

Bifurcation analysis of microbiome steady states

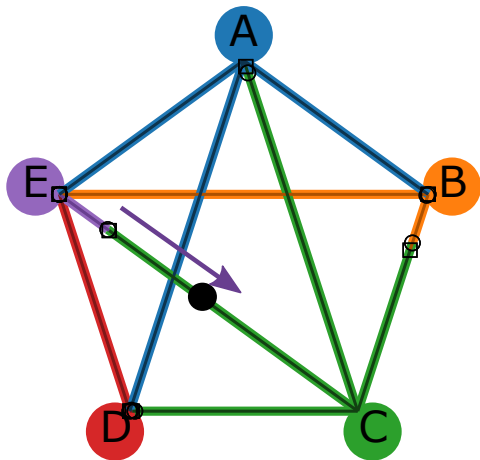
Jean Carlson group

UCSB

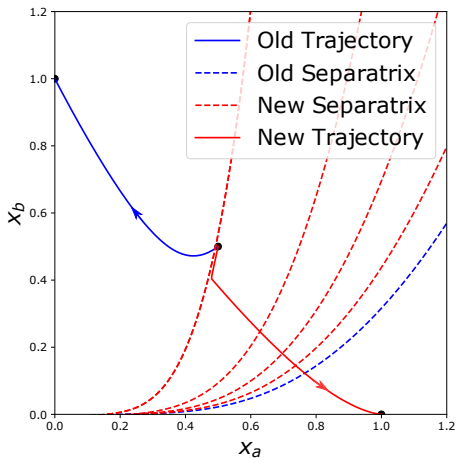
October 12, 2018

Project Goal

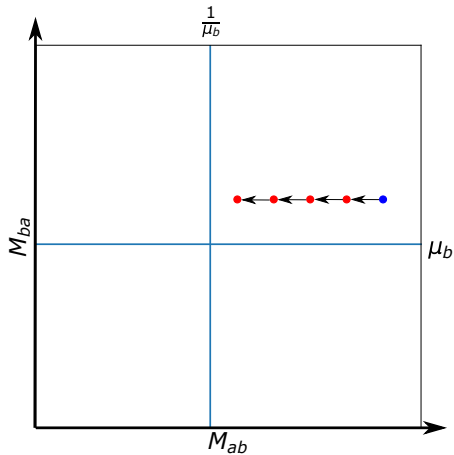
- ▶ Move separatrix to switch steady states
- ▶ Change interaction matrix using SSR as a guide



Change in 2-D matrix



Microbial Phase Space

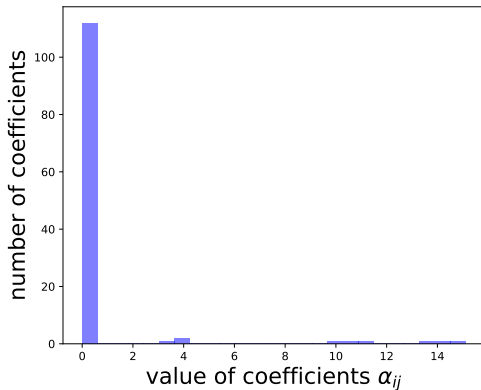


Parameter Space

Change in K

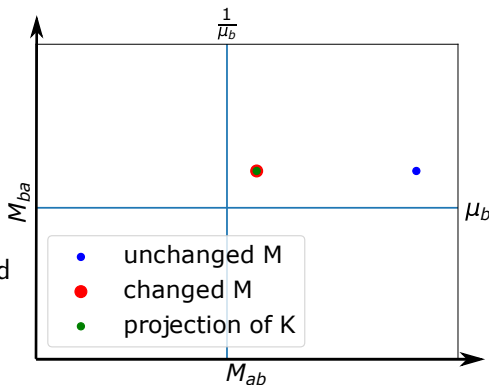
$$M_{ab} = \vec{y}_a^T K \vec{y}_b$$
$$= \sum_{i=1, j=1}^{11, 11} \alpha_{ij} K_{ij}$$

- ▶ 121 coefficients
- ▶ Most are 0
- ▶ M_{ab} most sensitive to change in k_{ij} with the largest α_{ij} coefficient



Projection of ΔK back to 2-D

- ▶ Change in K is possible to change M_{ba}
- ▶ In this case M_{ba} does not change
- ▶ SSR coefficients for M_{ba} and M_{ab} may be orthogonal

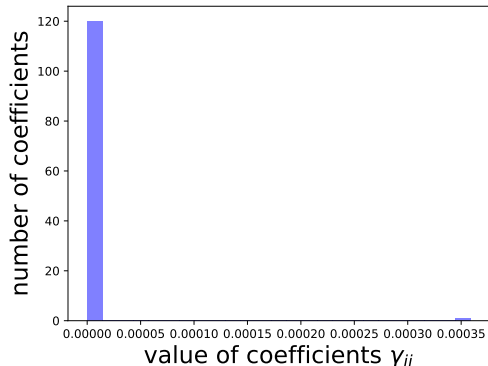


Projection of ΔK back to 2-D

$$M_{ab} = \sum_{i=1,j=1}^{11,11} \alpha_{ij} K_{ij}$$

$$M_{ba} = \sum_{i=1,j=1}^{11,11} \beta_{ij} K_{ij}$$

$$\gamma_{ij} = \alpha_{ij} \beta_{ij}$$



- check the value of γ_{ij}
- nearly orthogonal, except one coefficient