
Algorithm 1

Require: A quantum algorithm A such that $\nu(A) \geq 0$, an accuracy $\epsilon < 1/2$.

Ensure: An estimate of $\mathbb{E}[\nu(A)]$.

- 1: Set $k = \log_2(1/\epsilon)$, $t_0 = \frac{D\sqrt{\log_2 1/\epsilon}}{\epsilon}$, where D is a universal constant to be chosen later.
 - 2: Use algorithm 1 with $t = t_0$, $\delta = 1/10$ to estimate $\mathbb{E}[\nu(A_{0,1})]$. Let the estimate be $\tilde{\mu}_0$.
 - 3: For $l = 1, \dots, k$: Use algorithm 1 with $t = t_0$, $\delta = 1/(10k)$ to estimate $\mathbb{E}[\nu(A_{2^{l-1}, 2^l}/2^l)]$. Let the estimate be $\tilde{\mu}_l$.
 - 4: Output $\tilde{\mu} = \tilde{\mu}_0 + \sum_{l=1}^k 2^l \tilde{\mu}_l$.
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