

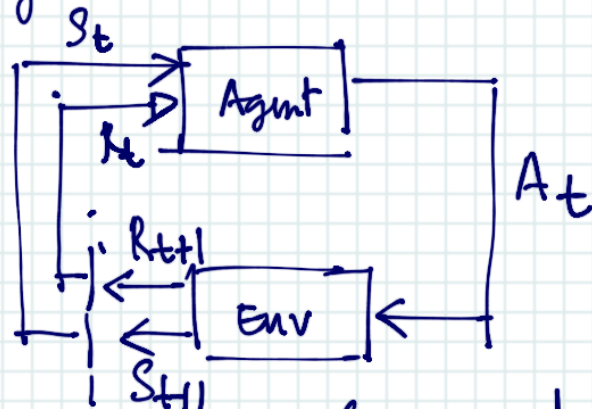
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## AI5001: Intro to Modern AI

Today: • Review

- Continue RL problem formulation.
  - states, actions
  - goals, rewards
  - characterising states

Review:



$$\text{Policy: } \pi_t(a|s) = \Pr(A_t = a | S_t = s)$$

Goal of RL is to learn the optimal policy from experience

$S_t \in \mathcal{S}$  where  $\mathcal{S}$  is a set of possible states

$A_t \in \mathcal{A}(S_t)$  where  $\mathcal{A}(S_t)$  is the set of possible actions corresponding to  $S_t$

Goals and rewards:

- $G_t = R_{t+1} + R_{t+2} + \dots + R_T$  (episodic)
- $G_t = \sum_{k=0}^{\infty} R_{t+k+1}$  (continuous).

Note that the above  $G_t$  could be unbounded even if  $\{R_k\}$  is finite

- Introduce  $\gamma$ , a discount factor that lies between 0 and 1 and define

$$G_t = \sum_{k=0}^{\infty} \gamma^k \cdot R_{t+k+1}$$

Unified goal definition:

$$\boxed{G_k = \sum_{k=0}^T \gamma^k R_{t+k+1}}$$

where  $T = \infty$  in the cont. case,

$\gamma = 1$  in the episodic case

Imp! Both these cannot be true simultaneously

Prob. review!

Q: What is a RV?

A: A RV  $X(\Omega): \Omega \rightarrow \mathbb{R}$

Q: What is CDF?

A:  $F_X(x) = \Pr\{X \leq x\}$

Q: What is PDF?

A:  $f_X(x) = \frac{d}{dx} F_X(x)$  (continuous case)

PMF  $f_X(x) = \Pr\{X=x\}$  (discrete case).

Q: Random process?

A: An indexed set  $\{x(t): t \in \mathcal{T}\}$  of random variables.  $\mathcal{T}$  could be countably infinite

Markov process:

$$f_{X_{n+1} | X_n, X_{n-1}}(x_{n+1} | x_n, x_{n-1})$$
$$= f_{X_{n+1} | X_n}(x_{n+1} | x_n)$$

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