

## Towers of Hanoi

In 1883, Edouard Lucas invented, or perhaps reinvented, one of the most popular puzzles of all times

– the Tower of Hanoi, as he called it – which is still used today in many computer science textbooks to demonstrate how to write a recursive algorithm or program. First of all, we will make a list of the rules of the puzzle:

- There are three pegs: *A*, *B* and *C*.
- There are  $n$  disks. The number  $n$  is constant while working the puzzle.
- All disks are different in size.
- The disks are initially stacked on peg *A* so that they increase in size from the top to the bottom.
- The goal of the puzzle is to transfer the entire tower from the *A* peg to one of the others pegs.
- One disk at a time can be moved from the top of a stack either to an empty peg or to a peg with a larger disk than itself on the top of its stack.

A good way to get a feeling for the puzzle is to write a program which will show a copy of the puzzle on the screen and let you simulate moving the disks around. The next step could be to write a program for solving the puzzle in an efficient way. You don't have to do neither, but only know the actual situation after a given number of moves by using a determinate algorithm.

### The Algorithm

It is well known and rather easy to prove that the minimum number of moves needed to complete the puzzle with  $n$  disks is  $2^n - 1$ . A simple algorithm which allows us to reach this optimum is as follows: for odd moves, take the smallest disk (number 1) from the peg where it lies to the next one in the circular sequence

*ABCABC . . .*; for even moves, make the only possible move not involving disk 1.

## Input

The input file will consist of a series of lines. Each line will contain two integers  $n$ ,  $m$ :  $n$ , lying within the range  $[0, 100]$ , will denote the number of disks and  $m$ , belonging

to  $[0, 2^n - 1]$ , will be the number of the last move. The file will end at a line formed by two zeros.

## Output

The output will consist again of a series of lines, one for each line of the input. Each of them will be formed by three integers indicating the number of disks in the pegs  $A$ ,  $B$  and  $C$  respectively, when using the algorithm described above.

## Sample Input

```
3 5
64 2
8 45
0 0
```

## Sample Output

```
1 1 1
62 1 1
4 2 2
```