

Probability Theory

Assignment-1

Max Marks: 100

Due date:12/11/18

1. If the discrete random variable X denotes the minimum of the two numbers that appear when a pair of fair dice is thrown once.
 - (a) Find the probability mass function (Also sketch the graph)
 - (b) Find Cumulative distribution function (Also sketch the graph)
 - (c) Find expectation, variance, standard deviation and skewness.
2. A random variable X has the following PMF

x	0	1	2	3	4	5	6	7
P(X=x)	0	k	2k	2k	3k	k ²	2k ²	7k ² +k

(a) Find k

(b) Evaluate $P(X < 6)$, $P(X \geq 6)$, $P(0 < X < 5)$

(c) If $P(X \leq a) > 0.5$. Find the minimum value of a

3. A player tosses 3 fair coins. He wins Rs.500 if 3 heads occur, Rs.300 if 2 heads occur, Rs.100 if one head occurs. On the other hand he loses Rs.1500 if 3 tails occur. Find the value of the game to the player. Is game favorable to the player?
4. If CDF of random variable X is given by $F_X(x) =$

0	$x < 0$
1/2	$0 \leq x < 1$
3/5	$1 \leq x < 2$
4/5	$2 \leq x < 3$
9/10	$3 \leq x < 3.5$
1	$x \geq 3.5$

Find the probability mass function of X .

5. If $E[X] = 10$, $\text{Var}[X] = 1$ and $Y = 2X(X+20)$ find $E[Y]$
 - (b) If $E[X] = 1$, $E[X^2] = 4$ and $Y = 2X - 3$. Find the second central moment of Y about $c = 3$.
6. If a ticket drawn from a box containing 10 tickets numbered 1 to 10 inclusive.
 - (a) Discuss about its probability distribution
 - (b) Find the probability that the number x drawn is
 - (i) even number
 - (ii) prime number
 - (iii) less than 4
 - (c) Find the mean and variance of the random variable X
7. The probability that a student is accepted in a prestigious college is 0.3. If five students from same school apply.
 - (a) Discuss about its probability distribution

- (b) What is the probability that at most two students are accepted
 - (c) Find mean and variance of the random variable
8. Suppose that on average one person in 1000 makes a numerical error in preparing income tax return. If 10000 forms are selected at random and examined.
- (a) Discuss about its probability distribution
 - (b) Find the probability that 6,7 or 8 of the forms will be in error.
 - (c) Find the mean and the variance of the random variable.
9. A man hits the target with probability 0.25.how many times would he fail on average before he hits the target.[Hint: Let X be the random variable the represents the number of failures before first success].Give the PMF and $E[X]$
10. The probability to find the defective item is 0.35 in an inspection. what is the probability that the inspector picks 25 items before he finds 8 defective pieces.
- (a) Discuss about its probability distribution
 - (b) Find mean and variance