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Complete List of Authors:	Favier, Benoit Dal'Maz Silva, Walter
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# Scaleformer: a scalable transformer with linear complexity and relative positional encoding

Benoit Favier<sup>1</sup> and Walter Dal'Maz Silva<sup>2</sup>

<sup>1</sup>Phealing <sup>2</sup>Unaffiliated

Abstract—To overcome the quadratic complexity of the original transformer, some previous works proposed a kernelized attention mechanism which scales linearly with sequence length. Other works proposed to change the way the position of each token is encoded so that the model depends on relative distance between tokens instead of absolute position. In this work we propose a novel algorithm to combine kernelized attention with relative positional encoding while still scaling linearly in complexity. The proposed algorithm can be implemented with usual functions of neural network frameworks.

#### I. Introduction

Vaswani et al. [12] introduced the transformers, a novel architecture for sequence-to-sequence tasks, tackling new heights of problem complexity. The improvements were due to the non sequential nature of its training process which allowed better parallelization and thus fast training of big models, and due to improved long term dependencies thanks to the intrinsic good gradient flows of the attention mechanism. However the original transformer presents some drawbacks. It has a quadratic complexity with sequences length. And its absolute position encoding is detrimental to its extrapolation to new sequence lengths.

Ever since, significant efforts have been made to alleviate these problems. These improvements have opened the path to the application of transformers to image analysis where scalability and positional invariance are essential. However most proposed architecture we are aware of only alleviated parts of the issues, by being incompatible with relative positional encoding, having no scheme for masked attention - thus being restrained to encoder-only models, or being complex to use/implement - needing custom operations programmed in CUDA or introducing stochastic methods.

In the present work we propose a complete encoder-decoder transformer model that scales linearly with sequence lengths, by putting together ideas developed across several works [2, 5, 7, 10–12]. It remains compatible with relative positional encoding, and can be implemented with usual functions of neural network frameworks without requiring custom CUDA code.

#### II. BACKGROUND

#### A. Multi-head attention

The scaled dot-product attention proposed by Vaswani et al. [12] transforms the vectorial embedding  $\vec{Y}_i$  of a token, as a

function of a sequence variable in size of other tokens  $\vec{X}_j$ , where  $\vec{Y}_i$  and  $\vec{X}_j$  are all vectors of size D. A key  $\vec{K}_j$  and value  $\vec{V}_j$  are attributed to each vector  $\vec{X}_j$ , and query  $\vec{Q}_i$  is attributed to  $\vec{Y}_i$ . The query keys and values are obtained by linear projection from dimension D to d using three matrices of learnable parameters. The transformed vector  $\vec{y}_i$  is a weighted sum of the  $\vec{V}_j$ . The weights are scores of matching between the query  $\vec{Q}_i$  and the keys  $\vec{K}_j$ , calculated as the dot product between the two vectors. The weights are also softmaxed to sum up to 1.

The transformation of  $L_Q$  vectors  $\vec{Y}_i$  as a function of  $L_K$  vectors  $\vec{X}_j$  can be efficiently computed with matrix multiplications:

$$A = \operatorname{softmax}\left(\frac{Q \times K^T}{\sqrt{d}}\right) \times V \tag{1}$$

with Q a matrix of shape  $(L_Q,d)$ , K a matrix of shape  $(L_K,d)$  and V a matrix of shape  $(L_K,d)$ . The  $\sqrt{d}$  at the denominator is a scaling factor used to avoid saturation in the exponential terms of the softmax function.

The multi-head attention performs h different projections into spaces of dimension d = D/h. The resulting vector  $\vec{Y}_i'$  is the concatenation of the h vectors  $\vec{y}_i'$ , thus the embedding dimension is preserved. Using multiple heads was found beneficial by the authors over using a single head of dimension d = D.

During training, the cross entropy of the  $n^{th}$  predicted token is calculated assuming all previous tokens have been generated correctly. This enables to parallelize training completely as there is no recurrence in the calculation process. However, as the  $n^{th}$  token should not depend of the following tokens, the cells in the upper right corner of the score matrix are set to  $-\infty$  such that after the softmax they are equal to 0, and the rows still sum up to one.

# B. Improving scalability

The original attention mechanism requires the computation of a score matrix  $Q \times K^T$  of shape  $(L_Q, L_K)$ , with complexity  $O(dL_QL_K)$ . If the query and key sequence lengths are multiplied by two, then the memory used and computation time are multiplied by four. To improve the scalability of the transformer with sequence length, several axis of research have been explored.

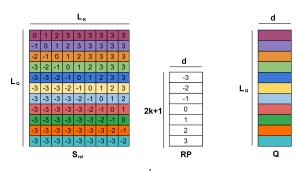


Fig. 1:  $S^{rel}$  calculation

Kitaev et al. [8] proposed the Reformer's architecture, which uses an hash-bucketting algorithm to reduce the complexity of the original multi-head attention operation from  $O(L^2)$  to  $O(L\log(L))$ .

Dai et al. [3] proposed the Transformer-XL's architecture, which cuts the sequence in segments of length L. The model predicts each stage of the current segment as a function of the previous and current segment. All the segments are computed sequentially with a recurrence mechanism. The complexity is linear with sequence length, but the computation cannot be completely parallelized due to the recurrence mechanism.

Other publications explored using a sparse attention matrix, such as the Longformer by Beltagy et al. [1] and the Big Bird model by Zaheer et al. [14]. As each token attends to a fixed number of all other tokens, the scalability is improved. These sparse attention models however require custom operations implemented in CUDA.

Some other works propose to modify the attention mechanism so that it's complexity scales linearly with sequence length. The Linformer by Wang et al. [13] projects the key and values onto a smaller sequence length dimension with matrix multiplication. It cannot however generalize to sequences longer than used during training, as the weights of the projection for such tokens would be undefined.

Shen et al. [11] proposed to replace the softmax attention score,  $A = \operatorname{softmax}\left(\frac{Q \times K^T}{\sqrt{d}}\right) \times V$  is changed into  $A = \rho(Q) \times \rho(K)^T \times V$ , with  $\rho$  the softmax function along the embedding dimension. Thanks to the matrix multiplication operator associativity property, the order of the operations can be chosen. If Q, K and V are of shape  $(L_Q, d)$ ,  $(L_K, d)$  and  $(L_K, d)$  respectively, the complexity of  $(\rho(Q) \times \rho(K)^T) \times V$  is  $O(L_Q \times d \times L_K)$  whereas the complexity of  $\rho(Q) \times (\rho(K)^T \times d)$ V) is  $O(\max(L_Q, L_k) \times d^2)$ . The right-side-first operation is linear in complexity with sequence length. The shape of the intermediate result matrix is also changed, allowing to scale better in memory requirements as well. The original softmaxed attention score matrix was giving rows of positive scores that sum up to one. With this change the elements of the score matrix remain positive as  $\rho(Q)$  and  $\rho(K)^T$  are matrices of positive values, but the rows of the score matrix do not sum up to 1. This work also does not give a linear complexity formulation for masked attention. If the right-side-first scheme is adopted, the attention score matrix  $\rho(Q) \times \rho(K)^T$  is never explicitly computed, and cannot be masked.

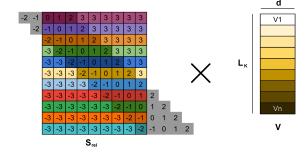


Fig. 2:  $A^{rel}$  naive calculation

Building on this idea of commutative attention function proposed by Shen et al. [11], Katharopoulos et al. [7] introduced their kernerlized attention function as:

$$A = \frac{\phi(Q) \times \phi(K)^T}{\sum_{i} (\phi(Q) \times \phi(K)^T)} \times V \tag{2}$$

The function  $\phi$  is applied element-wise and can be any positive function, for example  $\phi(x) = \mathrm{elu}(x) + 1$ . This attention is row-wise normalized so that all rows of the score matrix are sets of positive weights adding up to one. This preserves the objective of the original softmaxed attention scores, while allowing to perform operations in an optimal order.

The Performer by Choromanski et al. [2] exploits the same idea of a kernelized attention introduced by Katharopoulos et al. [7], with an algorithm that better approximates *softmaxed* attention. Most importantly they also give in annex a prefix sum algorithm to perform operations in the right-side-first order while giving the same result as masked left-side-first operation. Althought they give no insight in their paper as how the operation could be implemented without custom CUDA code.

In this work we will explicit an implementation of the rightside-first masked operation, with usual functions from neural network frameworks, that remains linear in complexity.

## C. Relative positional encoding

The original multi-head attention operation introduced by Vaswani et al. [12] was intrinsically invariant by token order permutation. As token position was an important information for machine translation models, they encoded the global position of each token in their embedding. Since then, some modified attention mechanisms, that depend on relative tokens position, have been proposed.

Shaw et al. [10] explored modifying the attention mechanism so that it depends on the relative distance between tokens. A second score matrix that is function of the query and the query/key relative distance is added to the original score matrix,  $A = softmax\left(\frac{Q \times K^T}{\sqrt{d}}\right) \times V$  becomes  $A = \left(\frac{Q \times K^T + S_{rel}}{\sqrt{d}}\right) \times V$  with  $S_{rel}$  of shape  $(L_Q, L_K)$  defined as  $S_{ij}^{rel} = \vec{Q_i} \cdot \vec{RP}_{clip(i-j,-k,k)}$ . Where k is the attention horizon length and  $\vec{RP}_n$  is one of 2k+1 relative positional embedding, vectors of size d. Shaw et al. [10] and Huang et al. [6] observed

that introducing this attention scheme improved performances. The naive calculation of this term however has a complexity of  $O(dL_QL_K)$ . No algorithm was provided to linearize the complexity.

More recently Liutkus et al. [9] gives a stochastic positional encoding that is linear in complexity with regards to sequence length. However the implementation is complex and its stochastic nature requires that the operations be repeated several times in parallel.

Horn et al. [5] noted that the term  $S^{rel} \times V$  can be computed with linear complexity for the case where  $RP_{-k} = RP_k$ . However this is restraining as the model cannot make the difference between tokens before the attention horizon or after.

In this work we will show that the computation of  $S^{rel} \times V$  can also be done with linear complexity, without concession.

#### III. LINEAR COMPLEXITY MASKED ATTENTION

In this section we will detail the prefix sum algorithm proposed by Choromanski et al. [2] for masked kernelized attention, and give an implementation with usual functions of neural network frameworks. The masked kernelized attention is defined as:

$$A^{masked} = \text{masked} \left(\phi(Q) \times \phi(K)^T\right) \times V$$
 (3)

In this expression, *masked* being the operation that set all cells above the diagonal to 0 in a matrix. The naive implementation of this operation has complexity  $O(dL_OL_K)$ .

We can change the complexity using the operation proposed by Choromanski et al. [2], as it will be derived here. To start with,  $A^{masked}$  is expressed as

$$A^{masked} = S^{masked} \times V \tag{4}$$

which in summation form is expressed as

$$A_{ij}^{masked} = \sum_{k} S_{ik}^{masked} \times V_{kj}$$
 (5)

and the elements of  $S^{masked}$  are defined as

$$S_{ik}^{masked} = \begin{cases} \sum_{l} \left( \phi(Q)_{il} \times \phi(K)_{kl} \right) & \text{if } k \le i \\ 0 & \text{otherwise} \end{cases}$$
 (6)

putting these elements together leads to

$$A_{ij}^{masked} = \sum_{k=1}^{i} \left( V_{kj} \times \sum_{l} \left( \phi(Q)_{il} \times \phi(K)_{kl} \right) \right) \tag{7}$$

which can be reworked as

$$A_{ij}^{masked} = \sum_{l} \left( \phi(Q)_{il} \times \sum_{k=1}^{i} \left( \phi(K)_{kl} \times V_{kj} \right) \right)$$
 (8)

In this work we make use of these ideas to implement the calculation of  $A^{masked}$  with complexity  $O(\max(L_Q, L_K) \times d^2)$  without custom CUDA code as per the algorithm 1. The following functions are provided:

- align(tensor, n, dim) the function that truncates or repeats the last value so that tensor has length n along the given dimension
- cumsum(tensor, dim) the function that returns the cumulated sum along the given dimension

```
Algorithm 1: O(L) calculation of _{\text{masked}}(\phi(Q) \times \phi(K)^T) \times V

Input: \phi(Q) tensor of shape (L_Q, d)
\phi(K) tensor of shape (L_K, d)
V tensor of shape (L_K, d)

Data: Expanded tensor of shape (L_K, d, d)
Summed tensor of shape (L_K, d, d)
Aligned tensor of shape (L_Q, d, d)

Result: A^{masked} tensor of shape (L_Q, d, d)

Expanded _{kjl} := V_{kj} \times \phi(K)_{kl}
Summed := cumsum (Expanded, dim=0)
```

 $\begin{array}{l} \text{Aligned} := align(\text{Summed}, L_Q, \text{dim=0}) \\ A^{masked}_{ij} := \sum_k \left( \phi(Q)_{ik} \times \text{Aligned}_{ikj} \right) \end{array}$ 

**Algorithm 2:** O(L) calculation of  $S^{rel} \times V$ 

```
Input: \phi(Q) tensor of shape (L_Q, d)
                            \phi(RP) tensor of shape (2k+1,d)
                            V tensor of shape (L_K, d)
       Data: W tensor of shape (L_Q, 2k+1)
                          Cumulated tensor of shape (L_O, d)
                          Summed tensor of shape (d)
                          Rcum tensor of shape (L_Q, d)
                          W^{horizon} tensor of shape (L_Q, 2k-1) V^{horizon} tensor of shape (L_Q, 2k-1, d)
                         W^{before/after} vectors of length L_Q V^{before/after} tensors of shape (L_Q, d) A^{before/horizon/after} tensors of shape (L_Q, d)
                          n_{before} := min(k, L_Q), scalar
                          n_{after} := min(L_Q + k, L_K), scalar
       Result: A^{rel} tensor of shape (L_Q, d)
       W := \phi(Q) \times \phi(RP)^T
\begin{split} &W := \phi(Q) \wedge \phi(\Pi) \\ &Cumulated := cumsum(V, dim = 0) \\ &W_i^{before} := W_{i,0} \\ &V_{ij}^{before} := \begin{cases} 0 & \text{if } i < n_{before} \\ Cumulated_{i-p_{before},j} & \text{otherwise} \end{cases} \\ &A_{ij}^{before} := W_i^{before} \times V_{ij}^{before} \\ &W_{ij}^{horizon} := W_{i+1,j} \\ &V_{ijl}^{horizon} := \begin{cases} V_{i-k+1+j,l} & \text{if } 0 \leq (i-k+1+j) < L_K \\ 0 & \text{otherwise} \end{cases} \\ &A_{il}^{horizon} := \sum_{j} \left(W_{ij}^{horizon} \times V_{ijl}^{horizon}\right) \\ &Summed_{j} := \sum_{i} \left(V_{ij}\right) \\ &Rcum_{ij} := \begin{cases} Summed_{j} & \text{if } i = 0 \\ Summed_{j} - Cumulated_{i-1,j} & \text{otherwise} \end{cases} \\ &W_{i}^{after} := W_{i,2k} \\ &V_{ij}^{after} := W_{i,2k} \\ &V_{ij}^{after} := W_{i}^{after} \times V_{ij}^{after} \\ &0 & \text{otherwise} \end{cases} \\ &A_{ij}^{after} := W_{i}^{after} \times V_{ij}^{after} \\ &A_{ij}^{rel} := A_{ij}^{before} + A_{ij}^{horizon} + A_{ij}^{after} \end{cases}
       Cumulated := cumsum(V, dim = 0)
```

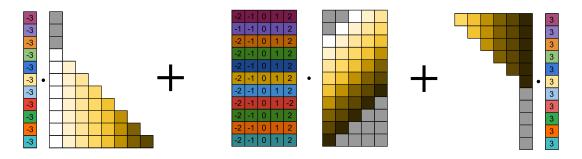


Fig. 3: linear complexity calculation of  $A^{rel}$ 

## IV. LINEAR COMPLEXITY RPE<sup>1</sup>

In this section we will detail how the relative positional encoding proposed by Shaw et al. [10] can in fact be computed with linear complexity. The  $S^{rel}$  matrix of scores is computed as  $S^{rel}_{ij} = \overrightarrow{Q_i} \cdot \overrightarrow{RP}_{clip(i-j,-k,k)}$ .

In figure 1 the colors represent the index of the query, and the number the index of the relative position.

The relative positional encoding term of the attention is calculated as  $A^{rel} = S^{rel} \times V$ . Each row of the  $A^{rel}$  matrix is a weighted sum of the value vectors  $V_i$ . Each row of  $S^{rel}$  is a set of weights.

One can observe in figure 2 that some weights are repeated several times in the  $S^{rel}$  matrix. Calculating the whole matrix can be avoided by instead calculating all possible weights only once, with complexity  $O(L_Q \times d \times (2k+1))$ ). As illustrated in figure 3, the matrix multiplication can then be replaced by a sum of three terms. The grey squares represent some zero-padding. The first term is a cumulated sum of the value vectors that is weighted by the before-horizon set of weights - complexity  $O(\max(L_Q, L_K))$ . The second term is a weighed sum of a moving window of the value vectors. Where the weights are the central diagonal of the  $S^{rel}$  matrix - complexity  $O(L_O \times (2k-1) \times d)$ . The last term is similar to the first term, but for the after-horizon set of weights complexity  $O(\max(L_O, L_K))$ . The implementation is given in algorithm 2. The algorithm can be extended to masked attention by setting all vectors of the RP matrix with strictly positive indexes to  $\vec{0}$ .

#### V. THE SCALEFORMER

The proposed model replaces the scaled-dot-product-attention and absolute positional encoding by a kernelized attention with relative positional encoding. In this work we have chosen the following formulation, with  $\phi(x) = \text{elu}(x) + 1$ .

$$A = \frac{\left(\phi(Q) \times \phi(K^T) + S^{rel}\right)}{\sum_{i} \left(\phi(Q) \times \phi(K^T) + S^{rel}\right)} \times V \tag{9}$$

This is essentially a combination of two terms, the kernelized attention proposed by Katharopoulos et al. [7], and the relative positional encoding proposed by Shaw et al. [10].

The left term is the score matrix of shape  $(L_Q, L_K)$ , with a denominator which scales all rows so that they sum to 1.

For the linear complexity implementation, the multiplication must be distributed as:

$$A = \frac{\left(\phi(Q) \times \phi(K^T) \times V\right) + \left(S^{rel} \times V\right)}{\sum_{j} \left(\phi(Q) \times \phi(K^T)\right) + \sum_{j} \left(S^{rel}\right)} \tag{10}$$

The denominator can be easily calculated by applying the linear complexity algorithms with V replaced by a matrix of shape  $(L_K, 1)$  full of 1, or by summing the rows of the score matrix for quadratic complexity algorithm.

For compatibility with the kernelized attention, as the scores are not *softmaxed* and must be positive, the function  $\phi$  must be applied to Q and RP before calculating  $S^{rel}$ :

$$S_{ij}^{rel} = \sum_{l} \phi(Q)_{il} \times \phi(RP)_{clip(i-j,-k,k),l}$$
 (11)

The linear complexity algorithms are a trade-off of quadratic complexity with sequence length for quadratic complexity with projection dimension d. Increasing expressiveness power of the model can however be done efficiently by increasing the number of heads. Both the naive and linear algorithm have linear complexity with the number of attention heads.

# VI. RESULTS

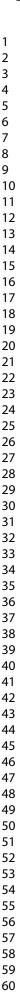
The various algorithms have been timed on CPU and runtimes have been plotted against sequences length in  $\log_2$ - $\log_2$  scale. Algorithms that scale linearly with sequence length have a slope of one, while algorithms that scale quadratically with sequence length have a slope of two. Figure 4 shows the timings of the  $A^{rel}$  matrix computation.

In Figure 5 the kernelized attention algorithms have been timed. We can observe that although our algorithm for masked attention has a linear complexity, it is still often slower than the quadratic complexity algorithm. The bottleneck in our implementation[4] is the cumulated sum operation.

#### VII. CONCLUSION

In the present work an algorithm to compute Shaw et al. [10] relative positional encoding with linear complexity has been presented. An implementation of Choromanski et al. [2] prefix sum algorithm that does not requires custom CUDA

<sup>&</sup>lt;sup>1</sup>Relative Positional Encoding



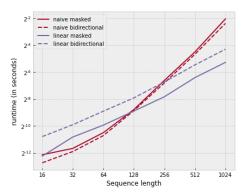


Fig. 4:  $S^{rel} \times V$  calculation runtimes for d=64 and k=16

code - while maintaining linear complexity - was presented as well. These two elements allowed to define a kernelized attention function with relative positional encoding that can be computed with linear complexity with regards to sequence length. This opens the path to sequence to sequence models trained on bigger document sizes, that better generalize to sequences longer than the ones used during training thanks to relative positional encoding.

Several tasks would benefit from being applied on longer sequences. Chat bots trained on full conversations could take into account informations delivered several exchanges before. Machine translation models applied on whole documents would have more information of the context than simple sentence to sentence translations.

#### TABLE OF SYMBOLS

 $\boldsymbol{A}$ result of the attention operation, tensor of shape  $(L_O, d)$ dprojection dimension Dembedding dimension hnumber of heads  $\boldsymbol{k}$ radius of the attention horizon  $\boldsymbol{K}$ keys linked to the attended sequence, tensor of shape  $(L_K, d)$  $L_K$ sequence length of the attended sequence  $L_Q$ sequence length of the transformed sequence query linked to the sequence to transform, tensor of shape  $(L_Q, d)$  $\vec{RP}$ relative position embeddings, tensor of shape (2k + 1, d) $S^{rel}$ matrix of relative position scores, tensor of shape  $(L_Q, L_K)$ values linked to the attended sequence, tensor of shape  $(L_K, d)$ 

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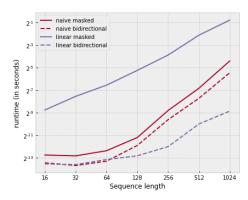


Fig. 5:  $\phi(Q) \times \phi(K^T) \times V$  calculation runtimes for d = 64

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