

# Introduction to Cryptography

Daniel Mancia

University of Texas at Austin

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Classical Cryptography

Modern Cryptography

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Figure 1: "Crypto"

# What is Cryptography?

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- ▶ The practice and study of techniques for secure communication in the presence of third parties called adversaries.
- ▶ Why do we need cryptography?

# Vocabulary

- ▶ **Plaintext:** Text that is plain.
- ▶ **Encryption:** Process of encoding plaintext data such that only the intended recipient can read it.
- ▶ **Ciphertext:** The result of encryption. Unreadable garbage.
- ▶ **Decryption:** The inverse of encryption. Given a ciphertext we decode it to get back the plaintext.
- ▶ **Key:** Secret piece of information that customizes the encryption.



## SAMPLE ENCRYPTION AND DECRYPTION PROCESS

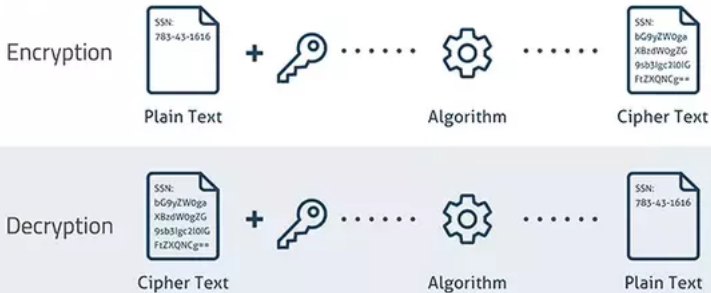


Figure 1: Crypto.

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# Classical Cryptography

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- ▶ Classical cryptography consists of encryption methods (ciphers) that don't require a machine or computer.
- ▶ Two types of ciphers were common: transposition and substitution.

# Transposition cipher

- ▶ A transposition cipher is a method of encryption that permutes or reorders the letters of the plaintext message.
- ▶ Encryption: Reorder the letters of the message
- ▶ Decryption: Do the reordering backwards.

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The diagram illustrates the Rail Fence cipher encryption process. It shows the plaintext 'W E C R L T E E R D S O E E F E A O C A I V D E N' being written in a zigzag pattern across three rows. Row 1 contains the letters at positions 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, and 21. Row 2 contains the letters at positions 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, and 22. Row 3 contains the letters at positions 3, 5, 7, 9, 11, 13, 15, 17, 19, and 21. The resulting ciphertext is the sequence of letters read row by row: W E R D S O E E F E A O C A I V D E N.

```
W . . . E . . . C . . . R . . . L . . . T . . . E  
. E . R . D . S . O . E . E . F . E . A . O . C .  
. . A . . . I . . . V . . . D . . . E . . . N . .
```

Figure 2: Rail Fence cipher

## Example of a transposition cipher



**Fig. 3 Scytale Tool**

Figure 3: Scytale Tool used by the Ancient Greeks

# Substitution Cipher

- ▶ A substitution cipher differs from a transposition cipher where the letters of the plaintext remain in the same position but each letter or group of letters is altered in some way.

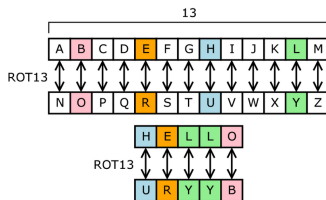


Figure 4: ROT13



# Types of substitution ciphers

- ▶ **Simple substitution:** Plaintext letters are substituted individually.
- ▶ **Polygraphic substitution:** Plaintext letters are substituted in groups.
- ▶ **Monoalphabetic cipher:** Fixed substitution alphabet is used throughout the entire message.
- ▶ **Polyalphabetic cipher:** Used different substitution alphabets on different parts of the message.

# Substitution Ciphers in History

- ▶ **Atbash cipher:** Used to encrypt the Hebrew alphabet.
- ▶ **Mlecchita vikalpa:** "the art of understanding writing in cypher, and the writing of words in a peculiar way"
- ▶ **Polybius Square:** 5x5 Grid
- ▶ **Cesar Cipher:** Simple substitution cipher used by Julius Caesar. Each letter shifted to the right by 3.
- ▶ **Hill Cipher:** Invented by Lester S. Hill. First cipher that was practical to operate on more than three symbols at once.

# One Time Pad

- ▶ The most secure encryption technique that cannot be cracked.
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- ▶ The most secure encryption technique that cannot be cracked.
- ▶  $\text{PLAINTEXT} \oplus \text{KEY} = \text{CIPHERTEXT}$
- ▶ Uncrackable if the following conditions are ALL met:
  - ▶ Truly random
  - ▶ At least as long as the plaintext
  - ▶ Never reused
  - ▶ Kept in complete secret.

# Crib Dragging

- ▶ If the key is reused then for plaintext  $p_1, p_2$  we have two ciphertext  $c_1, c_2$ .
- ▶ Notice that  $c_1 \oplus c_2 = (p_1 \oplus k) \oplus (p_2 \oplus k) = p_1 \oplus p_2$ .
- ▶ We can guess words and xor it with this result and if the output isn't garbage then that words is probably in the plaintext.

# Frequency Analysis

- ▶ **Frequency Analysis:** We can use statistics to crack ciphers.
- ▶ Count letters and determine their frequencies.

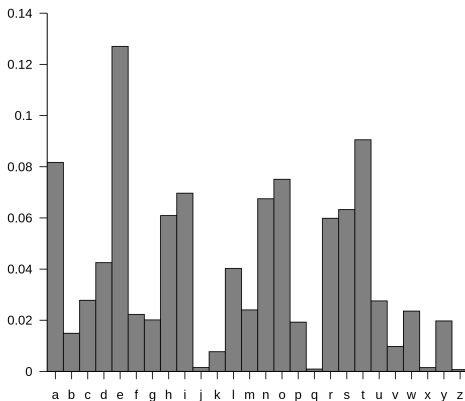


Figure 5: Etaoin shrdlu

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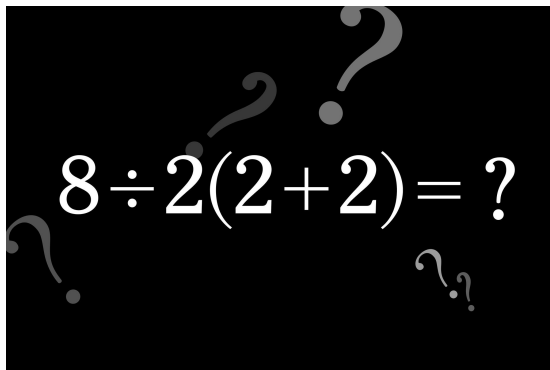

$$8 \div 2(2 + 2) = ?$$

Figure 6: Math



# Modern Cryptography

- ▶ Most modern cryptography algorithms are very secure.
- ▶ All ciphers before the 1970s were **symmetric key algorithms**.
- ▶ This means that the private key must be shared through a secure channel.

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# Public Key vs Private Key

Public Key vs Private Key		
	<b>Public Key</b>	<b>Private Key</b>
Definition	A published key that can be used to send a secure message to a receiver.	A secret key that can be used to decrypt messages encrypted with the corresponding public or private key.
Applies to	Asymmetric Encryption	Asymmetric Encryption  Symmetric Encryption

Figure 7: Keys

# Public Key Encryption

- ▶ Also known as Asymmetric Encryption.
- ▶ These algorithms are under the assumption that some problem is very hard to solve.
- ▶ As long as the private key is computationally "hard" to compute, we are safe.

# RSA Algorithm

## Key Generation

Select $p, q$	$p$ and $q$ , both prime; $p \neq q$
Calculate $n = p \times q$	
Calculate $\phi(n) = (p-1)(q-1)$	
Select integer $e$	$\gcd(\phi(n), e) = 1; 1 < e < \phi(n)$
Calculate $d$	$de \bmod \phi(n) = 1$
Public key	$KU = \{e, n\}$
Private key	$KR = \{d, n\}$

## Encryption

Plaintext:	$M < n$
Ciphertext:	$C = M^e \bmod n$

## Decryption

Plaintext:	$C$
Ciphertext:	$M = C^d \bmod n$

Figure 8: Cartoon rsa

# Diffie-Hellman

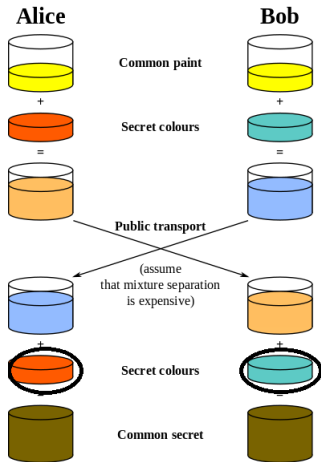


Figure 9: Diffie-Hellman with Paint



# Digital Signatures

- ▶ Alice first signs her message with her private key and sends the message to Bob.
- ▶ Bob can then verify that Alice sent the message by using her public key.

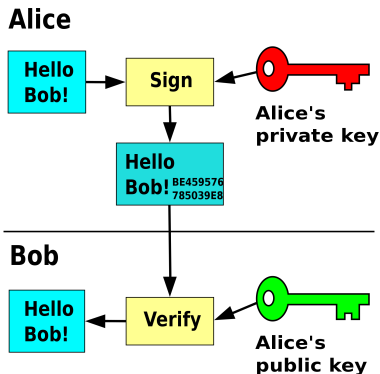


Figure 10: Digital Signatures

# Postmodern Cryptography

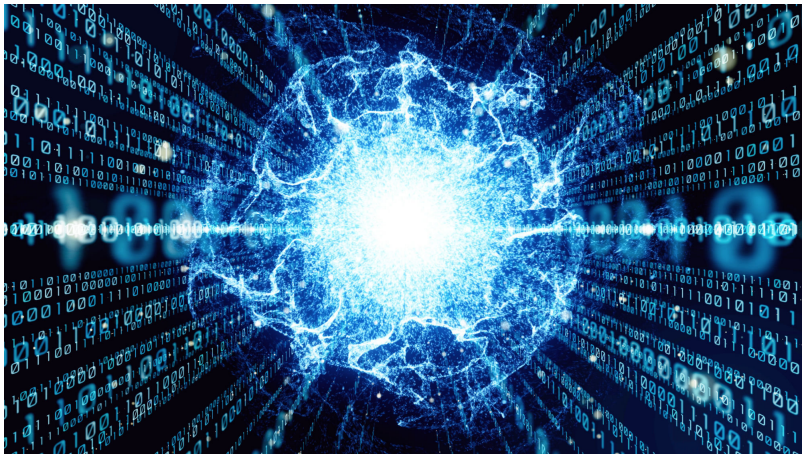


Figure 11: First google image result when searching "Quantum Computing"

# Future Topics

- ▶ Quantum Cryptography
- ▶ Math
- ▶ Stream/Block ciphers
- ▶ Hashing
- ▶ Advanced attacks