

~~Q~~ Array:

$$a = [10, 20, 30, 40, 50]$$

print(a)

Suppose, we have array , $\alpha = \begin{bmatrix} 10 & 20 & 30 & 40 & 50 \\ 0 & 1 & 2 & 3 & 4 \end{bmatrix}$ -

Let's say we're starting from 0.

15

while $i < \text{len}(a)$:

print(a[i])

↳ element accessing

$i = i + 1$

$$\text{output } \emptyset \quad a[0] = 10 \\ a[1] = 20$$

doing it in function:

```
def print_array(a):
```

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while i < len(a):

print(a[i])

i = i + 1

$$a = [10, 20, 30, 40, 50]$$

print_array(a)

array size & array len:

→ empty space

10	20	30	40	0	0
0	1	2	3	4	5

Here, array len is 6 ; size is 4

* if we wanna start from the end, I'll have to consider it as $i = \lceil \log(a) \rceil - 1$

printing array reversely:

$$a = [0] * 5$$

0|0|0|0|0

$$i = \text{len}(a) - 1$$

while $i >= 0$:

```
print(a[2])
```

$$l = l - 1$$

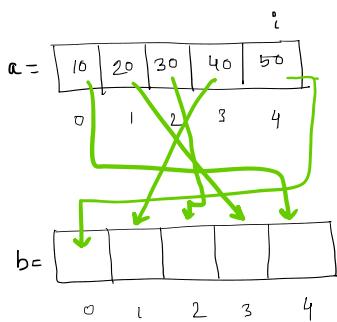
↳ here, we iterated the array reversely

If we wanna reverse an array:

means, if we have $\begin{bmatrix} 10 & 20 & 30 & 40 \end{bmatrix}$; it'll be as $\begin{bmatrix} 40 & 30 & 20 & 10 \end{bmatrix}$

So, this can be done in 2 ways:

i) out of place:



```
def reverse_out_of_place(arr):
    arr2 = np.zeros(len(arr), dtype=int)
    i=0
    while(i<=len(arr)-1):
        arr2[i]=arr[len(arr)-1-i]
        i+=1
    return arr2
arr=np.array([1,2,3,4])
print(reverse_out_of_place(arr))
arr=np.array([1,2,3,4,5])
print(reverse_out_of_place(arr))
```

In a, I'm starting my 'i' from 50. So, b array at j index a we can copy i

$$\therefore b[j] = a[i]$$

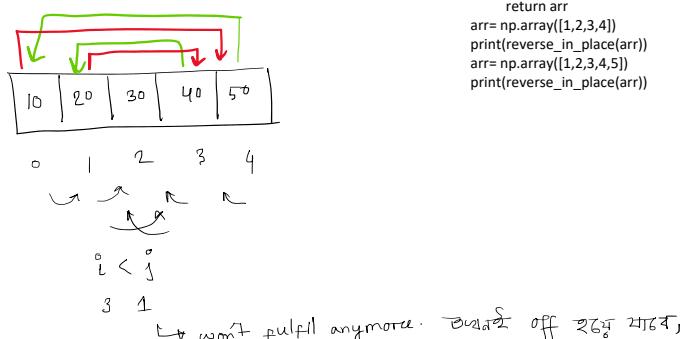
$$j+1 = 1$$

$$i-1 = 1$$

अथवा, नया array create करें तो उसके reverse copy करेंगे।

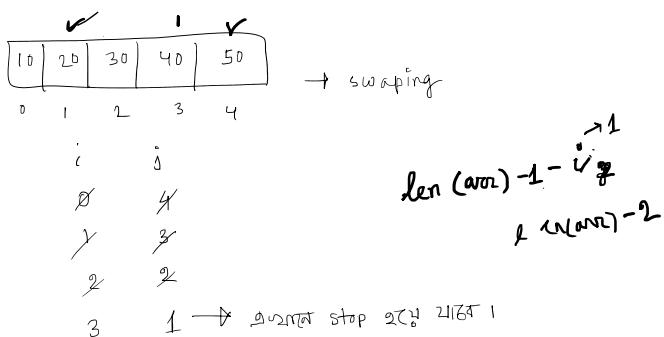
ii) in place:

first & last index swap करें फिर



```
def reverse_in_place(arr):
    x,j=0, len(arr)-1
    for i in range(len(arr)//2):
        arr[i], arr[j]=arr[j], arr[i]
        x+=1
        j-=1
    return arr
arr=np.array([1,2,3,4])
print(reverse_in_place(arr))
arr=np.array([1,2,3,4,5])
print(reverse_in_place(arr))
```

→ suppose, we are not creating any new array. just working on ...
tracing this

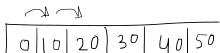


↳ Deletion / Shifting:

Array Rotating & Shifting:

Right shift :

10	20	30	40	50	60
0	1	2	3	4	5

1 block right shift → 

* Right shift must be start from last block. Shift 60 to 60 start 2662

Rotating ↗, temp ↗ first element ↗

Then, $a[0]$ = temp.

Some Operations:

Creating 1D array :

array_1D = [None] * 5

Creating 2D array [4x5] :

array_2D = [None] * 4

for i in range(len(array_2D)):

array_2D[i] = [None] * 5

How to access elements :

print(array_1D[3])

print(array_2D[2][3])

→ 3rd element of 2nd row

Creating array with Numpy :

numpy.empty(shape, data-type) → creates array filled with None
 numpy.zeros(shape, data-type) → " " " zeros

import numpy as np

arr = np.empty(2, dtype='int')

when creating an array, you must specify the length of its dimension that you can't change later.

```
1 # Let's look at the length property clearly
2 array = [None]*10
```

```

1 # Let's look at the length property clearly
2 array = [None]*10
3 #We just declared an array of 10 length. Let's fill it up with something.
4
5 Names = ['Emon', 'Nusrat', 'Joy', 'Abrar', 'Ifty', 'Ashik', 'Raisa', 'Suba', 'Sazid', 'Jawad']
6 for i in range(10):
7     array[i] = Names[i]
8 print(array)

['Emon', 'Nusrat', 'Joy', 'Abrar', 'Ifty', 'Ashik', 'Raisa', 'Suba', 'Sazid', 'Jawad']

```

Iteration : means checking value by index.

```

def iteration(source):
    for i in range(len(source)):
        print(source[i])

def reverse_iteration(source):
    for i in range(len(source) - 1, -1, -1):
        print(source[i])

```

Copy Array : [Pass by value]

↳ initializing new array with the same length given and then copying the value one by one.
as just memory location store ~~not~~, just copying value is not enough for array copying.

```

def copy_array(arr):
    new_arr = np.array([0]*len(arr))
    for i in range(len(new_arr)):
        new_arr[i] = arr[i]
    return new_arr
arr1 = np.array([1, 2, 3, 4])

```

Resize Array : fixed memory location ~~stratg~~ target we cannot resize array.

But resize ~~target~~ →

1. creating new array with new length
2. copying value from original array
3. if we have $\boxed{10 \ 20 \ 30 \ 40 \ 50} \rightarrow \text{len}(5)$

↓ resizing

10	20	30	40	50	None	None	None
len(8)							

Code :

```

import numpy as np
def resize_array(old_array, new_capacity):
    new_array = np.array([0]*new_capacity)
    for i in range(len(old_array)):
        new_array[i] = old_array[i]

```

```

new_array = np.array([0] * new_capacity)
for i in range(len(old_array)):
    new_array[i] = old_array[i]
return new_array

```

```

array1 = np.array([1, 2, 3])
x = len(array1)

```

Reversing an array:

↳ out of place operation :

- Creating new array with same size
- then copying value in reverse order

Code :

```

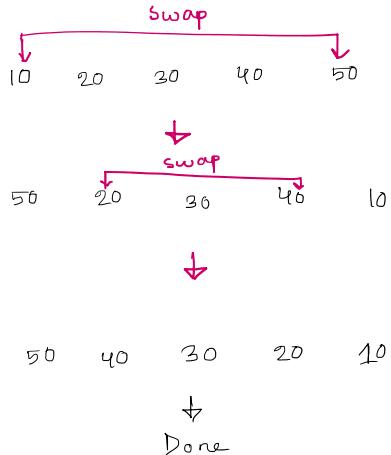
def rev_arra_op(arra):
    rev_arra = [None] * len(arra)
    i = 0
    j = len(arra) - 1
    while i < len(arra):
        rev_arra[i] = arra[j]
        i += 1
        j -= 1
    return rev_arra

```

↳ In place operation:

- swaping starting value with the end value
- it's reversing the array in the original array

Example :



Code :

```

def rev_arra_inplace(arra):
    l = 0

```

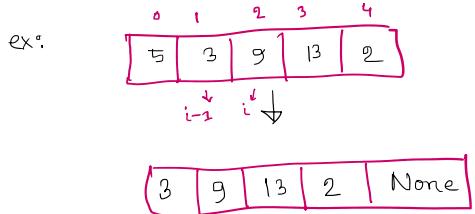
```

j = len(arr) - 1
while i < j:
    temp = arr[i]
    arr[i] = arr[j]
    arr[j] = temp
    i += 1
    j -= 1

```

Shifting:

Left shift: shift amount wise element शूलो वाले फिर अप्पे आवाये।



we'll lose 5!

Code:

```

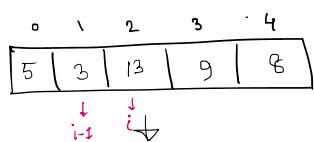
def left_shift(arr):
    for i in range(1, len(arr), -1):
        arr[i-1] = arr[i]
    arr[len(arr)-1] = None
    return arr
arr = np.array([1, 2, 3])

```

Right Shift: shift amount wise element शूली वाले फिर।

and first जूँ फिर ब्लैक रिटेन।

Last element will be lost forever.



Last value start 264,
* after left 3 or right 2 shifting
right 2 or left 3 iterating

None, 5, 3, 13, 9

Code:

```

def right_shift(arr):
    for i in range(len(arr)-1, 0, -1):
        arr[i] = arr[i-1]

```

```
arr[0] = None
```

```
return arr
```

Rotating :

Rotating array left :

↳ equiv. to shifting circular array left

↳ 1st element won't be lost as it'll move to last slot

3 9 5 13 2



9 5 13 2 3

Code :

```
def rotate_left(arr):  
    temp = arr[0]  
    for i in range(1, len(arr)):  
        arr[i-1] = arr[i]  
    arr[len(arr)-1] = temp  
    return arr
```

Rotating array right :

↳ last element will move to the 1st slot

↳ element shift right & ~~last element~~

2 5 3 9 13



13 2 5 3 9

}

Code :

```
def rotate_right(arr):  
    temp = arr[len(arr)-1]  
    for i in range(len(arr)-1, 0, -1):  
        arr[i] = arr[i-1]  
    arr[0] = temp
```

```

    return arr
arr = np.array([1, 2, 3])
print(rotate_right(arr))

```

Insertion :

* Inserting an element into an array *

1. making an empty slot, insert the value in array
2. to make empty slot, first check any slots are available. If not then we need to resize the array.
3. Using idea of right shift to have an empty slot.

[Initialization point of right shift would be index where we wanna insert value]

8. we need to check if asked index is valid or not

Example:

0	1	2	3	4	5
5	7	3	6	None	None

suppose, you wanna insert 10 at idx 1



5	10	7	3	6	None
---	----	---	---	---	------



Code :

```

def insert_element(arr, size, elem, index):
    if size == len(arr):
        print("No space. No insertion")
    else:
        for i in range(size, index, -1):
            arr[i] = arr[i-1] # shifting right till the index
        arr[index] = elem # Inserting element
    return arr

```

arr = np.zeros(4, dtype=int)



#Inserting anywhere

```

def insert_anywhere(arr, size, index, elem):
    if index < 0 or index > size:
        return "Insertion Not Possible"
    if size >= len(arr):
        arr = resizeArray(arr, len(arr)+3)
    for i in range(size, index, -1): # Right Shift
        arr[i] = arr[i-1]

```

#Inserting at the end

```

def insert_at_the_end(arr, size, elem):
    if size >= len(arr):
        arr = resizeArray(arr, len(arr)+5)
    arr[size] = elem
    return arr

arr = np.zeros(4, dtype=int)
arr[0], arr[1], arr[2] = 4, 6, 5
print(arr)

```

```

arr = resizeArray(arr, len(arr)+3)
for i in range(size, index, -1): #Right Shift
    arr[i] = arr[i-1]
arr[index] = elem
return arr

arr = np.zeros(4, dtype=int)
arr[0], arr[1], arr[2] = 4, 6, 5
print(arr)
print(insert_anywhere(arr, 3, 15)) #array, size, index, elem
print(insert_anywhere(arr, 4, 25)) #array, size, index, elem, the size increased

# If you want to insert at the end with this function too,
# all you have to do is provide the index value equal to the size

```



Removing Element from Array :

start left shifting from the index which value we wanna remove.

$a = [10 \ 6 \ 8 \ 11 \ 15 \ 20]$

\downarrow will rmv 8 [left shift]

$[10 \ 6 \ 11 \ 15 \ 20 \ None]$

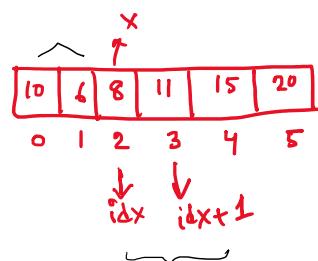
Code :

```

def rmv_element( arr, index, size):
    if size == 0 or (index < 0 and index > size):
        return "deletion not possible"
    for i in range(index + 1, size):
        arr[i-1] = arr[i] # shifting left from removing index
    arr[size-1] = None # making last space empty
    return arr

arr = np.zeros(5, dtype=int)
arr[0], arr[1], arr[2], arr[3] = 4, 6, 5, 2
print(arr)
print(rmv_element(arr, 4, 0)) # array, size, index

```



Multidimensional Array

RAM ဒါ အတိ များ multid. array 1D နောက် စွဲတဲ့ ပြုလုပ် ရတယ်!

How to determine the translated linear index of a multidimensional index from original array?

→ suppose 4D array:

dim: M × N × O × P

elem of box [w][x][y][z]

∴ index of that element in the linear array ??

$$W \times (N \times O \times P) + X \times (O \times P) + Y \times P + Z$$

Q: linear array length : 128

dim : 3D ; 4 × 4 × 8

what are the multidimensional indexes of the element stored at location 111 ?

Soln:

The dimension of the given array is [4][4][8] and length is 128. We need to map the dimension of linear index 111.

The equation we get is:

$$X * (4 * 8) + Y * 8 + Z = 111 \text{ where } 0 \leq X \leq 3, 0 \leq Y \leq 3 \text{ and } 0 \leq Z \leq 7.$$

Now to find the value of X, Y and Z we need to repeatedly divide the remainder of the linear index with the multiplication of the lengths of lower dimensions till you reach the last dimension.

So first $111 / (4 * 8)$ then the quotient is x and then you use the remainder R to do $R / 8$ to get y index. The remainder of that is the z index

Following the process we get,

$$X = 111 / (4 * 8) = 3 \text{ and } 111 \% (4 * 8) = 15$$

$$Y = 15 // 8 = 1 \text{ and } 15 \% 8 = 7$$

$$Z = 7$$

So, the dimension of linear index 111 is [3][1][7].

Initialization of a Multidimensional Array:

import numpy as np
Creating empty arrays
m = np.zeros((2,3), dtype=int)
m = np.array([[4,3,8], [2,5,1]])
[[0 0 0]
 [0 0 0]]
[[4 3 8]
 [2 5 1]]

creating m. arr. by using array() function

Creating empty 2D array taking input from user:

```
def create_array():  
    m = np.zeros((2,3), dtype=int)  
    for i in range(2):  
        for j in range(3):  
            print(f'element of [{i}] [{j}] index : ')  
            m[i][j] = int(input())
```

```
return m
```

Iteration of a 2D Matrix:

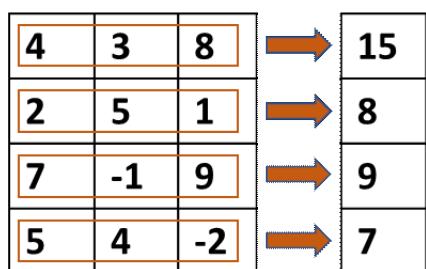
2. Row wise iteration:

```
def print_row(m):  
    row, col = m.shape  
    for i in range(row):  
        for j in range(col):  
            print(m[i][j], end=' ')  
        print()  
  
m = np.zeros((2,3), dtype='int')  
print(m.shape)
```

Sum of all elements in 2D matrix:

```
def array_sum(m):  
    sum = 0  
    row, column = m.shape  
    for i in range(row):  
        for j in range(column):  
            sum += m[i][j]  
  
    return sum
```

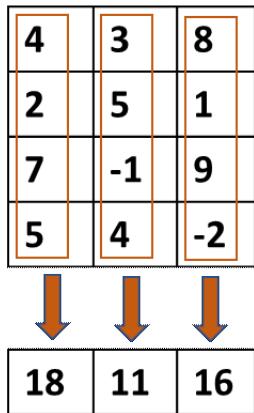
Sum of every row in a given matrix



Thus, the resulting matrix will always have 1 column to store row wise sum and equal number of rows of the main matrix.

```
def row_wise_sum(m):  
    row, col = m.shape  
    result = np.zeros((row,1), dtype = int)  
    for i in range(row):  
        for j in range(col):  
            result[i][0] += m[i][j]  
    return result
```

Sum of every column in a given matrix

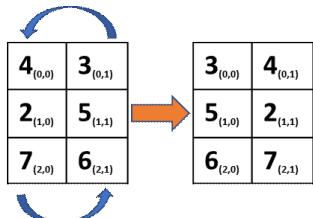


Thus, the resulting matrix will always have 1 row to store column wise sum and equal number of columns of the main matrix.

```
def column_wise_sum(m):
    sum = 0
    row, col = m.shape
    result = np.zeros((1,col), dtype = int)
    for i in range(col):
        for j in range(row):
            result[0][i] += m[j][i]
    return result
```

Swapping:

Swap the two columns of a $m \times 2$ matrix



```
def swap_2columns(m):
    row, col = m.shape
    for i in range(row):
        m[i][0], m[i][1] = m[i][1], m[i][0]
    return m
```

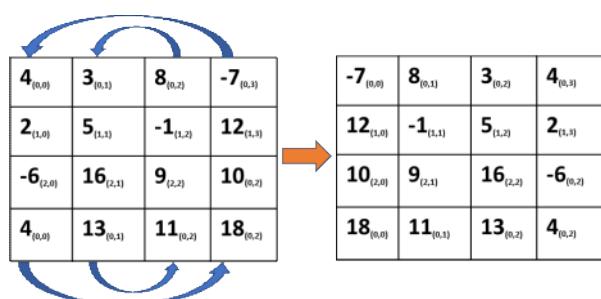
Swap the columns of a $m \times n$ matrix

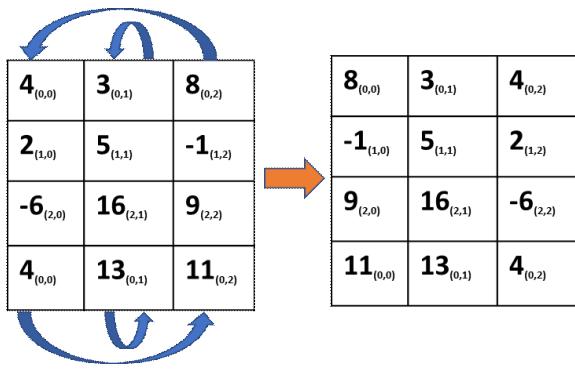
0th column \rightleftharpoons (n-1)th column

1st column \rightleftharpoons (n-2)th column

2nd column \rightleftharpoons (n-3)th column

and so on and so forth





```
def swap_columns(m):
    row,col = m.shape
    for i in range(row):
        for j in range(col//2):
            m[i][j],m[i][col-1-j] = m[i][col-1-j],m[i][j]
    return m
```

Addition:

Add the elements of the primary diagonal in a square matrix

4_{(0,0)}	3_{(0,1)}	8_{(0,2)}
2_{(1,0)}	5_{(1,1)}	1_{(1,2)}
7_{(2,0)}	6_{(2,1)}	9_{(2,2)}

The main diagonal of a square matrix are the elements who's row number and column number are equal, a_{ii}

```
def sum_primary_diagonal(m):
    row,col = m.shape
    assert (row==col), 'Not a square matrix'
    sum = 0
    for i in range(row):
        sum += m[i][i]
    return sum
```

Add the elements of the secondary diagonal in a square matrix

4_{(0,0)}	3_{(0,1)}	8_{(0,2)}	
2_{(1,0)}	5_{(1,1)}	1_{(1,2)}	
7_{(2,0)}	6_{(2,1)}	9_{(2,2)}	

Secondary diagonal of a 3x3 Matrix

4_{(0,0)}	3_{(0,1)}	8_{(0,2)}	-7_{(0,3)}
2_{(1,0)}	5_{(1,1)}	-1_{(1,2)}	12_{(1,3)}
-6_{(2,0)}	16_{(2,1)}	9_{(2,2)}	10_{(2,3)}

Secondary diagonal of a 4x4 Matrix

For an element a_{ij} in the secondary diagonal, can you find out the j for a particular i ?

Hint: try $i+j$ for a_{ij} in the secondary diagonal and find out the relation.

Add two matrices of same dimension

```
def add_matrix(m,n):
    r_m, c_m = m.shape
    r_n, c_n = n.shape
    assert (r_m == r_n and c_m == c_n), 'Dimension mismatch'
    result = np.zeros((r_m,c_m), dtype=int)
    for i in range(r_m):
        for j in range(c_m):
            result[i][j] = m[i][j]+n[i][j]
    return result
```

Multiply two matrices

```
def multiply(m,n):
    r_m, c_m = m.shape
    r_n, c_n = n.shape
    assert c_m == r_n, 'Cannot multiply'
    result = np.zeros((r_m,c_n), dtype=int)
    for i in range(r_m):
        for j in range(c_n):
            for k in range(c_m):
                result[i][j] += m[i][k]*n[k][j]
    return result
```