

# Update on simulation results and queries

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Designs

$D_{null}$  (No difference in distribution)  
 $D_{var_f}$  (Difference in distribution only across facets)  
 $D_{var_x}$  (Difference in distribution only across x-axis)  
 $D_{var_{all}}$  (Difference in distribution in both facets and x-axis)

## 1 Recap of last week

### 1.1 What worked?

We saw the effect on raw wpd for different choices of tuning parameter ( $\lambda$ ) and effect of different increments ( $\omega$ ). We saw that raw wpd has least values for null design  $D_{null}$  and gradually increase with more deviation from the null case with maximum for  $D_{var_{all}}$  (which was great). Values of  $\lambda$  for which  $D_{var_x}$  and  $D_{var_f}$  interact is 0.5 (nice as that's what we were expecting). Moreover, the raw wpd values increase with increasing  $\lambda$  for  $D_{var_x}$  and decrease with increasing  $\lambda$  for  $D_{var_f}$  (as expected since the measure is linearly related to  $\lambda$ .)

## 1.2 What didn't work?

Though the distribution of wpd remains the same with normal distribution with different means just by scaling the data as a preprocessing step. The same doesn't happen for a Gamma distribution where the location of the distribution changes with different locations of the Gamma distribution. Box-cox transformations on the raw data did not work. It was suggested that we try out quantile transformation to bring back the quantiles of the raw data to standard normal.

## 2 Results from this week

### 2.1 What worked?

- Preprocess data: quantile transformation of the data to standard normal.

[Sort the sample  $x_{(1)}, x_{(2)}, \dots, x_{(n)}$ . Estimate the cumulative probabilities for each point  $p_{(1)}, p_{(2)}, \dots, p_{(n)}$  such that  $p_{(i)} = P(X < x_{(i)})$ . Transform each observation  $x_{(i)}$  into observation  $y_{(i)} = \Phi^{-1}(p_{(i)})$ , where  $\Phi^{-1}$  is the inverse of the cumulative distribution of a standard normal distribution.]

(\*\* All of this is being done by the R function `qqnorm`. I checked that data from different distribution ( $z$ ) could be transformed to normal using `qqnorm(z)$x`. Please let me know if you think I am missing anything here\*\*)

- check if the distribution of the raw wpd starting from a Gamma (0,5, 1) and Gamma(2, 1) distribution looks similar to the distribution of the raw wpd starting from a N(0,1) distribution. (More or less it does, yippee. **(Please let me know if you think I am missing anything here Figure 4, Figure 5)**)
- how mean and sd of the distribution of raw wpd changes with increasing x-axis and facet categories - more understanding of which normalisation process to choose. (Figure 2)
- Now that quantile transformation has worked, we wanted to check which process of normalization works. Suppose  $\{d_1, d_2, \dots, d_D\}$  are the JS distances from a panel

a)  $wpd_{norm1} = wpd / \log(D)$

b)  $wpd_{norm2} = wpd - \text{mean}(wpd^*) / \text{sd}(wpd^*)$ , where  $wpd^*$  's are obtained by shuffling the data. The distribution of  $wpd_{norm2}$  is expected to have similar mean and sd for different x-axis and facet categories.

Approach a) did not work. But Approach b) is working. **(Please let me know if you think I am missing something in my conclusions by looking at Figure 8, Figure 7, Figure 6 )**

### 2.2 To do now?

#### 2.2.1 Alternate designs

Behavior of  $wpd_{norm2}$  under different designs need to be monitored. Designs need to be constructed such that there is no **confounding factors** while deciding how distribution of  $wpd_{norm2}$  changes with different x-axis and facet categories.

•

$$\mu_j = \mu + j\omega$$

(for design vary\_x)

- 

$$\mu_{.k} = \mu + k\omega$$

(for design vary\_f)

If the designs are like the above, it would mean that mean and sd of the panels would also increase when x-axis and facet categories increase.

One way to keep mean comparable across situations would be to do the following (as discussed last with Di) Suppose we will allow a highest mean difference of  $M$  unit for each panels, which means panels with different x-axis and facet categories would also have a highest mean difference of  $M$  units.

For example, if  $M = 5$  and design =  $D_{var_x}$  then

$$\mu_{j.} = \mu + j\omega$$

- $\omega = 5$ , for  $nx = 2$
- $\omega = 5/2$ , for  $nx = 3$
- $\omega = 5/3$ , for  $nx = 4$  and so on.

Should we be bothered about it or not since we are pre-processing the data to start with?

### 2.2.2 Structuring the simulation section of the paper

Follow the story line like this one? **Or you suggest some other ways?**

## 3 Detail results:

**Assumptions:** There is no difference in distribution between any facet or x-category since it is the null design. Process is run  $nsim$  times to plot the distribution.  $nsim = 200$   $\lambda = 0.67$

**Questions:** - How raw value of wpd changes with different nx and nfacet for different location and scale of a Normal and non-normal distribution

### 3.1 Standard normal distribution

### 3.2 How mean and sd changes with increasing x-axis and facet levels?

### 3.3 Normal distributions with different means

### 3.4 Gamma Distribution with different locations before quantile transformation

### 3.5 Gamma Distribution with different locations after quantile transformation

### 3.6 Normalise by permuting data

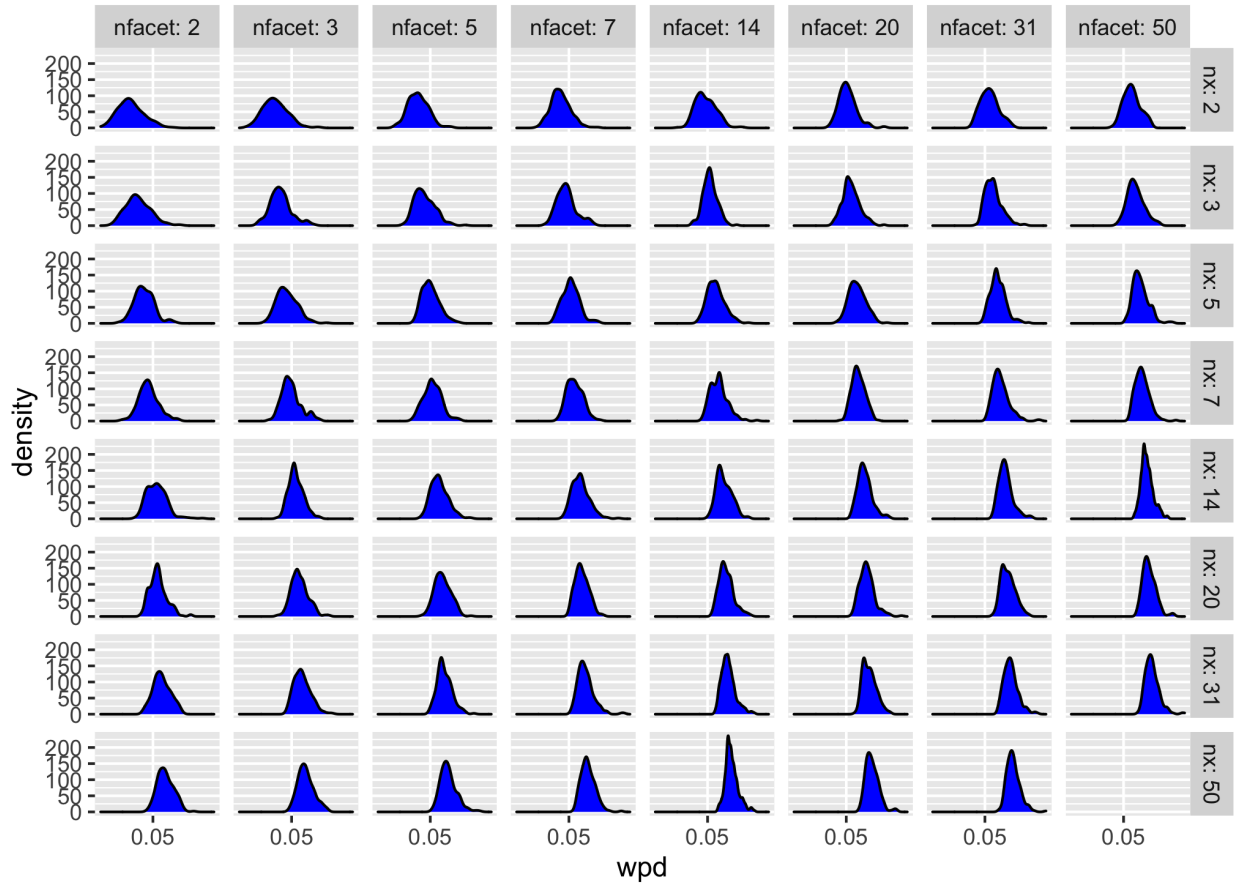


Figure 1: Density plots of raw wpd is shown for  $N(0,1)$  distribution. The densities change across different facet and x levels, which implies wpd value changes with increasing x and facet levels.

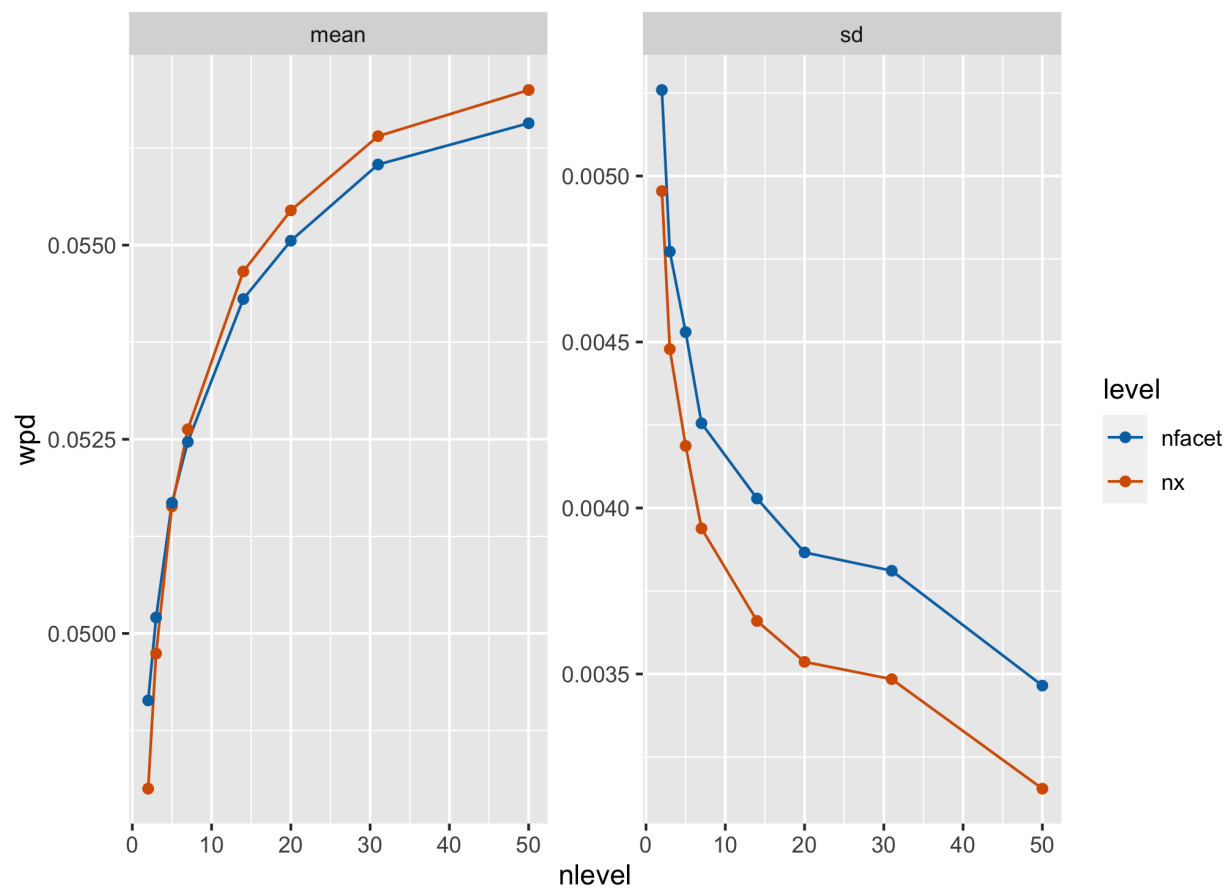


Figure 2: Movement of mean and sd for raw wpd is shown for different number of levels (nlevel) of x-axis and facets through line plots. Mean increases and sd decreases more sharply for increasing x-axis levels as compared to facet levels. It seems like both mean and standard deviation are affected more by change in the x-axis levels than the facet levels.

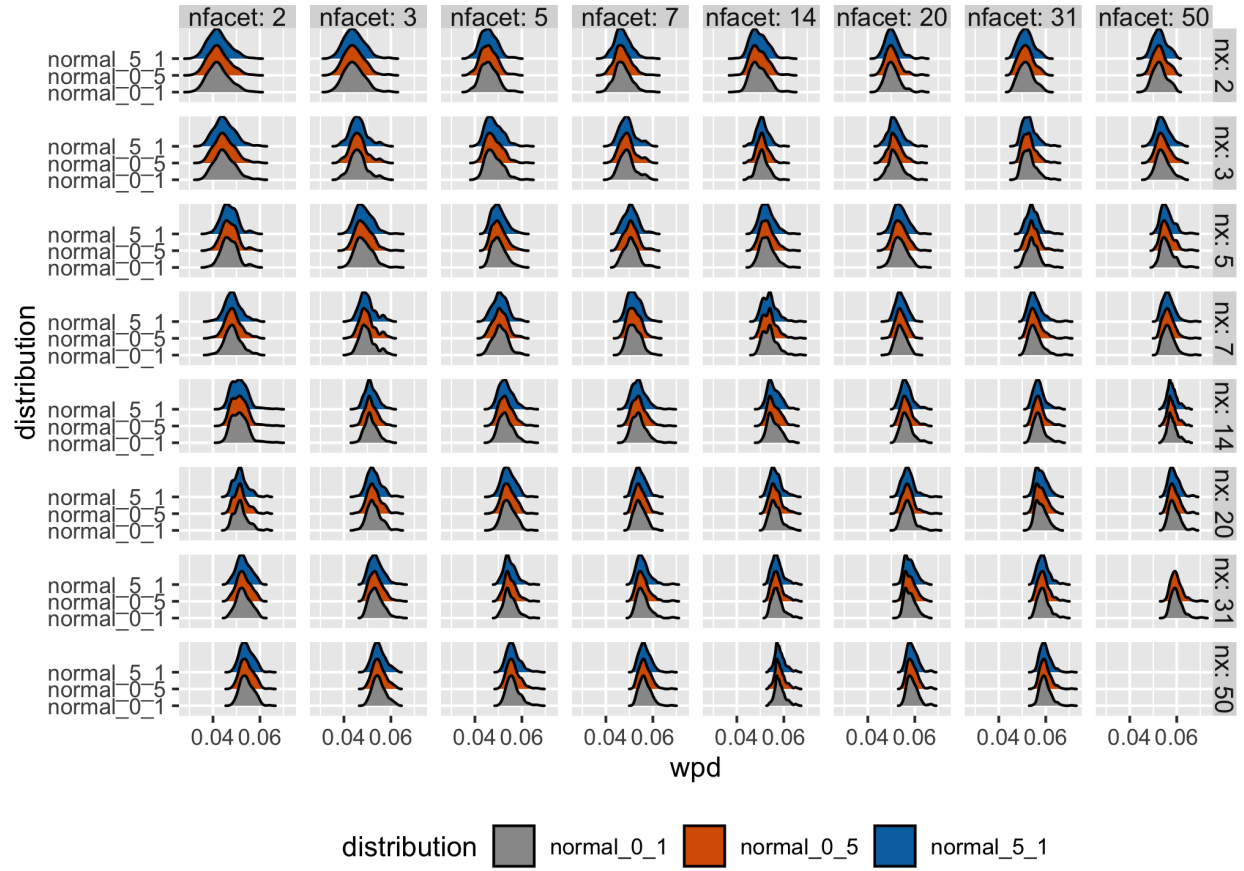


Figure 3: Ridge plots of raw wpd is shown for  $N(0,1)$ ,  $N(0,5)$  and  $N(5,1)$  distribution. The densities change across different facet and x levels but look same for the three normal distributions, which implies wpd value is unaffected by the change in mean value of the normal distribution.

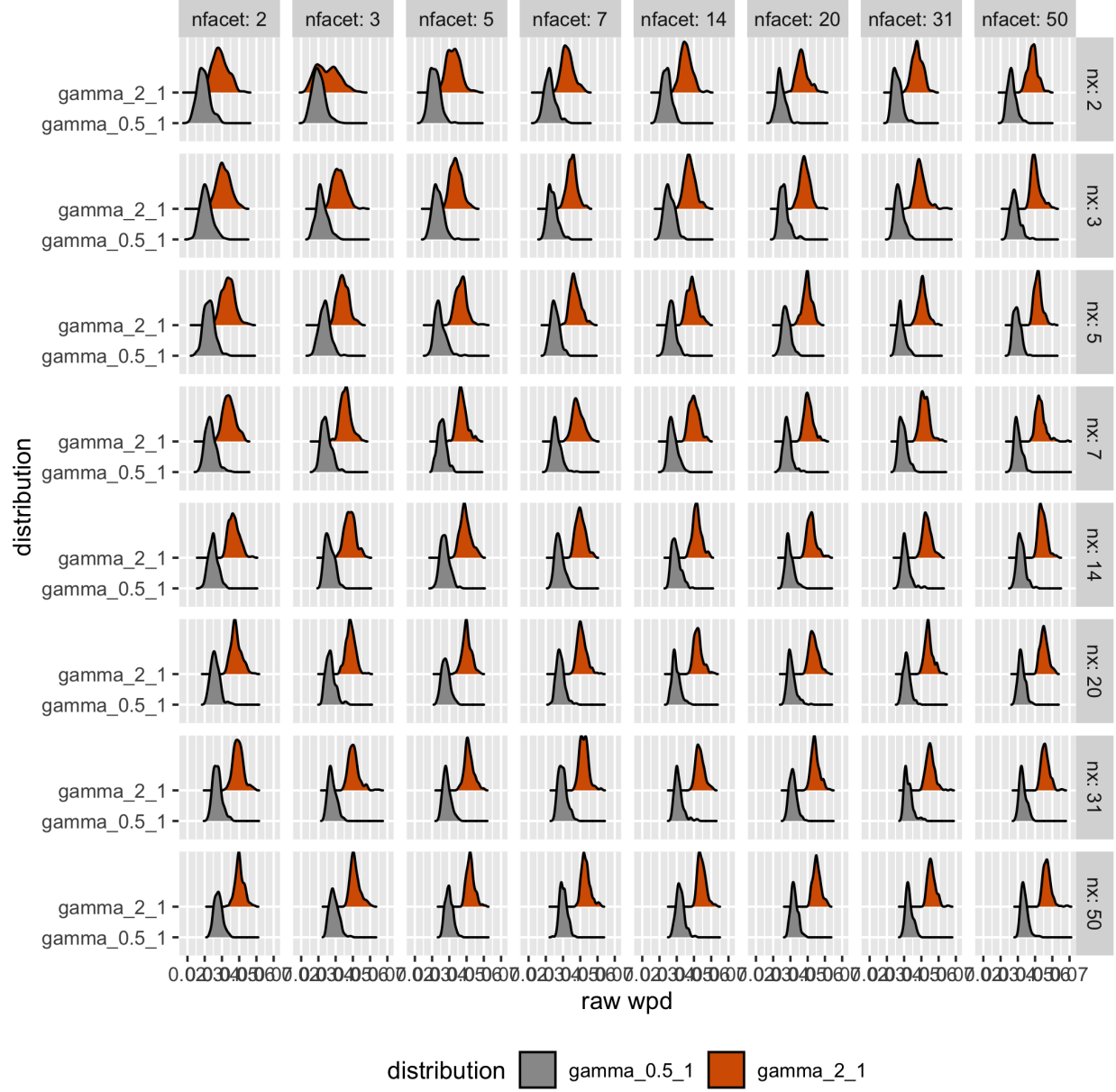


Figure 4: Ridge plots of raw wpd is shown for  $G(0.5,1)$  and  $G(2,1)$  distribution (before quantile transformation). The densities change across different facet and x levels and also for the two distributions, which implies wpd value is affected by the change in location value when distributions are not normal.

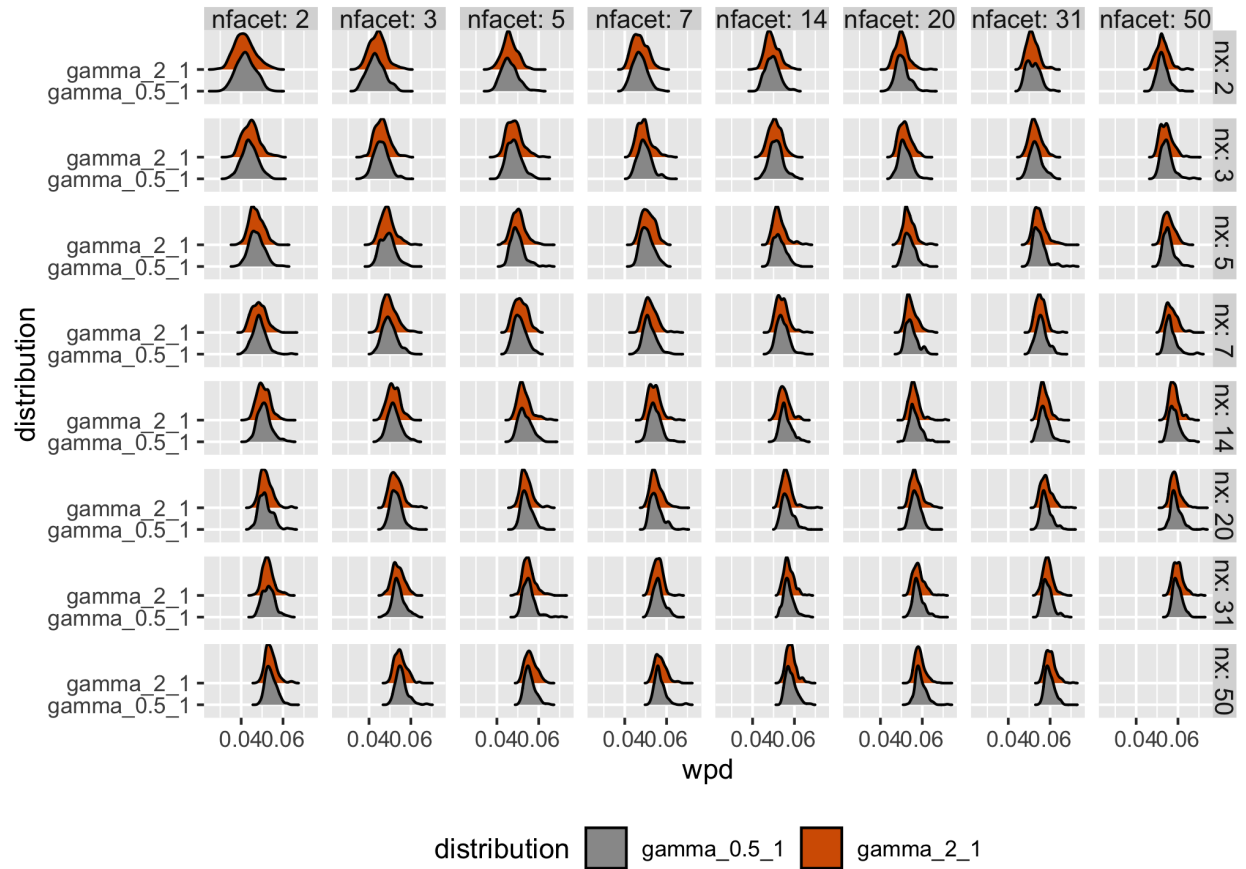


Figure 5: Ridge plots of raw wpd is shown for  $G(0.5,1)$  and  $G(2,1)$  distribution after quantile transformation looks similar and hence is unaffected by change in location.



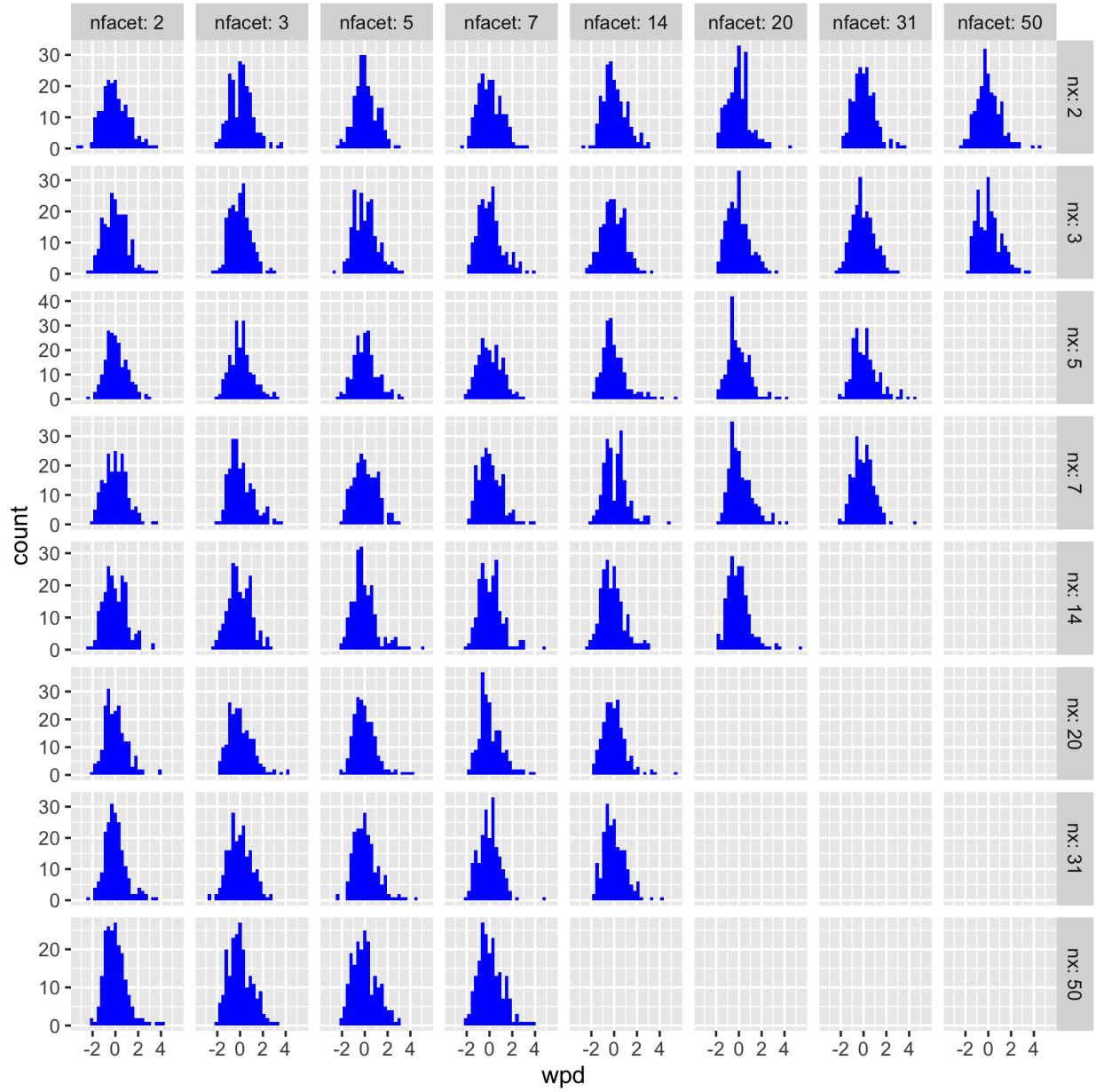


Figure 6: Density plots of normalised wpd is shown for Gamma(2,1) distribution. The mean and sd of the distribution looks almost similar for different facet and x-axis categories

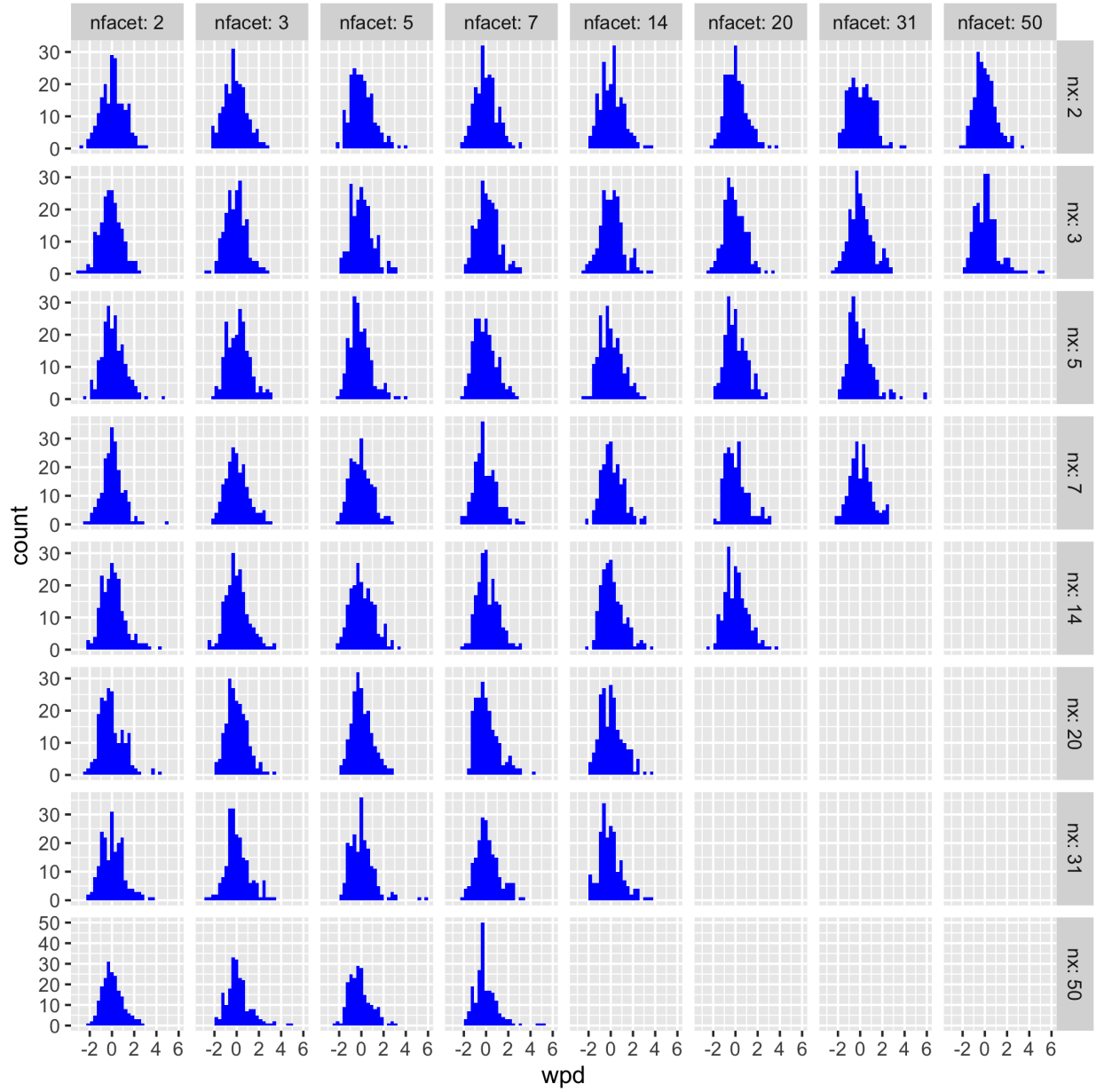


Figure 7: Density plots of normalised wpd is shown for Gamma(0.5,1) distribution, which is more skewed. The mean and sd of the distribution looks almost similar for different facet and x-axis categories

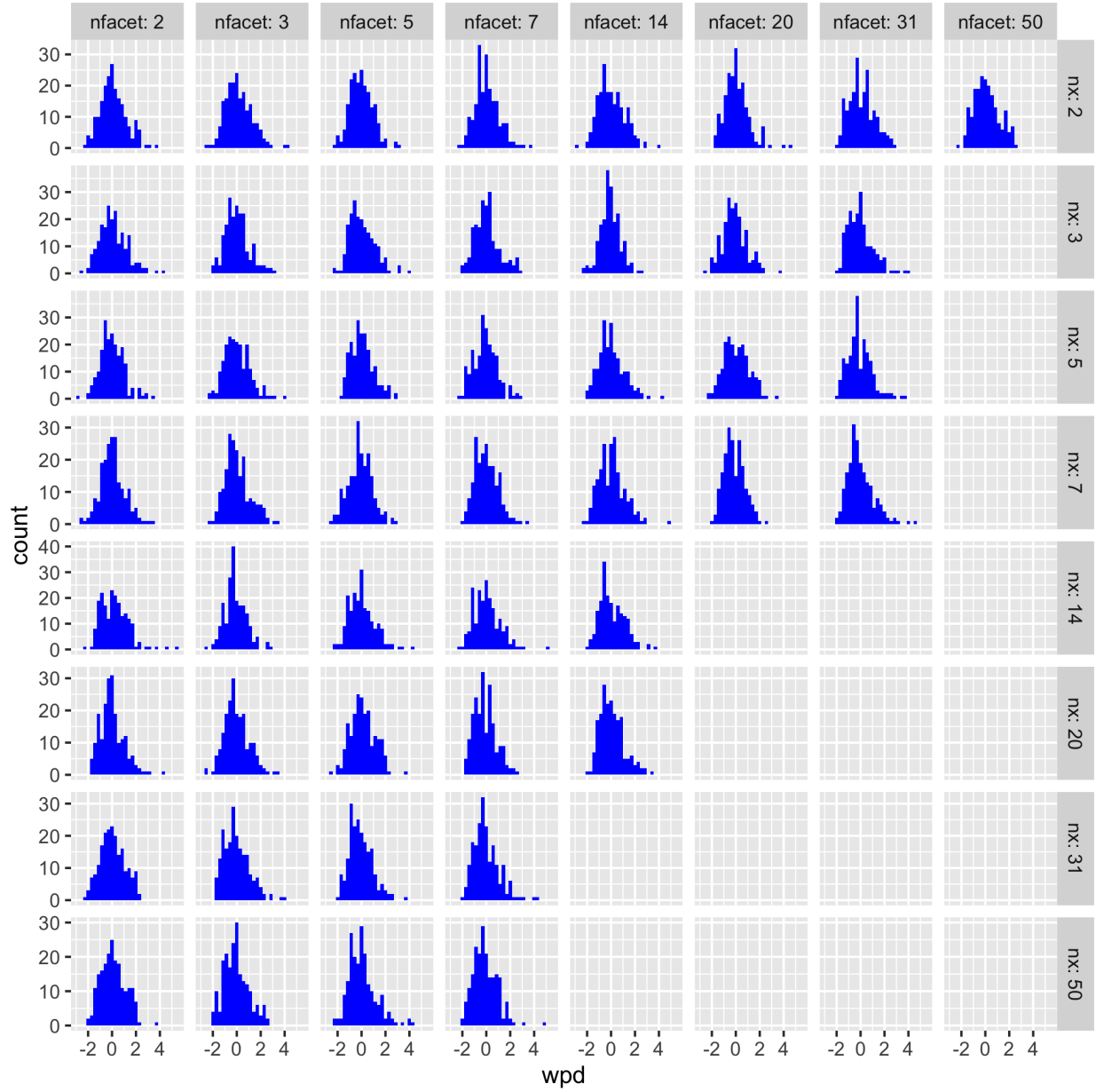


Figure 8: Density plots of normalised wpd is shown for Normal(0,1) distribution. The mean and sd of the distribution looks almost similar for different facet and x-axis categories.