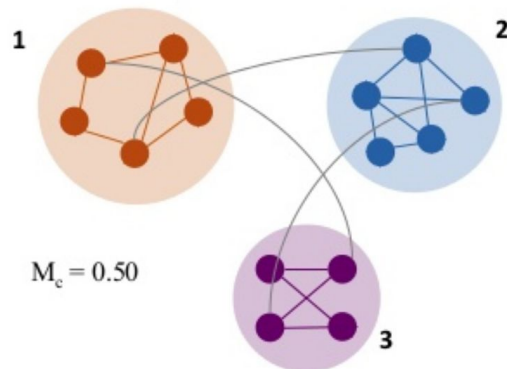
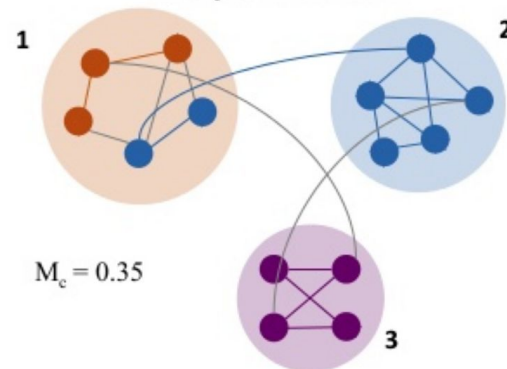


Graphs-Modularity

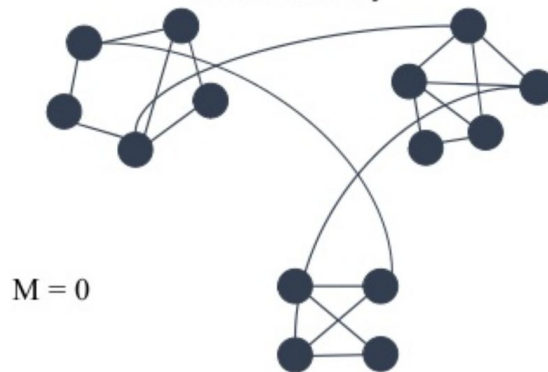
Optimal Partition



Suboptimal Partition



One Community



Modularity

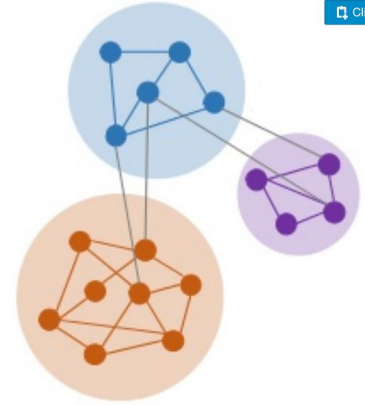
$$M_c = \sum_{c=1}^{n_c} \left[\frac{L_c}{L} - \left(\frac{k_c}{2L} \right)^2 \right]$$

Modularity

- Measure the **quality of a partition**

$$M_c = \sum_{c=1}^{n_c} \left[\frac{L_c}{L} - \left(\frac{k_c}{2L} \right)^2 \right]$$

“the fraction of edges that fall within communities, minus the expected value of the same quantity if edges fall at random without regard for the community structure”



Modularity

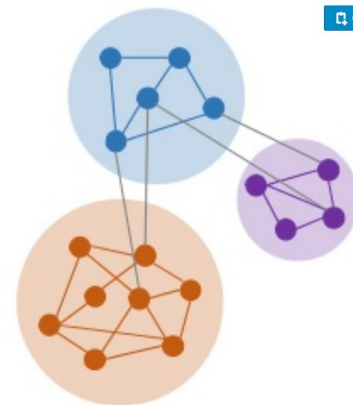
$$M_c = \sum_{c=1}^{n_c} \left[\frac{L_c}{L} - \left(\frac{k_c}{2L} \right)^2 \right]$$

Number of communities (points to n_c)

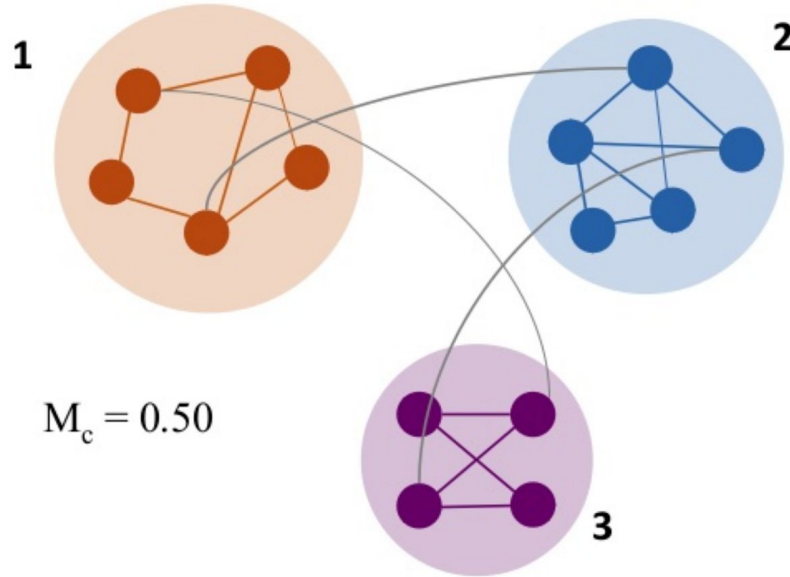
Total number of links in Community c (points to L_c)

Total node degrees in Community c (points to k_c)

Total number of links (points to L)



Modularity



Number of communities n_c Total number of links in Community c L_c Total node degree in Community c k_c [Clip slide](#)

$$M_c = \sum_{c=1}^{n_c} \left[\frac{L_c}{L} - \left(\frac{k_c}{2L} \right)^2 \right]$$

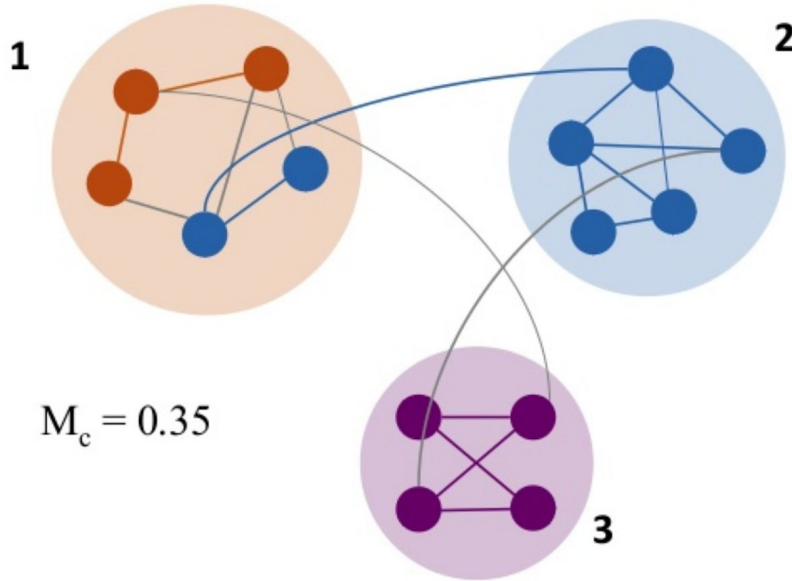
Total number of links L

Community 1: $\left[\frac{6}{20} - \left(\frac{14}{40} \right)^2 \right]$

Community 2: $\left[\frac{7}{20} - \left(\frac{16}{40} \right)^2 \right]$

Community 3: $\left[\frac{4}{20} - \left(\frac{10}{40} \right)^2 \right]$

Modularity



Number of communities n_c

Total number of links in Community c L_c

Total node degree in Community c k_c

Total number of links L

$$M_c = \sum_{c=1}^{n_c} \left[\frac{L_c}{L} - \left(\frac{k_c}{2L} \right)^2 \right]$$

Community 1: $\left[\frac{2}{20} - \left(\frac{8}{40} \right)^2 \right]$

Community 2: $\left[\frac{9}{20} - \left(\frac{22}{40} \right)^2 \right]$

Community 3: $\left[\frac{4}{20} - \left(\frac{10}{40} \right)^2 \right]$