

Алгоритмы поиска пути в графе

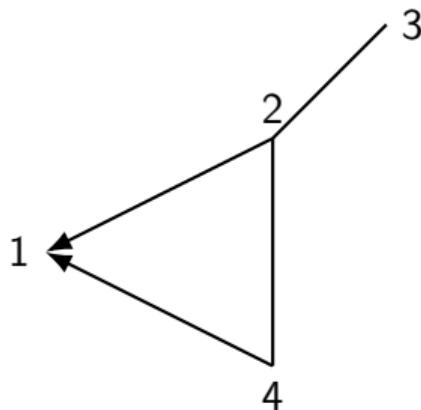
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Очень краткое введение в оценку ассимптотики

$$f(x) = O(g(x)) \Leftrightarrow \exists C = const : \forall x : \frac{|f(x)|}{|g(x)|} \leq C$$

Способы хранения графа



- Матрица смежности

	1	2	3	4
1	0	0	0	0
2	1	0	1	1
3	0	1	0	0
4	1	1	0	0

- Список смежности

1: —

2: 1 3 4

3: 2

4: 1 2

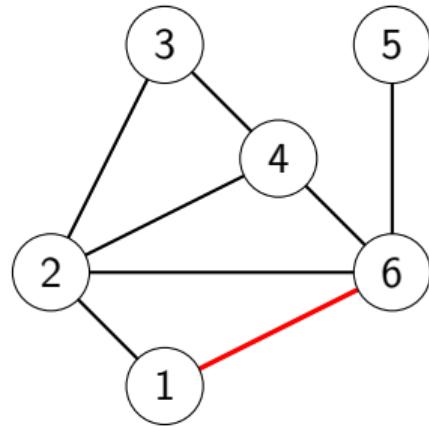
- Список ребер

2–1; 2–3; 2–4; 3–2; 4–1; 4–2

Обозначения

- G — матрица смежности
- g — список смежности
- E — список ребер
- $n = |V|$ — количество вершин
- $m = |E|$ — количество ребер

Depth-first search



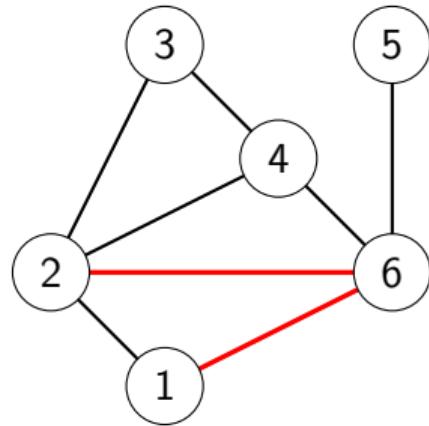
$O(n + m)$

```
doDfs(g: int[][] , s: int)  
    used = [0] * n
```

```
dfs(u: int)  
    used[u] = 1  
    for v ∈ g[u]  
        dfs(v)
```

dfs(s)

Depth-first search



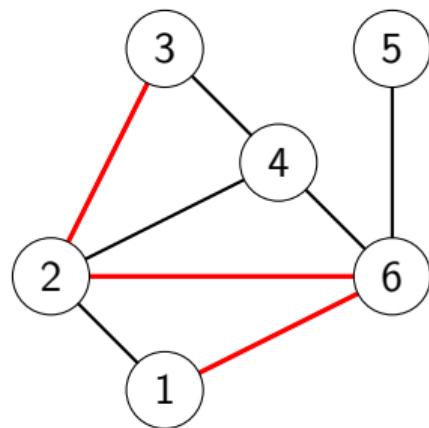
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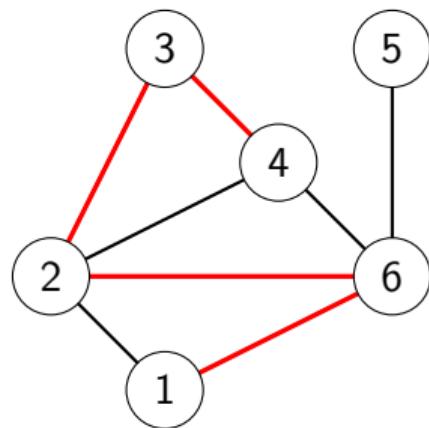
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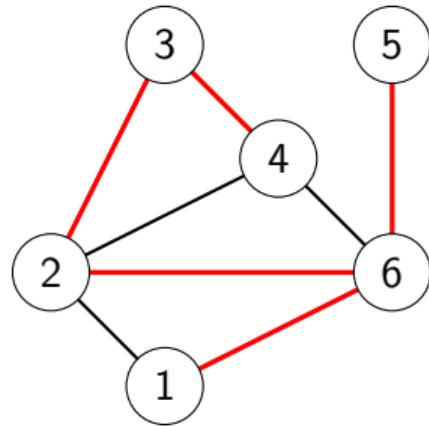
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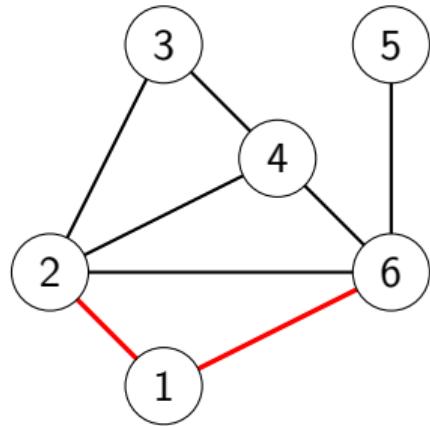
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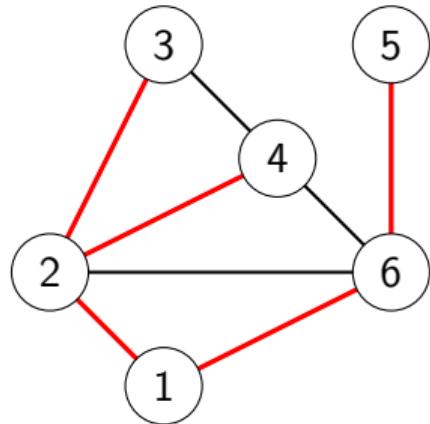
Breadth-first search



$O(n + m)$

```
doBfs(g: int[][] , s: int)
    dist = [-1] * n
    queue q
    q.push(s)
    dist[u] = 0
    while q ≠ ∅
        u = q.pop()
        for v ∈ g[u]
            if dist[v] == -1
                dist[v] = dist[u] + 1
                q.push(v)
```

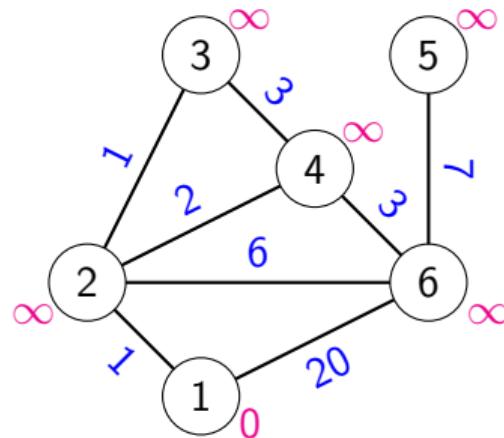
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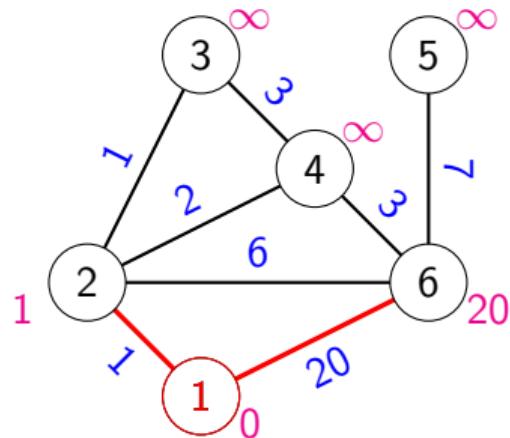
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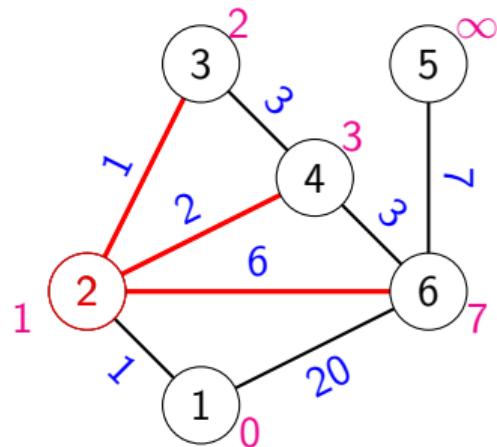
Dijkstra's algorithm



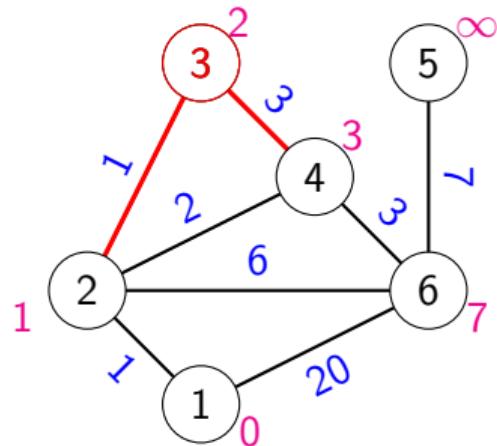
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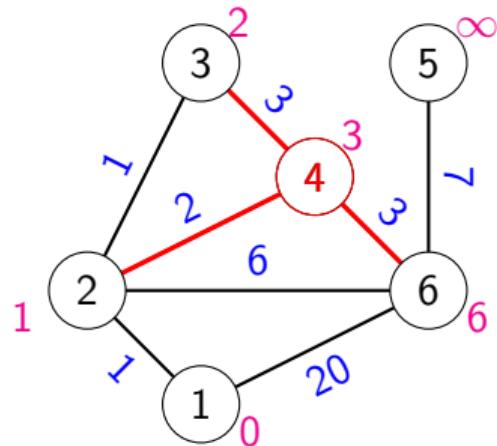
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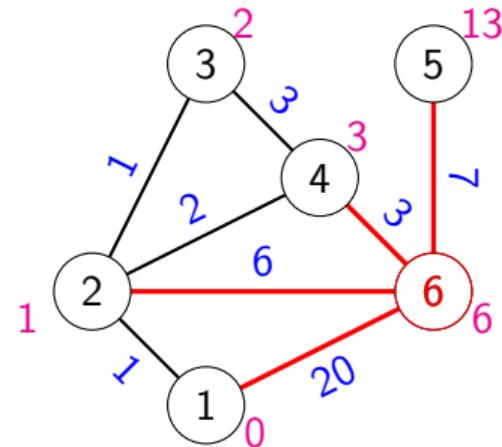
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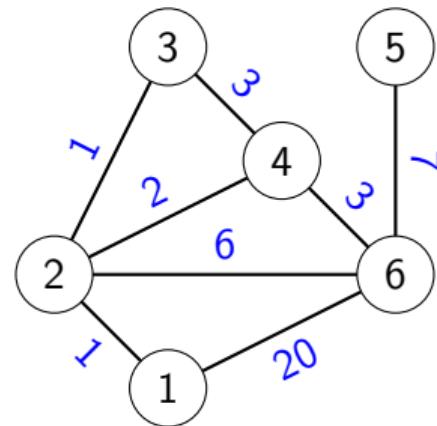
Dijkstra's algorithm



Dijkstra's algorithm



Dijkstra's algorithm



Dijkstra's algorithm

$O(m + n \log n)$

```
doDijkstra(g: int [][] , w: int [][])
    set<int , int> not_visited
    dist = [inf] * n
    dist[0] = 0
    for u = 0...n
        not_visited.insert(dist[u], u)
    while s ≠ ∅
        d, u = not_visited.pop()
        for v ∈ g[u]
            if dist[v] > dist[u] + w[u][v]
                s.erase(dist[v], v)
                dist[v] = dist[u] + w[u][v]
                s.insert(dist[v], v)
```