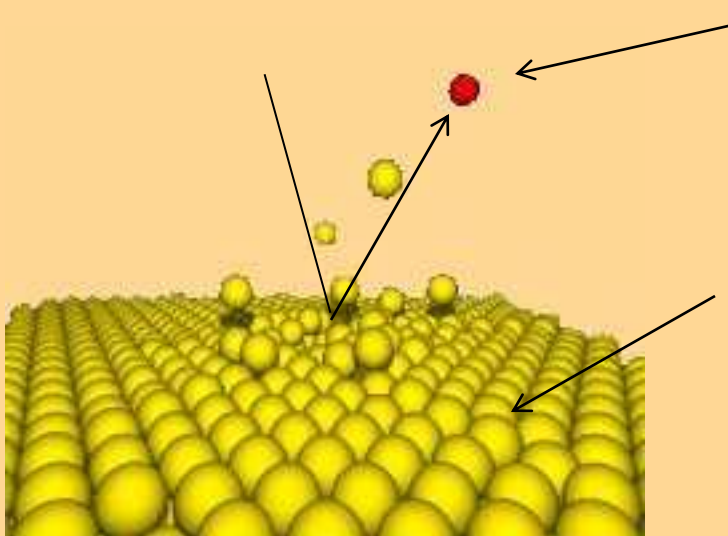
- no need for parameters  
(solution from first principles)



Classical approximation  
(Newton equations)

- a semiempirical classical  
interaction model is needed

Simulation of sputtering and deposition:



Projectile: an Ar or metal ion

- sputtering:  $E_{\text{kin}} \sim 200 \text{ eV} - \text{keV}$
- deposition:  $0 - 150 \text{ eV}$

Target: a metal crystal

- the size depends on  $E_{\text{kin}}$  of projectile
- for  $E_{\text{kin}} \sim 500 \text{ eV}$ :  $\sim 10\,000$  atoms,

# The interaction model

## Metal - metal:

$r \in (0, \approx 0.5 r_{NN})$ :

**Short range repulsive (pairwise) interaction**

screened Coulomb potential (ZBL)

$$E = \frac{1}{2} \sum_i \sum_{j \neq i} \frac{Z_\alpha Z_\beta e^2}{4\pi\epsilon_0 r_{ij}} \sum_{k=1}^4 c_k^{\alpha\beta} e^{-b_k^{\alpha\beta} r_{ij} / a^{\alpha\beta}}$$

$Z_{\alpha,\beta}$  - atomic no.  $c_k^{\alpha\beta}, b_k^{\alpha\beta}, a^{\alpha\beta}$  - params

$r \in (\approx 0.9 r_{NN}, r_{cut-off})$ :

**Attractive (many-body) interaction** (TB-SMA)

$E(123) \neq E(12) + E(13) + E(23)$

① ②  
③

$$E = \sum_i \left[ \sum_{j>i} A e^{-p x_{ij}} - \sqrt{\sum_{j \neq i} \xi^2 e^{-q x_{ij}}} \right]$$

$x_{ij} = \frac{r_{ij}}{r_0} - 1$   $A, \xi, p, q, r_0$  - parameters dependent on  $\alpha$  and  $\beta$

$r \in (\approx 0.5 r_{NN}, \approx 0.9 r_{NN})$ :

**A (pairwise) effective spline potential**

a connection between the repulsive potential and an effective attractive potential derived from the bulk environment

**Noble gas - metal: Short range repulsive potential only** (ZBL)

## MD code Kalypso

## The integration loop: Verlet algorithm

For each particle in the system:

$$\mathbf{r}_{n+1} = \mathbf{r}_n + \mathbf{v}_n \Delta t + 0.5 \mathbf{F}_n \Delta t^2 / m$$

$$\mathbf{v}_{n+1} = \mathbf{v}_n + 0.5(\mathbf{F}_{n+1} + \mathbf{F}_n) \Delta t / m$$

$m$  ... mass of the particle

$\mathbf{r}_n, \mathbf{v}_n$  ... position/velocity at time  $n\Delta t$

$\mathbf{F}_n$  ... force at time  $n\Delta t$   
 = negative gradient of the  
 interaction potential

$\Delta t$  ... time step ( $\sim 10^{-15}$  s)  
 - depends on  $E_{\text{kin}}$  and mass the  
 projectile  
 - can be set to vary during the  
 simulation (as the  $E_{\text{kin}}$  of particles is  
 decreasing)

## Program features

- default crystal structures and faces:

FCC (100, 110, 111)

BCC (100, 110) and so on

- processing the crystal

possibility to generate an arbitrary  
 crystal face

- impact zone (points)  
 relation to the primitive surface cell

- lattice vibrations (hot target)

- models for inelastic energy losses

- thermostating

- configurable output



## M.A. Karolewski

- **Kalypso: a software package for molecular dynamics simulation of atomic collisions at surfaces**
- A suite of graphically-oriented computer programs for molecular dynamics simulations of projectile collisions with metallic targets
- free-boundary or periodic targets
- many-body potentials
- a variety of inelastic loss models, able to carry out simulations of fluence-dependent processes

<https://sites.google.com/site/kalypsosimulation/Home/downloads>

[DEMO](#)

## **Results**

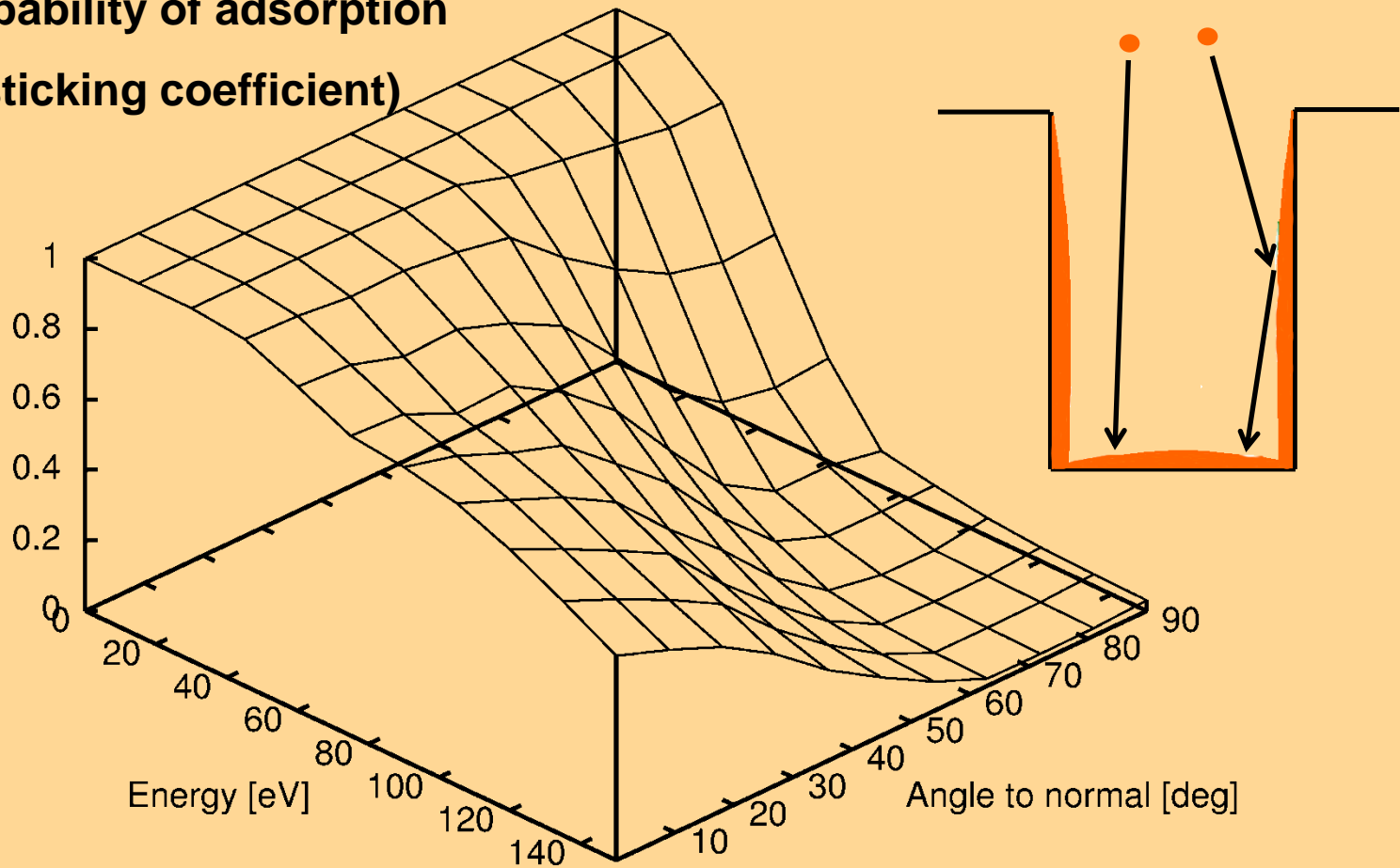
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IPVD Deposition:  $\text{Ti}^+$  (0-150eV)  $\longrightarrow$  bcc Ti(100)

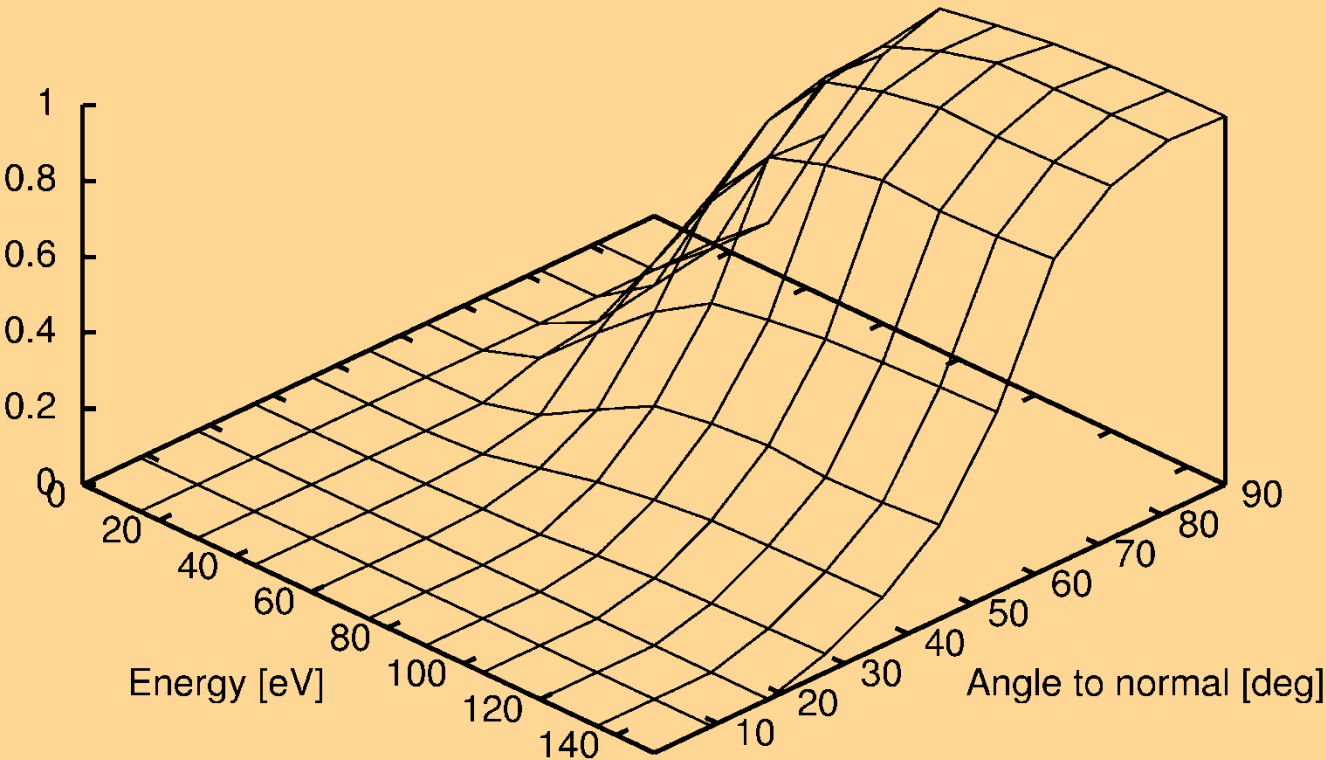
Probability of adsorption  
(sticking coefficient)



MD calculation by A. Kersch

IPVD Deposition:  $\text{Ti}^+$  (0-150eV)  $\longrightarrow$  bcc Ti(100)

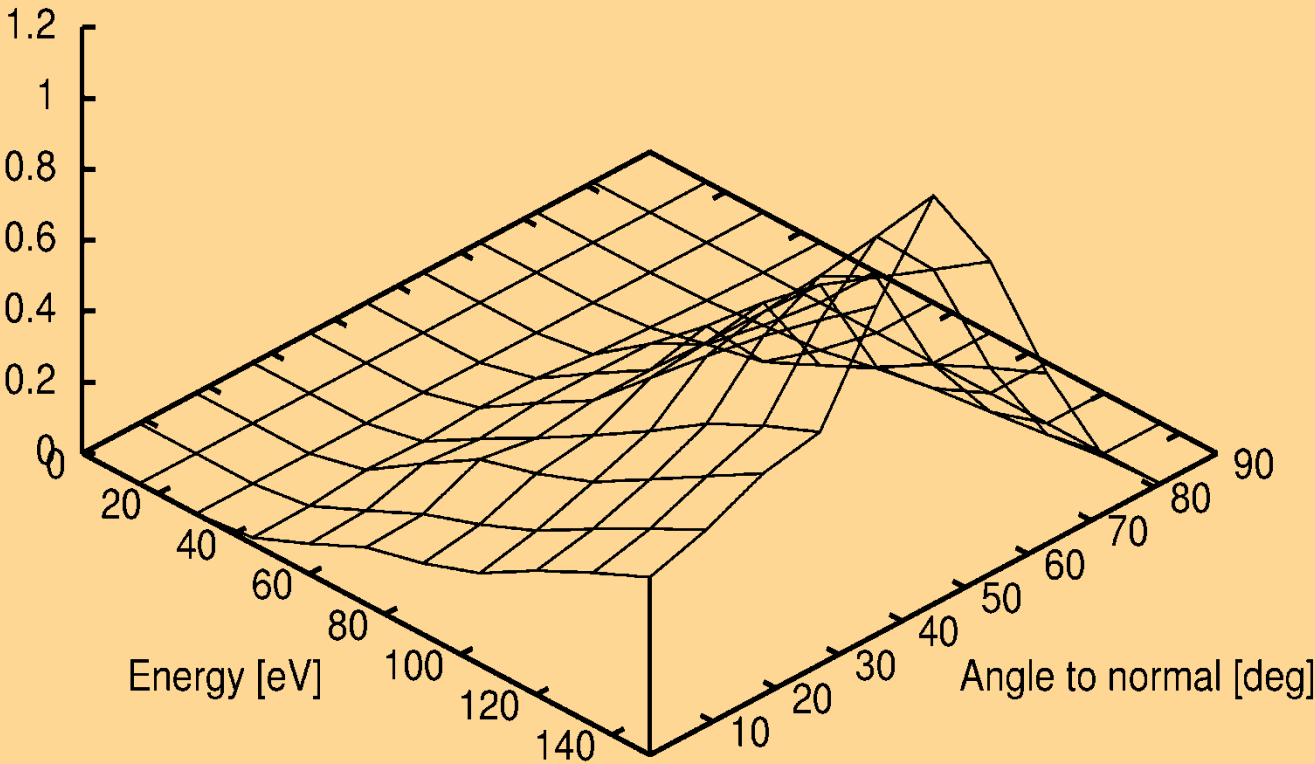
Probability of reflection



MD calculation by A. Kersch

IPVD Deposition:  $\text{Ti}^+$  (0-150eV)  $\longrightarrow$  bcc Ti(100)

Sputtering yield



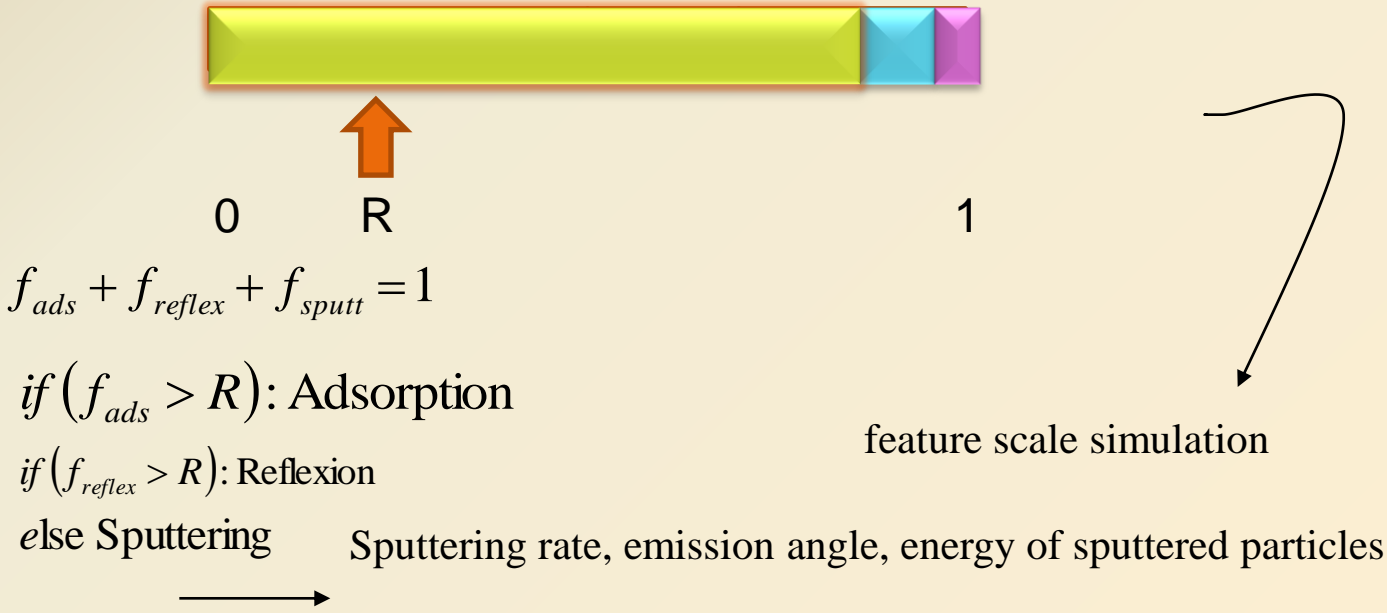
MD calculation by A. Kersch

6. Calculation of surface interaction

rsc = 1 ... save particle (position, direction, energy)  
or MD based calculation of adsorption/sputtering/reflexion probability

surface interaction

Adsorption	0,85 (rsc ... reactive sticking coefficient
Reflexion	0,1
Sputtering	0,05



## **Results**

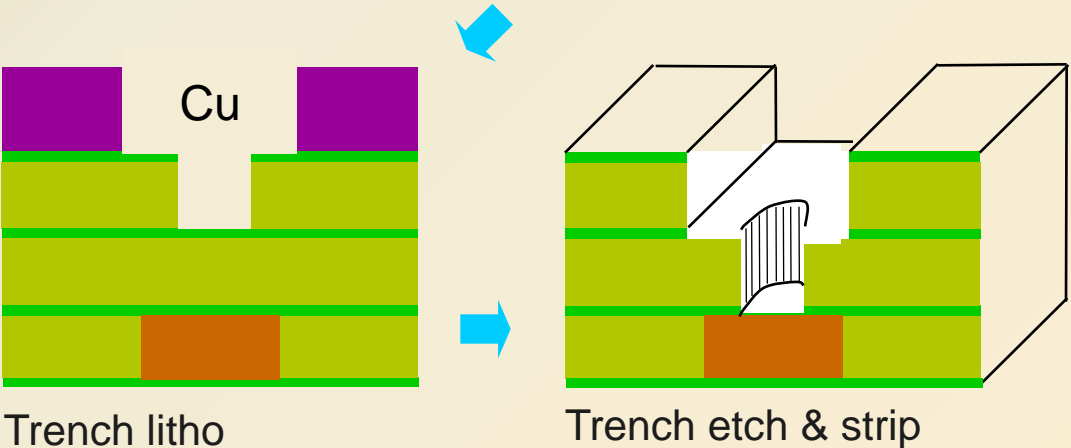
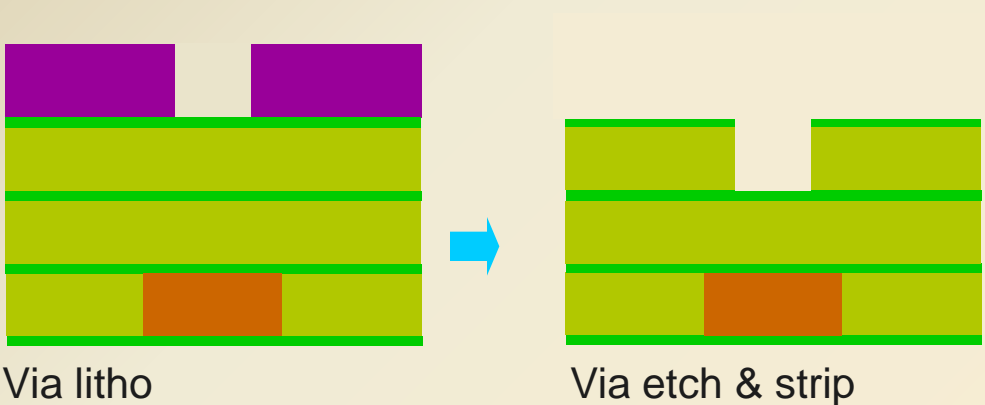
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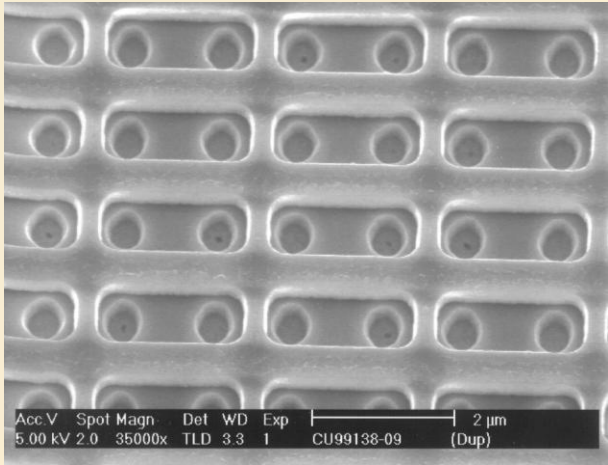




It uses two dielectric etch processes, one via etch and one trench etch  
Metal layers are deposited into via holes and trenches

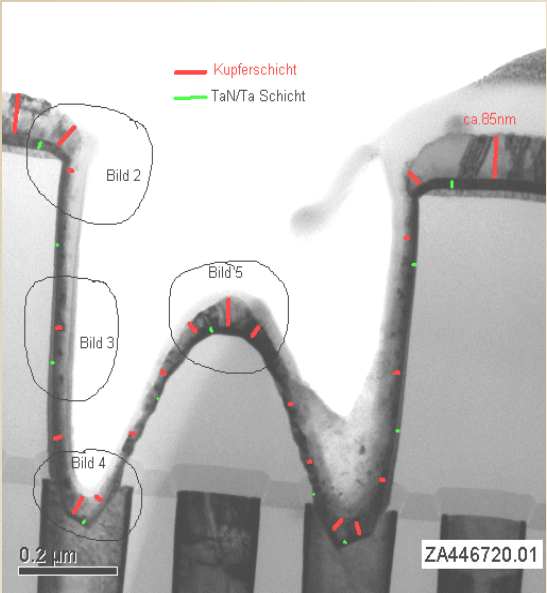


- Resist
- Si<sub>3</sub>N<sub>4</sub>, SiC
- SiO<sub>2</sub> or Low-k

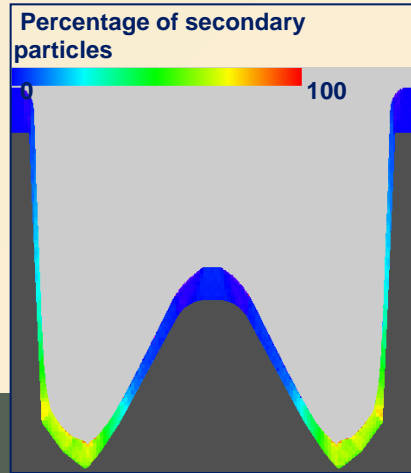
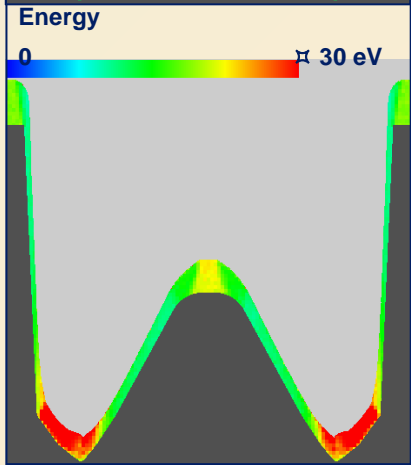
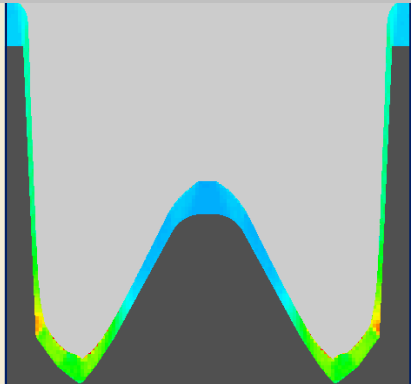
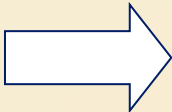
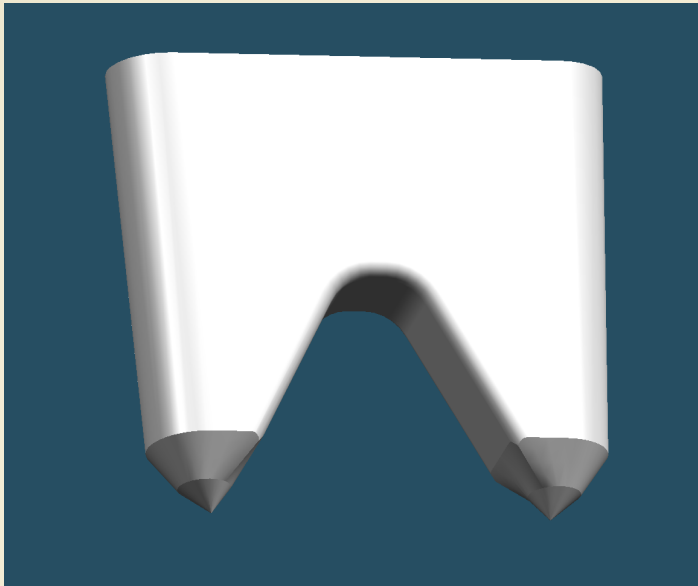


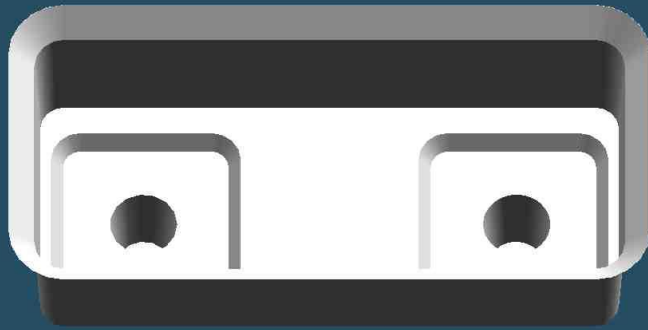
source: IMEC 2003

# Cu seed layer deposition in a minimum size dual damascene test structure

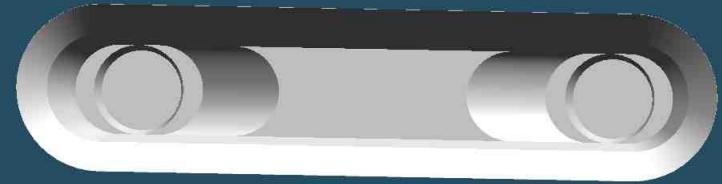


**PVD:**  
**Simulation of seed layer deposition**

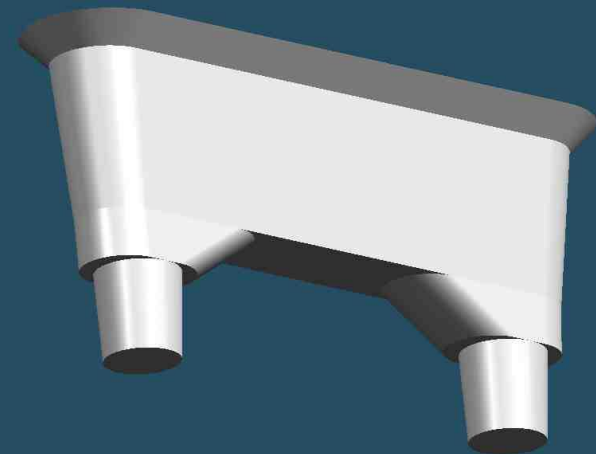
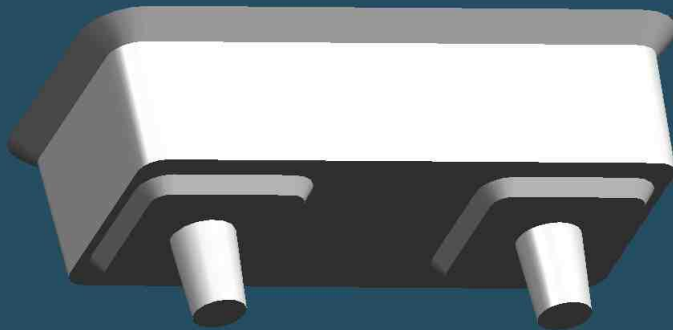




**V1 covered landed  
center**

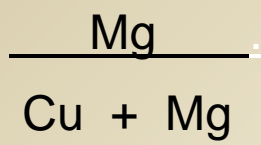


**V1 isolated  
center**

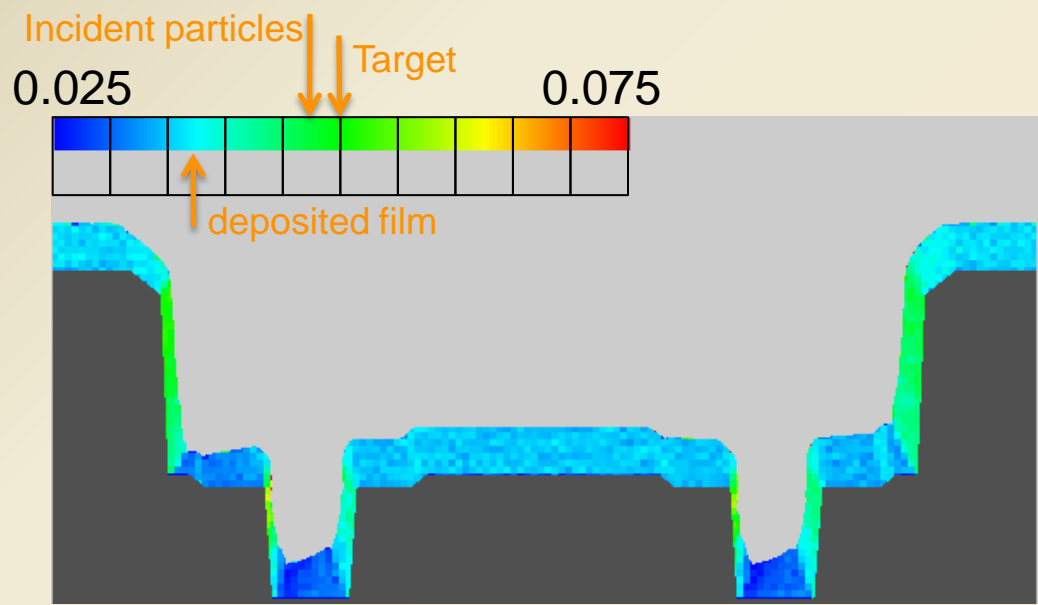


**PVD Feature Scale Simulation, Results, Self Forming Barriers**

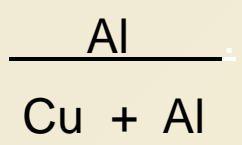
Composition



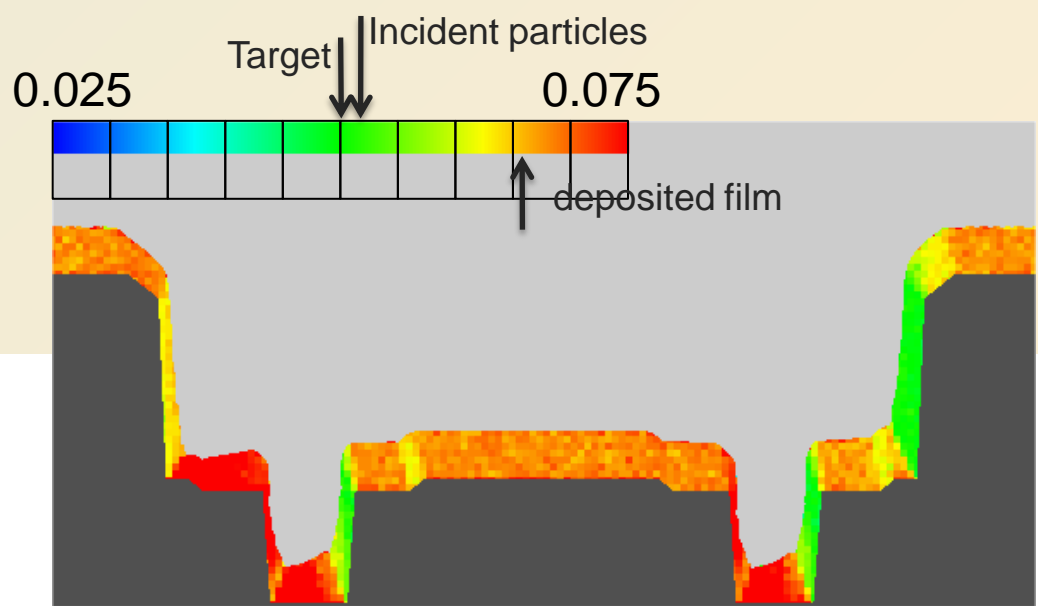
Target	0.0500
Incident parts	0.0468
Film (average)	0.0371



Cu95Mg05



Target	0.0500
Incident parts.	0.0519
Film (average)	0.0657



Cu95Al05

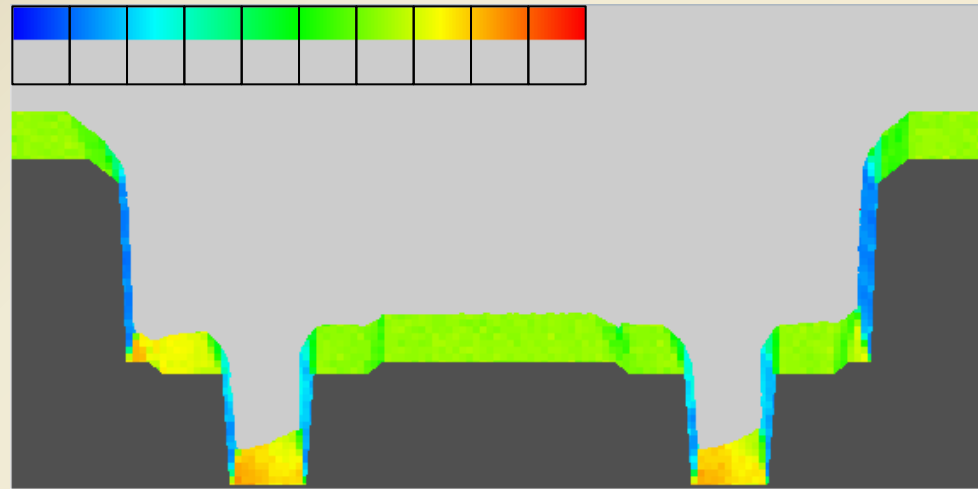
# PVD Feature Scale Simulation, Wafer edge

Energy

of incident particles

0

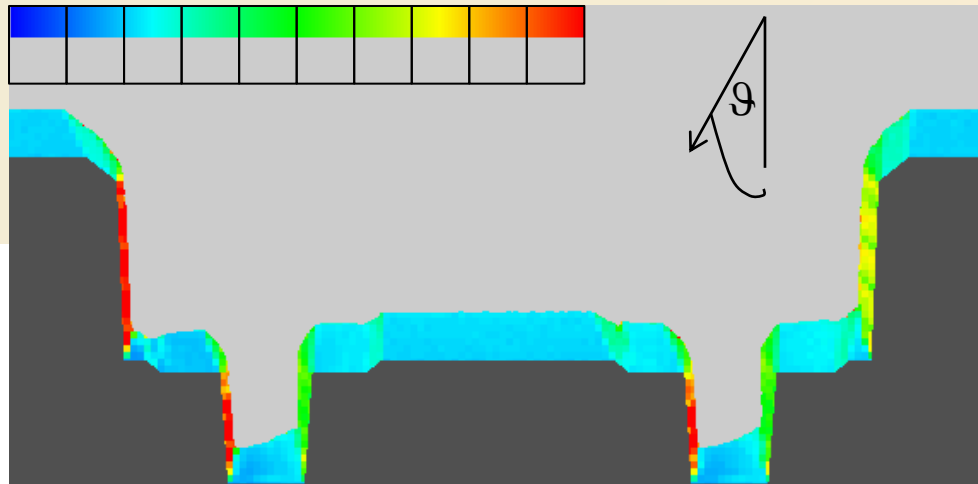
100 eV



Cu95Mn05

0°

90°



Cu95Mn05

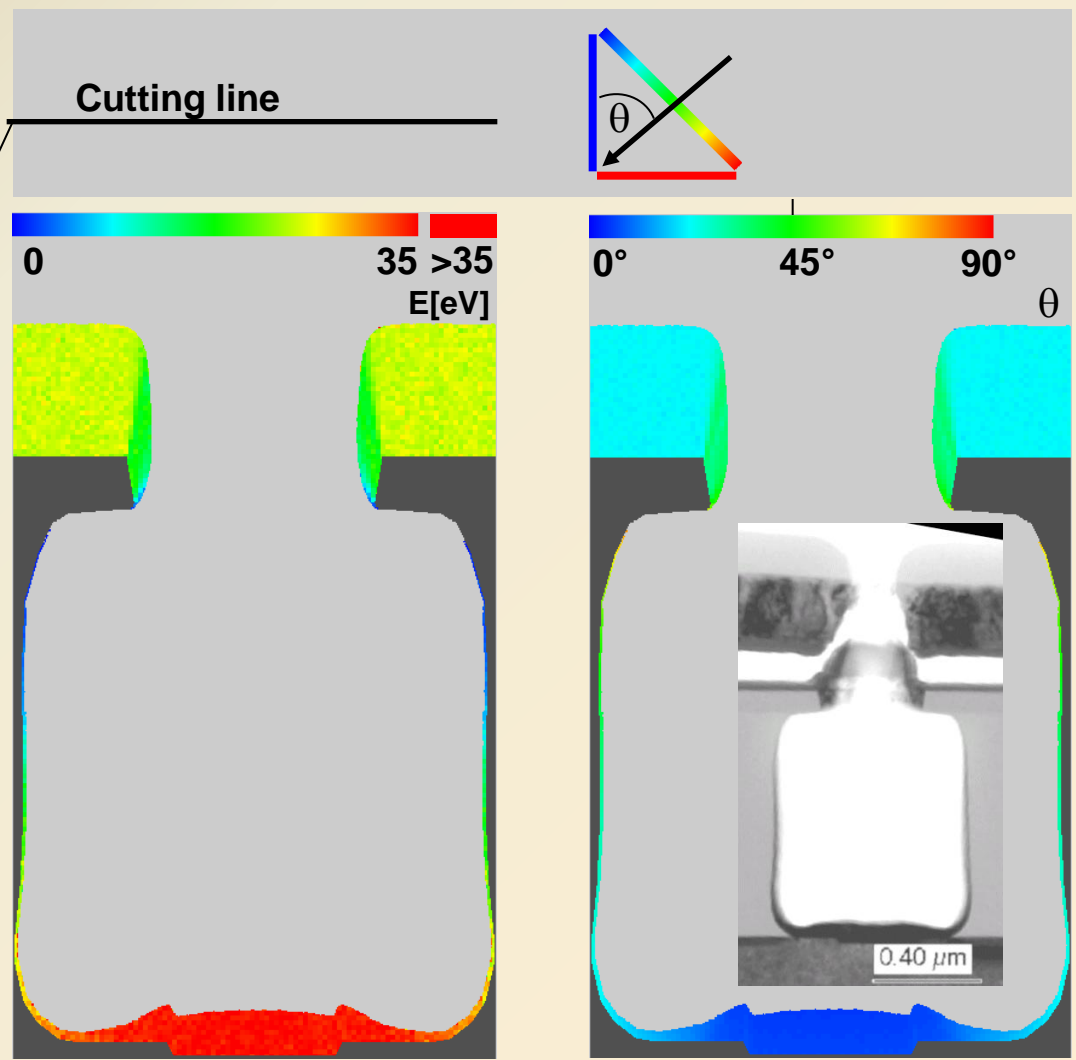
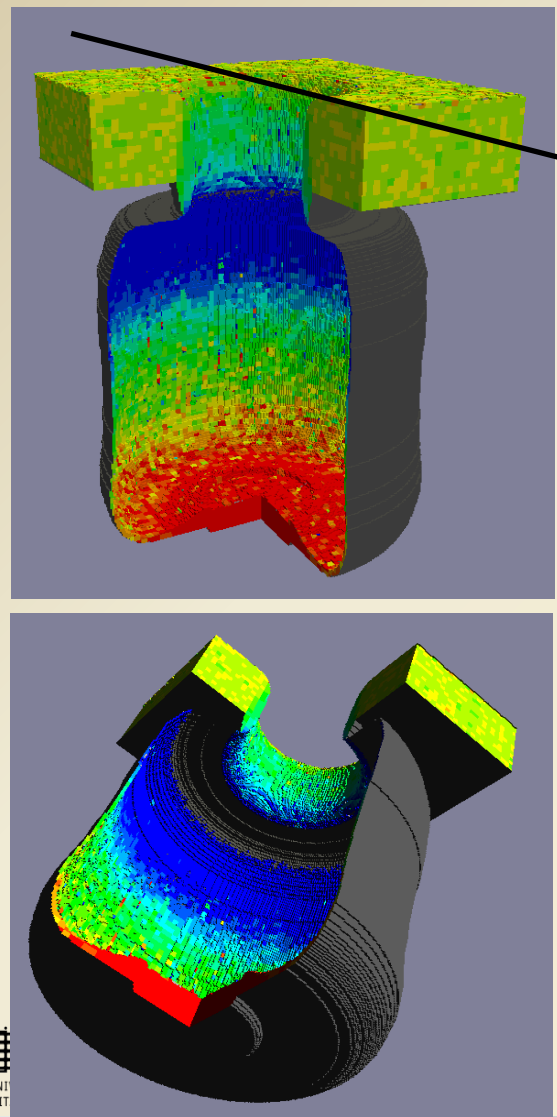
Polar angle

of incident particles

Direction towards  
the wafer center



# Ti deposition (Advanced HiFill process) in a bottle-shaped test structure



Energy deposition

in eV/atom

Influence on  
texture, density,  
surface diffusion

Average polar angle

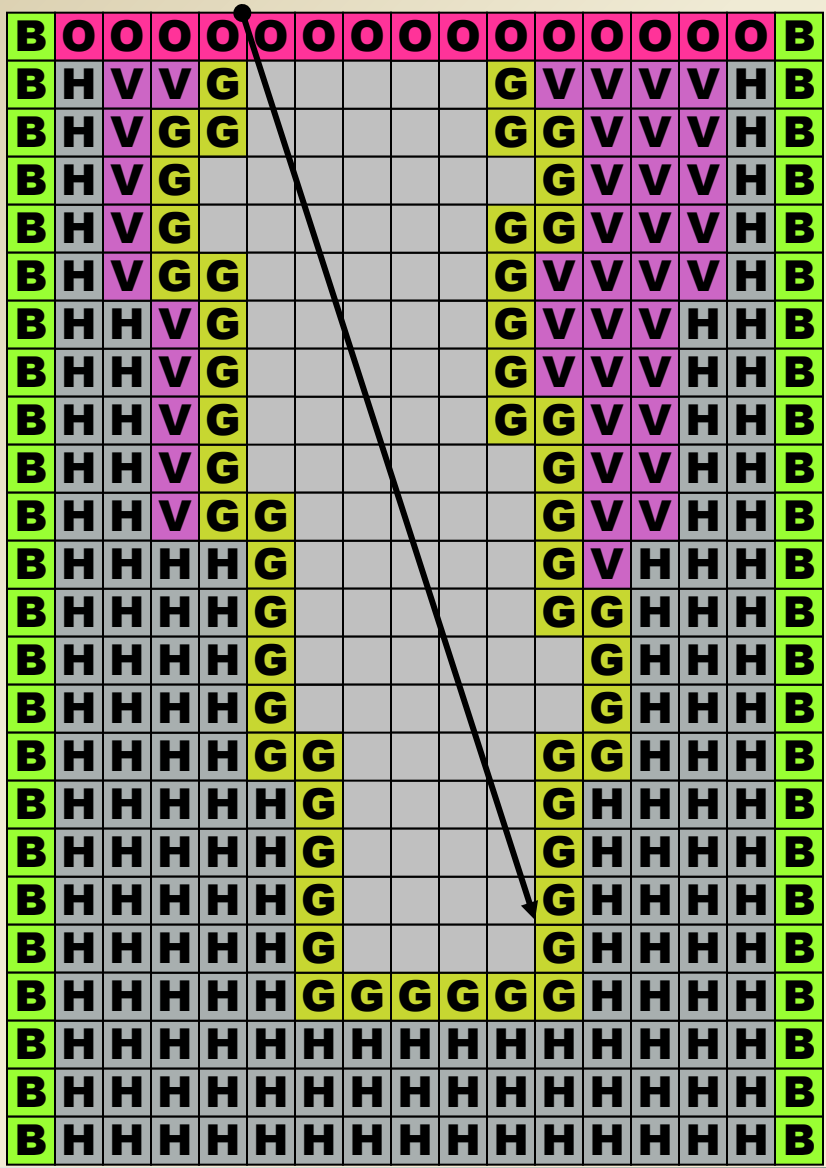
of incident Ti atoms

Influence on  
grain growth

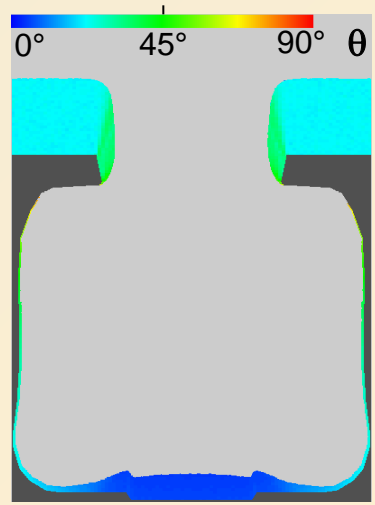
# Flow chart – Lattice Based Monte Carlo Topography Simulation in „T2“

Particle starts here

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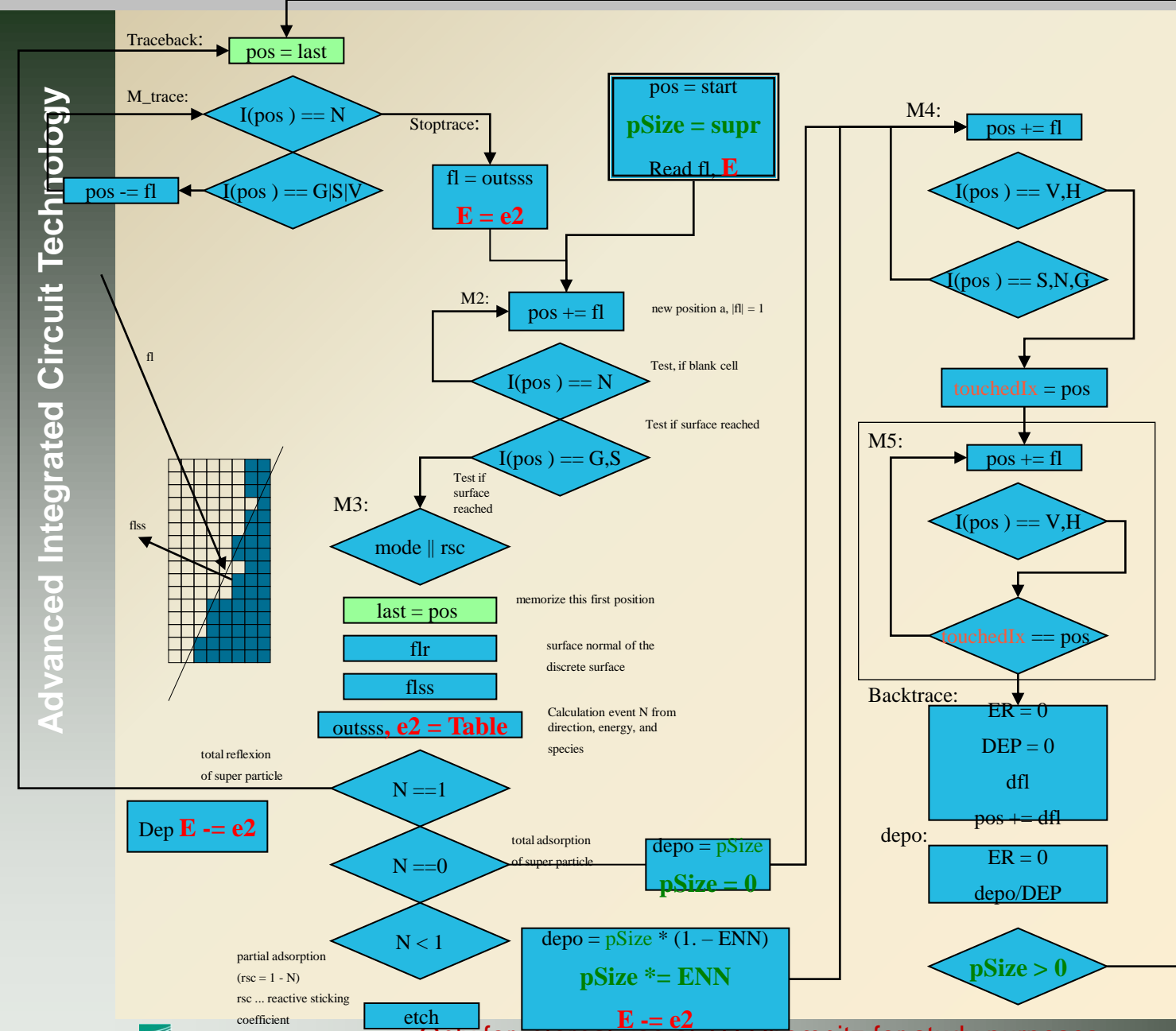
- H** Material cell, structure definition
- V** Material cell, grown
- B** Boundary cell
- O** Boundary cell
- G** Growing cell



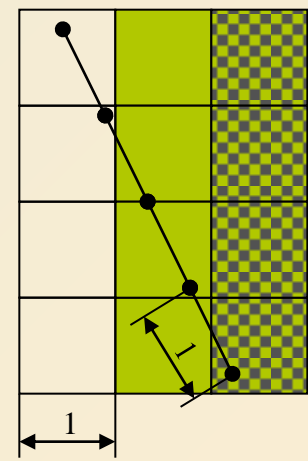
Average polar angle of incident atoms



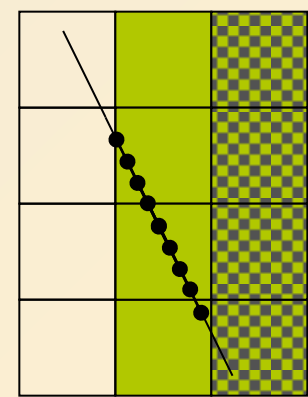
# Flow chart – Lattice Based Monte Carlo Topography Simulation in „T2“



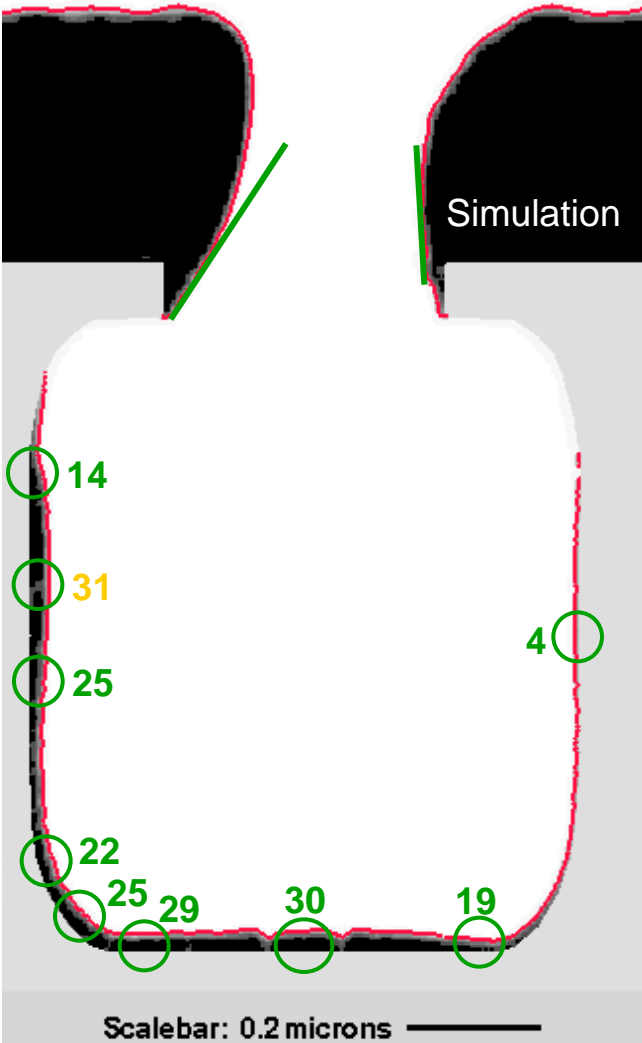
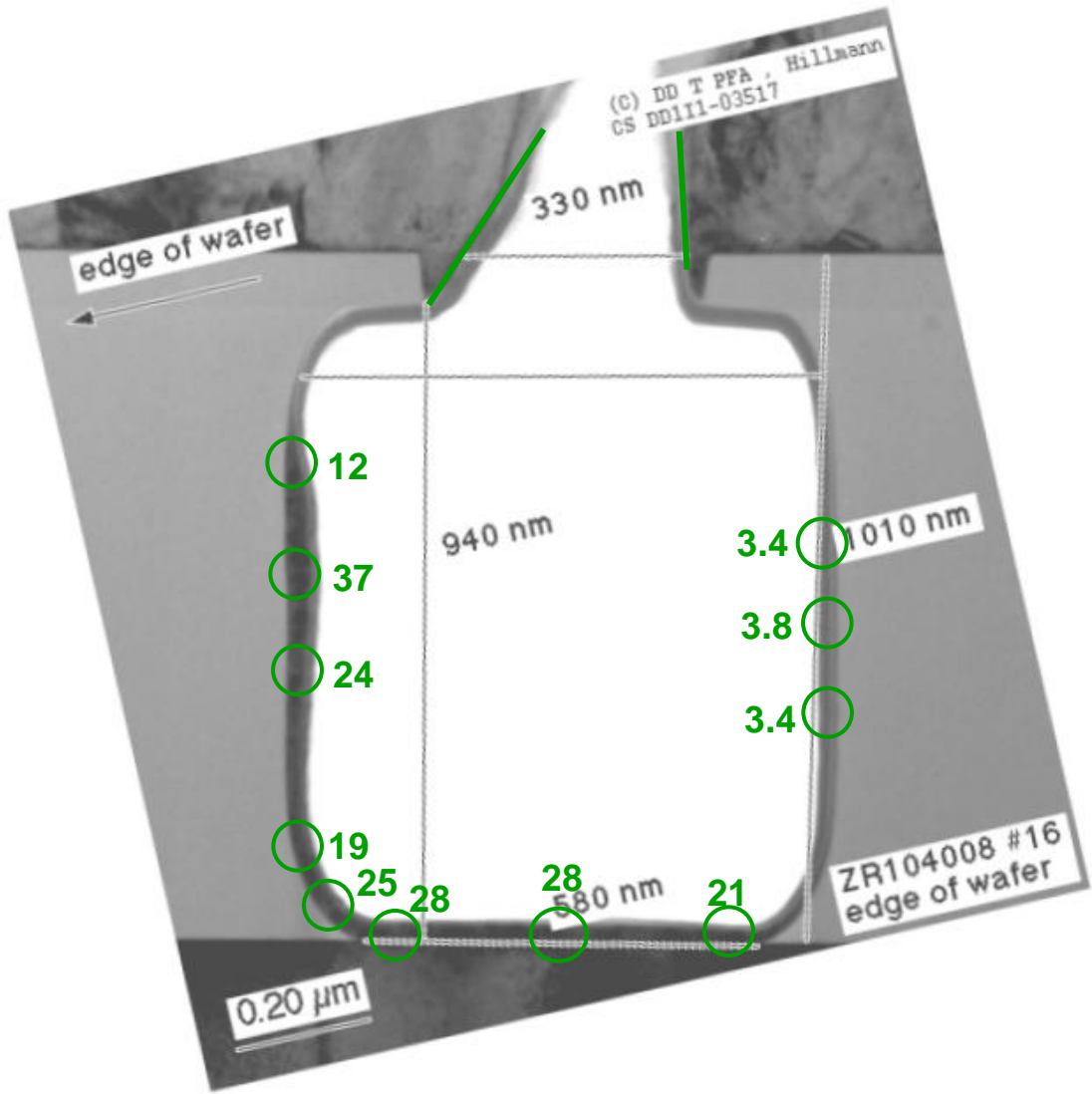
Transport:



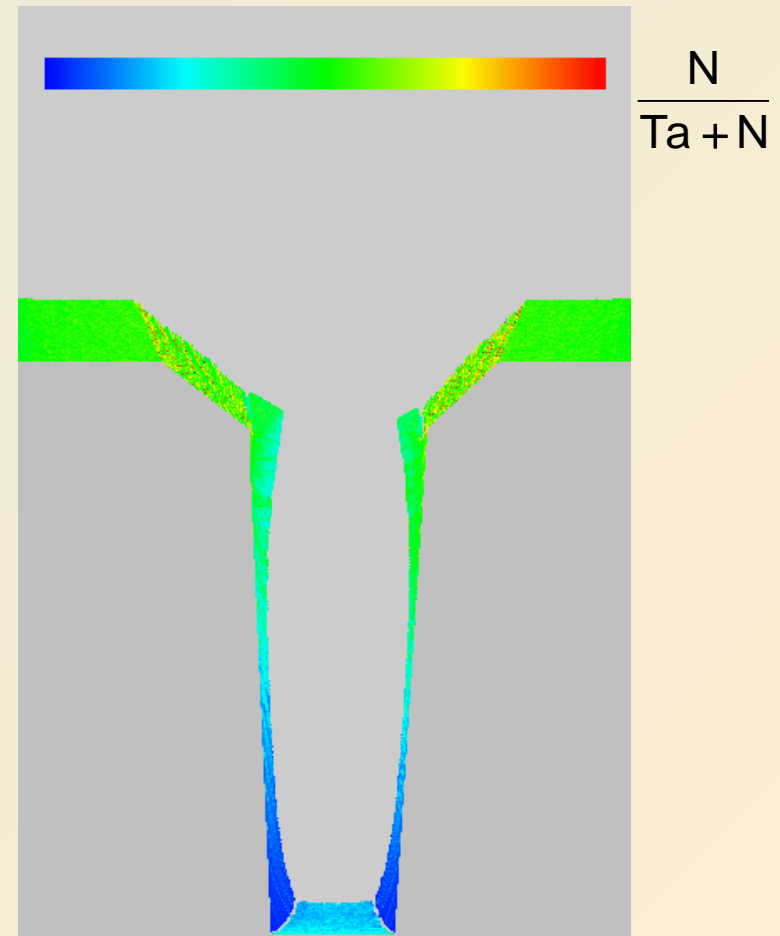
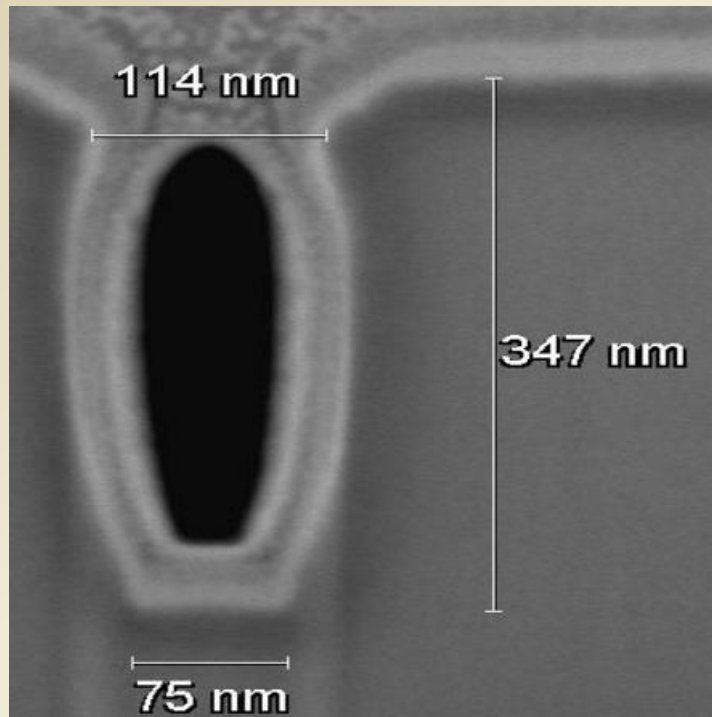
Backtracing:



Titanium, wafer edge, rsc = 1



TaN-PVD: Feature scale



- Modeling of thin film deposition helps to understand better chemical/physical background of deposition processes
- Simulation to improve deposition rates, uniformity, fill behavior of vias and trenches by optimization of process conditions and reactor configuration
- Calculation of layer properties difficult to measure (energy deposition, layer composition (TixNx), minimum film thickness in deep trenches/vias)
- Time savings
- Cost reduction  
(example: vertical CVD batch reactor: up to 200 200mm wafers!)



# Types of Computer Simulation

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## *Static Simulation*

*Time is no consideration, snap-shot*

## *Monte-Carlo Simulation*

*Is based on random numbers and/or stochastic theory*

## *Dynamic Simulation*

*Time is most important*

*Sequences and processes are the focus*

## *Continuous Simulation*

*Time flows in regular steps*

*Every time step causes a of state of system change*

*Models mostly systems of differential equations*

*Continuous simulation ist deterministic*

*Physical processes (e.g. vibration characteristics, analog circuits, fluid flow), chemical processes, weather and climate*

## *Discrete Simulation*

*In time step events are evoked which determine the next system state*

*Application in production and logistics, Supply-Chains etc.*

## *Hybride Simulation*

*Models representable with standard elements (e. g. random numbers, waiting lists, probability distributions)*

*Forecast of expected probabilities for different system states*

*Prognosis (traffic, airports, tollbooths, mail, etc.)*