

## Question 8

Age ( $x_1$ )	Score ( $x_2$ )	$y$	$\hat{y}$	$\hat{y} - y$
35	720	0	0,999	0,999
28	680	1	0,998	-0,002
45	750	0	0,999	0,999
31	600	1	0,997	-0,003
52	780	0	0,999	0,999
29	630	1	0,998	-0,002
42	710	0	0,998	0,998
33	640	1	0,998	-0,002

$$J(w) = -\frac{1}{m} \sum_{i=1}^m [y_i \log(\hat{y}_i) + (1-y_i) \log(1-\hat{y}_i)]$$

$$\frac{\partial J}{\partial w} = \frac{\partial J}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} \frac{\partial z}{\partial w}$$

$$\text{for } w_0: \frac{\partial J}{\partial w_0} = \frac{\partial J}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} \frac{\partial z}{\partial w_0}$$

$$w_0' = w_0 - \eta \frac{\partial J}{\partial w_0} = w_0 - \eta \frac{\partial J}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} \frac{\partial z}{\partial w_0}$$

$$= w_0 - \frac{1}{m} \sum_{i=1}^m (\hat{y}_i - y_i) x_{0i}$$

$$= 0.5 - \frac{1}{8} \sum_{i=1}^8 (\hat{y}_i - y_i) \cdot 1 = 0,498$$

$$w_1' = w_1 - \eta \frac{\partial J}{\partial w_1} = w_1 - \frac{1}{8} \sum_{i=1}^8 (\hat{y}_i - y_i) x_{1i}$$

$$= -2,427$$

$$w_2' = w_2 - \eta \frac{\partial J}{\partial w_2} = \frac{1}{8} \sum_{i=1}^8 (\hat{y}_i - y_i) x_{2i}$$

$$= -287,826$$