

# Recursion

# Objectives

After this lecture you will be able to:

- Define recursion (in computer science)
- List the two cases of a recursive algorithm
  - base case, recursive case
- Step through `factorial`, a classic example of recursion
- List advantages/disadvantages of using recursion in your code
- Describe an application of recursion used in a capstone
  - Route finding between two points

# Recursion (in computer science)

- Recursion is a method of solving a problem where the solution depends on solutions to smaller instances of the same problem.
- Recursion solves problems by using functions that call themselves from within their own code.
- Often iteration can be used to solve the same problem instead, but you need to determine the number of iterations beforehand to solve the problem.

[--Wikipedia](#)

# General structure of a recursive algorithm

```
def recursive_function(input):  
    check if input is some value  
        if so, return the base case (non-recursive value)  
    otherwise  
        return the recursive case (recursive_function(modified input))
```

# Classic recursion example: factorial

$$3! = 3 * 2 * 1 = 6$$

$$5! = 5 * 4 * 3 * 2 * 1 = 120$$

$$0! = 1$$

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```
def factorial(n):  
    if n == 0:  
        return 1  
    else:  
        return n * factorial(n - 1)
```

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    if n == 0:  
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```

*base case*

*recursive case*

# Code investigation

`factorial.py`



# Advantages / disadvantages of recursion

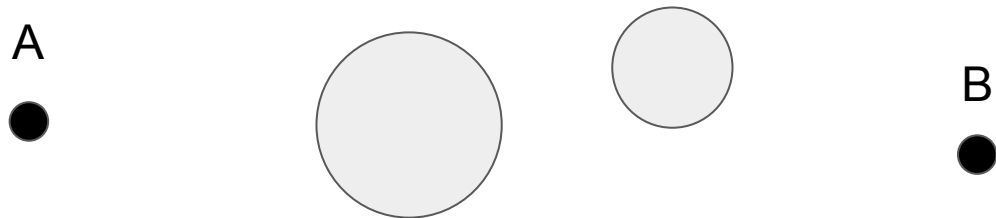
## Advantages

- Often results in easier-to-read code with less to debug
- Better than iteration if it's not known beforehand how many iterations are required (tree-traversal)

## Disadvantages

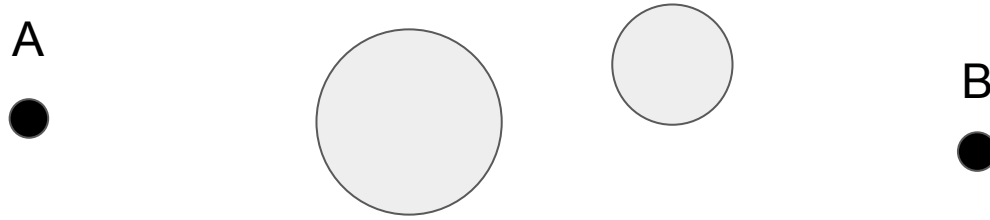
- Uses more memory (function add to the call stack with each recursive call)
- Can be slower than iteration (though saving results of past recursive calls - memoization - can mitigate this)

# Example used in a capstone: route-finding



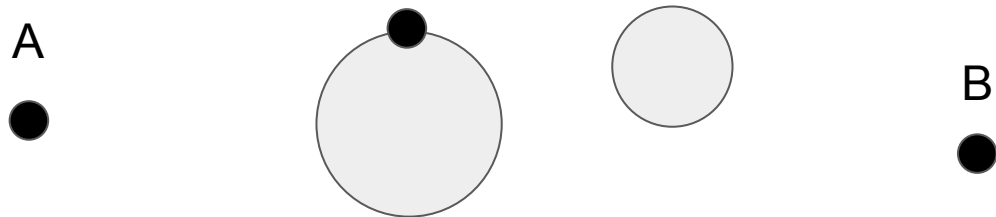
Find the shortest route between points A and B that doesn't go through a circle obstruction.

# Example used in a capstone: route-finding



```
get_route(start_pt, end_pt, obstructions)
    check if there are obstructions between the start_pt and end_pt
    if there are no obstructions:
        find the straight-line path (base case)
    if there are obstructions:
        determine a new_start_pt on the nearest obstruction
        remove that obstruction from possible obstruction list
        travel there
        get_route(new_start_pt, end_pt, obstructions) (recursive case)
```

# Example used in a capstone: route-finding



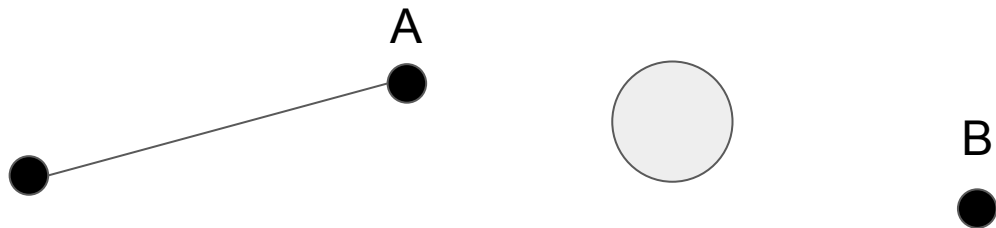
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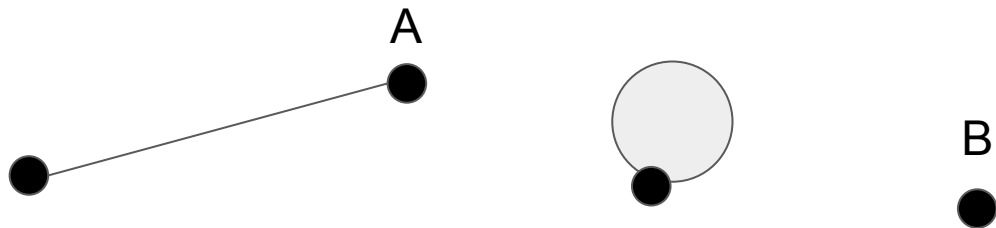
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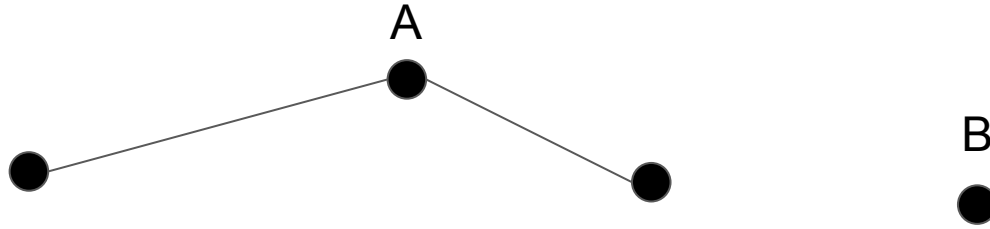
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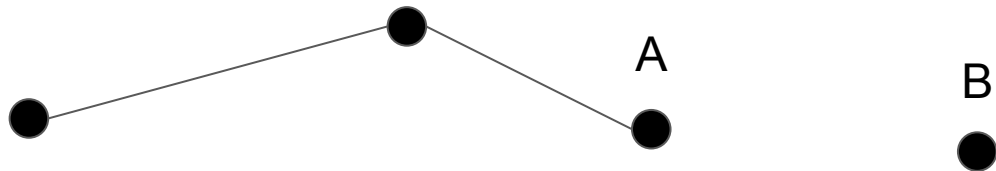
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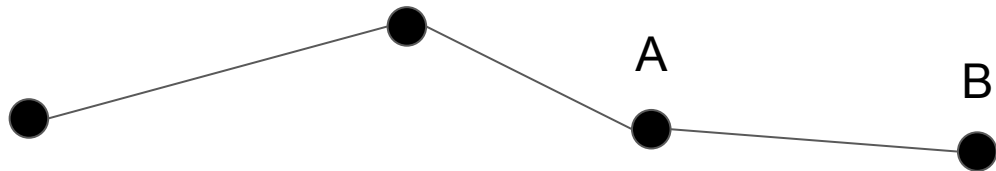


# Example used in a capstone: route-finding



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# See it in a Capstone: UAV package delivery

[https://github.com/Frank-W-B/UAV\\_delivery\\_project](https://github.com/Frank-W-B/UAV_delivery_project)

# Code example

```
randomized_test_routing_not_smoothed_occasional_failures.py
```

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