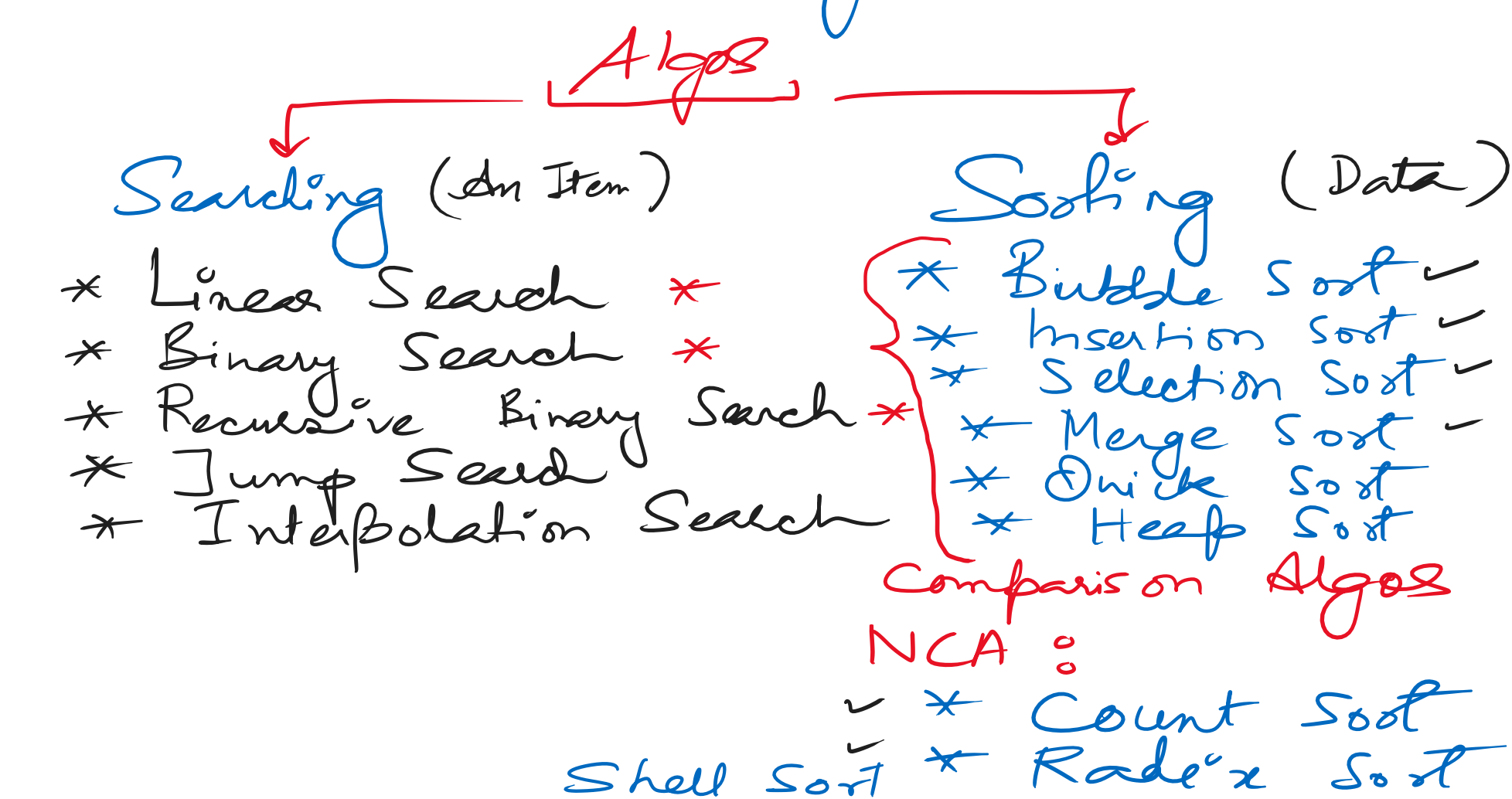


## Introduction to Algorithms : →



Linear Search : → Element  $\rightarrow$  Target key  
Normal Traversal Search

Big O Syntax

Notation 9 | 0 | 42 | 3 | 200 | 11  
0 1 2 3 4 5

key = 42 return index pos

$O(1)$  if (arr[i] == target)  
 $O(n)$  return i;

Binary Search: Pre-Condition Sorted Array key = 23

$\frac{s}{15}$  2 | 8 | 10 | 15 | 19 | 23 | 37  $\frac{e}{6}$

0 1 2 3 4 5 6

mid =  $\frac{s+e}{2}$

① if (arr[mid] == key) return mid;  $s \geq e$   $\frac{0+6}{2} = 3$

② if (arr[mid] < key)  $e = s_{m+1}$   $\frac{0+2}{2} = 1$   $15 < 23 \rightarrow$  go to right side  $s = m+1$

③ if (arr[mid] > key)  $s = m-1$   $15 > 8$  shift to left  $m = 3$  key = 8

DRY - RUN (Mercedes)  
(Pure Storage)

Binary Search Time Complexity

Initial size Array / Sorted  $\frac{N}{2^0} = 1$  mid =  $\frac{s+e}{2}$

left part | right part  $\frac{N}{2}$   $\frac{N}{2} = \frac{N}{2^1}$

$K = \log_2 N$   $\frac{N}{2^2} = \frac{N}{2^2}$   $\frac{N}{2^k} = 0, 1, 2, 3 \dots$

Big O  $\log N$

where  $k = 0, 1, 2, 3 \dots$

$k = \log_2 N$

Big O Notation  $\log N$

Optimal Mid Value Formula : →

Integer: short int long  
-128 to 127

$m = \frac{s+e}{2}$  INT\_MAX  $\rightarrow 2^{31} - 1$   
 INT\_MIN  $\rightarrow -2^{31}$

$= \frac{(\text{INT\_MAX} + \text{INT\_MIN})}{2}$

$\frac{s+e}{2} = \frac{s + \left\lfloor \frac{e-s}{2} \right\rfloor}{2}$  OOB TLE

$m = s + \frac{(e-s)}{2} = \frac{2s + e - s}{2} = \frac{s+e}{2}$

Important Binary Search Questions

for Placements: Leet Code  
Coding Ninjas

- \* Search In A 2D Matrix
- \* Square Root of a Given Number
- \* Aggressive Cows
- \* Book Allocation Problem
- \* Peak In A Mountain
- \* First / Last / Total Occurrences of an element.