

# Problem E Escape

Time limit: 2 seconds Memory limit: 512 megabytes

#### **Problem Description**

You are trapped in a grid maze of size  $2 \times n$ , and each grid cell is a room. The coordinates of a room can be represented by (r, c) where  $r \in [1, 2]$  and  $c \in [1, n]$ . Room (r, c) is located at the row r and column c.

You are now at room (1,1) and want to escape. The exits are at (1,n) and (2,n), but there are locked now. To unlock them, you have to press the toxic gas button in every room. Once you press the button, the toxic gas will start to fill in a few seconds. Before releasing the gas, the room opens doors to adjacent rooms. The doors will automactically close when the concentration of toxic gas in the room is high enough to kill people. Fortunately, you can run really fast. You still can escape to an adjacent room before the toxic gas kills you. However, you may not return to the room with toxic gas released.

In this problem, we define two rooms  $(r_1, c_1)$  and  $(r_2, c_2)$  are adjacent if all following conditions hold.

- 1.  $(r_1, c_1) \neq (r_2, c_2)$
- 2.  $|r_1 r_2| \le 1$
- 3.  $|c_1 c_2| \le 1$

You must press all toxic gas buttons, and the last button must be in either room (1, n) or (2, n). Otherwise, you cannot escape from the maze. It is better to have some plans to escape. You wonder how many different paths allow you to escape. The answer might be large, output the answer modulo 1,000,000,007.

## **Input Format**

The input contains a positive integer n indicating that the size of maze is  $2 \times n$ .

# **Output Format**

Print the number of paths allowing you to escape modulo 1,000,000,007 on a line.

## **Technical Specification**

$$1 \le n \le 10^{18}$$

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Sample Input 1	Sample Output 1  4
Sample Input 2  3	Sample Output 2
Sample Input 3	Sample Output 3
99999000099999	37422585

### Hint

The following figure illstrates the first sample test case.

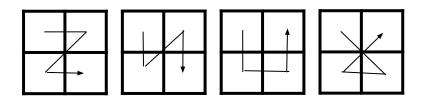


Figure 1: Four paths allow you to escape.