Bad data & Outliers

true

11/21/22

Cleaning data, dealing with missing data and comparing results for correlation and regression before vs. after removing an outlier from the data.

Table of contents

1	Data	2
	1.1 Import	2
	1.2 Goal	3
	1.3 Exploring	3
2	Missing Data?	6
3	Corr. & Reg.	7
4	Outlier?	9
	4.1 Step 1: Investigate	9
	4.2 Step 2: Act	10
5	Corr. & Reg again	10
	5.1 \mathbb{R}^2 - Coeff. of det	14
	# (install &) load packages	
	<pre>pacman::p_load(</pre>	
	broom,	
	conflicted,	
	here,	
	janitor,	
	naniar,	
	readxl,	
	tidyverse	

```
# handle function conflicts
conflict_prefer("filter", "dplyr")
conflict_prefer("select", "dplyr")
```

There are two download links:

- Download the **original** excel file here.
- Download the **formatted** excel file here.

1 Data

Imagine that this dataset was obtained by you. You spent an entire day walking around the campus of a university and asked a total of 29 people for things like how old they are and you also tested how well they could see on a scale of 1-10.

1.1 Import

Assuming you are working in a R-project, save the formatted file somewhere within the project directory. I have saved it within a sub folder called data so that the relative path to my file is data/vision_fixed.xls.

```
path <- here("data", "vision_fixed.xls")</pre>
dat <- read_excel(path)</pre>
dat
# A tibble: 29 x 9
   Person
             Ages Gender `Civil state` Height Profession Vision Distance PercDist
   <chr>
            <dbl> <chr>
                                           <dbl> <chr>
                                                               <dbl>
                                                                         <dbl>
                                                                                  <dbl>
                          <chr>
 1 Andrés
               25 M
                          S
                                             180 Student
                                                                  10
                                                                           1.5
                                                                                    15
 2 Anja
               29 F
                          S
                                             168 Professio~
                                                                  10
                                                                           4.5
                                                                                    45
 3 Armando
               31 M
                          S
                                             169 Professio~
                                                                   9
                                                                           4.5
                                                                                    50
 4 Carlos
               25 M
                                             185 Professio~
                                                                   8
                                                                           6
                                                                                    75
                          M
 5 Cristi~
               23 F
                          <NA>
                                             170 Student
                                                                  10
                                                                                    30
                                                                           3
               39 F
                                             158 Professio~
                                                                           4.5
                                                                                    75
 6 Delfa
                          M
                                                                   6
 7 Eduardo
               28 M
                          S
                                             166 Professio~
                                                                   8
                                                                           4.5
                                                                                    56.2
 8 Enrique
               NA <NA>
                          <NA>
                                              NA Professio~
                                                                  NA
                                                                                    NA
```

```
9 Fanny 25 F M 164 Student 9 3 33.3
10 Franci~ 46 M M 168 Professio~ 8 4.5 56.2
# i 19 more rows
```

This is optional, but we could argue that our column names are not in a desirable format. To deal with this, we can use the clean_names() functions of {janitor}. This package has several more handy functions for cleaning data that are worth checking out.

```
dat <- dat %>% clean_names()
dat
```

# A tibble: 29 x 9									
		_		h a d mb b			44-4		
perso	on age	s gender	civil_state	neight	profession	Vision	distance	perc_dist	
<chr< td=""><td>> <dbl< td=""><td><chr></chr></td><td><chr></chr></td><td><dbl></dbl></td><td><chr></chr></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td></dbl<></td></chr<>	> <dbl< td=""><td><chr></chr></td><td><chr></chr></td><td><dbl></dbl></td><td><chr></chr></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td></dbl<>	<chr></chr>	<chr></chr>	<dbl></dbl>	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	
1 Andre	és 2	5 M	S	180	Student	10	1.5	15	
2 Anja	2	9 F	S	168	Professio~	10	4.5	45	
3 Armai	ndo 3	l M	S	169	Professio~	9	4.5	50	
4 Carlo	os 2	5 M	M	185	Professio~	8	6	75	
5 Cris	tina 2	3 F	<na></na>	170	Student	10	3	30	
6 Delfa	a 3	9 F	M	158	Professio~	6	4.5	75	
7 Eduar	rdo 2	3 M	S	166	Professio~	8	4.5	56.2	
8 Enri	que N.	A <na></na>	<na></na>	NA	Professio~	NA	6	NA	
9 Fanny	y 2	5 F	M	164	Student	9	3	33.3	
10 Franc	cis~ 4	6 M	M	168	Professio~	8	4.5	56.2	
# i 19 more rows									

1.2 Goal

Very much like in the previous chapter, our goal is to look at the relationship of two numeric variables: ages and vision. What is new about this data is, that it (i) has missing values and (ii) has a potential outlier.

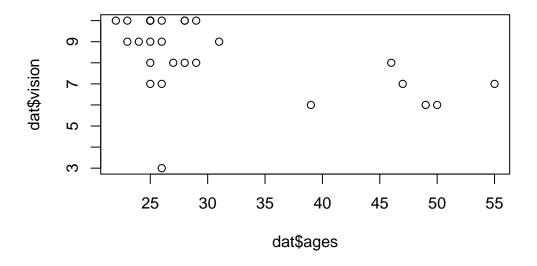
1.3 Exploring

To quickly get a first feeling for this dataset, we can use summary() and draw a plot via plot() or ggplot().

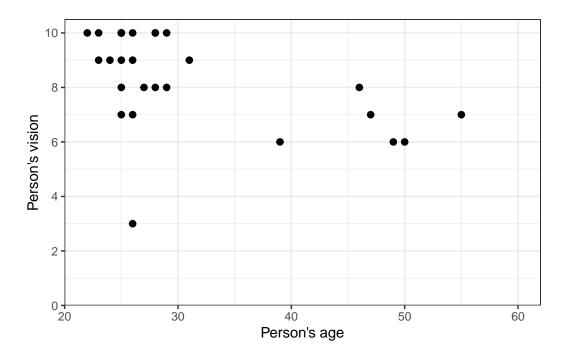
```
summary(dat)
```

```
person
                                   gender
                                                 civil_state
                     ages
Length:29
                 Min. :22.00
                               Length:29
                                                 Length:29
Class : character
                 1st Qu.:25.00
                                Class :character
                                                 Class : character
Mode :character
                 Median :26.00
                                Mode :character
                                                 Mode :character
                 Mean
                       :30.61
                 3rd Qu.:29.50
                 Max.
                       :55.00
                 NA's
                      :1
   height
               profession
                                   vision
                                                  distance
                                Min. : 3.000 Min.
Min. :145.0
              Length:29
                                                     :1.500
1st Qu.:164.8
              Class:character 1st Qu.: 7.000 1st Qu.:1.500
Median: 168.0 Mode: character
                               Median: 9.000 Median: 3.000
Mean :168.2
                                Mean : 8.357 Mean :3.466
3rd Qu.:172.8
                                3rd Qu.:10.000
                                               3rd Qu.:4.500
Max. :190.0
                                Max. :10.000
                                               Max. :6.000
NA's :1
                                NA's :1
 perc_dist
Min. : 15.00
1st Qu.: 20.24
Median : 40.18
Mean : 45.45
3rd Qu.: 57.19
Max. :150.00
NA's :1
```

plot(y = dat\$vision, x = dat\$ages)



```
ggplot(data = dat) +
  aes(x = ages, y = vision) +
  geom_point(size = 2) +
  scale_x_continuous(
    name = "Person's age",
    limits = c(20, 60),
    expand = expansion(mult = c(0, 0.05))
) +
  scale_y_continuous(
    name = "Person's vision",
    limits = c(0, NA),
    breaks = seq(0, 10, 2),
    expand = expansion(mult = c(0, 0.05))
) +
    theme_bw()
```



Apparently, most people are in their 20s and can see quite well, however some people are older and they tend to have a vision that's a little worse.

2 Missing Data?

While the data has 29 rows, it actually only holds vision and ages information for 28 people. This is because instead of values, there are NA (Not Available) for one person. Note that NA as missing values are treated somewhat special in R. As an example: If you want to filter for missing values, you cannot write value == NA, but must instead write is.na(value):

```
dat %>%
  filter(is.na(vision))
# A tibble: 1 x 9
  person
           ages gender civil_state height profession
                                                          vision distance perc_dist
  <chr>
                                      <dbl> <chr>
                                                           <dbl>
                                                                     <dbl>
                                                                                <dbl>
          <dbl> <chr>
                        <chr>
             NA <NA>
1 Enrique
                        <NA>
                                         NA Professional
                                                              NA
                                                                         6
                                                                                  NA
```

Moreover, if you want to count the missing observations (per group) in a dataset, the most basic way of doing it is sum(is.na(values)) (or for not-missing: sum(!is.na(values))). However,

if you are dealing with missing values a lot, you may also want to check out {naniar}, which provides principled, tidy ways to summarise, visualise, and manipulate missing data.

```
# standard functions
dat %>%
  group_by(profession) %>%
  summarise(
    n_{rows} = n(),
    n_NA = sum(is.na(vision)),
    n_notNA = sum(!is.na(vision))
  )
# A tibble: 2 x 4
  profession
               n_rows n_NA n_notNA
  <chr>
                <int> <int>
                               <int>
1 Professional
                    18
                           1
                                  17
2 Student
                    11
                           0
                                  11
# naniar functions
dat %>%
  group_by(profession) %>%
  summarise(
    n_{rows} = n(),
    n_NA = n_miss(vision),
    n_notNA = n_complete(vision)
  )
# A tibble: 2 x 4
               n_rows n_NA n_notNA
  profession
  <chr>
                <int> <int>
                               <int>
1 Professional
                    18
                           1
                                  17
2 Student
                           0
                    11
                                  11
```

3 Corr. & Reg.

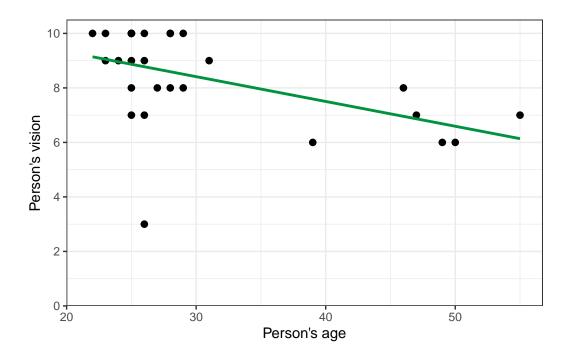
Let's estimate the correlation and simple linear regression and look at the results in a tidy format:

```
cor <- cor.test(dat$vision, dat$ages)</pre>
tidy(cor)
# A tibble: 1 x 8
  estimate statistic p.value parameter conf.low conf.high method
                                                                      alternative
               <dbl> <dbl>
                                 <int>
                                          <dbl>
                                                    <dbl> <chr>
                                                                      <chr>
   -0.497
               -2.92 0.00709
                                    26
                                         -0.734
                                                   -0.153 Pearson's~ two.sided
reg <- lm(vision ~ ages, data = dat)</pre>
tidy(reg)
# A tibble: 2 x 5
             estimate std.error statistic p.value
                 <dbl>
                          <dbl>
                                     <dbl>
1 (Intercept) 11.1
                          0.996
                                     11.2 1.97e-11
               -0.0910
                          0.0311
                                     -2.92 7.09e- 3
2 ages
```

Thus, we have a moderate, negative correlation of -0.497 and for the regression we have vision = 11.14 + -0.09 ages. We can plot the regression line, too:

```
ggplot(data = dat) +
  aes(x = ages, y = vision) +
  geom_point(size = 2) +
   geom_smooth(
   method = "lm",
    formula = "y \sim x",
    se = FALSE,
    color = "#00923f"
  ) +
  scale_x_continuous(
   name = "Person's age",
   limits = c(20, 55),
   expand = expansion(mult = c(0, 0.05))
  ) +
  scale_y_continuous(
    name = "Person's vision",
   limits = c(0, NA),
   breaks = seq(0, 10, 2),
    expand = expansion(mult = c(0, 0.05))
  ) +
```

theme_bw()



4 Outlier?

Looking at the plot, you may find one data point to oddly stick out from all others: Apparently there was one person in their mid-20s who had a vision score of only 3, which is the lowest by far.

Note

Here, we manually and thus subjectively identified a data point as a potential outlier. We do not discuss automatic and thus objective approaches for outlier detection, but see e.g. here or here.

4.1 Step 1: Investigate

In such a scenario, the first thing you should do is find out more about this suspicious data point. In our case, we would start by finding out the person's name. One way of doing this is by simply filtering the data:

```
dat %>%
  filter(vision == 3)
# A tibble: 1 x 9
  person
           ages gender civil_state height profession
                                                          vision distance perc_dist
                                                                               <dbl>
  <chr>>
          <dbl> <chr>
                        <chr>
                                      <dbl> <chr>
                                                           <dbl>
                                                                     <dbl>
                                                                       4.5
1 Rolando
             26 M
                                        180 Professional
                                                               3
                                                                                  150
                        M
```

We find that it was 26 year old Rolando who supposedly had a vision score of only 3.

4.2 Step 2: Act

Since we pretend it is you who collected the data, you should now

- think back if you can actually remember Rolando and if he had poor vision and/or
- find other documents such as your handwritten sheets to verify this number and make sure you did not make any typos transferring the data to your computer.

This may reaffirm or correct the suspicious data point and thus end the discussion on whether it is an outlier that should be removed from the data. However, you may also decide to delete this value. Yet, it must be realized, that deleting one or multiple values from a dataset almost always affects the results from subsequent statistical analyses - especially if the values stick out from the rest.

5 Corr. & Reg. - again

Let us estimate correlation and regression again, but this time excluding Rolando from the dataset. Note that there are multiple ways of obtaining such a subset - two are shown here:

```
dat_noRo <- dat %>%
  filter(person != "Rolando")

dat_noRo <- dat %>%
  filter(vision > 3)
```

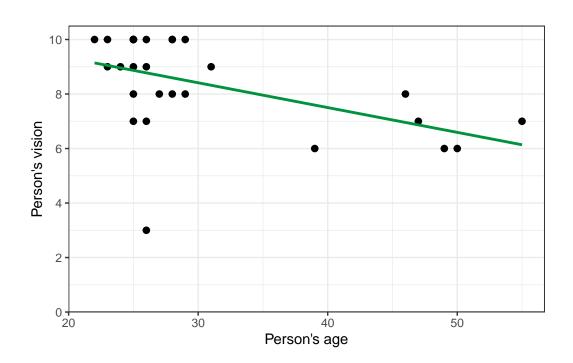
We now apply the same functions to this new dataset:

```
cor_noRo <- cor.test(dat_noRo$vision, dat_noRo$ages)
reg_noRo <- lm(vision ~ ages, data = dat_noRo)</pre>
```

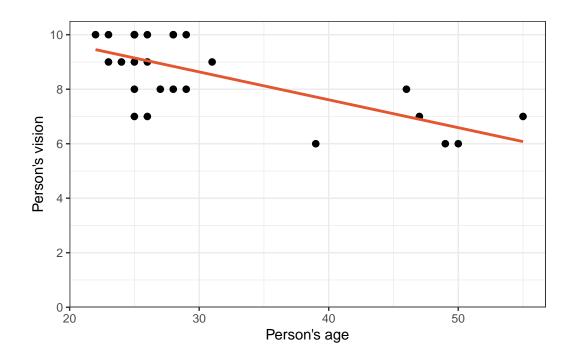
and directly compare these results to those from above:

```
tidy(cor) %>%
 select(1, 3, 5, 6)
# A tibble: 1 x 4
 estimate p.value conf.low conf.high
    <dbl> <dbl> <dbl> <dbl> <
1 -0.497 0.00709 -0.734
                            -0.153
tidy(reg) %>%
 select(1, 2, 3)
# A tibble: 2 x 3
 term estimate std.error
 <chr>
              <dbl> <dbl>
1 (Intercept) 11.1
                       0.996
2 ages
             -0.0910 0.0311
tidy(cor_noRo) %>%
 select(1, 3, 5, 6)
# A tibble: 1 x 4
 estimate p.value conf.low conf.high
    <dbl>
            <dbl> <dbl> <dbl>
   -0.696 0.0000548 -0.851
                              -0.430
tidy(reg_noRo) %>%
 select(1, 2, 3)
# A tibble: 2 x 3
 term estimate std.error
 <chr>
              <dbl>
                        <dbl>
1 (Intercept) 11.7
                       0.679
2 ages
              -0.102
                       0.0211
ggplot(data = dat) +
 aes(x = ages, y = vision) +
 geom_point(size = 2) +
```

```
geom_smooth(
  method = "lm",
  formula = "y \sim x",
  se = FALSE,
  color = "#00923f"
) +
scale_x_continuous(
  name = "Person's age",
  limits = c(20, 55),
  expand = expansion(mult = c(0, 0.05))
) +
scale_y_continuous(
  name = "Person's vision",
 limits = c(0, NA),
  breaks = seq(0, 10, 2),
  expand = expansion(mult = c(0, 0.05))
) +
theme_bw()
```



```
ggplot(data = dat_noRo) +
 aes(x = ages, y = vision) +
 geom_point(size = 2) +
    geom_smooth(
   method = "lm",
   formula = "y ~ x",
    se = FALSE,
    color = "#e4572e"
 ) +
 scale_x_continuous(
   name = "Person's age",
   limits = c(20, 55),
    expand = expansion(mult = c(0, 0.05))
 ) +
 scale_y_continuous(
   name = "Person's vision",
   limits = c(0, NA),
   breaks = seq(0, 10, 2),
    expand = expansion(mult = c(0, 0.05))
 ) +
  theme_bw()
```



As we can see, removing Rolando from the dataset changed the correlation quite a bit from -0.5 to -0.7. Furthermore, it's p-value became notably smaller. While it was already < 0.05 and thus statistically significant in this case, it must be realized that in other cases removing a single data point can indeed make the difference between a p-value larger and smaller 0.05.

Yet, regarding the parameter estimates - intercept (a) and slope (b) - of the simple linear regression, the changes are not as striking. Even with a visual comparison of the two regression lines, one must look closely to spot the differences.

5.1 R² - Coeff. of det.

Nevertheless, it is clear that the red line has a much better fit to the remaining data points, than the green line has - simply because Rolando's data point sticks out so much. One way of measuring how well a regression fits the data is by calculating the coefficient of determination R^2 , which measures the proportion of total variation in the data explained by the model and can thus range from 0 (=bad) to 1 (=good). It can easily obtained via glance(), which is another function from $\{broom\}$:

```
glance(reg)
# A tibble: 1 x 12
  r.squared adj.r.squared sigma statistic p.value
                                                       df logLik
                                                                   AIC
                                                                          BIC
      <dbl>
                     <dbl> <dbl>
                                     <dbl>
                                              <dbl> <dbl>
                                                           <dbl> <dbl> <dbl>
      0.247
                    0.218 1.54
                                      8.54 0.00709
                                                        1
                                                           -50.9
                                                                  108.
                                                                         112.
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
glance(reg_noRo)
# A tibble: 1 x 12
  r.squared adj.r.squared sigma statistic
                                                                     AIC
                                                                            BTC
                                             p.value
                                                         df logLik
      <dbl>
                     <dbl> <dbl>
                                     <dbl>
                                                <dbl> <dbl>
                                                             <dbl> <dbl> <dbl>
      0.485
                    0.464
                          1.04
                                      23.5 0.0000548
                                                             -38.4 82.7
                                                                          86.6
                                                          1
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```

Finally, we find that removing Rolando from the dataset increased the R^2 for the simple linear regression from 25% to 49%.