

Project_Euler_021

February 4, 2018

1 Project Euler Problem 21

Let $d(n)$ be defined as the sum of proper divisors of n (numbers less than n which divide evenly into n). If $d(a) = b$ and $d(b) = a$, where $a \neq b$, then a and b are an amicable pair and each of a and b are called amicable numbers.

For example, the proper divisors of 220 are 1, 2, 4, 5, 10, 11, 20, 22, 44, 55 and 110; therefore $d(220) = 284$. The proper divisors of 284 are 1, 2, 4, 71 and 142; so $d(284) = 220$.

Evaluate the sum of all the amicable numbers under 10000.

```
In [5]: from math import sqrt, ceil
```

```
amicable_sum = 0
```

```
# The function divisorsum(k) gets the sum of proper divisors of k  
# by going through all numbers i from 2 to sqrt(k) and checking  
# divisibility. If i is the square root of k, we just add that  
# to the sum of divisors. Otherwise, if i is a divisor of k  
# less than the square root of k, we add i and k/i to  
# the sum of divisors. Remember that 1 is always a divisor of  
# any integer, so we add that at the end.
```

```
def divisorsum(k):  
    total = 0  
    for i in range(2, int(ceil(sqrt(k))) + 1):  
        if k / i == i and k % i == 0:  
            total += i  
        elif i > sqrt(k):  
            total += 0  
        elif k % i == 0:  
            total += i  
            total += k/i  
    return int(total + 1)
```

```
# A number j is part of an amicable pair if the divisor sum of its  
# divisor sum is equal to j, and if the divisor sum of j isn't  
# equal to j.
```

```
for j in range(5, 10000):  
    if (divisorsum(divisorsum(j)) == j and  
        divisorsum(j) != j):  
        amicable_sum += j  
  
print("The sum of amicable numbers under 10000 is {}".  
      .format(amicable_sum))
```

The sum of amicable numbers under 10000 is 31626