

Final Year B. Tech., Sem VII 2022-23

Cryptography And Network Security

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Assignment No. 11

1. Aim:

Implementation of Diffie Hellman Key Exchange Algorithm

2. Theory:

The Diffie-Hellman algorithm is being used to establish a shared secret that can be used for secret communications while exchanging data over a public network using the elliptic curve to generate points and get the secret key using the parameters.

- For the sake of simplicity and practical implementation of the algorithm, we will consider only 4 variables, one prime P and G (a primitive root of P) and two private values a and b.
- P and G are both publicly available numbers. Users (say Alice and Bob) pick private values a and b and they generate a key and exchange it publicly. The opposite person receives the key and that generates a secret key, after which they have the same secret key to encrypt.

Example:

Step 1: Alice and Bob get public numbers $P = 23$, $G = 9$

Step 2: Alice selected a private key $a = 4$ and Bob selected a private key $b = 3$

Step 3: Alice and Bob compute public values

$$\text{Alice: } x = (9^4 \bmod 23) = (6561 \bmod 23) = 6$$

$$\text{Bob: } y = (9^3 \bmod 23) = (729 \bmod 23) = 16$$

Step 4: Alice and Bob exchange public numbers

Step 5: Alice receives public key $y = 16$ and Bob receives public key $x = 6$

Step 6: Alice and Bob compute symmetric keys

$$\text{Alice: } k_a = y^a \bmod p = 6^{536} \bmod 23 = 9$$

$$\text{Bob: } k_b = x^b \bmod p = 6^{216} \bmod 23 = 9$$

Step 7: 9 is the shared secret.

3. Code:

```

#include <bits/stdc++.h>

using namespace std;

long long powM(long long a, long long b, long long n)
{
    if (b == 1)
        return a % n;

    long long x = powM(a, b / 2, n);
    x = (x * x) % n;
    if (b % 2)
        x = (x * a) % n;
    return x;
}

bool checkPrimitiveRoot(long long alpha, long long q)
{
    map<long long, int> m;
    for (long long i = 1; i < q; i++)
    {
        long long x = powM(alpha, i, q);
        //cout << x << endl;
        if (m.find(x) != m.end())
            return 0;
        m[x] = 1;
    }
    return 1;
}

```

```

}

int main()
{
    long long q, alpha;

    q = 7; // A prime number q is taken
    alpha = 5; // A primitive root of q
    if (checkPrimitiveRoot(alpha, q) == 0)
    {
        cout << "alpha is not primitive root of q";
        return 0;
    }
    else
    {
        cout << alpha << " is private root of " << q << endl;
    }

    long long xa, ya;

    xa = 3; // xa is the chosen private key
    ya = powM(alpha, xa, q); // public key of alice
    cout << "\n Private key of alice is " << xa << endl;
    cout << "\n Public key of alice is " << ya << endl << endl;

    long long xb, yb;

    xb = 4; // xb is the chosen private key
    yb = powM(alpha, xb, q); // public key of bob
    cout << "\n Private key of bob is " << xb << endl;
    cout << "\n Public key of bob is " << yb << endl << endl;

    //key generation

```

```

long long k1, k2;

k1 = powM(yb, xa, q); // Secret key for Alice

k2 = powM(ya, xb, q); // Secret key for Bob

cout << "\n Generated key by a is " << k1 << endl;

cout << "\n Generated key by b is " << k2 << endl << endl;

return 0;

}

```

4. Output:

```

PS D:\Walchand\7 Semester\Crypto\Assignment 11> cd "d:\Walchand\7 Semester\Crypto\Assignment 1
1\" ; if ($?) { g++ diffie_helman.cpp -o diffie_helman } ; if ($?) { .\diffie_helman }
5 is private root of 7

Private key of alice is 3

Public key of alice is 6

Private key of bob is 4

Public key of bob is 2

Generated key by a is 1

Generated key by b is 1

PS D:\Walchand\7 Semester\Crypto\Assignment 11>

```

5. Conclusion:

Successfully implemented Diffie Hellman Key Exchange Algorithm.