

# Implementation of LISA - Variation of Income across different LGAs in Australia

May 9, 2018

# Why Spatial Econometrics

*Everything is related to everything else, but near things are more related than distant things*

## **Tobler's (1979) first law of geography**

- ▶ Spatial Dependence : Existence of functional relationship between what happens at one point in space and what happens elsewhere
- ▶ Spatial Heterogeneity: lack of uniformity of effect of space  
Example: Urban places have unequal population and income levels

# Why Spatial Econometrics

## Neighbors in Space

Expressing a way the structure of spatial dependence is to be incorporated in a model

- ▶ Lagged variable in time series analysis is unambiguous
- ▶ Spatial Lag?
  - ▶ Neighborhood and nearest neighbor  $\{j \mid P([x_i]) \neq P[x_i|x_j]$   
and  $d_{ij} < \epsilon\}$

# Why Spatial Econometrics

## Spatial Contiguity Matrices

- ▶ Binary Contiguity Matrix
- ▶ Rook Contiguity
- ▶ Bishop Contiguity
- ▶ Queen Contiguity
- ▶ Distance Based Weights
- ▶ K-nearest neighbor weights

# From where did we get the Data

## Income Data Source

- ▶ Australian Bureau Of Statistics (<http://stat.data.abs.gov.au>)
- ▶ Economy -> Finance -> Household Income -> Census 2016, Total Household Income (Weekly) by Household Composition (LGA)
- ▶ Customise layout():
  - Page - Census Year, Household Composition
  - Row - State, Region, Geography Level
  - Column - Total Household Income Weekly

# From where did we get the Data

## Shapefile Data Source

- ▶ Australian Bureau Of Statistics  
(<http://www.abs.gov.au/AUSSTATS/abs@.nsf/DetailsPage/1270.0.55.003July%202016?OpenDocument>)
- ▶ Name of the file (Zip) to download: Local Government Areas ASGS Ed 2016 Digital Boundaries in ESRI Shapefile Format

## How does the Data look

```
## # A tibble: 121,880 x 6
##   Weekly_Household_Income Annual_Household~ State LGA
##   <chr>                  <chr>      <chr> <chr>
## 1 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 2 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 3 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 4 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 5 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 6 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 7 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 8 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 9 $1,000-$1,249         $52,000-$64,999 New S~ 1
## 10 $1,000-$1,249        $52,000-$64,999 New S~ 1
## # ... with 121,870 more rows
```

# Analysis

- ▶ Number of people for 21 income categories provided for each regions (Histogram for different LGAs with bins as the income categories)
- ▶ A density plot created using the histogram
- ▶ Compute  $p = 0.01, 0.02, \dots, 0.99$  for each LGA



# Analysis

## Table2

```
## # A tibble: 1,662 x 3
## # Groups:   LGA_2016 [?]
##   LGA_2016 Weekly_Household_Income Number_People
##   <int> <chr> <int>
## 1 10050 High 13715
## 2 10050 Low 6075
## 3 10050 Medium 15489
## 4 10130 High 7178
## 5 10130 Low 3138
## 6 10130 Medium 8104
## 7 10250 High 11057
## 8 10250 Low 4869
## 9 10250 Medium 13679
## 10 10300 High 518
## # ... with 1,652 more rows
```

# Analysis

Obtain one representative income for each LGA

Weekly household median incomes assumed for each class:

- Low: 250A\$
- Medium: 1000A\$
- High: 5000A\$

## Reading LGA Data

- ▶ Reading OGR vector maps into Spatial objects
- ▶ The Geospatial Data Abstraction Library (GDAL) is a computer software library for reading and writing raster and vector geospatial data formats
- ▶ The rgdal package has been around for more than a decade and provides bindings to the incredible Geospatial Data Abstraction Library (GDAL) for reading, writing and converting between spatial formats

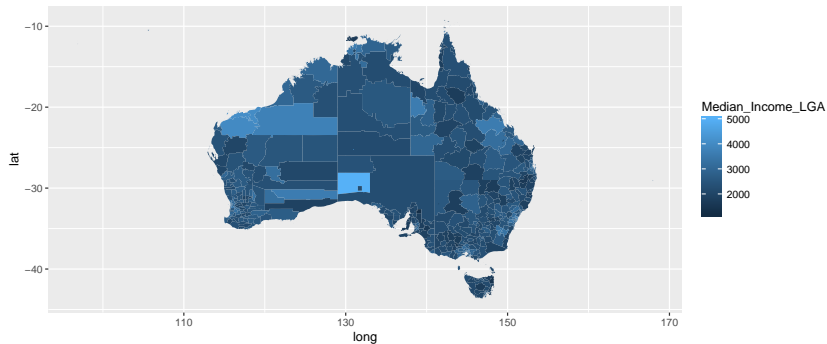
```
## OGR data source with driver: ESRI Shapefile
## Source: "/Users/sgup0008/Documents/ABS_Income/ABS_Income"
## with 563 features
## It has 5 fields

## Warning in rgdal::readOGR("../LGA_shapefiles", layer = "LGA") :
## Dropping null geometries: 131, 132, 213, 214, 293, 294,
## 536, 537, 556, 557, 559, 560, 562, 563

## Regions defined for each Polygon
```

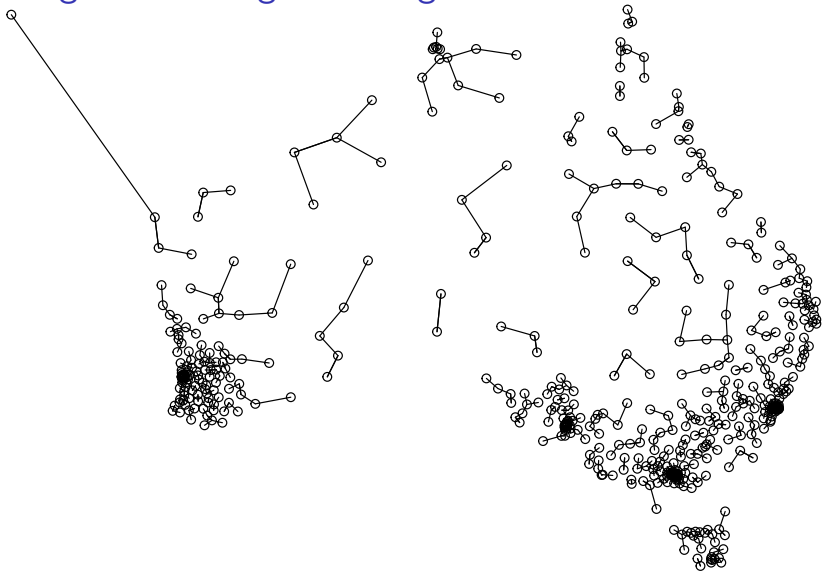
# HeatMap - Maps with Structural Breaks

```
## Joining, by = "id"
```



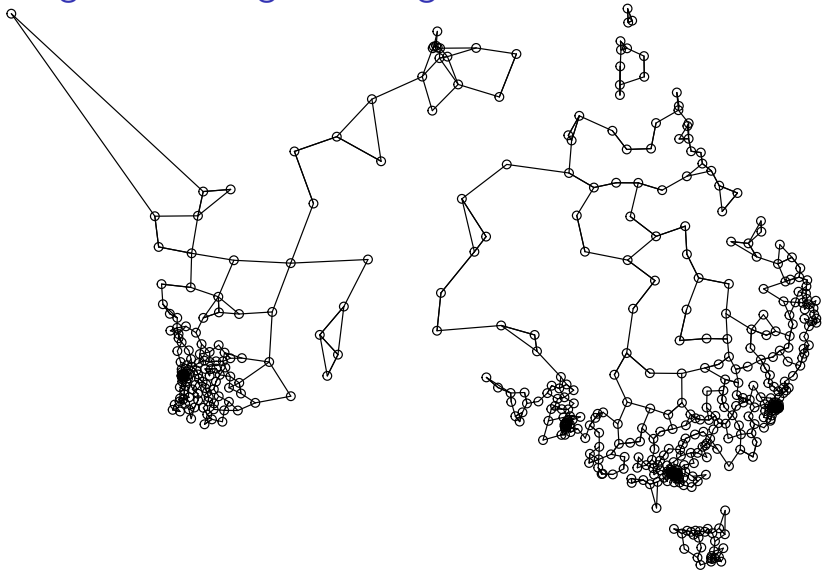
```
## [1] 1090
```

## Plotting nearest neighbors neighbours K=1



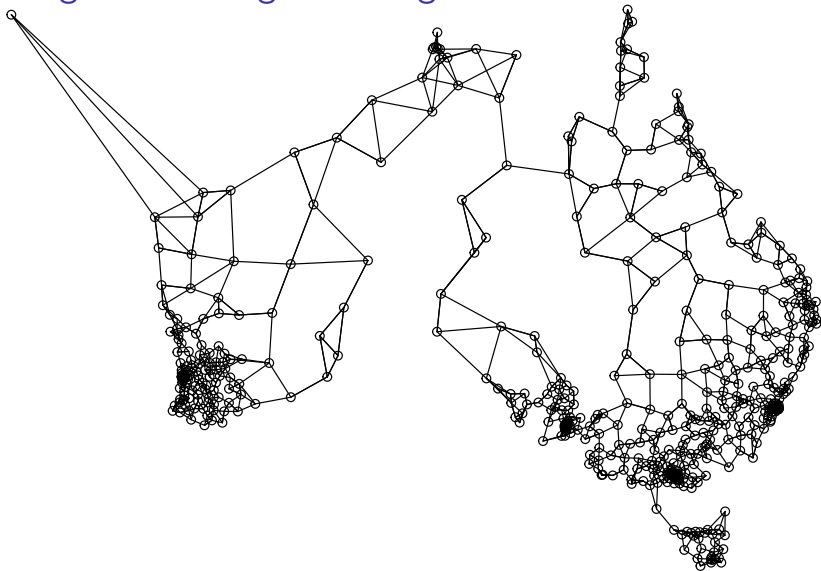
## [1] 1612.478

## Plotting nearest neighbors neighbours K=2



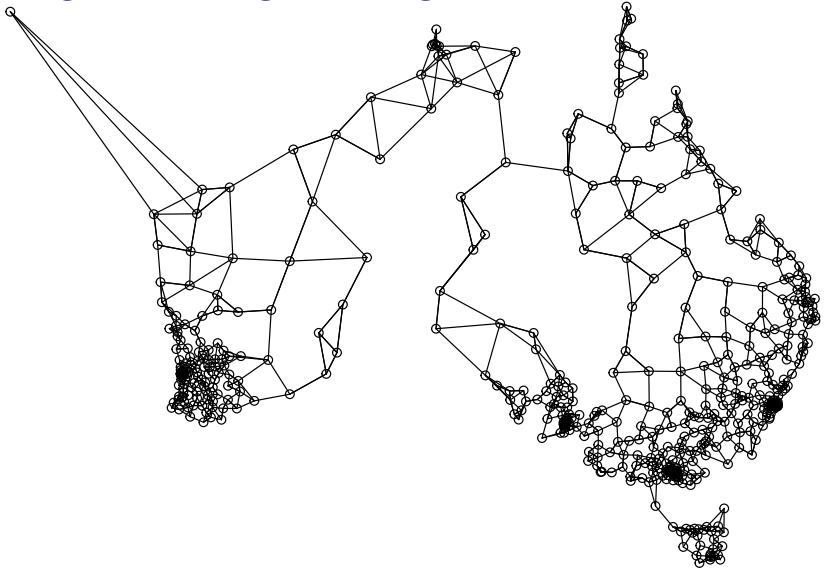
## [1] 1690.147

## Plotting nearest neighbors neighbours $K=3$



## [1] 1778.608

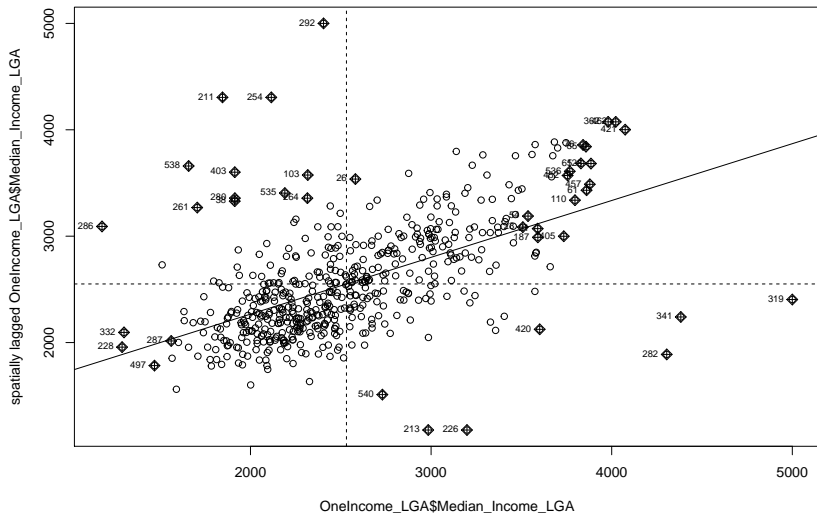
## Plotting nearest neighbors neighbours $K=4$



## [1] 1792.845



# Moran Scatterplot



## Local Moran

##	Ii	E.Ii	Var.Ii
##	Min. : -4.079221	Min. : -0.001838	Min. : 0.3305
##	1st Qu.: -0.000144	1st Qu.: -0.001838	1st Qu.: 0.4966
##	Median : 0.258115	Median : -0.001838	Median : 0.9951
##	Mean : 0.534091	Mean : -0.001838	Mean : 0.7399
##	3rd Qu.: 0.739304	3rd Qu.: -0.001838	3rd Qu.: 0.9951
##	Max. : 7.714157	Max. : -0.001838	Max. : 0.9951
##	Z.Ii	Pr(z > 0)	
##	Min. : -6.642709	Min. : 0.0000	
##	1st Qu.: 0.001698	1st Qu.: 0.1726	
##	Median : 0.299093	Median : 0.3824	
##	Mean : 0.646667	Mean : 0.3524	
##	3rd Qu.: 0.944061	3rd Qu.: 0.4993	
##	Max. : 10.794443	Max. : 1.0000	

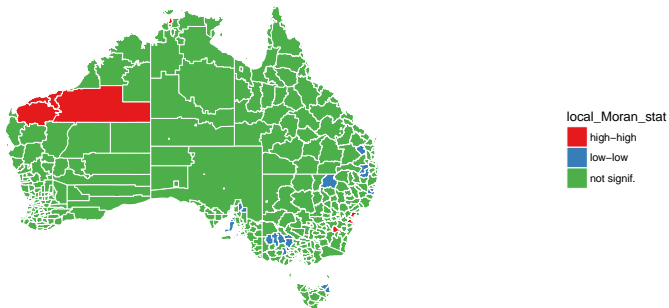
## Local Significance Plot using Moran's Statistic

```
## # A tibble: 3 x 2
##   local_Moran_stat      n
##   <chr>             <int>
## 1 high-high         51
## 2 low-low           25
## 3 not signif.      469
```

# Local Significance Plot using Moran's Statistic

```
## Joining, by = c("LGA_2016", "Median_Income_LGA", "Median
```

```
## Joining, by = "id"
```



## Local Significance Plot using Gi star Statistic

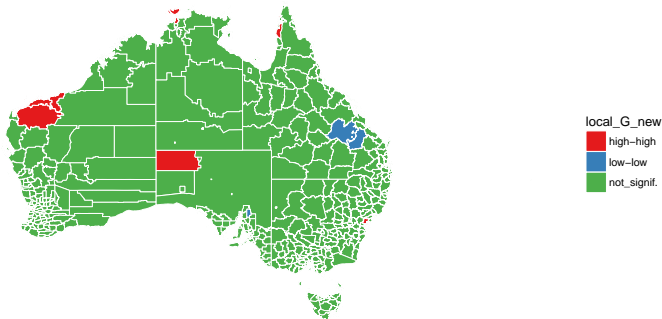
```
##      Min.  1st Qu.  Median    Mean  3rd Qu.    Max.
## -2.49074 -0.78212 -0.16746  0.04306  0.79739  4.51540
```

```
## # A tibble: 3 x 2
##   local_G_new      n
##   <fct>         <int>
## 1 high-high      35
## 2 low-low        4
## 3 not_signif.   506
```

# Local Significance Plot using Gi star Statistic

```
## Joining, by = c("LGA_2016", "Median_Income_LGA", "Median
```

```
## Joining, by = "id"
```



## Regions spatially significant in local Moran and not in local Gi star

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x

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Bayside (C)

Boroondara (C)

Camden (A)

Canada Bay (A)

Cockburn (C)

East Fremantle (T)

East Pilbara (S)

Georges River (A)

Hornsby (A)

Inner West (A)

Joondalup (C)

Manningham (C)

Melville (C)

Nillumbik (S)

Subiaco (C)

## Regions spatially significant in local Moran and not in local Gi star

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x

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Anangu Pitjantjatjara (AC)

Armadale (C)

Aurukun (S)

Mapoon (S)

Tiwi Islands (R)

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