

A new tidy data structure to support exploration and modeling of temporal data

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18 August 2019

JEL classification: C88, C81, C82, C22, C32

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Abstract

Mining temporal data for information is often inhibited by a multitude of formats: irregular or multiple time intervals, point events that need aggregating, multiple observational units or repeated measurements on multiple individuals, and heterogeneous data types. On the other hand, the software supporting time series modeling and forecasting, makes strict assumptions on the data to be provided, typically requiring a matrix of numerical data with implicit time indexes. Going from raw data to model-ready data is painful. This work presents a cohesive and conceptual framework for organizing and manipulating temporal data, which in turn flows into visualization, modeling and forecasting routines. Tidy data principles are extended to temporal data by: (1) mapping the semantics of a dataset into its physical layout; (2) including an explicitly declared index variable representing time; (3) incorporating a “key” comprising single or multiple variables to uniquely identify units over time. This tidy data representation most naturally supports thinking of operations on the data as building blocks, forming part of a “data pipeline” in time-based contexts. A sound data pipeline facilitates a fluent workflow for analyzing temporal data. The infrastructure of tidy temporal data has been implemented in the R package **tsibble**.

Keywords: time series, data wrangling, tidy data, R, forecasting, data science, exploratory data analysis, data pipelines

1 Introduction

Temporal data arrives in many possible formats, with many different time contexts. For example, time can have various resolutions (hours, minutes, and seconds), and can be associated with different time zones with possible adjustments such as daylight saving time. Time can be regular (such as quarterly economic data or daily weather data), or irregular (such as patient visits to a doctor’s office). Temporal data also often contains rich information: multiple observational units

of different time lengths, multiple and heterogeneous measured variables, and multiple grouping factors. Temporal data may comprise the occurrence of events, such as flight departures, that need to be reduced to a regular structure.

Despite this variety and heterogeneity of temporal data, current software typically requires time series objects to be model-oriented matrices. Analysts are expected to do their own data preprocessing and take care of anything else needed to allow model fitting, which leads to a myriad of ad hoc solutions and duplicated efforts.

Wickham & Grolemund (2016) proposed the tidy data workflow, which provides a conceptual framework for processing data (as described in Figure 1). Currently, time series modeling and forecasting enters this framework at the *modeling* stage, while temporal data enters at the start. This paper integrates time series analysis into this tidy framework, providing a coherent way for getting temporal data into the matrix format for modeling.

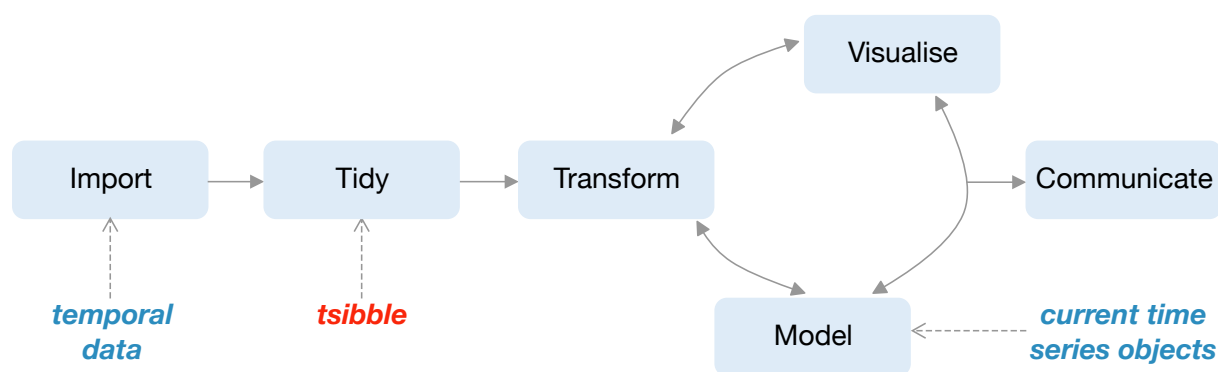


Figure 1: Illustration of the data science workflow, drawn from Wickham & Grolemund (2016), showing how current time series tools interface with the workflow and how the *tsibble* structure and tools integrate. The new data structure, *tsibble*, makes the connection between temporal data input, and specialist modeling formats. It provides elements at the “tidy” step, which produce tidy temporal data for time series visualization and modeling.

The paper is structured as follows. Section 2 reviews temporal data structures corresponding to time series and longitudinal analysis, and discusses “tidy data” and the grammar of data manipulation. Section 3 proposes contextual semantics for temporal data, built on top of tidy data. The concept of data pipelines with respect to the time domain will be discussed in depth in Section 4, followed by a discussion of the design choices made in the software structure in Section 5. Two case studies are presented in Section 6 illustrating temporal data exploration using the newly implemented infrastructure. Section 7 discusses future work.

2 Data structures

2.1 Time series and longitudinal data

Temporal data problems are typically grouped into two types of analysis, time series and longitudinal. Despite being exactly the same data input, the representation of time series and longitudinal data diverges due to different modeling approaches.

Time series can be univariate or multivariate, and for modeling require relatively long lengths (i.e., large T). Time series researchers and analysts who are concerned with this large T property, are mostly concerned with stochastic processes, for the primary purpose of forecasting, and characterizing temporal dynamics. Most statistical software represent such time series as vectors or matrices. Multivariate time series are typically assumed to be in the format where each row is assumed to hold observations at a time point and each column to contain a single time series. (The tidy data name for this would be **wider format**.) This implies that data are columns of homogeneous types: numeric or non-numeric, but there are limited supporting methods for non-numeric variables. In addition, time indexes are stripped off the data and implicitly inferred as attributes or meta-information. There is a strict requirement that the number of observations must be the same across all the series. Data wrangling, from the form that data arrives in, to this specialist format, can be frustrating and difficult, inhibiting the performance of downstream tasks.

For longitudinal analysis, researchers and analysts are primarily interested in explaining trends across and variations among individuals, and making inference about a broader population. Longitudinal data or panel data typically assumes fewer measurements (small T) over a large number of individuals (large N). It often occurs that measurements for individuals are taken at different time points, resulting in an unbalanced panel. Thus, the primary format required for modeling such data is stacked series, blocks of measurements for each individual, with columns indicating individual, times of measurement and the measurements themselves. (The tidy data name for this would be **longer format**.) Evidently, this data organization saves storage space for many sparse cells, compared to structuring it into wider format which would have missing values in many cells. A drawback of this format is that information unique to each individual is often repeated for all time points. An appealing feature is that data is structured in a semantic manner with reference to observations and variables, with the time index stated explicitly. This opens the door to easily operating on time to make calculations and extract different temporal

components, such as month and day of the week. It is conducive to examining the data in many different ways and leading to more comprehensive exploration and forecasting.

2.2 Tidy data and the grammar of data manipulation

Wickham (2014) coined the term “tidy data”, which is a rephrasing of the second and third normal forms in relational databases but in a way that makes more sense to data scientists by referring rows to observations and columns to variables. The principles of “tidy data” attempt to standardize the mapping of the semantics of a dataset to its physical representation. This data structure is the fundamental unit of the **tidyverse**, which is a collection of R packages designed for data science. The ubiquitous use of the **tidyverse** is testament to the simplicity, practicality and general applicability of the tools. The **tidyverse** provides abstract yet functional grammars to manipulate and visualize data in easier-to-comprehend form. One of the **tidyverse** packages, **dplyr** (Wickham et al. 2019), showcases the value of a grammar as a principled vehicle to transform data for a wide range of data challenges, providing a consistent set of verbs: `mutate()`, `select()`, `filter()`, `summarize()`, and `arrange()`. Each verb focuses on a singular task. Most common data tasks can be rephrased and tackled with these five key verbs, by composing them sequentially.

The **tidyverse** largely formalizes exploratory data analysis. Many in the R community have adopted the **tidyverse** way of thinking and extended it to broader domains, such as simple features for spatial data in the **sf** package (Pebesma 2018) and missing value handling in the **nanian** package (Tierney & Cook 2018). This paper and the associated **tsibble** R package (Wang, Cook & Hyndman 2019) extends the tidy way of thinking to temporal data.

2.3 Existing time series standards in R

Current standards, provided by the native **ts** object in R, and extended by **zoo** (Zeileis & Grothendieck 2005) and **xts** (Ryan & Ulrich 2018), assemble temporal data into matrices with implicit time indexes. These objects were designed for modeling methods. The diagram in the style of Figure 1 would place the model at the center of the analytical universe, and all the transformations and visualizations would hinge on that format. This is contrary to the **tidyverse** conceptualization, which holistically captures the full data workflow.

A new temporal data class is needed in the upstream of the workflow, which could incorporate all the downstream modules. A relatively new R package **tibbletime** (Vaughan & Dancho 2018b) proposed a data class of *time tibble* to represent temporal data in heterogeneous tabular format.

It only requires an index variable to declare a temporal data object, thus placing it at the import stage. However, as proposed in Section 3 a more rigid data structure is required for time series analytics and models.

This paper describes a new tidy representation to encompass both time series and longitudinal data, and a unified framework to streamline the workflow from data preprocessing to visualization and forecasting, as an integral part of a tidy data analysis.

3 Contextual semantics

The choice of tidy representation of temporal data arises from a data- and model-oriented perspective, which can accommodate all of the operations that are to be performed on the data in time-based contexts. Figure 1 marks where this new abstraction is placed in the “tidy” model, which is referred to as a “tsibble”. Adhering to the “tidy data” principles, in tsibble:

1. Index is a variable with inherent ordering from past to present.
2. Key is a set of variables that define observational units over time.
3. Each observation should be uniquely identified by index and key.
4. Each observational unit should be measured at a common interval, if regularly spaced.

Figure 2 sketches out the data form required for a tsibble, an extension of the “tidy” format to the time domain. Beyond the layout, tsibble gives the contextual meaning to variables in order to construct the temporal data object, as newly introduced “index” and “key” semantics stated in the definitions 1 and 2 above. Variables other than “index” and “key” are considered as measurements. The definitions of 3 and 4 imply that tsibble is *tidier* than “tidy data”, positioning itself as a model input that gives rise to more robust and reliable downstream analytics.

index	key		measurements	

Figure 2: The architecture of the tsibble structure is built on top of the “tidy data” principles, with temporal semantics: index and key.

To materialize the abstraction of the tsibble, a subset of tuberculosis cases estimated by World Health Organization (2018) presented in Table 1 is used as an example. It contains 12 observations and 5 variables landing in a tidy data form. Each observation comprises the number of

people who are diagnosed with tuberculosis for each gender at three selected countries in the years of 2011 and 2012. From tidy data to tsibble data, “index” and “key” should be declared: column `year` as the “index” variable, and column `country` together with `gender` as the “key” variable forming the observational units. Column `count` is the only measured variable in this data, but the data structure is sufficiently flexible to hold more measurements; for example, slotting the corresponding population size (if known) into the data column for normalizing the count later. Note this data further satisfies the must-have for the distinct rows determined by index and key, and regularly spans over one-year interval.

Table 1: *A small subset of estimates of tuberculosis burden collected by World Health Organization in 2011 and 2012, with 12 observations and 5 variables. The index refers to column `year`, the key to multiple columns: `country` and `gender`, and the measured variable to column `count`.*

country	continent	gender	year	count
Australia	Oceania	Female	2011	120
Australia	Oceania	Female	2012	125
Australia	Oceania	Male	2011	176
Australia	Oceania	Male	2012	161
New Zealand	Oceania	Female	2011	36
New Zealand	Oceania	Female	2012	23
New Zealand	Oceania	Male	2011	47
New Zealand	Oceania	Male	2012	42
United States of America	Americas	Female	2011	1170
United States of America	Americas	Female	2012	1158
United States of America	Americas	Male	2011	2489
United States of America	Americas	Male	2012	2380

The new tsibble structure bridges the gap between wild temporal data and the tamed state of model inputs. The proposed contextual semantics is the new addition to tidy data in order to support more intuitive time-related manipulations and enlighten new perspectives for time series and panel model inputs. Index, key and time interval build the three stone pillars to this new semantically structured temporal data. Each is now described in more detail.

3.1 Index

Index is a variable with inherent ordering from past to present.

Time provides the contextual basis for temporal data. Time can be seen in numerous representations, from sequential numerics to the most commonly accepted date-times. Regardless of this diversity, time should be inherently ordered from past to present, so should the index variable to a tsibble.

Index is an explicit data variable rather than a masked attribute (such as in the `ts` and `zoo` classes), exposing a need for more accessible and transparent time operations. It is often to visualize and model seasonal effects of measurements of interest, meaning that time components such as time of day and day of week from the index should be easily extracted upon request. But when the index is available only as meta information, an obstacle is inevitably created for analysts to write such simple queries in an ad hoc and programmatic manner. From an analytical point of view it should be discouraged.

3.2 Key

Key is a set of variables that define observational units over time.

What subjects/entities to be observed over time leads to the second component of a `tsibble`—key. Key can consist of empty, single, or multiple variables identifying units measured along the way. When only a single observational unit is present in the table, key can be left with no variables to be specified. However, when multiple units exist in the data, key should be supplied by identifying variables to sufficiently define the units. In longitudinal data, key can be thought of as “panel” (such as in the `Stata`) and is constrained to a single variable. In `tsibble`, key allows for multiple variables of nesting, crossing, or union relations (Wilkinson 2005) to be useful for forecasting reconciliation (Hyndman & Athanasopoulos 2017; Hyndman et al. 2018) and other advanced models. For example, Table 1 describes the number of tuberculosis cases for each gender across the countries every year. This suggests that the key comprises at least columns gender and country. Since country is nested within continent, it is a free variable to be included in the key specification.

Each observation should be uniquely identified by index and key.

Inspired by “primary key” (Codd 1970), a unique identifier for each observation in a relational database, `tsibble` key also uniquely identifies each observational unit over time. When constructing a `tsibble`, any duplicates of key-index (i.e. key-value) pairs will fail, because duplicates signal a data quality issue, which would likely affect subsequent analyses and hence decision making. For example, either gender or country alone is not enough to be the key for the tuberculosis data. Analysts are encouraged to better understand the data, or reason about the process of data cleaning when handling duplicates. Figure 3 peels the “tidy” module with clear routes required for a `tsibble`. The rigidity of `tsibble`, as the fundamental data infrastructure, warrants the validity of temporal data analysis for the later stage.

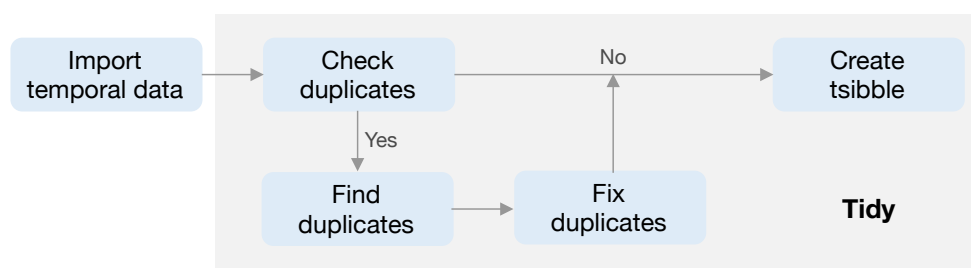


Figure 3: Details about the “tidy” stage for a tsibble. Built on top of “tidy data”, each observation should be uniquely identified by index and key, thereby no duplicated key-index pairs.

Since observational units are embedded, modelling and forecasting for each unit in a tsibble will be accelerated. The tsibble key plays a role of the central transit hub in connecting multiple tables managed by the data, models, and forecasts. This neatly decouples the expensive data copy from downstream summaries, significantly reducing the storage space.

3.3 Interval

Each observational unit should be measured at a common interval, if regularly spaced.

The principal divide of temporal data is regularly versus irregularly spaced data. Event data typically involves irregular time intervals, such as flight schedules or customer transactions. This type of data can flow into event-based data modeling, but would need to be processed or regularized to fit models that expect data with a fixed interval. When data indexed in regular time space, tsibble computes the greatest common divisor as the time interval from the index, or an unknown interval if one observation is available for each unit.

By extending one of the “tidy data” rules, “Each type of observational units should form a table”, each observational unit shares a common interval in a tsibble. Although tsibble reports one single interval despite data of fixed or mixed intervals, data of mixed intervals should be organized in separate tsibbles instead for well-tailored analysis and models.

This tiny piece of information will be carried over for tsibble-centric functions, for example to make implicit missing time handling handy and be in harmony with statistics and models that use seasonal periods.

4 Temporal data pipelines

A data pipeline describes the flow of data through an analysis, and can generally assist in conceptualizing the process for a stream of problems. Mcilroy, Pinson & Tague (1978) coined the term “pipelines” in software development while developing Unix at Bell Labs. In Unix-based computer operating systems, a pipeline chains together a series of operations based on their standard streams, so that the output of each program becomes the input to another. The Extract, Transform, and Load (ETL) process from recent data warehousing literature dating back to Kimball & Caserta (2011) outlines the workflow to prepare data for analysis, and can also be considered a data pipeline. Buja et al. (1988) describes a viewing pipeline for interactive statistical graphics, that takes control of the transformation from data to plot. Swayne, Cook & Buja (1998), Swayne et al. (2003), Sutherland et al. (2000), Wickham et al. (2010) and Xie, Hofmann & Cheng (2014) implemented data pipelines for the interactive statistical software **XGobi**, **GGobi**, **Orca**, **plumbr** and **cranvas**, respectively.

A fluent data pipeline anticipates a standard data structure. The **tsibble** data abstraction lays the plumbing for data analysis modules of transformation, visualization and modeling in temporal contexts. It provides a data infrastructure to a new ecosystem, **tidyverts**, a play on tidyverse that acknowledges the time series analysis purpose, in the spirit of “tidy data” to the **tidyverse**.

4.1 Transformation

The **tsibble** package not only provides a “tsibble” data object but also a domain specific language in R for transforming temporal data. It takes advantage of the wrangling verbs implemented in the **dplyr** package, and develops a suite of new tools for facilitating temporal manipulation with ease primarily in two aspects: implicit missingness handlers and time-aware aggregations.

Implicit missingness are values that should be present but are absent. Regarding regularly-spaced temporal data, data entries that should be available at certain time points but are missing, leaving gaps in time. It will be a problem when temporal models and operations like lag/lead are applied. A family of verbs help to explore implicit missing values and turn them into the state of explicitness to eliminate potential concerns, listed as follows:

- `has_gaps()` checks the existence of time gaps.
- `scan_gaps()` reveals all implicit missing observations.
- `count_gaps()` summarizes the time ranges that are absent from the data.
- `fill_gaps()` turns them into explicit ones, along with imputing by values or functions.

These verbs are evocative and of simple interface. They by default look into gaps for each individual time period. Switching on the option `.full = TRUE` will fill in the full-length time span, creating fully balanced panels with respect to longitudinal study.

The other key function, an adverb `index_by()`, is the counterpart of `group_by()` in **dplyr**, grouping and partitioning the index only. It is most useful to be used in conjunction with `summarize()`, and thus aggregations to upper-level time resolutions will take place. This combination automatically produces new index and interval, and helps to regularize data of irregular interval.

Besides new verbs, the **dplyr** vocabulary has been adapted and expanded to facilitate temporal transformations. The **dplyr** suite showcases the general-purpose verbs for effectively manipulating tabular data. But these verbs need handling with care due to the context switch. A perceivable difference is summarizing variables between normal data and tsibble using `summarize()`. The former will reduce to a single summary, whereas the latter will obtain the index and their corresponding summaries.

Attention has been paid to warning and error handling. The principle that underpins all the verbs is a tsibble in and a tsibble out, thereby striving to maintain a valid tsibble over the course of transformation. If the desired temporal ordering is changed by row-wise verbs (such as `arrange()` and `slice()`), a warning is broadcast. If a tsibble cannot be maintained in the output of a pipeline module (likely occurring to column-wise verbs), for example the index is dropped by `select()`-ing, an error informs users of the problem and suggests alternatives. This avoids surprising users and reminds them of the time context. In general, users who are already familiar with the **tidyverse**, should have less resistance to learning the new semantics and verbs.

4.2 Visualization

The **ggplot2** package (as the implementation of grammar of graphics) builds a powerful graphical system to declaratively visualize data. The data underpinning of **ggplot2** is tidy data, and in turn tsibble integrates well with **ggplot2**. The integration encourages more flexible graphics for exploring temporal structures via index, and individual or group differences via key.

Line charts are universally accepted for ordered data, such as time series plots or spaghetti plots, depending on the fields. But they end up with exactly the same grammar: chronological time mapped to the horizontal axis, and the interested measurement on the vertical axis, for each unit. Many specialist plots centering around time series or longitudinal data, hence can be described and re-created under the umbrella of the grammar and **ggplot2**.

4.3 Model

Modeling is crucial to explanatory and predictive analytics, where time series and longitudinal data analysis start to diverge. Nevertheless, `tsibble` as a model-oriented object can flow into both types of models, with new semantics (index and key) to be internally utilized.

Most time series models are univariate, such as ARIMA and Exponential Smoothing, modelling temporal dependency for each series independently. The **fable** package (**R-fable**) provides a tidy forecasting framework built on top of `tsibble` is under development, with the goal of promoting transparent and human-centered forecasting practices. With the presence of the key, `tsibble` holds many series. Since models are fundamentally scalable, the `model()` and `forecast()` generics will take care of fitting and forecasting univariate models to each series across time in a `tsibble` at once.

Panel data models, however, put emphases on overall, within, and between variations both across individuals and time. Fixed and random effects models can be developed in line with the **fable** design.

4.4 Summary

The `tsibble` abstraction provides a formal organization of forwarding tidy data to model-oriented temporal data. The supporting operations can be chained for sequencing analysis, articulating a data pipeline. As Friedman & Wand (2008) stated, “No matter how complex and polished the individual operations are, it is often the quality of the glue that most directly determines the power of the system.” A mini snippet below glues transformation and forecasting together, to envision the fluent pipeline. The `pedestrian` dataset [cite] contains hourly tallies of pedestrians at four counting sensors in 2015 and 2016 in inner Melbourne, available in the **tsibble** package.

```
pedestrian %>%  
  fill_gaps() %>% # turn implicit missingness to explicit  
  filter(year(Date_Time) == 2016) %>% # subset data of year 2016  
  model(arima = ARIMA(Count)) %>% # fit arima to each sensor  
  forecast(h = days(2)) # forecast 2 days ahead
```

The pipe operator `%>%` introduced in the **magrittr** package (Bache & Wickham 2014) chains the verbs, read as “then”. A sequence of functions are composed in a way that can be naturally read from left to right, which improves the code readability.

It coordinates a user's analysis making it cleaner to follow, and permits a wider audience to document the data analysis through code without getting lost in a jungle of computational intricacies. It helps (1) break up a big problem to into manageable blocks, (2) generate human readable analysis workflow, (3) avoid introducing mistakes, at least making it possible to trace them through the pipeline.

5 Software structure and design decisions

5.1 Data first

The primary force that drives the software's design choices is "data". All functions in the package **tsibble** start with data or its variants as the first argument, namely "data first". This lays out a consistent interface and addresses the significance of the data throughout the software.

Beyond the tools, the print display provides a quick and comprehensive glimpse of data in temporal context, particularly useful when handling a large collection of data. The contextual summary provided by the print function, shown below on the data from Table 1, contains (1) data dimension with its shorthand time interval, alongside time zone if date-times, (2) variables that constitute the "key" with the number of series. These details aid users in understanding their data better.

```
#> # A tsibble: 12 x 5 [1Y]
#> # Key:      country, gender [6]
#>   country    continent gender  year count
#>   <chr>      <chr>      <chr>  <dbl> <dbl>
#> 1 Australia Oceania   Female  2011   120
#> 2 Australia Oceania   Female  2012   125
#> 3 Australia Oceania   Male    2011   176
#> 4 Australia Oceania   Male    2012   161
#> 5 New Zealand Oceania   Female  2011    36
#> # ... with 7 more rows
```

5.2 Functional programming

Rolling window calculations are widely used techniques in time series analysis, and often apply to other applications. These operations are dependent on having an ordering, particularly time

ordering for temporal data. Three common types of variations for sliding window operations are:

1. **slide**: sliding window with overlapping observations.
2. **tile**: tiling window without overlapping observations.
3. **stretch**: fixing an initial window and expanding to include more observations.

Figure 4 shows the animations of rolling windows for sliding, tiling and stretching, respectively, on annual tuberculosis cases for Australia. A block of consecutive elements with a window size of 5 are initialized and started rolling sequentially till the end of series by computing average counts.

Figure 4: *An illustration of window of size 5 computing rolling averages over annual tuberculosis cases in Australia with respect to sliding, tiling and stretching. (Animation needs to be viewed with Adobe Acrobat Reader.)*

Rolling window uses a programming paradigm—functional programming, which is different from those table verbs listed in Table ???. Table verbs expect and return a `tsibble`, and does what the function name suggests. On the contrary, these rolling window functions could accept arbitrary input types and would return arbitrary sorts of output, depending on which method is put into the rolling window. For example, computing moving averages requires numerics and a function like `mean()`, and produces averaged numerics. However, rolling window regression takes a data frame and a linear regression method like `lm()`, and generates a complex object that contains coefficients, fitted values, and etc.

The **purrr** package (Henry & Wickham 2019a) provides a good example of functional programming in R. It provides a complete and consistent set of tools to iterate each element of a vector with a function. Rolling window does not just iterate but rolls over a sequence of elements, namely `slide()`, `tile()` and `stretch()`. `slide()` expects one input, `slide2()` two inputs, and `pslide()` multiple inputs. For type stability, the functions always return lists. Other variants including `*_lgl()`, `*_int()`, `*_dbl()`, `*_chr()` return vectors of the corresponding type, as well as `*_dfr()` and `*_dfc()` for row-binding and column-binding data frames respectively. Their multiprocessing equivalents prefixed by `future_*` enable rolling in parallel (Bengtsson 2019; Vaughan & Dancho 2018a). This family of functions empowers users to incorporate window-related operations in their workflows.

5.3 Modularity

Modular programming is adopted in the design of the **tsibble** package. Modularity benefits users by providing small focused and manageable chunks, and provides developers with simpler maintenance.

All user-facing functions can be roughly organized into three major chunks according to their functionality: vector functions (1d), table verbs (2d), and window family. Each chunk is an independent module, but works interdependently. Vector functions in the package mostly deal with time. The atomic functions (such as `yearmonth()` and `yearquarter()`) embedded in the `index_by()` table verb collapses a `tsibble` to a less granular interval. The substitution of another time function in the `index_by()` results in the aggregation of different time resolution. Since these time functions are not exclusive to a `tsibble`, they can be used in a variety of applications in conjunction with other packages. The extensible design of the `tsibble` package means that the table verbs can incorporate many third-party vector functions. It is also generally easier to

trace back the errors users encounter from separating 1d and 2d functions, and increase the code readability.

5.4 Extensibility

As a fundamental infrastructure, extensibility is a design decision that was employed from the start of **tsibble**'s development. Contrary to the “data first” principle for end users, extensibility is developer focused and would be mostly used in dependent packages, which heavily relies on S3 classes and methods in R (Wickham 2018). The package can be extended in two major aspects: custom index and new **tsibble** class.

Time representation could be arbitrary, for example R's native **POSIXct** and **Date** for versatile date-times, nano time for nanosecond resolution implemented in **nanotime** (Eddelbuettel & Silvestri 2018), and pure numbers in simulations. Ordered factors can also be a source of time, such as month names, January to December, and weekdays, Monday to Sunday. The **tsibble** package supports an extensive range of index types from numerics to nano time, but there might be custom indexes used for some occasions, for example school semesters. These academic terms vary from one institution to another, within an academic year which is defined differently from a calendar year. A new index would be immediately recognized by the software upon defining `index_valid()`, as long as it can be ordered from past to future. The interval regarding semesters is further outlined through `interval_pull()`. As a result, the rest of the software methods such as `has_gaps()` and `fill_gaps()` will have instant support for data that contains this new index.

The class of **tsibble** is an underlying basis of temporal data, and there is a demand for subclassing a **tsibble**. For example, a **fable** is actually an extension of a **tsibble**, mentioned in Section 4.3. A low-level constructor `new_tsibble()` provides a vehicle to easily create a new subclass. This new object itself is a **tsibble**. It perhaps needs more metadata than those of a **tsibble**, that gives rise to a new data extension, like prediction distributions to a **fable**. **Tsibble** verbs are also S3 generics. Developers will be able to implement these verbs for the new class, if necessary.

5.5 Tidy evaluation

The **tsibble** packages leverages the **tidyverse** grammars and pipelines through tidy evaluation (Henry & Wickham 2019c) via the **rlang** package (Henry & Wickham 2019b). In particular, the table verbs extensively use tidy evaluation to evaluate computation in the context of **tsibble** data and spotlights the “tidy” interface that is compatible with the **tidyverse**. This not only saves a

few keystrokes without explicitly repeating references to the data source, but the resulting code is typically cleaner and more expressive.

6 Case studies

6.1 On-time performance for domestic flights in U.S.A

The dataset of on-time performance for US domestic flights in 2017 represents event-driven data caught in the wild, sourced from US Bureau of Transportation Statistics (Bureau of Transportation Statistics 2018). It contains 5,548,445 operating flights with many measurements (such as departure delay, arrival delay in minutes, and other performance metrics) and detailed flight information (such as origin, destination, plane number and etc.) in a tabular format. This kind of event describes each flight scheduled for departure at a time point in its local time zone. Every single flight should be uniquely identified by the flight number and its scheduled departure time, from a passenger's point of view. In fact, it fails to pass the tsibble hurdle due to duplicates in the original data. An error is immediately raised when attempting to convert this data into a tsibble, and closer inspection has to be carried out to locate the issue. The **tsibble** package provides tools to easily locate the duplicates in the data with `duplicates()`. The problematic entries are shown below.

```
#>   flight_num sched_dep_datetime sched_arr_datetime dep_delay arr_delay
#> 1      NK630 2017-08-03 17:45:00 2017-08-03 21:00:00      140      194
#> 2      NK630 2017-08-03 17:45:00 2017-08-03 21:00:00      140      194
#>   carrier tailnum origin dest air_time distance origin_city_name
#> 1      NK  N601NK   LAX  DEN     107      862    Los Angeles
#> 2      NK  N639NK   ORD  LGA     107      733      Chicago
#>   origin_state dest_city_name dest_state taxi_out taxi_in carrier_delay
#> 1           CA      Denver          CO      69      13              0
#> 2           IL    New York          NY      69      13              0
#>   weather_delay nas_delay security_delay late_aircraft_delay
#> 1           0       194              0              0
#> 2           0       194              0              0
```

The issue was perhaps introduced when updating or entering the data into a system. The same flight is scheduled at exactly the same time, together with the same performance statistics but

different flight details. As flight NK630 is usually scheduled at 17:45 from Chicago to New York (discovered by searching the full database), a decision is made to remove the first row from the duplicated entries before proceeding to the tsibble creation.

This dataset is intrinsically heterogeneous, encoded in numbers, strings, and date-times. The tsibble framework, as expected, incorporates this type of data without any loss of data richness and heterogeneity. To declare the flight data as a valid tsibble, column `sched_dep_datetime` is specified as the “index”, and column `flight_num` as the “key”. As a result of event timing, the data are irregularly spaced, and hence switching to the irregular option is necessary. The software internally validates if the key and index produce distinct rows, and then sorts the key and the index from past to recent. When the tsibble creation is done, the print display is data-oriented and contextually informative, including dimensions, irregular interval (5,548,444 x 22) and the number of time-based observational units (NA).

```
#> # A tsibble: 5,548,444 x 22 [!] <UTC>
#> # Key:      flight_num [22,562]
```

Transforming a tsibble for exploratory data analysis with a suite of time-specific and general-purpose manipulation verbs can result in well-constructed pipelines. From the perspective of a passenger, for example, one needs to travel smart by choosing an efficient carrier to fly with and the time of day to avoid congestion. To explore this data, we drill down starting with annual carrier performance and followed by disaggregation to finer time resolutions.

Figure 5 visually presents the end product of aggregating the number of on-time and delayed flights to the year interval by carriers. This pipeline is initialized by defining a new variable if the flight is delayed, and involves summarizing the tallies of on-time and delayed flights for each carrier annually. To prepare the summarized data for a mosaic plot, it is further manipulated by melting new tallies into a single column. The flow chart (Figure 6) demonstrates the operations undertaking in the data pipeline. The input to this pipeline is a tsibble of irregular interval, and the output ends up with a tsibble of unknown interval (as each carrier ends up with only one annual summary). The final data set includes each carrier along with a single year, with the interval undetermined, which in turn feeds into the mosaic display. Note that Southwest Airlines (WN), as the largest carrier, operates less efficiently than Delta (DL).

A closer examination of some big airports across the US will give an indication of how well the busiest airports manage the outflow traffic on a daily basis. A subset that contains observations for Houston (IAH), New York (JFK), Kalaoa (KOA), Los Angeles (LAX) and Seattle (SEA)

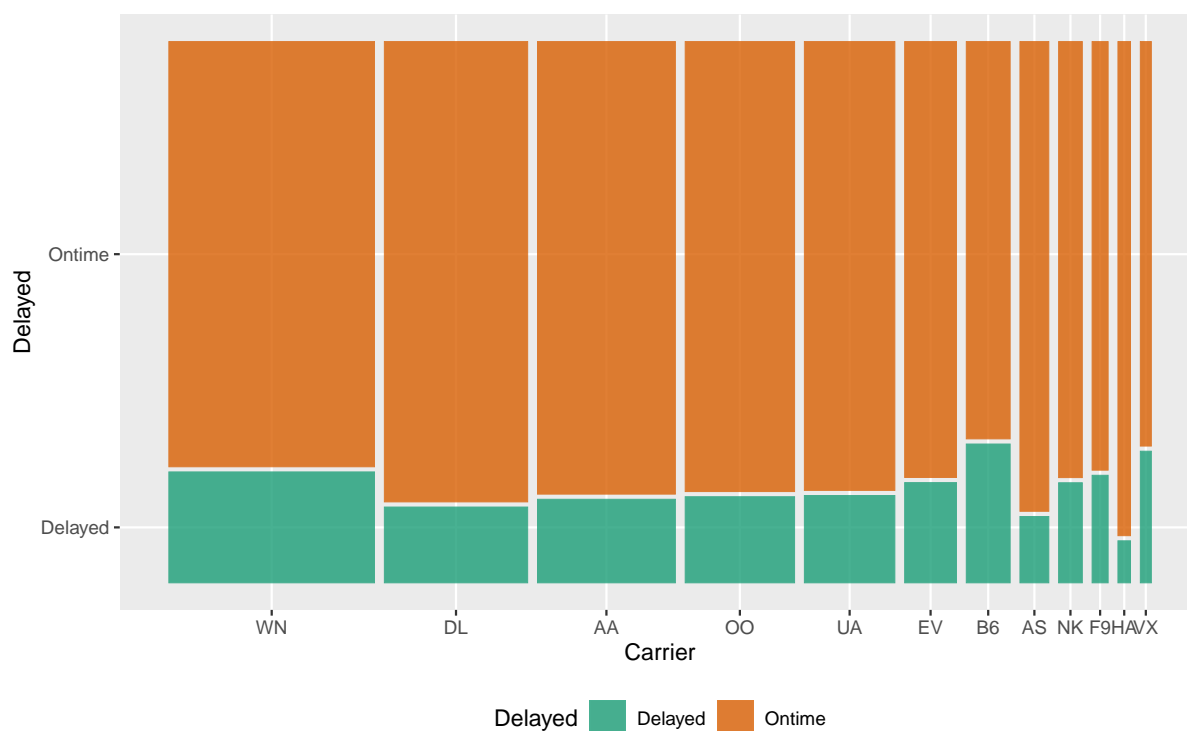


Figure 5: Mosaic plot showing the association between the size of airline carriers and the delayed proportion of departures in 2017. Southwest Airlines is the largest operator, but does not operate as efficiently as Delta. Hawaiian Airlines, a small operator, outperforms the rest.

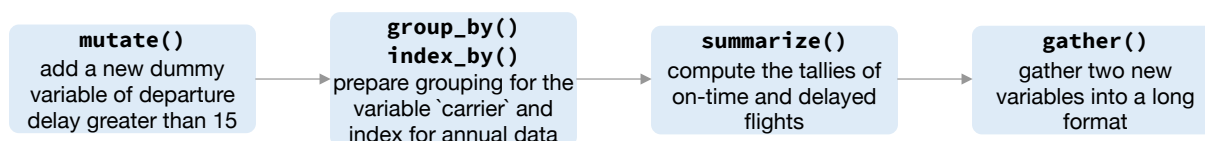


Figure 6: Flow chart illustrating the pipeline that preprocessed the data for creating Figure 5.

airports is obtained first. The succeeding operations compute delayed percentages every day at each airport, which are framed as grey lines in Figure 7. Winter months tend to fluctuate a lot compared to the summer across all the airports. Superimposed on the plot are two-month moving averages, so the temporal trend is more visible. The number of days for each month is variable. Moving averages for two months call for computing weighted mean. But this can also be accomplished using a pair of commonly used verbs—`nest()` and `unnest()` to handle list-columns, without weight specification. The sliding operation with a large window size smooths out the fluctuations and gives a stable trend around 25% over the year. LAX airport has seen a gradual decline in delays over the year, whereas the SEA airport has a steady number delays over time. The IAH and JFK airports have more delays in the middle of year, while the KOA has the inverse pattern with higher delay percentage in both ends of the year.

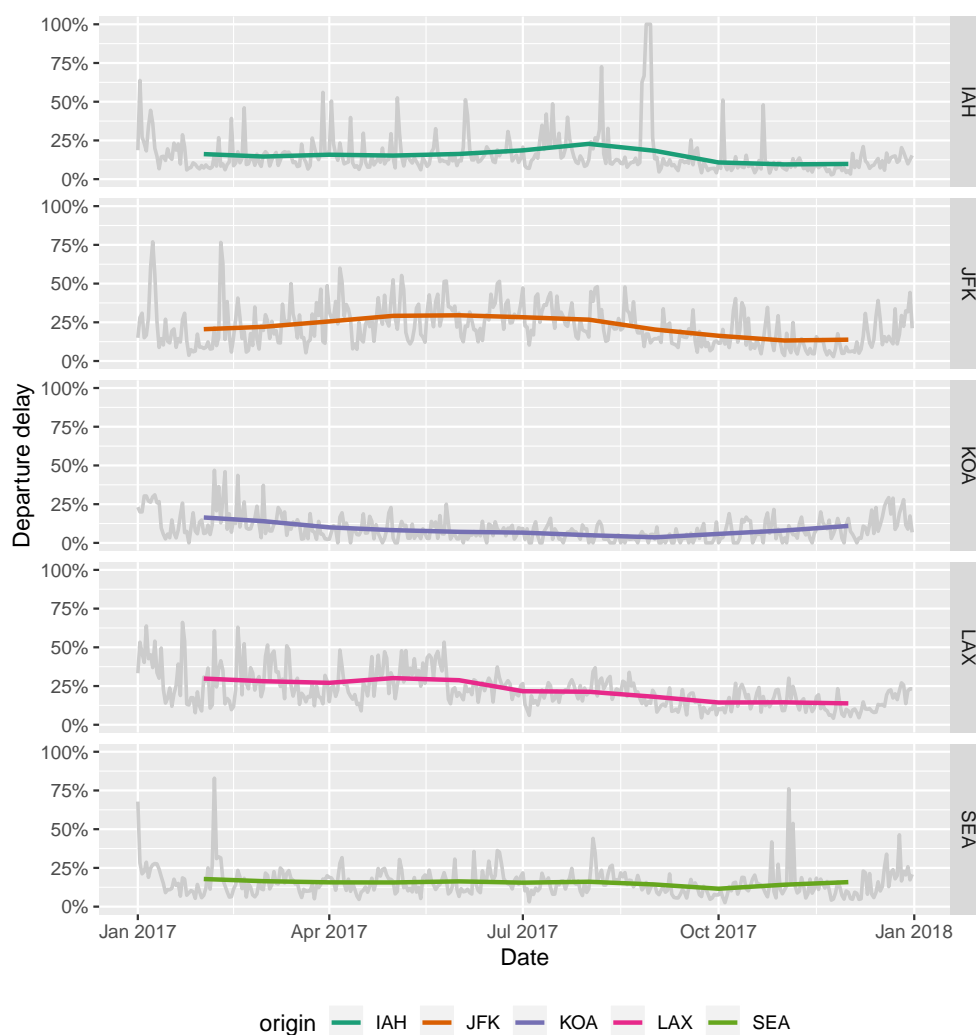


Figure 7: Daily delayed percentages for departure with two-month moving averages overlaid at five international airports. There are least fluctuations and relatively fewer delays observed at KOA airport. The estimates of temporal trend are around 25% across the other four airports, but highlight different time periods of severe delays.

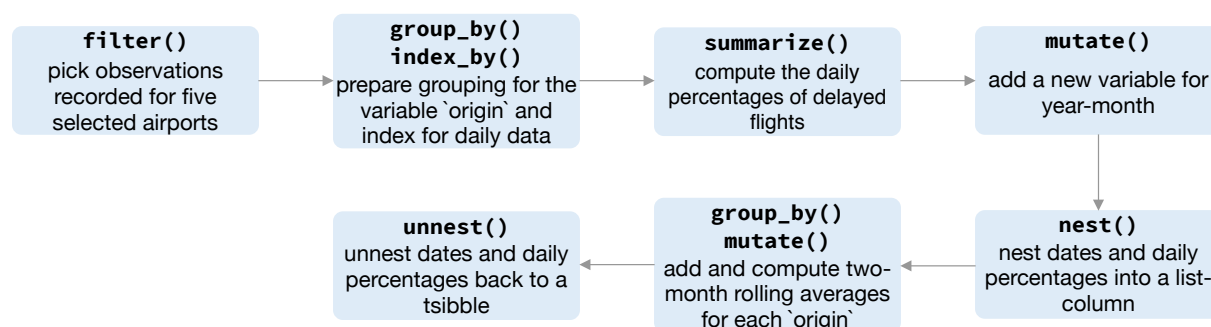


Figure 8: Flow chart illustrating the pipeline that preprocessed the data for creating Figure 7.

What time of day and day of week should we travel to avoid suffering from horrible delay? Figure 9 plots hourly quantile estimates across day of week in the form of small multiples. The upper-tail delay behaviors are of primary interest, and hence 50%, 80% and 95% quantiles are

shown. To reduce the likelihood of suffering a delay, it is recommended to avoid the peak hour around 6pm (18).

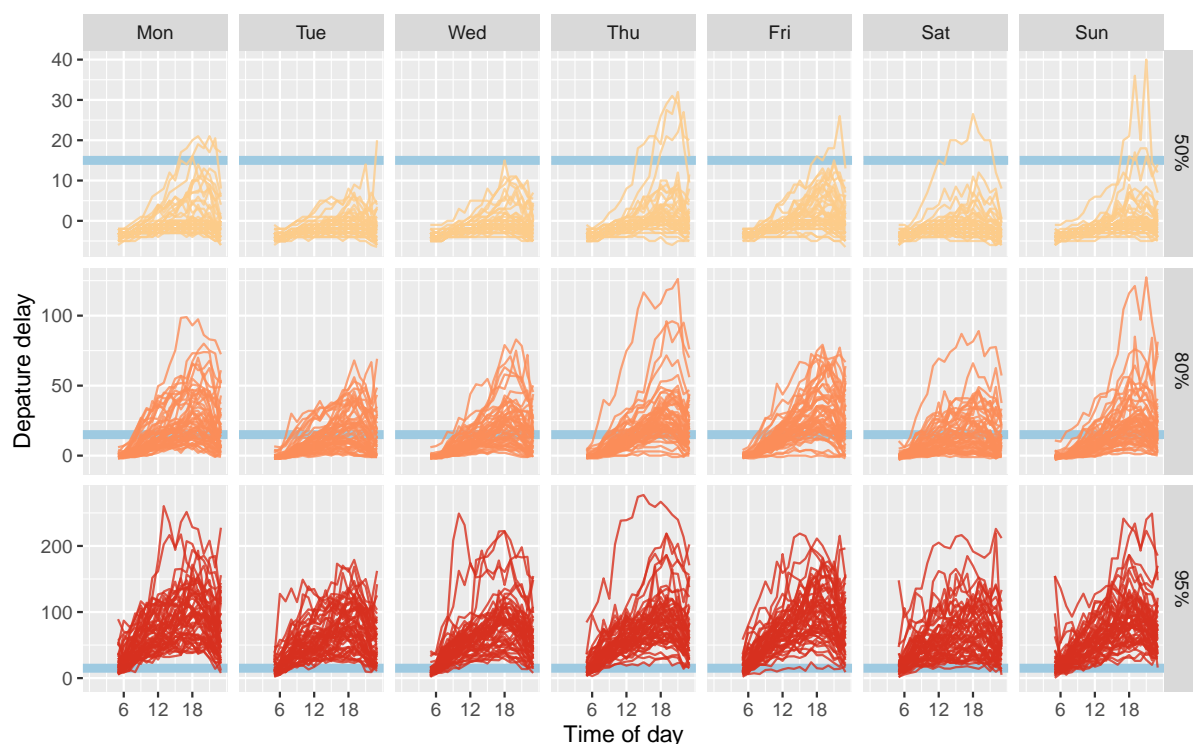


Figure 9: Small multiples of lines about departure delay against time of day, faceting day of week and 50%, 80% and 95% quantiles. A blue horizontal line indicates the 15-minute on-time standard to help grasp the delay severity. Passengers are apt to hold up around 18 during a day, and are recommended to travel early. The variations increase substantially as the upper tails.

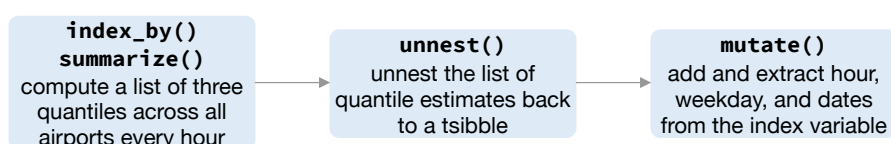


Figure 10: Flow chart illustrates the pipeline that preprocesses the data for creating Figure 9.

6.2 Smart-grid customer data in Australia

Sensors have been installed in households across major cities in Australia to collect data for the smart city project. One of the trials is monitoring households' electricity usage through installed smart meters in the area of Newcastle over 2010–2014 (Department of the Environment and Energy 2018). Data from 2013 have been sliced to examine temporal patterns of customer's energy consumption with **tsibble** for this case study. Half-hourly general supply in kWh have been recorded for 2,924 customers in the data set, resulting in 46,102,229 observations in total. Daily high and low temperatures in Newcastle in 2013 provides explanatory variables other than time in a different data table (Bureau of Meteorology 2019), obtained using the R package

bomrang (Sparks et al. 2018). Two data tables might be joined to explore how local weather can contribute to the variations of daily electricity use when needed.

During a power outage, electricity usage for some households may become unavailable, thus resulting in implicit missing values in the database. Gaps in time occur to 17.9% of the households in this dataset. It would be interesting to explore these missing patterns as part of a preliminary analysis. Since the smart meters have been installed at different dates for each household, it is reasonable to assume that the records are obtainable for different time lengths for each household. Figure 11 shows the gaps for the top 49 households arranged in rows from high to low in tallies. (The remaining households values have been aggregated into a single batch and appear at the top.) Missing values can be seen to occur at any time during the entire span. A small number of customers have undergone energy unavailability in consecutive hours, indicated by a line range in the plot. On the other hand, the majority suffer occasional outages with more frequent occurrence in January.

Aggregation across all individuals helps to sketch a big picture of the behavioral change over time, organized into a calendar display (Figure 12). Each glyph represents the daily pattern of average residential electricity usage every thirty minutes. Higher consumption is indicated by higher values, and typically occurs in daylight hours. Color indicates hot days. The daily snapshots vary depending on the season in the year. During the summer months (December and January), the late-afternoon peak becomes predominant driven by the use of air conditioning, especially on hot days with daily average temperature greater than 25 degrees Celsius. However, the winter time (July and August) sees two peaks in a day, which is probably due to heating in the morning and evening. This plot illustrates how the tsibble data can easily integrate with other tools and graphics.

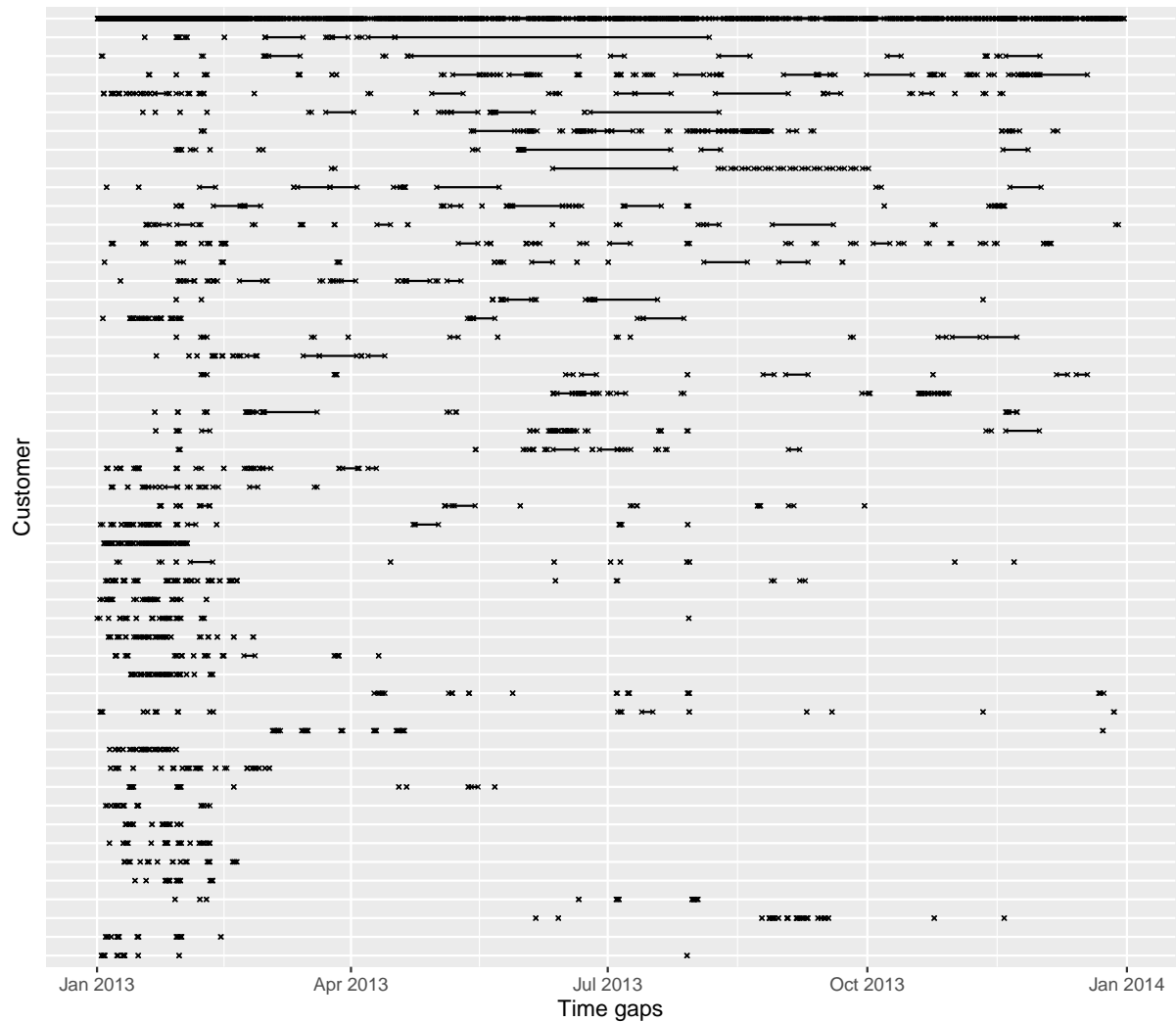


Figure 11: Time gap plots for the 49 customers with most implicit missing values, and the remaining customers grouped into the one line at top. Each cross represents an observation missing in time and a line between two dots shows continuous missingness over time. Each row corresponds to one customer. Missing values occur at various times, with more in January and February than other months.

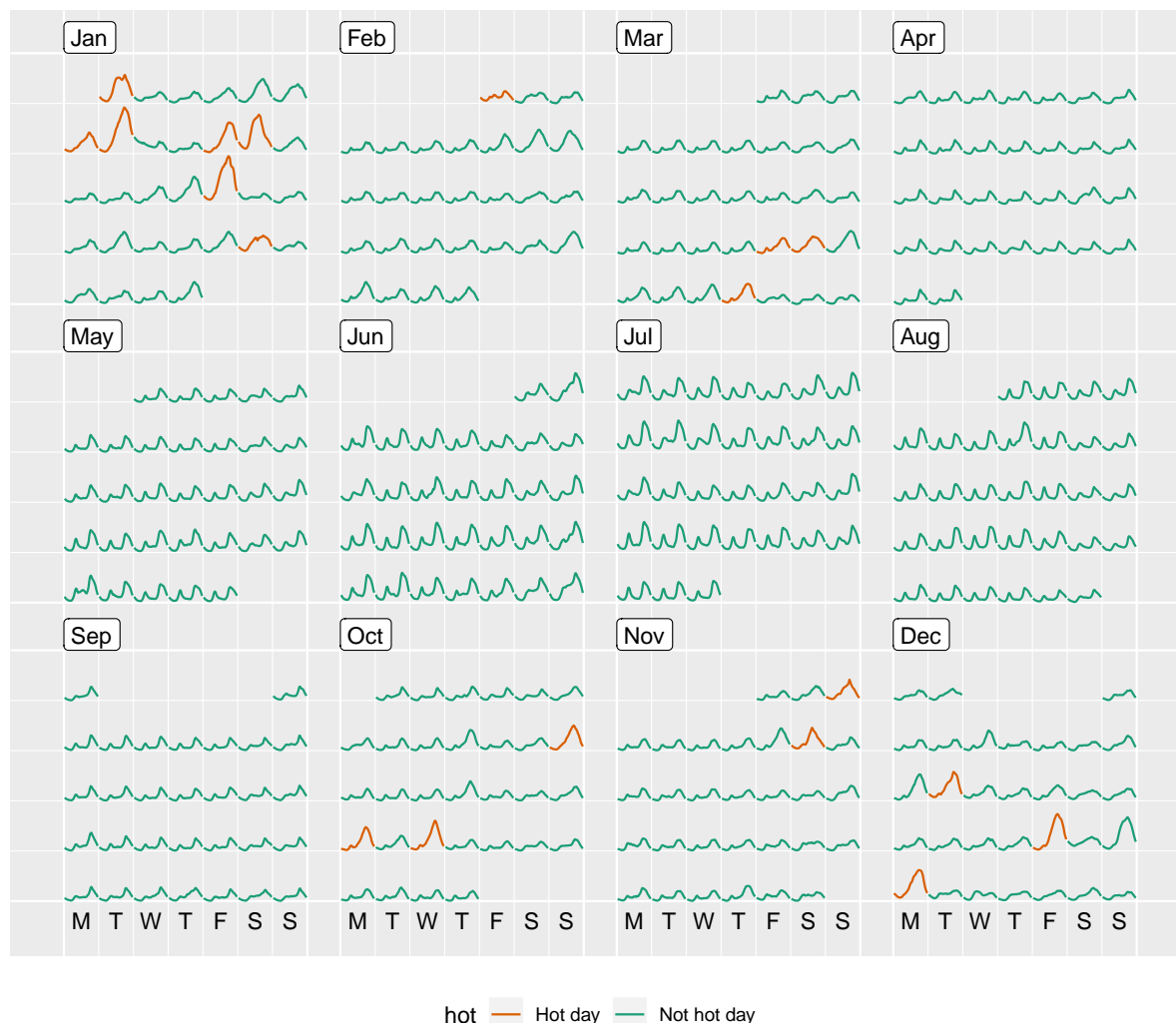


Figure 12: Half-hourly average electricity use across all customers in the region, organized into calendar format, with color indicating hot days. Energy use of hot days tends to be higher, suggesting air conditioner use. Days in the winter months have a double peak suggesting heater use.

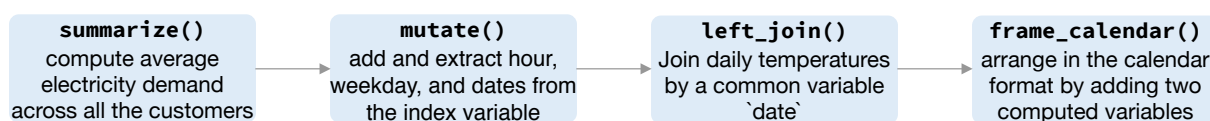


Figure 13: Flow chart illustrating the pipeline that preprocessed the data for creating Figure 12.

7 Conclusion and future work

The “tsibble” is a new data abstraction to represent temporal data, allowing the “tidy data” principles to be brought to the time domain. Tidy data begins to take shape in the state of time with the introduction of the contextual semantics of index and key. A declared index provides direct support to the time variable; variables that comprise the key define observations over time. These semantics further determine unique data entries required for a valid tsibble. No matter how temporal data arrives, a tsibble respects a time index and maintains the data richness. A tsibble frictionlessly allows transformation, visualization and modeling, and smoothly shifts between them, allowing for rapid iteration to gain data insights.

A missing piece of the **tsibble** package is to enable user-defined calendars and to respect structurally missing observations. For example, a call center may operate only between 9:00 am and 5:00 pm on week days, and stock trading resumes on Monday straight after Friday. No data available outside trading hours would be labeled as structural missingness, which tsibble currently disregards. However, a few R packages provide functionality to create and manage many sorts of calendars, including market-specific business calendars. Generally, custom calendars are easily embedded into the tsibble framework. Consequently these tsibble operators, like `fill_gaps()`, would work out of the box, and forecasts would be generated within its definable time range.

The **tsibble** package provides the grammar of temporal data manipulation, regardless of how the data is stored. Currently, it works for managing and manipulating temporal data frames in memory locally. But it is possible to work with remote tables stored in databases, such as SQLite and MySQL, using exactly the same tsibble code. This is left for future work.

Acknowledgments

The authors would like to thank Mitchell O’Hara-Wild for many discussions on the software development and Davis Vaughan for contributing ideas on rolling window functions. We also thank Stuart Lee for the feedback on this manuscript. This article was created with knitr (Xie 2015) and R Markdown (Xie, Allaire & Golemund 2018). The project’s Github repository <https://github.com/earowang/paper-tsibble> houses all materials required to reproduce this article and a history of the changes.

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