

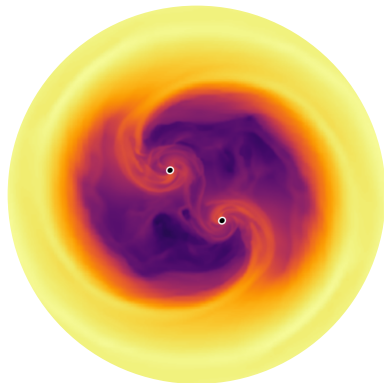
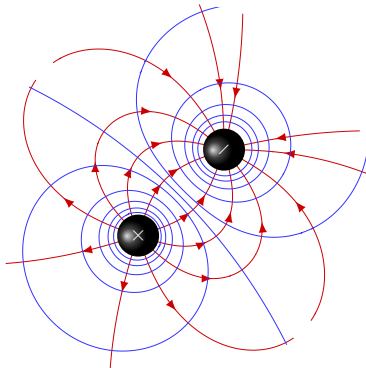


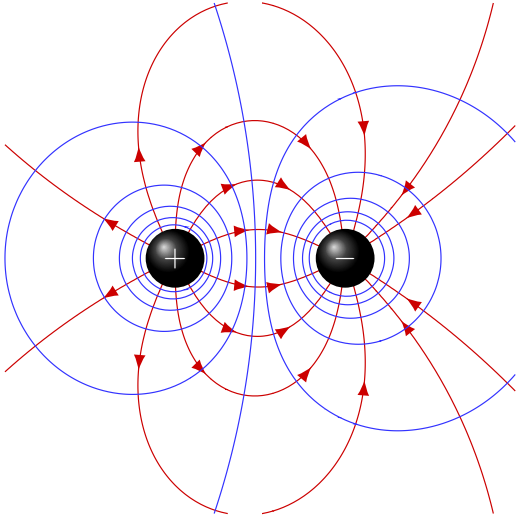
# EXPLORING NONLINEAR INTERACTIONS BETWEEN CHARGED BLACK HOLES WITH NUMERICAL RELATIVITY: GRAVITATIONAL WAVES & FUNDAMENTAL PHYSICS

October 28, 2022

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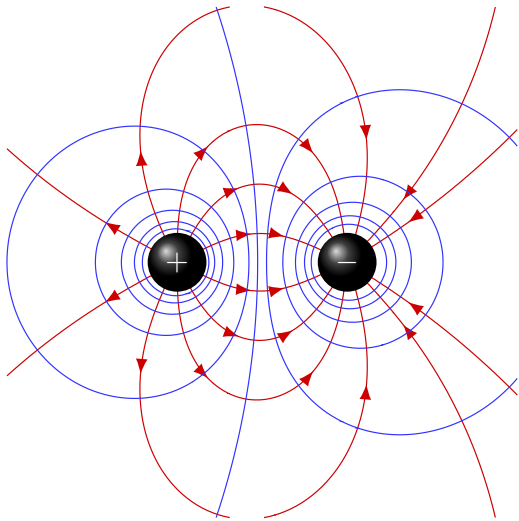
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The nonlinear interaction between  
charged binary black holes is  
**unexplored**

Orbits? Emission? ...?



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charged binary black holes is  
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Orbits? Emission? ...?

1. Results apply to stellar-mass, supermassive, and microscopic BHs
2. Charge does not have to be electromagnetic

# Nonlinear interaction is important for

Astrophysics



Constraints on charge  
GW templates for LIGO-Virgo



- BH charge is largely unconstrained
- GW models do include charge

More on this later!

# Nonlinear interaction is important for

Exotic Astrophysics



Constraints on charged dark matter  
and magnetic monopoles

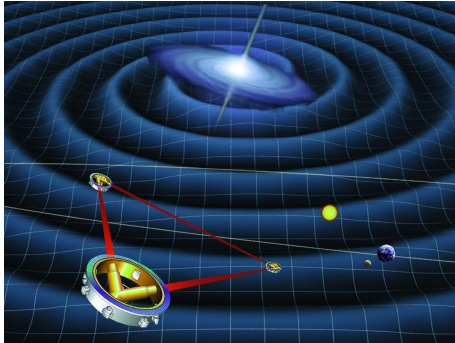


- Primordial BH could have (electric or magnetic) charge
- Dark matter could be (darkly) charged

# Nonlinear interaction is important for

Modified Gravity

↔ Springboard and proxy for other theories  
(e.g. Einstein-Maxwell-Scalar)



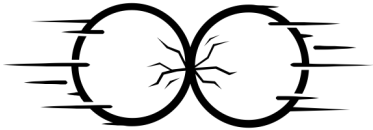
- Well defined way to go beyond GR
- Some theories are mathematically identical in specific limits
- Better understanding for future facilities

# Nonlinear interaction is important for

First Principles



Ultra-relativistic collisions  
Scattering  
Cosmic censorship



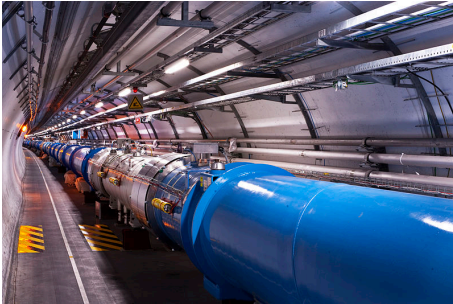
- Exceptional laboratories for controlled numerical experiments
- Interplay between extreme electromagnetic and gravitational fields

# Nonlinear interaction is important for

Energetic Particles



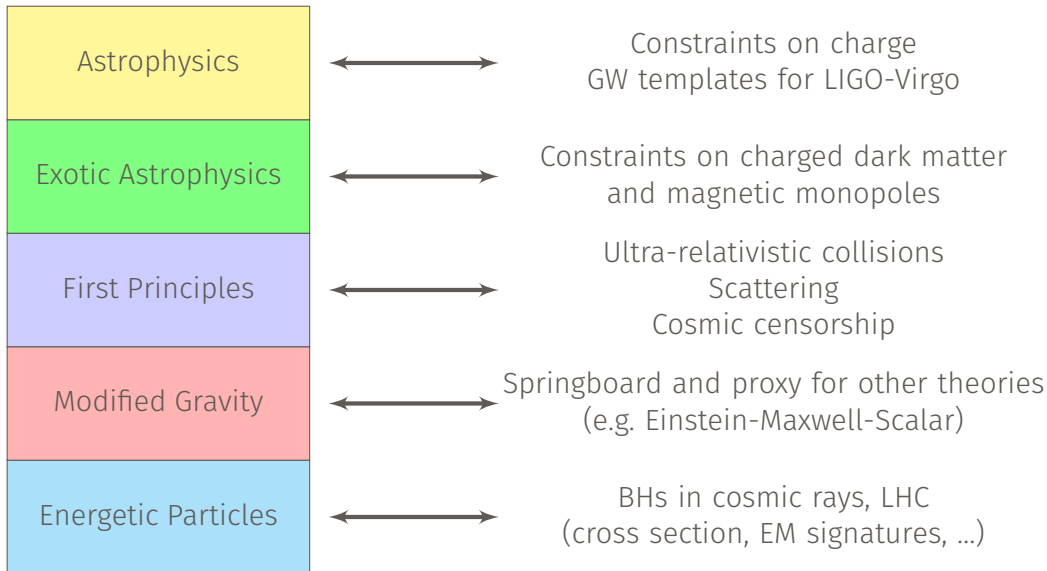
BHs in cosmic rays, LHC  
(cross section, EM signatures, ...)



- Microscopic black hole production and detection
- Tests of specific grand unified theories

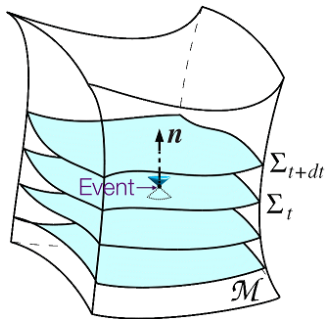


# Nonlinear interaction is important for



*This list is incomplete; you can help by expanding it.*

# Exploring nonlinear interactions = Solving Einstein-Maxwell's equations



Numerical solution of  
Einstein-Maxwell's equations as  
initial-value-problem

Issues with stability, gauge, initial  
data, ...

HARD PROBLEM!

Numerical Relativity



Improved/novel methods

Astrophysical black holes are expected to be neutral...

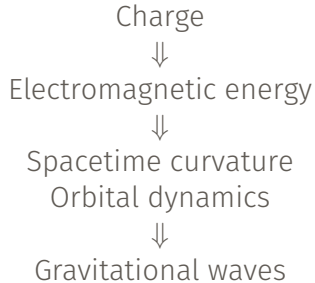
Discharge limits rely on  $\frac{1}{\sqrt{G}} \frac{Q_{\text{BH}}}{M_{\text{BH}}} < \sqrt{G} \frac{m_{\text{proton}}}{q_{\text{proton}}} \sim 10^{-18}$

Evaded if:

- Mini-charged dark matter ( $\sqrt{G}m/q \sim 1$ )
- Dark electromagnetism (different EM coupling)
- Magnetic monopoles (no discharge)
- Gravitational charge (SVTG\*,  $Q/(\sqrt{G}M) = \sqrt{\alpha/(1+\alpha)}$ , with  $\alpha$  coupling)

\* = Scalar-Vector-Tensor Gravity

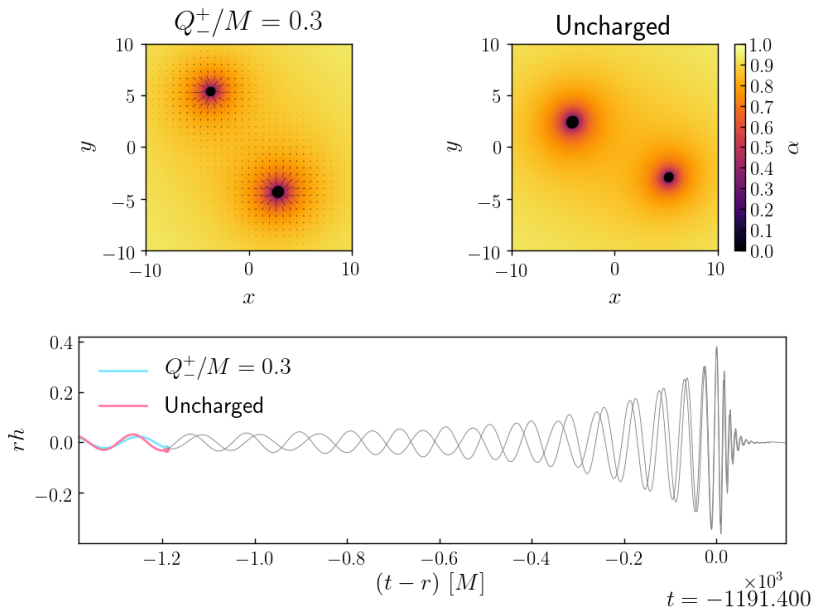
## How can we test this?

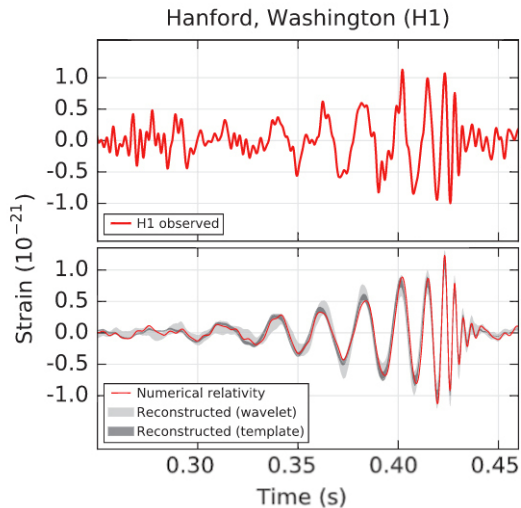


Strengths:

- Little modeling required
- Applicable to exotic astrophysics

**GWs know about charge**





GW150914:

- First confirmed GW event
- Loud and well-characterized (SNR = 25)
- Mass-ratio 29/36
- (Disputed) coincident EM observations

Full Bayesian analysis requires GW templates (= *currently impossible*)

First constraints on:

Black hole charge from GW150914:

Opposite charge:  $Q/(\sqrt{GM}) < \mathbf{0.2}$

Single charge:  $Q/(\sqrt{GM}) < \mathbf{0.35}$

Same charge:  $Q/(\sqrt{GM}) < \mathbf{0.4}$

(charge imbalance  $< 10^{-17} M_{\odot}$ )

Tightest constraint on STVG  
(Scalar-Vector-Tensor Gravity)  
in strong-field:

$$\alpha < \mathbf{0.19} \text{ (before } \alpha \lesssim 9)$$

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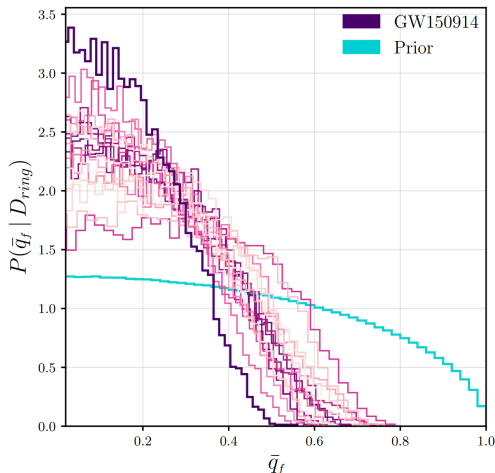
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Later confirmed by Carullo+, 2022:



$\bar{q}_f$  = final charge-to-mass-ratio



## Why charged BHs?

- Constraints w/ GWs
- Testing conjectures
- Advancing NR

## Astrophysics

- Full NR waveforms
- Bounds on  $Q/M$

## Modified Gravity

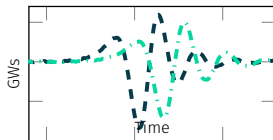
- Bound on SVTG  $\alpha$

## Current work

- GW template bank for LIGO/Virgo
- Effects of plasma (+ R. Luna, M. Zilhão, V. Cardoso)
- Quasi-normal-modes and 3G detectors (+ G. Carullo, M. de Amicis, V. Cardoso)
- Hyperbolic encounters (+ M. Smith)
- Censorship in quasi-circular mergers (+ C. Worley)



Ask me about:



High-energy collision