

# ASSIGNMENT SOLUTION - STATISTICS (MAJOR)

Example - 1,  $N = 19$

$$\text{Median} \Rightarrow \frac{n+1}{2} \Rightarrow \frac{19+1}{2} \Rightarrow \frac{20}{2} = 10$$

So, the Median is the 10<sup>th</sup> value that is 48.

Example - 2,

$$\text{Mean } (\bar{x}) = \frac{45+39+53+45+43+48+50+45}{8}$$

$$\Rightarrow \frac{368}{8} = 46$$

So, the Mean ( $\bar{x}$ ) is 46.

Example - 3, Total Monthly Salary of <sup>10</sup> workers = ?

No. of workers = 10

Mean = 1445

$$\therefore \text{Mean} = \frac{\text{Total Salaries}}{\text{No. of workers}}$$



$$1445 = \frac{\text{Total Salaries}}{10}$$

$$\text{Total Salaries} = 14450$$

After joining of New worker

$$\text{Total Salaries} \Rightarrow 14450 + 1500 = 15950$$

$$\text{No. of workers} \Rightarrow 10 + 1 = 11$$

$$\text{Mean} \Rightarrow ?$$

$$\text{Mean} = \frac{\text{Total Salaries}}{\text{No. of workers}}$$

$$= \frac{15950}{11}$$

$$= 1450$$

So the Mean of 11 worker's Monthly Salary is 1450



Example - 4,

Height	No. of girls
120 - 130	4
130 - 140	7
140 - 150	$12 = f_0$
$L = 150 - 160$	$20 = f_1$
160 - 170	$8 = f_2$
	<u>50</u>

$$L_1 = 150$$

$$f_0 = 12$$

$$f_1 = 20$$

$$f_2 = 8$$

$$i = 10$$

$$\therefore \text{Mode} = L_1 + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times i$$

$$\text{or} = 150 + \frac{20 - 12}{(2 \times 20) - 12 - 8} \times 10$$

$$\text{or} = 150 + \frac{8}{40 - 20} \times 10$$

$$\text{or} = 150 + \frac{8}{20} \times 10$$

$$\text{or} = 150 + \frac{80}{20}$$

$$\text{or} = 150 + 4$$

$$\text{or} \therefore = 154$$

So the Mode is 154



Example - 5,

$$\begin{aligned}\text{Range} &= 13.67 \\ \text{Largest value} &= 70.08 \\ \text{Smallest value} &= ?\end{aligned}$$

$$\text{Smallest value} = \text{Largest value} - \text{Range}$$

$$\begin{aligned}\text{P.S} &= 70.08 - 13.67 \\ &= 56.41\end{aligned}$$

So, the smallest value of the range is 56.41

Example - 6,

$$\text{Mean} \Rightarrow \frac{11.4 + 12.5 + 12.8 + 16.3 + 17.8 + 19.2}{6}$$

$$\Rightarrow \frac{90}{6} = 15$$

$x_i$	$d_i = x_i - \bar{x}$ $= x - 15$	$d_i^2$
11.4	-3.6	12.96
12.5	-2.5	6.25
12.8	-2.2	4.84
16.3	1.3	1.69
17.8	2.8	7.84
19.2	4.2	17.64

$$\sum d_i^2 = 51.22$$



$$\text{Standard Deviation}(\sigma) = \sqrt{\frac{\sum d_i^2}{n}}$$

$$= \sqrt{\frac{51.22}{6}}$$

$$= \sqrt{8.53}$$

$$\text{Hence } \sigma = 2.9$$

$$\text{Example-7, Normal distribution} = Z = \frac{500 - 527}{112} = 0.24107$$

$$\mu = 527$$

$$\sigma = 112$$

$$P(x > 500) = P(z > -24)$$

$$\Rightarrow 1 - 0.4052$$

$$\Rightarrow 0.5948$$

20.51

25.2

18.4

10.1

18.4

10.1

2.5 -

2.5 -

5.5 -

2.1

8.5

5.1

10.1

2.51

8.51

10.3

8.41

5.11



Example - 8;

$X$  = Random Variable

$$Z = \frac{X - \mu}{S}$$

$\mu$  = Mean

$S$  = Stand. deviation.

$$\mu = 266 \text{ Days}$$

$$S = 16 \text{ Days}$$

$$X_1 = 240 \text{ Days}; X_2 = 270 \text{ Days}$$

$$Z_1 = \frac{X_1 - \mu}{S} = \frac{240 - 266}{16} = -1.625 = -1.63$$

$$Z_2 = \frac{X_2 - \mu}{S} = \frac{270 - 266}{16} = 0.25$$

$$P(Z_2) - P(Z_1) = ?$$

$$P(Z_1 < Z < Z_2) = P(Z_2) - P(Z_1)$$

$$P(-1.63) = 0.05155$$

$$P(0.25) = 0.59871$$

$$P(Z_1 < Z < Z_2) = 0.59871 - 0.05155 = 0.54716$$



Example - 9, 10, 50, 30, 20, 10, 20, 70, 30

(1) Minimum = 10

(2) 1<sup>st</sup> Quartile = ~~10~~ = 17.5

(3) Median = 25

(4) 3<sup>rd</sup> Quartile = 35

(5) Maximum = 70

Example - 10, Given  $P(A) = 0.4$

$$P(B) = p, P(A \cap B) = 0.6$$

$$\text{So, } P(A \cap B) = P(A) \cdot P(B)$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\Rightarrow 0.6 = 0.4 \times p - \cancel{0.4 \times p} P(A) \cdot P(B)$$

$$0.6 = 0.4 \times p - 0.4 \times p$$

$$0.2 = 0.6 \times p$$

$$p = 0.2/0.6 = 1/3$$

$$\text{Hence } p = 1/3$$



Example-11, Let  $A$  = Passing the 1st test &  
 $B$  = Passing the 2nd test

$$P(B|A) = \frac{P(B \cap A)}{P(A)}$$

$$P(B|A) = \frac{0.6}{0.8}$$

$$P(B|A) = 0.75$$

Example-13,

$$P(\text{Selecting Any Number}) = \frac{1}{10} = 0.1$$

$$P\left(\begin{array}{l} \text{Selecting 1 from 1st bin} \\ \text{1 from 2nd bin \& } \\ \text{1 from 3rd bin} \end{array}\right) = 0.1 \times 0.1 \times 0.1$$

$$= 0.001$$

Example-12, Let  $A$  = First die is 5  
 Let  $B$  = total of 2 dice is greater than 9

$$P(A) = \frac{1}{6}$$

Possible outcomes for  $A$  And  $B$  :  $\{(5,5), (5,6)\}$



$$P(A \text{ and } B) = \frac{2}{36} = \frac{1}{18}$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

$$\rightarrow \frac{1}{18} \times 6 = \frac{1}{3}$$

Example -14

Let A = Democrats

B = Independent

$$\text{Sample Space} = (20 + 13 + 6) = 39$$

$$P(A \text{ or } B) = \frac{13}{39} + \frac{6}{36} = \frac{19}{39}$$

Thank you...