

Iran University of Science and Technology (8 silandr)  
Notebook

## Contents

|                                      |    |
|--------------------------------------|----|
| <b>1 Sublime Config</b>              | 3  |
| <b>2 Template</b>                    | 3  |
| <b>3 C++</b>                         | 3  |
| 3.1 STL . . . . .                    | 3  |
| 3.2 Compress . . . . .               | 3  |
| 3.3 Random . . . . .                 | 3  |
| 3.4 Set Intersection . . . . .       | 3  |
| 3.5 Ordered Set . . . . .            | 3  |
| 3.6 Overload . . . . .               | 3  |
| <b>4 Implementation</b>              | 4  |
| 4.1 Token . . . . .                  | 4  |
| 4.2 Convert(String-Double) . . . . . | 4  |
| <b>5 Math - Number Theory</b>        | 4  |
| 5.1 Combine . . . . .                | 4  |
| 5.2 Most Divisors . . . . .          | 4  |
| 5.3 Number Theory . . . . .          | 5  |
| 5.4 NTT . . . . .                    | 5  |
| <b>6 DP</b>                          | 5  |
| 6.1 SOS . . . . .                    | 5  |
| 6.2 Matrice . . . . .                | 5  |
| <b>7 Data Structure</b>              | 6  |
| 7.1 Segment Tree . . . . .           | 6  |
| 7.2 Segment Tree - Class . . . . .   | 6  |
| 7.3 Fenwick 2D . . . . .             | 6  |
| 7.4 Fenwick Pro . . . . .            | 7  |
| 7.5 HLD . . . . .                    | 7  |
| 7.6 MO's Algo . . . . .              | 7  |
| <b>8 String</b>                      | 7  |
| 8.1 Hash . . . . .                   | 7  |
| 8.2 Z-Function . . . . .             | 7  |
| 8.3 Ahoo . . . . .                   | 8  |
| 8.4 SuffixArray . . . . .            | 8  |
| <b>9 Graph</b>                       | 8  |
| 9.1 Dijkstra . . . . .               | 8  |
| 9.2 Scc . . . . .                    | 8  |
| 9.3 2sat . . . . .                   | 9  |
| 9.4 Centroid . . . . .               | 9  |
| 9.5 Dinitz . . . . .                 | 9  |
| 9.6 Eularian Tour . . . . .          | 10 |

|                                  |    |
|----------------------------------|----|
| 9.7 Min Cost Max Flow . . . . .  | 10 |
| <b>10 Geometry</b>               | 11 |
| 10.1 Geometry 1 . . . . .        | 11 |
| 10.2 Geometry 2 . . . . .        | 13 |
| 10.3 Convex hull . . . . .       | 13 |
| 10.4 Convex hull trick . . . . . | 13 |
| 10.5 Circle . . . . .            | 14 |
| 10.6 Point in Circle . . . . .   | 15 |
| 10.7 Circle Line . . . . .       | 15 |

[illegible]



```

MyInt operator+(const MyInt& rhs) const { return MyInt(value + rhs
    .value); }
// Same as - * /

MyInt& operator++() { ++value; return *this; } // Prefix increment
MyInt& operator--() { --value; return *this; } // Prefix decrement

MyInt& operator+=(const MyInt& rhs) { value += rhs.value; return *
    this; }
// same as -= *= /= %=

bool operator==(const MyInt& rhs) const { return value == rhs.
    value; }
// Same as != < <= > >=

MyInt operator&(const MyInt& rhs) const { return MyInt(value & rhs
    .value); }
// Same as | ^ ~

MyInt& operator&=(const MyInt& rhs) { value &= rhs.value; return *
    this; }
// Same as |= ^= <<= >>=

MyInt operator<<(const int shift) const { return MyInt(value <<
    shift); }
MyInt operator>>(const int shift) const { return MyInt(value >>
    shift); }

// Address-of operators
MyInt* operator&() { return this; }
const MyInt* operator&() const { return this; }
};

int main() {
    return 0;
}

```

## 4 Implementation

### 4.1 Token

```

vector<string> token(string& s, string& del)
{
    // string inp = "Hello,World;This|is.GeeksForGeeks pam";
    // string del = " ,;.| ";
    // vector<string> ans = token(inp, del);
    vector<string> ans;
    int start = 0, last = 0;
    while ((last = s.find_first_of(del, start)) != string::npos)
    {
        if (last != start)
            ans.pb(s.substr(start, last - start));
        start = last + 1;
    }
    if (start != s.length())
        ans.pb(s.substr(start));
    return ans;
}

```

### 4.2 Convert(String-Double)

```

double d = 3.0;
string str = to_string(d);
double D = stod(str)

```

## 5 Math - Number Theory

### 5.1 Combine

```

const ll mod = 1e9 + 7;

ll power(ll a, ll b)
{
    if(b == 0) return 1;
    return power((a * a) % mod, b / 2) * (b % 2 ? a : (ll)1) % mod;
}

ll comb(ll k, ll n)
{
    ll ans = 1;
    for(int i = 1; i <= k; i++) ans = ans * i % mod;
    ans = power(ans, mod - 2);
    for(int i = n; i > n - k; i--) ans = ans * i % mod;
    return ans;
}

```

### 5.2 Most Divisors

```

<= 1e2: 60 with 12 divisors
<= 1e3: 840 with 32 divisors
<= 1e4: 7560 with 64 divisors
<= 1e5: 83160 with 128 divisors
<= 1e6: 720720 with 240 divisors
<= 1e7: 8648640 with 448 divisors
<= 1e8: 73513440 with 768 divisors
<= 1e9: 735134400 with 1344 divisors
<= 1e10: 6983776800 with 2304 divisors
<= 1e11: 97772875200 with 4032 divisors
<= 1e12: 963761198400 with 6720 divisors
<= 1e13: 9316358251200 with 10752 divisors
<= 1e14: 97821761637600 with 17280 divisors
<= 1e15: 866421317361600 with 26880 divisors
<= 1e16: 8086598962041600 with 41472 divisors
<= 1e17: 74801040398884800 with 64512 divisors
<= 1e18: 897612484786617600 with 103680 divisors

```

```

//number of primes
30: 10
60: 17
100: 25
1000: 168
10000: 1229
100000: 9592
1000000: 78498
10000000: 664579

```

## 5.3 Number Theory

```
ll _gcd(ll a , ll b)
{
    if (a < b) swap(a, b);
    if(b==0) return a;
    a%=b;
    return _gcd(b,a);
}
// BIG p : 1000000000000037 , 1000000000003s
ll poww(ll a, ll b, ll md) {
    return (!b ? 1 : (b & 1 ? a * poww(a * a % md, b / 2, md) % md :
        poww(a * a % md, b / 2, md) % md));
}
```

## 5.4 NTT

```
inline void fix(ll &x){
    if (x<0) x+=mod;
    if (x>=mod) x-=mod;
}
ll powmod(ll a, ll b){
    ll res=1;
    for (; b; b>>=1, a=a*a%mod) if (b&1) res=res*a%mod;
    return res;
}
ll nCr(int n, int r){
    if (r<0 || r>n) return 0;
    return F[n]*I[r]%mod*I[n-r]%mod;
}

void NTT(ll* F, int n, bool inv){
    int lg=ceil(log2(n));
    n=1<<lg;
    //debug2(n, lg)
    for (int i=0; i<n; i++) rev[i]=(rev[i>>1]>>1) | ((i&1)<<(lg-1));
    for (int i=0; i<n; i++) if (i<rev[i]) swap(F[i], F[rev[i]]);
    for (int len=1; len<n; len<<=1){
        ll wn=powmod(3, (mod-1)/(2*len));
        if (inv) wn=powmod(wn, mod-2);
        for (int i=0; i<n; i+=2*len){
            ll w=1;
            for (int j=i; j<i+len; j++){
                ll x=(F[j] + F[j+len]*w)%mod;
                ll y=(F[j] - F[j+len]*w)%mod;
                F[j]=x;
                F[j+len]=y;
                w=w*wn%mod;
            }
        }
    }
    if (inv){
        ll invn=powmod(n, mod-2);
        for (int i=0; i<n; i++) F[i]=F[i]*invn%mod;
    }
}
```

## 6 DP

### 6.1 SOS

```
// iterate over all the masks
for (int mask = 0; mask < (1<<n); mask++){
    F[mask] = A[0];
    // iterate over all the subsets of the mask
    for(int i = mask; i > 0; i = (i-1) & mask){
        F[mask] += A[i];
    }
}
```

### 6.2 Matrice

```
struct MAT {
    long long n , m , A[200][200] ;
    MAT (const long long &n2 ,const long long &m2 ){
        n = n2 , m = m2 ;
        for (int i = 0 ; i < n ; i++){
            for (int j = 0 ; j < m ; j++){
                A[i][j] = 0 ;
            }
        }
    }
    MAT operator * (const MAT &B){
        MAT C = MAT(n , m) ;
        for (int i = 0 ; i < n ; i++){
            for (int j = 0 ; j < m ; j++){
                for (int k = 0 ; k < m ; k++){
                    C.A[i][j] = (C.A[i][j] + 1ll *
                        A[i][k] * B.A[k][j] % (
                            mod-1)) % (mod - 1) ;
                }
            }
        }
        return (C) ;
    }
}

void eq(const ll (&a)[5][5] , int n , int m )
{
    for(int i = 0 ; i < n ; i ++ )
    {
        for(int j = 0 ; j < m ; j ++ )
        {
            A[i][j] = a[i][j] ;
        }
    }
}

MAT operator + (const MAT &B){
    MAT C = MAT(n , m) ;
    for (int i = 0 ; i < n ; i++){
        for (int j = 0 ; j < m ; j++){
            C.A[i][j] = (A[i][j] + B.A[i][j]) %
                mod ;
        }
    }
    return (C) ;
}

void printt (){
    for (int i = 0 ; i < n ; i++){
        for (int j = 0 ; j < m ; j++){
            cout<<A[i][j]<<" ";
            cout<<"\n" ;
        }
    }
}
```

```

    }
    MAT operator ^ (long long x){
        MAT R = MAT(n , m) ;
        for (int i = 0 ; i < n ; i++)
            R.A[i][i] = 1 ;
        MAT T = MAT(n , m) ;
        for (int i = 0 ; i < n ; i++)
            for (int j = 0 ; j < m ; j++)
                T.A[i][j] = A[i][j] ;

        while (x > 0){
            if (x%2)
                R = R * T ;
            T = T * T ;
            x/=2 ;
        }
        return R ;
    }
};

```

## 7 Data Structure

### 7.1 Segment Tree

```

const ll maxn = 1e5 + 5;
ll seg[maxn << 2];

void update(ll index, ll val, ll L = 0, ll R = maxn, ll i = 1)
{
    if(R - L == 1)
    {
        seg[i] = val;
        return;
    }
    ll mid = R + L >> 1;
    if(index < mid)
        update(index, val, L, mid, i << 1);
    else
        update(index, val, mid, R, i << 1 | 1);
    seg[i] = seg[i << 1] + seg[i << 1 | 1];
}

ll get(ll l, ll r, ll L = 0, ll R = maxn, ll i = 1)
{
    if(r <= L || l >= R)
        return 0;
    if(l <= L && R <= r)
        return seg[i];
    ll mid = R + L >> 1;
    return get(l, r, L, mid, i << 1) + get(l, r, mid, R, i << 1 | 1);
}

```

### 7.2 Segment Tree - Class

```

class Seg
{
public:
    ll seg, pref, suf, sum;
    Seg(ll val = 0)

```

```

    {
        seg = suf = pref = sum = val;
    }
};

const ll maxn = 1e5 + 5, inf = 1e9 + 7;
Seg seg[maxn << 2];

Seg merge(Seg l, Seg r)
{
    Seg ans(0);
    ans.pref = max(l.pref, l.sum + r.pref);
    ans.suf = max(r.suf, r.sum + l.suf);
    ans.seg = max(l.suf + r.pref, max(l.seg, r.seg));
    ans.sum = l.sum + r.sum;
    return ans;
}

void update(ll index, ll val, ll L = 0, ll R = maxn, ll i = 1)
{
    if(R - L == 1)
    {
        seg[i].seg = seg[i].suf = seg[i].pref = seg[i].sum = val;
        return;
    }
    ll mid = R + L >> 1;
    if(index < mid)
        update(index, val, L, mid, i << 1);
    else
        update(index, val, mid, R, i << 1 | 1);
    seg[i] = merge(seg[i << 1], seg[i << 1 | 1]);
}

Seg get(ll l, ll r, ll L = 0, ll R = maxn, ll i = 1)
{
    Seg ans(0);
    if(l >= R || r <= L)
        return ans;
    if(l <= L && R <= r)
        return seg[i];
    ll mid = R + L >> 1;
    return merge(get(l, r, L, mid, i << 1), get(l, r, mid, R, i << 1 | 1));
}

```

### 7.3 Fenwick 2D

```

map<pair<int,int>,int>tree;
int MAXX = 1e5 + 5, MAXY = 1e5+5;

void update( int x, int y, int val )
{
    while( x <= MAXX )
    {
        int now = y;
        while( now <= MAXY )
        {
            tree[{x,now}] += val;
            now += now&(-now);
        }
        x += x&(-x);
    }
}

```

```

    }
}

int get( int x, int y )
{
    int ans = 0;
    while( x > 0 )
    {
        int now = y;
        while( now > 0 )
        {
            if( tree.find({x,now}) != tree.end() )
                ans += tree[{x,now}];
            now -= now&(-now);
        }
        x -= x&(-x);
    }
    return ans;
}

```

## 7.4 Fenwick Pro

```

inline void add(int ind , ll i , ll v){
    for(i ++ ; i < mod ; i += i & -i){
        fen[ind][i] += v ;
        //cout << " bomb " << i << endl ;
    }
}

inline void ADD(ll l , ll r , ll x){
    add(0 , l , x) ;
    add(0 , r+1 , -1 * x) ;
    add(1 , l , x * (1 - 1ll)) ;
    add(1 , r + 1 , -1 * x * r) ;
}

ll get(int ind , ll i){
    ll res = 0 ;
    for(i ++ ; i > 0 ; i -= i & -i){
        if(fen[ind].find(i) != fen[ind].end())
            res += fen[ind][i] ;
    }
    return res ;
}

ll GET(ll i){
    return get(0 , i) * i - get(1 , i) ;
}

```

## 7.5 HLD

```

void predfs(int v , int p){
    sz[v] = 1 ; if(p != -1) h[v] = h[p] + 1; par[v] = p ;
    for(auto u : adj[v]){
        if(u != p){
            predfs(u , v) ;
            if(bc[v] == -1 || sz[u] > sz[bc[v]]) bc[v] = u ;
            sz[v] += sz[u] ;
        }
    }
}

void dfs(int v , int p , int id){

```

```

    t.pb(v) ;
    st[v] = cnt ;
    cnt++ ;
    if(id) hd[v] = v ;
    else hd[v] = hd[p] ;
    if(bc[v] != -1){
        dfs(bc[v] , v , 0) ;
    }
    for(auto u : adj[v]) {
        if(u != p && u != bc[v]) dfs(u , v , 1) ;
    }
}

void getp(int v){
    while(v != -1){
        path.pb({st[hd[v]] , st[v] + 1}) ;
        v = par[hd[v]] ;
    }
}

```

## 7.6 MO's Algo

```

bool cmp(Query A, Query B)
{
    if (A.l / S == B.l / S) return A.l / S < B.l / S;
    return A.r > B.r
}

```

# 8 String

## 8.1 Hash

```

ll hsh(int l , int r){
    return (h[r] - h[l] * pt[r-l] % mod + mod) % mod ;
}

```

## 8.2 Z-Function

```

const ll maxn = 2e5 + 10;
ll z[maxn];
// Pattern matching : maximum character matching of start at index i
// to prefix
// text && pattern -----> s = pattern + '$' + text
// z[i] = number of match prefix start index i

```

```

void z_function(string s)
{
    ll left = 0, right = 0;
    for(int i = 1; i < s.size(); i++){
        if(i <= right && z[i - left] < right - i + 1)
            z[i] = z[i - left];
        else
        {
            if(i <= right)
                left = i;
            else
                left = right = i;
            while(right < s.size() && s[right] == s[right - left])

```





```

{
    if(comp[v] == 0 ) sfd(v , cnt++) ;
}

```

### 9.3 2sat

```

//harki mesle i khodesh 2 * i notesh 2 * i + 1 he
//yale u -> v yani agar u yek baseh v ham bayad yek bashe
vector<int> out[maxn * 2] , in[maxn * 2] , topol , adj[maxn];

bool visited[maxn * 2];

int color[maxn * 2] , c , val[maxn] , r[maxn] ;

void add_edge(int v , int u)
{
    out[v].pb(u);
    in[u].pb(v);
}

void dfs(int v)
{
    visited[v] = 1;
    for(auto u : out[v])
        if(!visited[u])
            dfs(u);

    topol.pb(v);
}

void sfd(int v)
{
    visited[v] = 1;
    color[v] = c;
    for(auto u : in[v])
        if(!visited[u])
            sfd(u);
}

for(int i = 0; i < 2 * n; i++)
    if(!visited[i])
        dfs(i);

reverse(topol.begin() , topol.end());
memset(visited , 0 , sizeof visited);
for(int v = 1 ; v <= 2 * m + 1 ; v++ )
    if(!visited[v])
        sfd(v) , c++;

for(int i = 1; i <= m; i++)
    if(color[2 * i] == color[2 * i + 1])
        return cout << "NO" << endl , 0;

```

### 9.4 Centroid

```

void plant(int v , int p = -1)
{
    sz[v] = 1;
    for(auto u : adj[v])
        if(u != p && !hide[u])
        {
            plant(u , v);
            sz[v] += sz[u];
        }
}

```

```

} //
int find_centroid(int v , int n , int p = -1)
{
    bool found = 1;
    while(found)
    {
        found = 0;
        for(auto u : adj[v])
            if(u != p && !hide[u] && sz[u] * 2 > n)
            {
                found = 1;
                p = v;
                v = u;
                break;
            }
        return v;
    }
}

void solve(int v , int h = 0)
{
    plant(v);
    v = find_centroid(v , sz[v]);
    cout << v << " level " << h << endl ;
    hide[v] = 1;
    for(auto u : adj[v])
        if(!hide[u])
            solve(u , h + 1);
}

```

### 9.5 Dinitz

```

Dinic:
int from[MAXE] , to[MAXE] , cap[MAXE] , prv[MAXE] , head[MAXN] , pt[MAXN] ,
    ec;
void addEdge(int u , int v , int uv , int vu = 0){
    from[ec] = u , to[ec] = v , cap[ec] = uv , prv[ec] = head[u] ,
    head[u] = ec++;
    from[ec] = v , to[ec] = u , cap[ec] = vu , prv[ec] = head[v] ,
    head[v] = ec++;
}
int lv[MAXN] , q[MAXN];
bool bfs(int source , int sink){
    memset(lv , 63 , sizeof(lv));
    int h = 0 , t = 0;
    lv[source] = 0;
    q[t++] = source;
    while (t-h){
        int v = q[h++];
        for (int e = head[v]; ~e; e = prv[e])
            if (cap[e] && lv[v] + 1 < lv[to[e]]){
                lv[to[e]] = lv[v] + 1;
                q[t++] = to[e];
            }
    }
    return lv[sink] < 1e8;
}

int dfs(int v , int sink , int f = 1e9){
    if (v == sink || f == 0)
        return f;
    int ret = 0;
    for (int &e = pt[v]; ~e; e = prv[e])

```

```

        if (lv[v]+1 == lv[to[e]]){
            int x = dfs(to[e], sink, min(f, cap[e]));
            cap[e] -= x;
            cap[e^1] += x;
            ret += x;
            f -= x;
            if (!f) break;
        }
        return ret;
    }
    int dinic(int source, int sink){
        int ret = 0;
        while (bfs(source, sink)){
            memcpy(pt, head, sizeof(head));
            ret += dfs(source, sink);
        }
        return ret;
    }

    memset(head, -1, sizeof(head));
}
//mohem

```

## 9.6 Eulerian Tour

```

void tour(int v, int b)
{
    if(b == 0) M[v] = 1;
    while( adj[v][b].size())
    {
        auto k = adj[v][b].back(); int u = k.X, id = k.Y;
        adj[v][b].pop_back();
        if(mark[id] == 0)
        {
            mark[id] = 1;
            tour(u, 1 - b);
        }
    }
    ans.pb(v);
    a.pb({v, b});
}

```

## 9.7 Min Cost Max Flow

```

template<typename F, typename C, int MAXN, int MAXM>
struct MinCostMaxFlow {
    struct Edge {
        int from, to;
        F cap;
        C cost;
    };

    Edge E[2 * MAXM];
    int m, par[MAXN], s, t;
    C dist[MAXN], cost = 0;
    F mn[MAXN], flow = 0;
    vector<int> adj[MAXN];

```

```

    inline void add_edge(int u, int v, F cap, C cost) {
        adj[u].push_back(m);
        E[m++] = {u, v, cap, cost};
        adj[v].push_back(m);
        E[m++] = {v, u, 0, -cost};
    }

    inline void SPFA() {
        fill(dist, dist + MAXN, numeric_limits<C>::max());
        fill(par, par + MAXN, -1);
        queue<int> q;

        dist[s] = 0;
        q.push(s);
        mn[s] = numeric_limits<F>::max();

        while (!q.empty()) {
            int v = q.front();
            q.pop();

            for (int id : adj[v]) {
                int u = E[id].to;
                if (!E[id].cap) continue;

                if (dist[u] > dist[v] + E[id].cost) {
                    dist[u] = dist[v] + E[id].cost;
                    q.push(u);
                    par[u] = id;
                    mn[u] = min(mn[v], E[id].cap);
                }
            }
        }

    }

    inline F solve() {
        SPFA();

        if (par[t] == -1) return 0;
        F c = mn[t], v = t;
        flow += c;
        cost += c * dist[t];

        while (v != s) {
            int id = par[v];
            E[id].cap -= c;
            E[id^1].cap += c;
            v = E[id].from;
        }

        return c;
    }

    inline pair<F, C> max_flow(int _s, int _t) {
        s = _s, t = _t;
        while (true) {
            F c = solve();
            if (!c) break;
        }

        return {flow, cost};
    }

```

```

    }
};

const ll MAXN = 402;
MinCostMaxFlow<int, double, MAXN * 2, MAXN * MAXN> flow;

```

## 10 Geometry

### 10.1 Geometry 1

```

#include <bits/stdc++.h>
#include <bits/extc++.h>
using namespace std;

#define rep(i, a, b) for(int i = a; i < (b); ++i)
#define trav(a, x) for(auto& a : x)
#define all(x) x.begin(), x.end()
#define sz(x) (int)(x).size()
typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;
typedef vector<int> vi;
typedef vector<ll> vl;
typedef long double ld;

const ll nils = 1000000007;

template <class T> int sgn(T x) { return (x > 0) - (x < 0); }
template<class T>
struct Point {
    typedef Point P;
    T x, y;
    explicit Point(T x=0, T y=0) : x(x), y(y) {}
    bool operator<(P p) const { return tie(x,y) < tie(p.x,p.y); }
    bool operator==(P p) const { return tie(x,y)==tie(p.x,p.y); }
    P operator+(P p) const { return P(x+p.x, y+p.y); }
    P operator-(P p) const { return P(x-p.x, y-p.y); }
    P operator*(T d) const { return P(x*d, y*d); }
    P operator/(T d) const { return P(x/d, y/d); }
    T dot(P p) const { return x*p.x + y*p.y; }
    T cross(P p) const { return x*p.y - y*p.x; }
    T cross(P a, P b) const { return (a-*this).cross(b-*this); }
    T dist2() const { return x*x + y*y; }
    double dist() const { return sqrt((double)dist2()); }
    // angle to x-axis in interval [-pi, pi]
    double angle() const { return atan2(y, x); }
    P unit() const { return *this/dist(); } // makes dist()==1
    P perp() const { return P(-y, x); } // rotates +90 degrees
    P normal() const { return perp().unit(); }
    // returns point rotated 'a' radians ccw around the origin
    P rotate(double a) const {
        return P(x*cos(a)-y*sin(a), x*sin(a)+y*cos(a)); }
    friend ostream& operator<<(ostream& os, P p) {
        return os << "(" << p.x << ", " << p.y << ")"; }
};

struct Angle {
    int x, y;

```

```

    int t;
    Angle(int x, int y, int t=0) : x(x), y(y), t(t) {}
    Angle operator-(Angle b) const { return {x-b.x, y-b.y, t}; }
    int half() const {
        assert(x || y);
        return y < 0 || (y == 0 && x < 0);
    }
    Angle t90() const { return {-y, x, t + (half() && x >= 0)}; }
    Angle t180() const { return {-x, -y, t + half()}; }
    Angle t360() const { return {x, y, t + 1}; }
};
bool operator<(Angle a, Angle b) {
    // add a.dist2() and b.dist2() to also compare distances
    return make_tuple(a.t, a.half(), a.y * (ll)b.x) <
           make_tuple(b.t, b.half(), a.x * (ll)b.y);
}

template<class P> bool onSegment(P s, P e, P p) {
    return p.cross(s, e) == 0 && (s - p).dot(e - p) <= 0;
}

template<class P> vector<P> segInter(P a, P b, P c, P d) {
    auto oa = c.cross(d, a), ob = c.cross(d, b),
        oc = a.cross(b, c), od = a.cross(b, d);
    // Checks if intersection is single non-endpoint point.
    if (sgn(oa) * sgn(ob) < 0 && sgn(oc) * sgn(od) < 0)
        return {(a * ob - b * oa) / (ob - oa)};
    set<P> s;
    if (onSegment(c, d, a)) s.insert(a);
    if (onSegment(c, d, b)) s.insert(b);
    if (onSegment(a, b, c)) s.insert(c);
    if (onSegment(a, b, d)) s.insert(d);
    return {all(s)};
}

template<class T>
T polygonArea2(vector<Point<T>>& v) {
    T a = v.back().cross(v[0]);
    rep(i, 0, sz(v)-1) a += v[i].cross(v[i+1]);
    return a;
}

vi num, st;
vector<vector<pii>> ed;
int Time;
int comps = 0;
int bridges = 0;
int dfs(int at, int par) {
    int me = num[at] = ++Time, top = me;
    for (auto [y, e] : ed[at]) if (e != par) {
        if (num[y]) {
            top = min(top, num[y]);
            if (num[y] < me)
                st.push_back(e);
        } else {
            int si = sz(st);
            int up = dfs(y, e);
            top = min(top, up);
            if (up == me) {
                st.push_back(e);
                comps++;
            }
        }
    }
}

```

```

        st.resize(si);
    }
    else if (up < me) st.push_back(e);
    else {bridges++;}
}
}
return top;
}

void bicomps() {
    num.assign(sz(ed), 0);
    rep(i,0,sz(ed)) if (!num[i]) dfs(i, -1);
}

int n = 0;
int m = 0;
vector<vl> segments;
map<ll,int> M;
vector<Point<ll>> pts;
vector<vi> C;
vector<vi> taken;

int geti(ll x, ll y){
    ll h = x*nils + y;
    if(M.find(h) != M.end())return M[h];
    M[h] = n;
    pts.push_back(Point<ll>(x, y));
    n++;
    vi temp;
    C.push_back(temp);
    taken.push_back(temp);
    vector<pii> temp2;
    ed.push_back(temp2);
    return n-1;
}

int from;
bool comp(int i, int j){
    Point<ll> pi = pts[i]-pts[from];
    Point<ll> pj = pts[j]-pts[from];
    return Angle(pi.x, pi.y) < Angle(pj.x, pj.y);
}

map<ll,ll> I;

int index(ll i, ll to){
    ll h = i*nils+to;
    assert(I.find(h) != I.end());
    return I[h];
}

vl areas;

ll get_area(int i, int j){
    vector<Point<ll>> polygon;
    int p = i;
    int q = j;
    while(1){
        polygon.push_back(pts[i]);
        taken[i][j] = 1;
        int i2 = C[i][j];
        int j2 = index(i,i2);

```

```

        j2 = (j2+1)%sz(C[i2]);
        i = i2;
        j = j2;
        if(i == p && j == q)break;
    }

    return polygonArea2(polygon);
}

int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);

    cin >> m;

    rep(c1,0,m){
        ll x1,y1,x2,y2;
        cin >> x1 >> y1 >> x2 >> y2;
        segments.push_back({x1,y1,x2,y2});
        int i = geti(x1,y1);
        int j = geti(x2,y2);
        assert(i != j);
        C[i].push_back(j);
        C[j].push_back(i);
        ed[i].push_back({j, 2*c1});
        ed[j].push_back({i, 2*c1+1});
        taken[i].push_back(0);
        taken[j].push_back(0);
    }

    bool planar = 1;

    rep(c1,0,min(m,1000)){
        rep(c2,c1+1,min(m,1000)){
            Point<ll> p1 = Point<ll>(segments[c1][0], segments[c1][1]);
            ;
            Point<ll> q1 = Point<ll>(segments[c1][2], segments[c1][3]);
            ;
            Point<ll> p2 = Point<ll>(segments[c2][0], segments[c2][1]);
            ;
            Point<ll> q2 = Point<ll>(segments[c2][2], segments[c2][3]);
            ;
            vector<Point<ll>> inter = segInter(p1,q1,p2,q2);
            if(sz(inter) == 0)continue;
            if(sz(inter) > 1){
                planar = 0;
                continue;
            }
            if(!(inter[0] == p1 || inter[0] == q1)){
                planar = 0;
            }
        }
    }

    assert(planar);
    bicomps();
    //assert(comps == 1);
    assert(bridges == 0);

    rep(c1,0,n){
        from = c1;
        sort(all(C[c1]), comp);

```

```

rep(c2,0,sz(C[c1])){
    ll from2 = C[c1][c2];
    ll h = from2*nils+ll(c1);
    l[h] = c2;
}
}
rep(c1,0,n){
    rep(c2,0,sz(C[c1])){
        if(!taken[c1][c2]){
            areas.push_back(abs(get_area(c1, c2)));
        }
    }
}
sort(all(areas));
double ans = 0.0;

rep(c1,0,sz(areas)-1){
    ans += areas[c1]*areas[c1];
}

cout << setprecision(18) << fixed << ans / 4.0 << "\n";

return 0;
}

```

## 10.2 Geometry 2

```

double area(const vector<point>& fig) {
    double res = 0;
    for (unsigned i = 0; i < fig.size(); i++) {
        point p = i ? fig[i - 1] : fig.back();
        point q = fig[i];
        res += (p.x - q.x) * (p.y + q.y);
    }
    return fabs(res) / 2;
}

struct pt {
    long long x, y;
    pt() {}
    pt(long long _x, long long _y) : x(_x), y(_y) {}
    pt operator+(const pt &p) const { return pt(x + p.x, y + p.y); }
    pt operator-(const pt &p) const { return pt(x - p.x, y - p.y); }
    long long cross(const pt &p) const { return x * p.y - y * p.x; }
    long long dot(const pt &p) const { return x * p.x + y * p.y; }
    long long cross(const pt &a, const pt &b) const { return (a - *this).cross(b - *this); }
    long long dot(const pt &a, const pt &b) const { return (a - *this).dot(b - *this); }
    long long sqrLen() const { return this->dot(*this); }
};

bool pointInTriangle(pt a, pt b, pt c, pt point) {
    long long s1 = abs(a.cross(b, c));
    long long s2 = abs(point.cross(a, b)) + abs(point.cross(b, c)) + abs(point.cross(c, a));
    return s1 == s2;
}

```

Area of triangle with sides a, b, c:  $\sqrt{S(S-a)(S-b)(S-c)}$  where  $S = (a+b+c)/2$   
 Area of equilateral triangle:  $s^2 * \sqrt{3} / 4$  where is side length  
 Pyramid and cones volume:  $1/3 \text{ area}(\text{base}) * \text{height}$

if  $p1=(x1, x2)$ ,  $p2=(x2, y2)$ ,  $p3=(x3, y3)$  are points on circle, the center is

$$x = -((x2^2 - x1^2 + y2^2 - y1^2)*(y3 - y2) - (x2^2 - x3^2 + y2^2 - y3^2)*(y1 - y2)) / (2*(x1 - x2)*(y3 - y2) - 2*(x3 - x2)*(y1 - y2))$$

$$y = -((y2^2 - y1^2 + x2^2 - x1^2)*(x3 - x2) - (y2^2 - y3^2 + x2^2 - x3^2)*(x1 - x2)) / (2*(y1 - y2)*(x3 - x2) - 2*(y3 - y2)*(x1 - x2))$$

## 10.3 Convex hull

## 10.4 Convex hull trick

```

#include <bits/stdc++.h>
using namespace std;

struct Line {
    long long m, c;
    Line(long long _m = 0ll, long long _c = 0ll) {m = (long long)_m; c = (long long)_c;}
    long long find_y(int x) { return (m * (long long)(x)) + c;}
    long double intersect_x(Line l) {return (long double)(l.c - c) / (long double)(m - l.m); }
};
deque < Line > dq;

const int MAXN = 1e6 + 12;
int n, p[MAXN], q[MAXN];
long long dp[MAXN], ans, a[MAXN];
vector < int > points;

int32_t main() {
    cin >> n;
    for (int i = 0; i < n; i++) {
        cin >> p[i] >> q[i] >> a[i];
        points.push_back(i);
    }
    sort(points.begin(), points.end(), cmp);

    dq.push_back(Line(0, 0));
    for (int i = 0; i < n; i++) {
        int ind = points[i];
        while(dq.size() >= 2
            && dq.back().find_y(q[ind]) <= dq[dq.size() - 2].find_y(q[ind]))
            dq.pop_back();

        dp[i] = ((long long)(p[ind]) * (long long)(q[ind])) - (long long)a[ind] + dq.back().find_y(q[ind]);
        Line new_line(-1ll * p[ind], (long long)(dp[i]));

        while (dq.size() >= 2
            && dq[0].intersect_x(new_line) >= dq[0].intersect_x(dq[1])
            )
            dq.pop_front();
        dq.push_front(new_line);
        ans = max(ans, dp[i]);
    }
}

```

```

    cout << ans;
    return 0;
}

// Salam
struct pt {
    double x, y;
    bool typ;
    bool operator == (pt const& t) const {
        return x == t.x && y == t.y;
    }
};

int orientation(pt a, pt b, pt c) {
    double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);
    if (v < 0) return -1; // clockwise
    if (v > 0) return +1; // counter-clockwise
    return 0;
}

bool cw(pt a, pt b, pt c, bool include_collinear) {
    int o = orientation(a, b, c);
    return o < 0 || (include_collinear && o == 0);
}

bool collinear(pt a, pt b, pt c) { return orientation(a, b, c) == 0; }

void convex_hull(vector<pt>& a, bool include_collinear = false) {
    pt p0 = *min_element(a.begin(), a.end(), [](pt a, pt b) {
        return make_pair(a.y, a.x) < make_pair(b.y, b.x);
    });
    sort(a.begin(), a.end(), [&p0](const pt& a, const pt& b) {
        int o = orientation(p0, a, b);
        if (o == 0)
            return (p0.x-a.x)*(p0.x-a.x) + (p0.y-a.y)*(p0.y-a.y)
                < (p0.x-b.x)*(p0.x-b.x) + (p0.y-b.y)*(p0.y-b.y);
        return o < 0;
    });
    if (include_collinear) {
        int i = (int)a.size()-1;
        while (i >= 0 && collinear(p0, a[i], a.back())) i--;
        reverse(a.begin()+i+1, a.end());
    }

    vector<pt> st;
    for (int i = 0; i < (int)a.size(); i++) {
        while (st.size() > 1 && !cw(st[st.size()-2], st.back(), a[i],
            include_collinear))
            st.pop_back();
        st.push_back(a[i]);
    }

    if (include_collinear == false && st.size() == 2 && st[0] == st[1])
        st.pop_back();

    a = st;
}

```

## 10.5 Circle

```

#define _USE_MATH_DEFINES
const int MAX_N = 2e5+10;
const int INF = 1e9;
const ld eps = 1e-8;
struct circle {
public:
    ld r;
    point o;
    circle(ld rr, ld x, ld y) {
        r = rr;
        o.x = x;
        o.y = y;
    }
    ld S() {
        return M_PI*r*r;
    }
    ld distance(point p1, point p2) { return hypot(p2.x-p1.x, p2.y-p1.y); }
    /*
    0 = other is inside this, zero point
    1 = other is tangent inside of this, one point
    2 = other is intersect with this, two point
    3 = other is tangent outside of this, one point
    4 = other is outside of this, zero point
    */
    pair<int, vector<point>> intersect(circle other) {
        vector<point> v;
        ld sumr = other.r + r;
        ld rr = r - other.r;
        ld dis = distance(o, other.o);
        ld a = (r*r - other.r*other.r + dis*dis)/(2*dis);
        ld h = sqrt(r*r-a*a);
        point p2(o.x, o.y);
        p2.x = a*(other.o.x - o.x)/dis;
        p2.y = a*(other.o.y - o.y)/dis;
        if (is_zero(sumr-dis)) {
            v.push_back(p2);
            return make_pair(3, v);
        }
        if (is_zero(rr - dis)) {
            v.push_back(p2);
            return make_pair(1, v);
        }
        if (dis <= rr)
            return make_pair(0, v);
        if (dis >= sumr)
            return make_pair(4, v);
        point p3(p2.x + h*(other.o.y - o.y)/dis, p2.y - h*(other.o.x - o.x)/dis);
        point p4(p2.x - h*(other.o.y - o.y)/dis, p2.y + h*(other.o.x - o.x)/dis);
        v.push_back(p3);
        v.push_back(p4);
        return make_pair(2, v);
    }
    ld f(ld l, ld r, ld R) {
        ld cosa = (l*l + r*r - R*R)/(2.0*r*l);
        ld a = acos(cosa);
        return r*r*(a - sin(2*a)/2);
    }
    ld intersection_area(circle c2) {

```

```

ld l = distance(o, c2.o);
if(l >= r + c2.r) return 0;
else if(c2.r >= l + r) return S();
else if(r >= l + c2.r) return c2.S();
return f(l, r, c2.r) + f(l, c2.r, r);
}
};

```

## 10.6 Point in Circle

```

// returns positive if d is outside circle ABC, positive if d is
// inside it and 0 if it's on border
int inCircle (point a, point b, point c, point d){
    if (cross(b - a, c - a) < 0)
        swap(b, c);
    int x[4][4] = {
        1, a.first, a.second, a.first * a.first + a.second * a
            .second,
        1, b.first, b.second, b.first * b.first + b.second * b
            .second,
        1, c.first, c.second, c.first * c.first + c.second * c
            .second,
        1, d.first, d.second, d.first * d.first + d.second * d
            .second
    };
};
// you can replace the following with any faster way
// of calculating determinant.
int y[] = {0, 1, 2, 3};
int ans = 0;

```

```

do {
    int mul = 1;
    for (int i = 0; i < 4; i++)
        for (int j = i + 1; j < 4; j++)
            if (y[i] > y[j])
                mul *= -1;
    for (int i = 0; i < 4; i++)
        mul *= x[i][y[i]];
    ans += mul;
} while (next_permutation(y, y + 4));
return ans;
}

```

## 10.7 Circle Line

```

typedef pair<point, point> ppp;
const ld INF = 1e18;
const ld eps = 1e-15;
ppp line_circle_intersection(point p1, point p2, point o, ld r){
    point q = dot(o-p1, p2-p1)/dist(p1, p2)*(p2-p1) + p1;
    ld d = r*r - dist(o, q);
    if(d < eps && d > -eps) return ppp(q, point(INF, INF));
    if(d < 0) return ppp(point(INF, INF), point(INF, INF));
    point dif = sqrt(d/dist(p1, p2))*(p1-p2);
    return ppp(q-dif, q+dif);
}

```