

One-way latin square design

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One-way ANOVA & pairwise comparison post hoc tests in a latin square design.

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```
# (install &) load packages
pacman::p_load(
  agridat,
  conflicted,
  desplot,
  emmeans,
  ggtext,
  multcomp,
  multcompView,
  tidyverse)

# handle function conflicts
conflicts_prefer(dplyr::filter)
conflicts_prefer(dplyr::select)
```

1 Data

This example data is taken from `{agridat}`. It considers data published in Bridges (1989) from a cucumber yield trial with four genotypes set up as a Latin square design. Notice that the original dataset considers two trials (at two locations), but we will focus on only a single trial here.

1.1 Import

```
dat <- agridat::bridges.cucumber %>%  
  as_tibble() %>%  
  filter(loc == "Clemson") %>% # filter data from only one location  
  select(-loc) # remove loc column which is now unnecessary
```

dat

```
# A tibble: 16 x 4  
   gen      row  col yield  
   <fct>   <int> <int> <dbl>  
1 Dasher     1     3  44.2  
2 Dasher     2     4  54.1  
3 Dasher     3     2  47.2  
4 Dasher     4     1  36.7  
5 Guardian   1     4   33  
6 Guardian   2     2  13.6  
7 Guardian   3     1  44.1  
8 Guardian   4     3  35.8  
9 Poinsett   1     1  11.5  
10 Poinsett  2     3  22.4  
11 Poinsett  3     4  30.3  
12 Poinsett  4     2  21.5  
13 Sprint    1     2  15.1  
14 Sprint    2     1  20.3  
15 Sprint    3     3  41.3  
16 Sprint    4     4  27.1
```

1.2 Format

For our analysis, `gen`, `row` and `col` should be encoded as factors. However, the `desplot()` function needs `row` and `col` as formatted as integers. Therefore we create copies of these

columns encoded as factors and named `rowF` and `colF`. Below are two ways how to achieve this:

```
dat <- dat %>%
  mutate(
    colF = as.factor(col),
    rowF = as.factor(row)
  )

dat <- dat %>%
  mutate(across(
    .cols = c(row, col),
    .fns = ~ as.factor(.x),
    .names = ("{.col}F")
  ))
```

1.3 Explore

We make use of `dlookr::describe()` to conveniently obtain descriptive summary tables. Here, we get can summarize per genotype, per row and per column.

```
dat %>%
  group_by(gen) %>%
  dlookr::describe(yield) %>%
  select(2:sd) %>%
  arrange(desc(mean))

# A tibble: 4 x 5
  gen          n    na mean    sd
<fct>    <int> <int> <dbl> <dbl>
1 Dasher         4     0  45.6  7.21
2 Guardian       4     0  31.6 12.9
3 Sprint         4     0  26.0 11.4
4 Poinsett       4     0  21.4  7.71

dat %>%
  group_by(rowF) %>%
  dlookr::describe(yield) %>%
  select(2:sd) %>%
  arrange(desc(mean))
```

```
# A tibble: 4 x 5
  rowF      n    na mean    sd
  <fct> <int> <int> <dbl> <dbl>
1 3         4     0  40.7  7.36
2 4         4     0  30.3  7.28
3 2         4     0  27.6 18.1
4 1         4     0  26.0 15.4
```

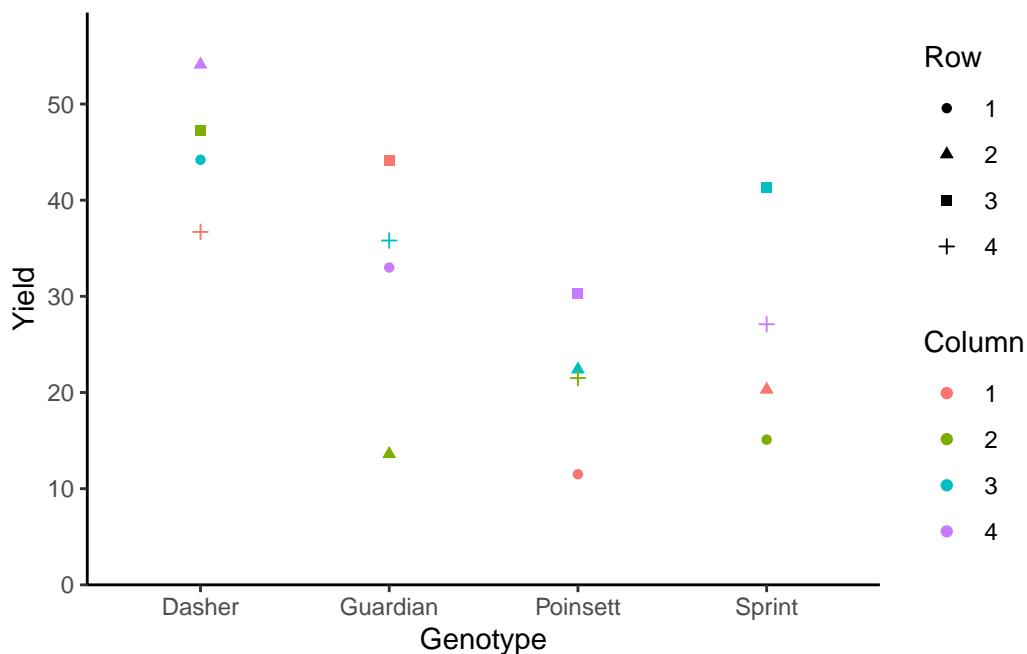
```
dat %>%
  group_by(colF) %>%
  dlookr::describe(yield) %>%
  select(2:sd) %>%
  arrange(desc(mean))
```

```
# A tibble: 4 x 5
  colF      n    na mean    sd
  <fct> <int> <int> <dbl> <dbl>
1 4         4     0  36.1 12.2
2 3         4     0  35.9  9.67
3 1         4     0  28.2 14.9
4 2         4     0  24.4 15.6
```

Additionally, we can decide to plot our data:

```
ggplot(data = dat) +
  aes(y = yield, x = gen, color = colF, shape = rowF) +
  geom_point() +
  scale_x_discrete(
    name = "Genotype"
  ) +
  scale_y_continuous(
    name = "Yield",
    limits = c(0, NA),
    expand = expansion(mult = c(0, 0.1))
  ) +
  scale_color_discrete(
    name = "Column"
  ) +
  scale_shape_discrete(
    name = "Row"
  ) +
```

```
theme_classic()
```



Finally, since this is an experiment that was laid with a certain experimental design (= a Latin square design) - it makes sense to also get a field plan. This can be done via `desplot()` from `{desplot}`. We can even create a second field plan that gives us a feeling for the yields per plot.

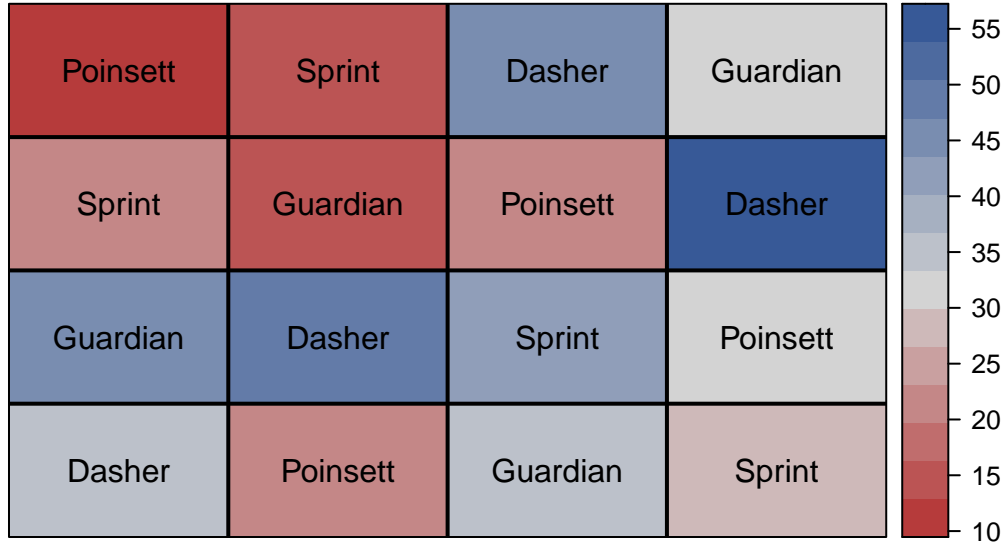
```
desplot(
  data = dat,
  flip = TRUE, # row 1 on top, not on bottom
  form = gen ~ col + row, # fill color per genotype
  out1 = rowF, # line between rows
  out2 = colF, # line between columns
  out1.gpar = list(col = "black", lwd = 2), # out1 line style
  out2.gpar = list(col = "black", lwd = 2), # out2 line style
  text = gen, # gen names per plot
  cex = 1, # gen names: font size
  shorten = FALSE, # gen names: don't abbreviate
  main = "Field layout", # plot title
  show.key = FALSE # hide legend
)
```

Field layout

Poinsett	Sprint	Dasher	Guardian
Sprint	Guardian	Poinsett	Dasher
Guardian	Dasher	Sprint	Poinsett
Dasher	Poinsett	Guardian	Sprint

```
desplot(  
  data = dat,  
  flip = TRUE, # row 1 on top, not on bottom  
  form = yield ~ col + row, # fill color according to yield  
  out1 = rowF, # line between rows  
  out2 = colF, # line between columns  
  out1.gpar = list(col = "black", lwd = 2), # out1 line style  
  out2.gpar = list(col = "black", lwd = 2), # out2 line style  
  text = gen, # gen names per plot  
  cex = 1, # gen names: font size  
  shorten = FALSE, # gen names: don't abbreviate  
  main = "Yield per plot", # plot title  
  show.key = FALSE # hide legend  
)
```

Yield per plot



Thus, **Dasher** seems to be the most promising genotype in terms of yield. Moreover, it can be seen that yields were generally higher in column 4 and row 3.

2 Model

Finally, we can decide to fit a linear model with **yield** as the response variable and (fixed) **gen**, **rowF** and **colF** effects.

```
mod <- lm(yield ~ gen + rowF + colF, data = dat)
```

! Important

It is crucial to add **rowF/colF** and not **row/col** to the model here, since only the former are formatted as factors. They should be formatted as factors, so that the model estimates one effect for each of their levels. The model would estimate a single slope for **row** and **col**, respectively, which is nonsensical: It would suggest that row 4 is twice as much as row 2 etc.

⚠ Model assumptions met? (click to show)

It would be at this moment (i.e. after fitting the model and before running the ANOVA), that you should check whether the model assumptions are met. Find out more in the [summary article “Model Diagnostics”](#)

3 ANOVA

Based on our model, we can then conduct an ANOVA:

```
ANOVA <- anova(mod)
ANOVA
```

```
Analysis of Variance Table
```

```
Response: yield
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
gen	3	1316.80	438.93	9.3683	0.01110 *
rowF	3	528.35	176.12	3.7589	0.07872 .
colF	3	411.16	137.05	2.9252	0.12197
Residuals	6	281.12	46.85		

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Accordingly, the ANOVA’s F-test found the genotype effects to be statistically significant ($p = 0.011^*$).

4 Mean comparison

Besides an ANOVA, one may also want to compare adjusted yield means between genotypes via post hoc tests (t-test, Tukey test etc.).

```
mean_comp <- mod %>%
  emmeans(specs = ~ gen) %>% # adj. mean per genotype
  cld(adjust = "Tukey", Letters = letters) # compact letter display (CLD)

mean_comp
```


gen	emmean	SE	df	lower.CL	upper.CL	.group
Poinsett	21.4	3.42	6	9.43	33.4	a
Sprint	25.9	3.42	6	13.95	37.9	a
Guardian	31.6	3.42	6	19.63	43.6	ab
Dasher	45.5	3.42	6	33.55	57.5	b

Results are averaged over the levels of: rowF, colF

Confidence level used: 0.95

Conf-level adjustment: sidak method for 4 estimates

P value adjustment: tukey method for comparing a family of 4 estimates

significance level used: alpha = 0.05

NOTE: If two or more means share the same grouping symbol,
then we cannot show them to be different.

But we also did not show them to be the same.

Note that if you would like to see the underlying individual contrasts/differences between adjusted means, simply add `details = TRUE` to the `cld()` statement. Furthermore, check out the [Summary Article “Compact Letter Display”](#).

Finally, we can create a plot that displays both the raw data and the results, *i.e.* the comparisons of the adjusted means that are based on the linear model.

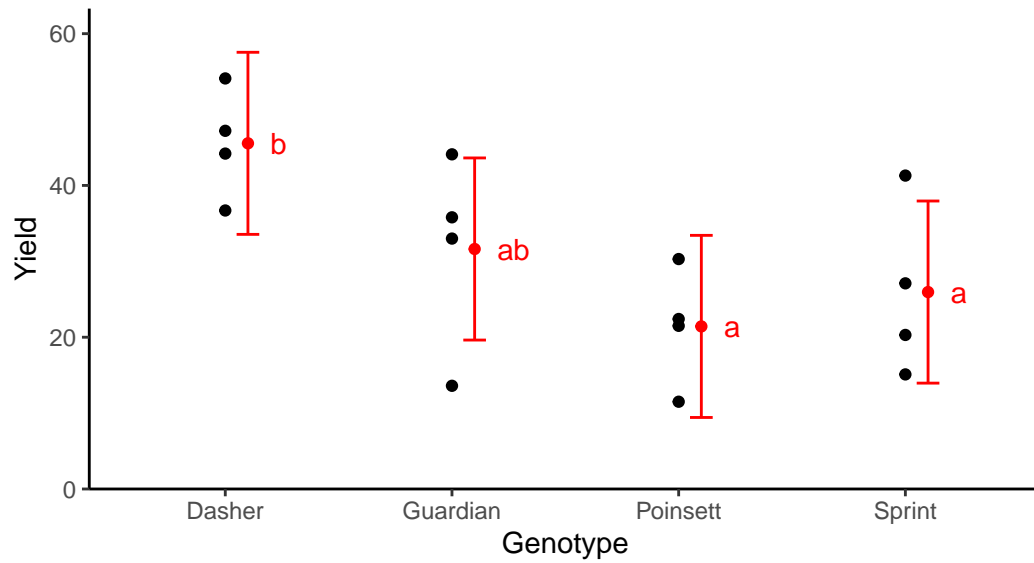
```
my_caption <- "Black dots represent raw data. Red dots and error bars represent adjusted means"

ggplot() +
  aes(x = gen) +
  # black dots representing the raw data
  geom_point(
    data = dat,
    aes(y = yield)
  ) +
  # red dots representing the adjusted means
  geom_point(
    data = mean_comp,
    aes(y = emmean),
    color = "red",
    position = position_nudge(x = 0.1)
  ) +
  # red error bars representing the confidence limits of the adjusted means
  geom_errorbar(
    data = mean_comp,
    aes(ymin = lower.CL, ymax = upper.CL),
```

```

    color = "red",
    width = 0.1,
    position = position_nudge(x = 0.1)
  ) +
  # red letters
  geom_text(
    data = mean_comp,
    aes(y = emmean, label = str_trim(.group)),
    color = "red",
    position = position_nudge(x = 0.2),
    hjust = 0
  ) +
  scale_x_discrete(
    name = "Genotype"
  ) +
  scale_y_continuous(
    name = "Yield",
    limits = c(0, NA),
    expand = expansion(mult = c(0, 0.1))
  ) +
  scale_color_discrete(
    name = "Block"
  ) +
  theme_classic() +
  labs(caption = my_caption) +
  theme(plot.caption = element_textbox_simple(margin = margin(t = 5)),
        plot.caption.position = "plot")

```



Black dots represent raw data. Red dots and error bars represent adjusted means with 95% confidence limits per genotype Means followed by a common letter are not significantly different according to the Tukey-test.

Bridges, William. 1989. "Analysis of a Plant Breeding Experiment with Heterogeneous Variances Using Mixed Model Equations." *Applications of Mixed Models in Agriculture and Related Disciplines*, 45–51.