

Short answer: your slate is strong, but there are high-leverage gaps. Below are the biggest additions I'd make—each chosen to boost *out-of-sample* predictability for multi-horizon bqx across all 8 pairs while staying leakage-safe.

## Quick gap scan (what's missing)

1. **Structure-aware FX math** beyond triangles (cointegration / ECM).
  2. **Regime/change detection** (statistical, not just heuristics).
  3. **Spectral/shape features** (frequency bands, wavelets, SSA).
  4. **Realized-volatility family** (range-based, bipower, quarticity).
  5. **Impact/liquidity proxies** beyond spread/volume (Kyle/Amihud style).
  6. **Cross-sectional signals** (ranks/dispersion/relative value) baked into features.
  7. **Learned representations** (panel autoencoders / contrastive encoders).
  8. **Target & loss shaping** for multi-horizon coherence and uncertainty.
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## What to add (and why)

### A) FX structure & error-correction (high impact)

- **Johansen cointegration** on each USD triangle and key clusters (EUR–GBP–USD, AUD–NZD–USD).
  - Add: cointegration vectors, **error-correction term (ECT)**, and  $\Delta ECT$ .
  - Why: ECT mean-reverts; its level/velocity is predictive for 15–75 min horizons.
- **Cross-pair regression residuals with parabolic terms** (you have triangles; extend to *sister pairs*):
  - Add residual level/z, residual curvature ( $\tilde{a}_2$ ) and slope ( $\tilde{a}_1$ ).
  - Why: highlights transient mispricings your bqx will often “catch up” to.

### B) Robust realized-volatility set (cheap, powerful)

Compute on 1m and 5m bars (up to i only):

- **Parkinson, Garman–Klass, Rogers–Satchell, Yang–Zhang** vol.
- **Bipower variation** and **realized quarticity** (proxy for jump risk).
- **Vol-of-vol** and **vol acceleration** ( $\Delta EWMAvol$ , second difference).  
Why: bqx predictability is regime-dependent; these quantify regime cleanly and are orthogonal to your current std/EWMA.

### C) Regime & change-point detection

- **HMM/Markov regimes** on returns or vol ( $K=3$ : calm/trend/shock). Use filtered state probs ( $P(\text{state}=k)_i$ ).
- **Bayesian Online Change Point Detection (BOCPD)** run-length & hazard features.
- **CUSUM statistics** on returns and on your ( $\tilde{a}_2$ ) curvature stream.  
Why: sharp improvements in forecasts when models know if the distribution just shifted.

## D) Spectral / shape analytics (multi-scale, orthogonal)

- **FFT band energies** (very-short 2–4m, short 5–15m, medium 20–60m) on bqx and rate; include band-energy ratios and dominant frequency.
- **Wavelet packet energy** (e.g., Daubechies 4) at 3–4 levels; add **cross-window coherence** flags.
- **Singular Spectrum Analysis (SSA)**: first 2–3 reconstructed components' slopes/curvatures.  
Why: picks up cyclic build-ups and microstructure rhythms that precede breakouts/reversions.

## E) Microstructure impact proxies (if you have basic volume/tick)

- **Amihud illiquidity**:  $|\text{ret}| / \text{volume}$  (1m, 5m).
- **Kyle's  $\lambda$  surrogate**: slope of  $\Delta\text{price}$  on signed volume (rolling OLS).
- **VPIN-lite**: imbalance of up- vs down-volume (you already have uptick/downtick—aggregate to a toxicity score).
- **Spread\*vol interactions and book-pressure proxy**: spread  $z \times \text{volume } z$ .  
Why: future bqx (a momentum derivative) is especially sensitive to flow/impact regimes.

## F) Cross-sectional (8-pair panel) features

- **Cross-sectional ranks/percentiles** of: return, bqx, ( $\tilde{a}_1$ ), ( $\tilde{a}_2$ ), vol, ECT.
- **Dispersion** metrics (std across 8 pairs) for those same quantities.
- **Breadth**: fraction of pairs with positive ( $\tilde{a}_2$ ) (acceleration breadth) and positive ( $\tilde{a}_1$ ) (trend breadth).  
Why: panel context (synchrony vs rotation) is a leading indicator for continuation odds.

## G) Multi-resolution: add 30m & 60m layers

You have 1m/5m/15m. Add:

- 30m/60m **vol, trend slope**, ( $\tilde{a}_2$ ), and **alignment flags** (e.g., sign agreement of ( $\tilde{a}_2$ ) across 5→15→30→60).  
Why: horizons up to +75m benefit from information carried at 30–60m.

## H) Dual-domain *derivative* comparisons (rate $\leftrightarrow$ bqx)

You compare levels; add **differential dynamics**:

- **Gap velocity/acceleration:**  $\Delta(\tilde{a}_1^{\text{rate}} - \tilde{a}_1^{\text{bqx}}), \Delta(\tilde{a}_2^{\text{rate}} - \tilde{a}_2^{\text{bqx}})$ .
- **Apex timing spread:**  $(t_{\text{rate}} - t_{\text{bqx}})$  from parabola.  
Why: the *speed of decoupling/recoupling* often predicts the next 15–45 minutes.

## I) Learned representations (panel-wise, leakage-safe)

- **Autoencoder on feature blocks** (per timestamp  $\times$  8 pairs): keep the bottleneck (e.g., 8–16 dims) as **system embeddings**.
- **Temporal contrastive learning** (TS-TCC/SimCLR-style) on bqx panels; use embeddings as features.  
Why: compresses nonlinear cross-pair structure and denoises hand-engineered redundancy.

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## Target & loss shaping (often bigger lift than more features)

- **Vol-scaled  $\Delta$  targets** (you already plan this) + **quantile heads** ( $\tau=.1/.5/.9$ ) to get calibrated uncertainty.
- **Multi-horizon coherence**: add penalty if predicted  $|\Delta\text{bqx}|$  is *not* non-decreasing with horizon (soft monotonicity).
- **Directional auxiliary**: BCE on  $\text{sign}(\Delta\text{bqx})$  per horizon to sharpen turns.
- **Horizon embeddings** (if using a shared model) so the encoder learns horizon-specific patterns.

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## Data-health & stability features (cheap insurance)

- **Missing-rate, FFILL-count, stale-tick flag** per pair.
- **Feature drift z-scores** vs trailing 24h means for key blocks (vol, spread,  $(\tilde{a}_2)$ ).  
Why: models behave better when they *see* data quality/regime drift.

# What to ship first (12 additions with best ROI)

1. **ECT (error-correction term)** per triangle +  $\Delta$ ECT.
  2. **Garman–Klass & bipower variation** (1m & 5m).
  3. **Vol-of-vol and vol acceleration.**
  4. **HMM state probabilities** ( $K=3$ ) on returns.
  5. **BOCPD run-length** on returns.
  6. **FFT band energies** (short/medium) on bqx; band-energy ratios.
  7. **Wavelet energy** level-1/2 on bqx.
  8. **Amihud illiquidity** and **Kyle  $\lambda$  proxy**.
  9. **Cross-sectional ranks** of ( $\tilde{a}_2$ ), ( $\tilde{a}_1$ ), and vol across 8 pairs.
  10. **Apex timing spread** ( $t^{\{rate\}} - t^{\{bqx\}}$ ).
  11. **30m/60m layer**: vol, ( $\tilde{a}_2$ ), alignment flags.
  12. **Autoencoder bottleneck** (8–16 dims) from the full panel at time i.
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## Guardrails & pruning

- Keep all windows **ending at i**; no peeking.
  - Winsorize extreme z-scores (e.g., at  $4-5\sigma$ ) to stabilize training.
  - Expect multicollinearity—**groupwise PCA/PLS** per block (volatility, parabolic, spectral) and keep a few principal components + a handful of interpretable “anchor” features.
  - Run **rolling feature importance** (e.g., time-slice SHAP) to prevent over-fitting to a single regime.
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