

Neural network knowledge distillation in tensor networks

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Abstract

1 Introduction

void

2 Approches in knowledge distillation

2.1 Response-Based Knowledge Distillation

The first approach is to look exclusively at the outputs of the student and teachers. Each

3 Layer-by-layer approach

It has been common to each layer of a neural network as a certain abstracted representation of the previous information and their for generalisability. Thus, we propose to change the cost, we use a tensor for multilinear mapping and train each mapping individually according to the output of it's paired set of layers.

$$x \longrightarrow H_1 \longrightarrow H_2 \longrightarrow (\dots) \xrightarrow{g} \hat{y}$$

Each hidden layer is of the form;

$$a^l = \sigma^l(W^l a^{l-1})$$

In tensor layer form, it will be defined as

$$\mathbf{a}^l = \mathbf{T}^l \cdot \Phi(\mathbf{a}^{l-1})$$

b The main difference is that in the tensor approach, the "heavy" part is done by the non-linear transformation while a little work is done with the linear mapping. The opposite is true with neural networks. Here, $\Phi(X)$ (X begin the input vector) is a tensor product of several identical non-linear mappings of each element x_i . Thus, we have

$$\Phi(X) = \phi(x_1)\phi(x_2) \dots \phi(x_n)$$

Were each $\phi : \mathbb{R} \rightarrow \mathbb{R}^d$, and each $d > 1$. Thus, our $\Phi(X) : \mathbb{R}^n \rightarrow \mathbb{R}^{(d \times n-1)d}$. In other words, our Φ returns a tensor of order n , where each indices run from 1 to d .

4 Tensor networks

4.1 The *Matrix Product State* Tensor Network

4.2 Expressivity of MPS combinations with transformation $[1, x]^t$

Soit $f(x) : \mathbb{R}^d \mapsto \mathbb{R}^{2^d}$ une fonction qui prend un vecteur de variables et qui renvoie un tenseur de dimensions quelconques dont les éléments contiennent les bases de la fonction multilinéaire des variables du vecteur x .

The vector given by $f(x)$ will return a tensor containing every combination of monomes of degree z , where z is the smallest repeating variable in the input vector.

Soit $m(f, \theta) : \mathbb{R}^{2^d} \mapsto (\mathbb{R}^d \mapsto \mathbb{R})$ une fonction qui effectue une combinaison linéaire des éléments de f and returns an *instance* of a multilinear function. Let this *instance* depend on θ .

Let S_v be a set of n_v variables. Let v^* be a vector where each variable in the set S_v is repeated n_v times.

Since the vector given by $f(x)$ will return a tensor containing every combination of monomes of degree z and $z = n_v$, the elements of the output of $f(x)$ will return the basis for the space of n_v -degree polynomial over the set of variables S_v .