Алгоритмы поиска пути в графе

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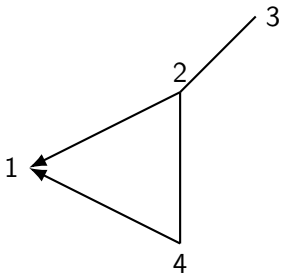
Очень краткое введение в оценку ассимптитики

$$f(x) = O(g(x)) \Leftrightarrow \exists C = const : \ \forall x : \frac{|f(x)|}{|g(x)|} \leq C$$

Способы хранения графа



- Матрица смежности

	1	2	3	4
1	0	0	0	0
2	1	0	1	1
3	0	1	0	0
4	1	1	0	0

- Список смежности

  1: —

  2: 1 3 4

  3: 2

  4: 1 2

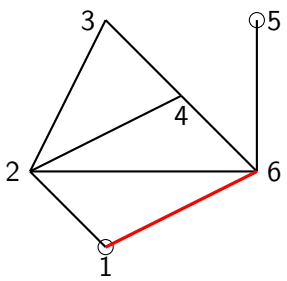
- Скисок ребер

  2–1; 2–3; 2–4; 3–2; 4–1; 4–2

Обозначения

- G — матрица смежности
- g — список смежности
- E — список ребер
- $n = |V|$ — количество вершин
- $m = |E|$ — количество ребер

Depth-first search



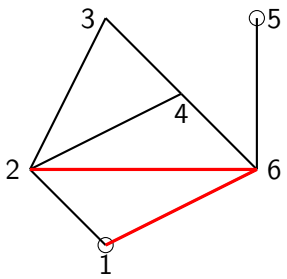
$O(n+m)$

```
doDfs(g: int[n][], s: int)
    used = [0] * n

    dfs(u: int)
        used[u] = 1
        for v ∈ g_u
            dfs(v)

    dfs(s)
```

Depth-first search



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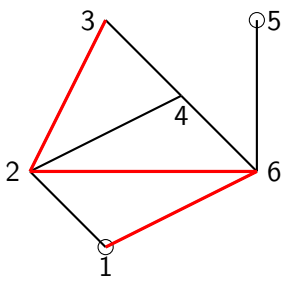

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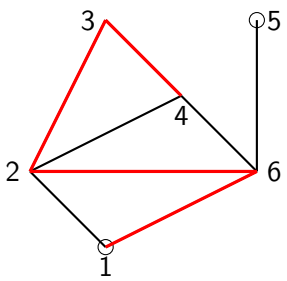

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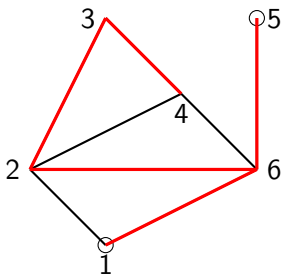

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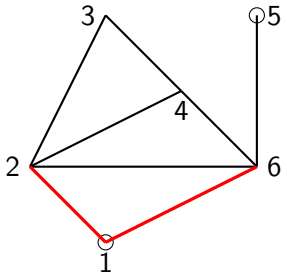
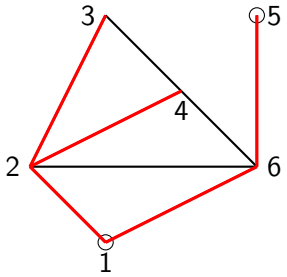
Breadth-first search



$O(n+m)$

```
doBfs(g: int[n][], s: int)
    dist = [−1] * n
    queue q
    q.push(s)
    dist[u] = 0
    while q ≠ ∅
        u = q.pop()
        for v ∈ g_u
            if dist[v] == −1
                dist[v] = dist[u] + 1
                q.push(v)
```

Breadth-first search



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