

## Relational Calculus-1

- Relational algebra is a procedural in nature
- procedural: How: what the sequence of steps need to obtain the desired Relation

### Diff b/w Relation cal & Algebra

#### - Relational cal

- language of defining new relation in a DB
- Form the basis of a query language
- Non-procedural in some sense
- It uses the concepts of formal logic to express relational queries

### Formulation of Relation cal

- Tuple Relation cal
- Domain Relation cal

#### Tuple Relation cal

- Relation is expressed as a set

$$\{t \mid P(t)\} \quad t \rightarrow \text{tuple variable}$$

$\downarrow$   
 $P(t) \rightarrow$  predicate of tuple variable  
must be true for every element of the set

$$S = \{t \mid P(t)\} \text{ i.e., } P(t) \text{ must be true for each tuple in}$$

## DB Scheme

### \* Set of attributes

Acc-no, Yr-pub, title, Card-no, B-name,  
B-Add, S-name, S-Addr, DOZ, Price, DCS

### \* Set of Relation Schemes

Book-Scheme (Acc-No, YR-Pub, title)

User-Scheme (Card-No, B-name, B-add)

Supplier-Scheme (S-name\*, S-addr\*)

B-By-Scheme (Acc-no\*, Card-no, DOZ)

S-by-Scheme (Acc-No, S-name, price, DCS)

### \* Set of Relations

book (book-scheme)

user (user-scheme)

Supplier (Supplier-scheme)

borrow (borrow-scheme)

Supp (Supp S-by-scheme)

Acc-No	Yr-Pub	Title

$\{t \mid t \in \text{book} \wedge t[\text{YR-PUB}] = '1991'\}$   
 $\{t \mid t \in \text{book} (t[\text{YR-PUB}] = '1991')\}$   
Equivalent Relation Algebra

$\sigma_{\text{YR-PUB} = 1991}(\text{book})$

- we don't want year

- How to select attribute of Subq

$\{ t \mid \exists u \in \text{book} (u[\text{yr-pub}] = '1991' \wedge t[\text{Acc-no}] = u[\text{Acc-no}] \wedge t[\text{Title}] = u[\text{Title}]) \}$

Some tuple

S

Acc no	Title

Book

Acc-no	YR-pub	Title

Supp

Accno	Sname	Price	DOS

S

S-NAME

$\{ t \mid \exists s \in \text{Supp} \wedge s[\text{price}] > 1000$

$\wedge s[\text{Sname}] = t[\text{S-name}] \}$

① get the names of Supplier who has supplied at

least one book for 1000 (or) more



④ Find the names of all Suppliers who have the same address as 'NAROSA'

$$\{t \mid \exists s \in \text{Supplier} (t[\text{S-name}] = s[\text{S-name}] \wedge \exists u \in \text{Supplier} (u[\text{S-Addr}] = s[\text{S-Addr}] \wedge u[\text{S-name}] = \text{"NAROSA"}))\}$$

⑤ Find the Suppliers who has supplied same title issued by "VIJAY" (may not be same book by Acc-no)  
Supp, user, book, borrow

$$\{t \mid \exists s \in \text{Supp} (t[\text{S-name}] = s[\text{SNAME}] \wedge u[\text{S-name}] = \text{"NAROSA"})\}$$

⑥ Find the names of those Suppliers who have supplied titles corresponding to all books issued by "VIJAY"

$$\{t \mid \forall s \in \text{User} (s[\text{S-name}] = \text{"VIJAY"} \Rightarrow \exists p \in \text{borrow} (p[\text{Acc-no}] = s[\text{Acc-no}] \wedge \exists v \in \text{book} (v[\text{Acc-no}] = p[\text{Acc-no}] \wedge \exists r \in \text{book} (v[\text{Title}] = r[\text{Title}]) \wedge \exists m \in \text{Supp} (r[\text{Acc-no}] = m[\text{Acc-no}]) \wedge t[\text{S-name}] = m[\text{S-name}]))))\}$$

For correct of all

$$\{t \mid \forall u \in \text{book} (t[\text{YR\_POS}] = u[\text{YR\_POS}]) \wedge t[\text{TITLE}] = u[\text{TITLE}]\}$$

↑  
For all

$$\wedge t[\text{TITLE}] = u[\text{TITLE}]$$

$$\{t \mid \forall u \in \text{book} (t[\text{YR\_POS}] = u[\text{YR\_POS}] \Rightarrow t[\text{TITLE}] = u[\text{TITLE}])\}$$

⊆

book		book		
T	Y	A	T	Y

Ex:

Student (Roll no, Name, Dept No, Sex)

Query: Find Roll no and name of Student in dept no 2

$$\{t. \text{Roll.No}, t. \text{Name} \mid \text{Student}(t) \wedge t. \text{Dept} = 2 \wedge t. \text{Sex} = \text{Male}\}$$

$$\{t_1 A_1, t_2 A_2, \dots \mid \text{Condition}(t_1, t_2, \dots)\}$$

↑  
Attribute

↑  
tuple variable



## using Quantifiers

$\exists$  : Existential Quantifier

$\forall$  : Universal Quantifier

Ex: Emp (eid, Name, sal)  
Dep (Dir, Name, Eid)

Query: Employee (Name) who has no dependents

$e.Name / Emp(e) \wedge (\neg \exists d (Dep(d) \wedge d.Eid = e.Eid))$   
 $\neg$  (True for e having <sup>Some</sup> ~~Super~~ <sub>depend</sub>)

Transformation formula

$$(\forall x) (P(x)) \equiv \neg (\exists x) (\neg P(x))$$

$$\neg \exists () \equiv \forall \neg ()$$

$$\neg \forall () \equiv \exists \neg ()$$

$$\neg \neg \forall x (P(x)) \equiv \neg (\exists x) (\neg P(x))$$

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$$(\exists x) (P(x)) \equiv \neg (\forall x) (\neg P(x))$$

$$\neg \neg (\exists x) (P(x)) \equiv \neg (\forall x) (\neg P(x))$$

Query: List the name of employees who have no dependents

$$\{ e\_Name \mid Employee(e) \wedge (\neg \exists d (Depend(d) \wedge (e.EID = d.EID))) \}$$

$$\{ e\_Name \mid employee(e) \wedge \forall d \neg (Depends(d) \wedge (e.EID = d.EID)) \}$$

If we apply De Morgan's law

$$\{ e\_Name \mid employee(e) \wedge (\neg \exists d (\neg Depend(d) \vee \neg (e.EID = d.EID))) \}$$

Ex: depositor (cust\_name, acc-no)

borrower (cust\_name, loan-no)

loan (loan-no, branch-name, amount)

Customer (cust\_name, city, street)

Account (Acc-no, branch-name, balance)

Branch (Branch-name, branch-city, acc-no)

Q1

Find the loan details above 1200

$\{t \mid \text{loan}(t) \wedge t[\text{amount}] > 1200\}$

Q2

Find the name of all customers who have a loan from branch 'x'.

$b.\text{name} \mid \text{borrower}(b) \wedge \exists l (\text{loan}(l) \wedge$

$l.\text{loan-no} = b.\text{loan-no} \wedge$

$l.\text{branch-name} = 'x')$

(or)

$\{b.\text{name} \mid \exists b \in \text{borrower} \wedge \exists l \in \text{loan}$

$\wedge l.\text{loan-no} = b.\text{loan-no}$

$\wedge l.\text{branch-name} = 'x'\}$



⑤ customer who have account or loan or both

$$\{t \mid \text{cust}(t) \wedge (\exists b (\text{borrower}(b)))\}$$

✓ b. Customer = t-test - none )

$$\exists b \text{ (depositor (d))} \wedge$$

d. (rest - now = +. (carbon)) ) }

Do main Retraction Query

List the name of employee who have no dept to manager.

Employee (First name, Lastname, EId, DOB, ~~Adh~~, Sex,  
a b c d e f  
Salary, Dno)  
g h

Dent (Duo, Dhamer, mid)

$$\{a, b \mid \exists c (\text{Employee}(a, b, c, f, g, h) \wedge \neg \exists z (\text{Dept}(x, y, z) \wedge z = c))\}$$