Statistics for Engineers (MAT2001)- Lab Experiment-II: Correlation and Regression

1 Karl Pearson's Coefficient of Correlation

1.1 Scatter Diagram

Problem:

Illustrate the relationship between the average age versus the time spent in the library, by using scatterplot.

AGE GROUP	REPRESENTATIVE AGE	HOURS SPEND IN THE LOCAL LIBRARY
10-19	15	302.38
20-29	25	193.63
30-39	35	185.46
40-49	45	198.49
50-59	55	224.30
60-69	65	288.71

1.2 Manual method

Problem:

Find the correlation coefficient for the given data: x=(23,27,28,28,29,30,31,32,33,35), y=(18,20,22,27,21,29,27,29,28,29). Give a scatter plot to the x and y

```
x=c(23,27,28,28,29,30,31,32,33,35)
    [1] 23 27 28 28 29 30 31 32 33 35
##
length(x)
## [1] 10
y=c(18,20,22,27,21,29,27,29,28,29)
   [1] 18 20 22 27 21 29 27 29 28 29
length(y)
## [1] 10
var(x)
## [1] 11.6
var(y)
## [1] 18.22222
var(x, y)
## [1] 12.11111
r=var(x,y)/sqrt(var(x)*var(y))
## [1] 0.8330179
```

Therfore there is positive correlation between the x and y.

1.3 Using R code

1.3.1 Method 1

```
cor(x,y, method ="pearson" )
## [1] 0.8330179
```

1.3.2 Method 2

```
cor.test(x,y,method="pearson")

##

## Pearson's product-moment correlation

##

## data: x and y

## t = 4.2587, df = 8, p-value = 0.002766

## alternative hypothesis: true correlation is not equal to 0

## 95 percent confidence interval:

## 0.4277335 0.9594318

## sample estimates:

## cor

## 0.8330179
```

2 Spearman's Rank Correlation Coefficient

Problem:

Twelve recruits were subjected to selection test to ascertain their suitability for a certain course of training. At the end of training they were given a proficiency test. The marks scored by the recruits are recorded below

Recruit	1	2	3	4	5	6	7	8	9
Selection Test Score	44	49	52	54	47	76	65	60	63
Proficiency Test Scrore	48	55	45	60	43	80	58	50	77

```
selection =c(44,49,52,54,47,76,65,60,63,58,50,67)
proficiency =c(48,55,45,60,43,80,58,50,77,46,47,65)
cor(selection,proficiency,method ="spearman")

## [1] 0.7202797

# (or)
cor.test(selection,proficiency,method ="spearman")

##
## Spearman's rank correlation rho
```

```
##
## data: selection and proficiency
## S = 80, p-value = 0.01102
## alternative hypothesis: true rho is not equal to 0
## sample estimates:
## rho
## 0.7202797
```

There is a positive correlation between selection and proficiency.

Problem:

Import the iris data set.

- i) Find the Pearson correlation coefficient using the manual method for the features sepal length and sepal width when the Species is setosa. Give a plot visualization. Describe the relationship.
- ii) Find the rank correlation coefficient for the features petal length and petal width when the Species is versicolor and describe the relationship.
- iii) Find the Pearson correlation coefficient for the features petal length and petal width when the Species is virginica and describe the relationship.

```
data <- iris
head(data)
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
##
## 1
              5.1
                          3.5
                                       1.4
                                                    0.2 setosa
## 2
              4.9
                          3.0
                                        1.4
                                                    0.2 setosa
## 3
              4.7
                          3.2
                                       1.3
                                                    0.2 setosa
              4.6
                          3.1
                                       1.5
## 4
                                                    0.2 setosa
              5.0
## 5
                          3.6
                                        1.4
                                                    0.2 setosa
## 6
              5.4
                          3.9
                                        1.7
                                                    0.4 setosa
setosa_data <- subset(data, Species == "setosa")</pre>
r=var(setosa_data$Sepal.Length, setosa_data$Sepal.Width
      )/sqrt(var(setosa_data$Sepal.Length)*
               var(setosa_data$Sepal.Width))
r
## [1] 0.7425467
```

```
plot(setosa_data$Sepal.Length, setosa_data$Sepal.Width,
    main = "Length vs Width", xlab = "Sepal Length",
    ylab = "Sepal Width", col= "green")
```

There is a positive correlation between sepal length and sepal width.

There is a positive correlation between petal length and petal width.

There is a positive correlation between petal length and petal width.

Experiment

- 1. Import the Orange data set. Find the Pearson correlation coefficient for each type of tree age and circumference. Also draw the scatter plot.
- 2. Import the trees data set.
- i) Find the rank correlation for Girth and Volume. Draw a plot.
- ii) Find the rank correlation for Height and Volume. Draw a plot.