

# VERIFICATION, VALIDATION AND REPLICATION



# A WORD ABOUT MODELS..

Essentially, all models are wrong, but some are useful. —George Box

The word model sounds more scientific than the word fable or tale, but I think we are talking about the same thing. —Ariel Rubinstein



# THE THREE TESTS

- Model verification is the process of determining whether a given model corresponds to the conceptual model
- Model validation is the process of determining the implemented model corresponds to, and explains, some phenomenon in the real world.
- Model replication is the implementation by one researcher or group of researchers of a conceptual model previously implemented by someone else.



# IN OTHER WORDS

- Verification – Test if your implementation of the concepts is correct
- Validation – Test if your conceptualization itself is correct
- Replication – Peer Review



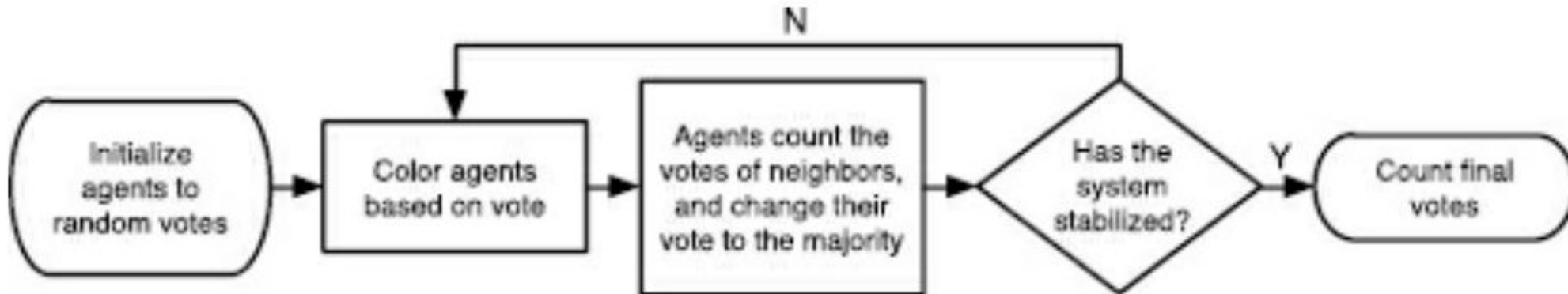
# VERIFICATION

- A general guideline for enabling model verification involves building the model simply to begin with, expanding the complexity of the model only as necessary.
- Two ways of designing
  - The onion
  - The Lego bricks



# DESCRIBING CONCEPTUAL MODELS

- We already saw this in ODD
- Flowchart is a good way to describe the conceptual models
- Example: Simple model of voting behavior



# TESTING IMPLEMENTATION OF CONCEPTS

- Expand the flowchart into pseudocode
- Compute consequences of extrema in parameters
- Unit Testing – Or Similar
- As we grow we need to spawn unit tests for extrema pairs/tuples
  - Assume you have params A and B
  - You should test for (Amax, Bmin) (Amax, Bmax) (Amin, Bmax) (Amin, Bmin)
- The consequences should be written before testing (probably even test driven development)
- You can have in-model unit testing (next slides) or there are ways to external/offline testing (we *might* look into during advanced topics)



# Example: Voting Distribution Model

Voting distribution model is a simple cellular automaton that simulates voting distribution by having each patch take a “vote” of its eight surrounding neighbors.





# TESTING IMPLEMENTATION OF CONCEPTS

```
patches-own
[
  vote ;; my vote (0 or 1)
  total ;; sum of votes around me
]

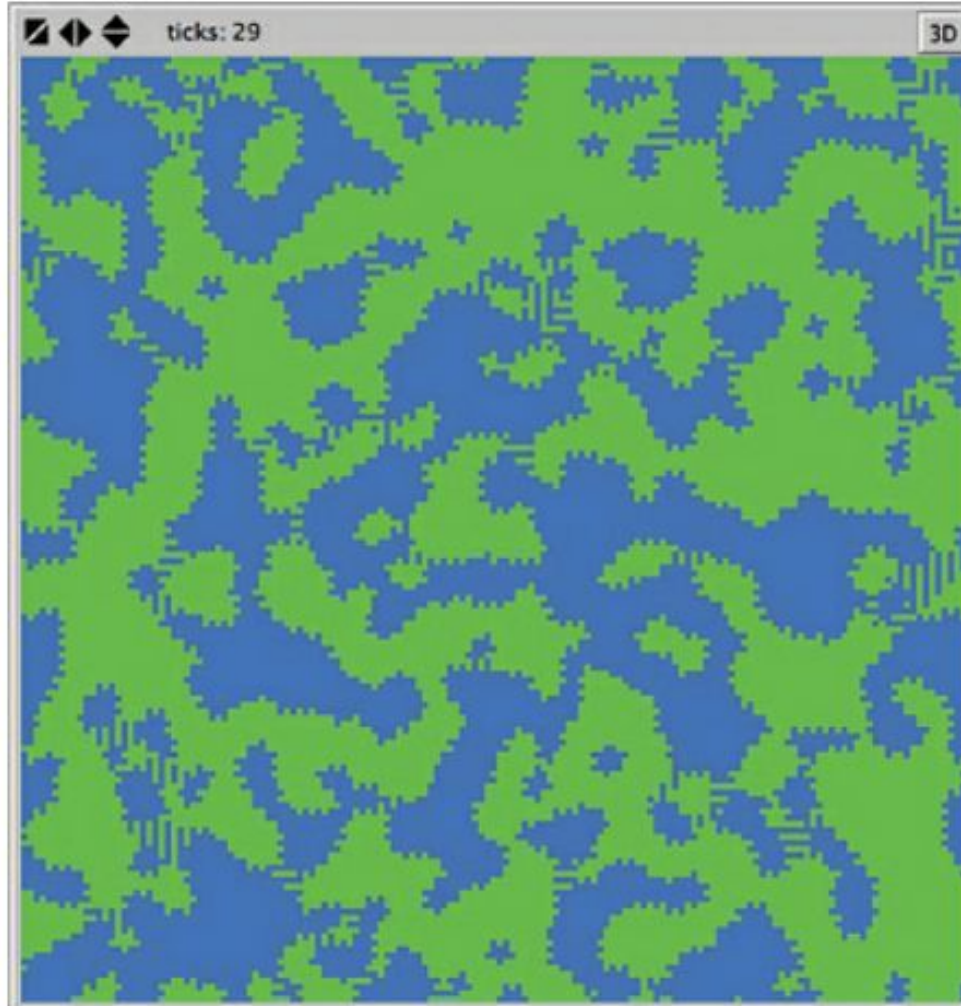
to setup
  clear-all
  ask patches [
    if (random 2 = 0) ;; half a chance of this
    [ set vote 1 ]
  ]
  ask patches [
    if (random 2 = 0) ;; half a chance of this
    [ set vote 0 ]
  ]
  ask patches [
    recolor-patch
  ]
end

to recolor-patch ;; patch procedure
  ifelse vote = 0
  [ set pcolor green ]
  [ set pcolor blue ]
end
```

```
to check-setup
  ;; count the difference between the number of green and the number of
  ;; blue patches
  let diff abs (count patches with [ vote = 0 ] - count patches with
    [ vote = 1 ])
  if diff > .1 * count patches [
    print "Warning: Difference in initial voters is greater than 10%."4
  ]
end
```



# COMMON MISTAKES (EXAMPLE: JAGGED EDGES)



# COMMON MISTAKES

- Ties for limit-points
  - Leverage-points of state/behavior change
- Oscillating patterns
  - Causes of local oscillations or saturation
  - (say) if you help your neighbor good-karma goes up
  - A and B are neighbors, they might go into local cycle
    - A helps/gives B and B helps/gives A
- Implement Tie-breaking logic
- Avoid oscillations using memory/history/memento variables



# SENSITIVITY ANALYSIS

- Extremum gives us a quick test
- But, if the model is not computationally too expensive
  - It pays off doing sensitivity analysis
  - Even if the model takes more time, you can adjust the intervals to do a broad sweep
- Sensitivity analysis is an examination of the impact of varying model parameters on model results.
- To determine how sensitive a model is
  - we examine the effect that different initial conditions and agent mechanisms have on the model results.



# VALIDATION

- Validation is the process of ensuring that there is a correspondence between the implemented model and reality.
- Validation, by its nature, is complex, multilevel, and relative. Models are **simplifications** of reality
- **Remember** that it is impossible for a model to exhibit all of the same characteristics and patterns that exist in reality



# AXES OF VALIDATION (RAND & RUST 2011)

- The level or abstraction of the validation process
  - **Microvalidation** vs **Macrovalidation**
- The level of detail of the validation process
  - (expert) **Face validation** vs **Empirical Validation**



# CONSIDERED EXAMPLE: FLOCKING MODEL

- Attempts to recreate patterns of birds flocking behavior
- Its based on Boids model by Reynolds (1987)
- Demonstrated that flocks can arise without necessity of a leader
- Lets see the model
- Just three rules: alignment, cohesion and separation



# MICROVALIDATION

- Compare Individual agent (bird) behavior to known behavior observed by experts
- This might explain the sufficiency of modeling the individual
  - Do we need to add additional property (like vision range) ?
  - Or may be one property does not add much value shall we eliminate it
- There are several ways of doing this
  - Let's switch to the other axes and come back....





# FACE VALIDITY (EXPERTS)

- On its face does the model (animation) looks correct
- Does the way the flock coalesces somewhat look reasonable?
- Tracing – Trace everything a select subset of individuals see and do
  - Think of it like inspecting a specific turtle using go-once
  - Does the action of the agent is close to real world observations



# EMPRICAL VALIDITY (DATA)

- Even with stochasticity the effect of parameters on certain emergent phenomenon should be within an acceptable range
  - Should change in meaningful predictable ways (predictive validation)
  - If unable to see the pattern, you should be able to investigate and explain it
- Internal validity: Run experiments multiple times and subject important numbers to statistical analysis
- Data driven validation: See if the results qualitatively match the real world observed data (Only when Historical data exists)



# MACROVALIDATION

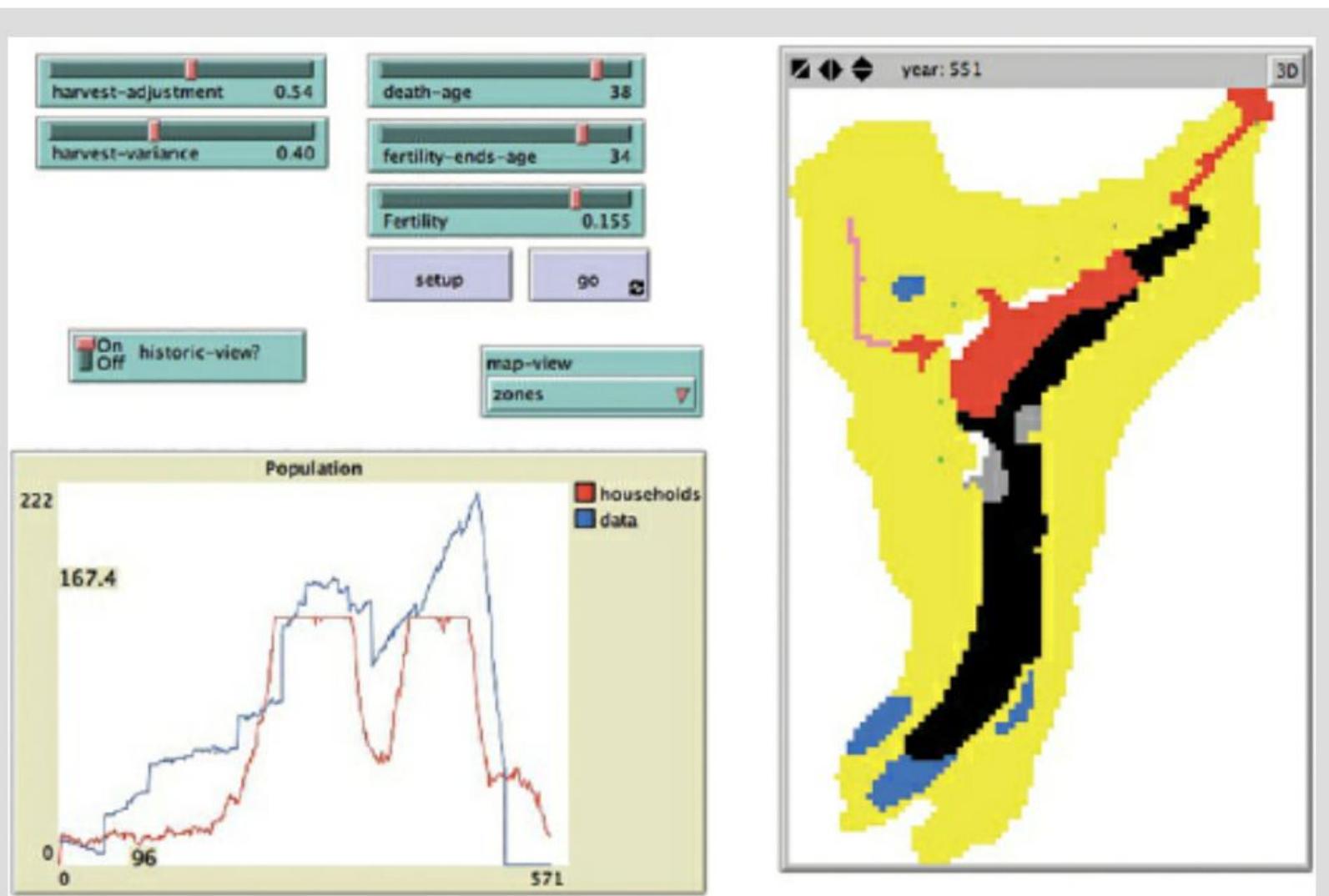
- Same idea of doing face validation and data driven validation but on a different scale
- Instead of individual, we analyze on a much higher level
- How does the flock (groups) behave
  - When they come together
  - When they break apart
- Internal validation across runs (we anyway do that as part of testing our hypothesis)
- Think of Micro-Macro validation not as binary but as a spectrum



# CASE STUDY - ARTIFICIAL ANASAZI MODEL

- A good model highly appreciated for the level of validation
- Native Indians – Kayenta Anasazi lived in Arizona, US
- The model explains their disappearance from the region based on social and environmental changes
- We will see this tomorrow!





[Figure 7.10](#) NetLogo version of the Artificial Anasazi model. In the population plot, the red line plots the simulated population and the blue line the real population data.



# REPLICATION

- Across hardware
- Across languages
- Across platforms

