THE WILLIAM LOWELL PUTNAM MATHEMATICAL COMPETITION

held on December 3, 2016 OF WINNERS of the seventy-seventh competition ANNOUNCEMENT

WINNING TEAMS

| Team Members (in alphabetical order) | Joshua D. Brakensiek, Thomas E. Swayze, and Samuel Zbarsky | Eric D. Schneider, Zhuo Qun Song, and Xiaoyu Xu | Pakawut Jiradilok, Dong Ryul Kim, and David W. Stoner | Robert C. Shen, David H. Yang, and Yunkun Zhou | Jie Jun Ang, Huy T. Pham, and Albert R. Zhang |
|--------------------------------------|--|---|---|--|---|
| School | CARNEGIE MELLON UNIVERSITY | PRINCETON UNIVERSITY | HARVARD UNIVERSITY | MASSACHUSETTS INSTITUTE OF TECHNOLOGY | STANFORD UNIVERSITY |
| Rank | - | 2 | Э | 4 | Ŋ |

The first place team receives an award of \$25,000 and each member of the team receives \$1,000. The awards for second place are \$20,000 and \$800; for third place, \$15,000 and \$600; for fourth place \$10,000 and \$400; and for fifth place \$5,000 and \$200.

THE PUTNAM FELLOWS — THE FIVE HIGHEST RANKING INDIVIDUALS In each of the following categories, the listing is in alphabetical order.

Each receives an award of \$2,500.

| Carnegie Mellon University | Harvard University | Carnegie Mellon University | Carnegie Mellon University | Massachusetts Institute of Technology |
|----------------------------|--------------------|----------------------------|----------------------------|---------------------------------------|
| JOSHUA D. BRAKENSIEK | DONG RYUL KIM | THOMAS E. SWAYZE | SAMUEL ZBARSKY | YUNKUN ZHOU |

THE NEXT NINE HIGHEST RANKING INDIVIDUALS

Each receives an award of \$1,000.

| Harvard University | Massachusetts Institute of Technology | University of California, Los Angeles | Massachusetts Institute of Technology | Massachusetts Institute of Technology | Princeton University | Princeton University | University of Waterloo | Princeton University |
|--------------------|---------------------------------------|---------------------------------------|---------------------------------------|---------------------------------------|----------------------|----------------------|------------------------|----------------------|
| CALVIN DENG | JIYANG GAO | XIAOYU HUANG | ALLEN X. LIU | SAMMY Y. LUO | ERIC D. SCHNEIDER | ZHUO QUN SONG | DANIEL SPIVAK | MURILO C. ZANARFILA |

NKING INDIVIDUALS THE NEXT ELEVEN HIGHEST RA

Each receives an award

| Massachusetts Institute of Technology Massachusetts Institute of Technology | Massachusetts Institute of Technology Massachusetts Institute of Technology | Massachusetts Institute of Technology Massachusetts Institute of Technology | Harvard University Harvard University | Harvard University Massachusetts Institute of Technology |
|---|---|---|--|---|
| EVAN CHEN ANDREW HE HYTIN GIR HWANG | RAVI JAGADEESAN ESHAAN NICHANI | MARK A. SELLKE ROBERT C. SHEN | STEFAN SPATARU DAVID W. STONER | SCOTT WU LINGFU ZHANG |

HONORABLE MENTION — TEAMS

UNIVERSITY OF CALIFORNIA, LOS ANGELES CALIFORNIA INSTITUTE OF TECHNOLOGY UNIVERSITY OF WASHINGTON UNIVERSITY OF WATERLOO HARVEY MUDD COLLEGE

William L. Dana, Jasper P. Hugunin, and Austin Stromme Zachary Chase, Matthew Jin, and Matthew A. Weidner Emre Girgin, Xiaoyu Huang, and Konstantin Miagkov Adam R. Busis, Jordan Haack, and Abram Sanderson Antonio M. Lovett, Daniel Spivak, and Anzo Z. Teh

HONORABLE MENTION — INDIVIDUALS

KRITKORN KARNTIKOON, Massachusetts Institute of Technology MICHAEL J. KURAL, Massachusetts Institute of Technology KUSHAL A. AGARWAL, California Institute of Technology RYAN N. ALWEISS, Massachusetts Institute of Technology WILLIAM B. CHRISTERSON, Carnegie Mellon University MEGHAL GUPTA, Massachusetts Institute of Technology SAMUEL KORSKY, Massachusetts Institute of Technology BRICE HUANG, Massachusetts Institute of Technology CALVIN J. LEE, Massachusetts Institute of Technology BRIAN H. GU, Massachusetts Institute of Technology BRIAN D. BURKS, University of California, Berkeley MATTHEW JIN, California Institute of Technology YIBO GAO, Massachusetts Institute of Technology JASPER P. HUGUNIN, University of Washington LEWIS CHEN, University of California, Berkeley KYLE A. GETTIG, University of Florida ALBERT GEVORGYAN, University of Waterloo DAVID J. ALTIZIO, Carnegie Mellon University WILLIAM L. DANA, University of Washington HEEJONG LEE, University of California, Irvine JACOB J. IMOLA, Carnegie Mellon University RODRIGO S. ANGELO, Princeton University PAKAWUT JIRADILOK, Harvard University SIMONA DIACONU, Princeton University ANDRE A. ARSLAN, Princeton University ITAI BAR-NATAN, University of Toronto ADAM R. BUSIS, Harvey Mudd College QUANG VU DAO, Columbia University MYEONHU KIM, Columbia University JACOB J. KLEGAR, Harvard University SINA ABBASE, University of Waterloo AARON J. BERGER, Yale University RAY LI, Carnegie Mellon University JIE JUN ANG, Stanford University QIAN LIE, University of Chicago

SUCHAN VIVATSETHACHAI, Massachusetts Institute of Technol-KONSTANTIN MIAGKOV, University of California, Los Angeles WEERACHAI NEERANART VONG, Massachusetts Institute of TING-CHUN LIN, Massachusetts Institute of Technology TAHSIN SAFFAT, Massachusetts Institute of Technology SUNG GI PARK, Massachusetts Institute of Technology MEHTAAB S. SAWHNEY, University of Pennsylvania JUSTIN K. LIM, Massachusetts Institute of Technology ERIK A. METZ, University of Maryland, College Park MINH PHUONG NGUYEN, Stony Brook University KEVIN SUN, Massachusetts Institute of Technology ZACHARY H. POLANSKY, University of Rochester YANG LIU, Massachusetts Institute of Technology SEAN SHI, Massachusetts Institute of Technology SHYAM S. NARAYANAN, Harvard University NIHAL PEDNEKAR, University of Waterloo JASON A. SCHUCHARDT, Yale University ANZO Z. TEH, University of Waterloo ERIC NEYMAN, Princeton University HUY T. PHAM, Stanford University MEL Y. SHU, Princeton University Technology

MATTHEW A. WEIDNER, California Institute of Technology DAVID H. YANG, Massachusetts Institute of Technology JIANQIAO XIA, Massachusetts Institute of Technology KEVIN ZHOU, Massachusetts Institute of Technology YUNBEI XU, University of California, Los Angeles HUA WANG, University of California, Berkeley VICTOR Z. XU, Carnegie Mellon University ALBERT R. ZHANG, Stanford University ZIYANG ZHANG, Harvey Mudd College ROY H. ZHAO, Princeton University JEFFREY YAN, Harvard University XIAOYU XU, Princeton University

ELIZABETH LOWELL PUTNAM PRIZE

The winner receives an award of \$1,000.

SIMONA DIACONU

Princeton University

QUESTIONS COMMITTEE

Henry Cohn (chair), Microsoft and Massachusetts Institute of Technology; Byron Walden, Santa Clara University; Harm Derksen, University of Michigan, Ann Arbor.

A total of 4164 students from 568 colleges and universities in Canada and the United States participated in the Competition. There were teams from 415 institutions. More complete details will appear in the American Mathematical Monthly.

Leonard F. Klosinski (Santa Clara University), Director; Gerald L. Alexanderson (Santa Clara University) and Mark Krusemeyer (Carleton College), Associate Directors March 17, 2017

THE WILLIAM LOWELL PUTNAM MATHEMATICAL COMPETITION

March 17, 2017

Dear Colleague:

Enclosed is a report on your contestants in the 77th Competition and your team rank (if it was in the range 1—150), a list of the top 500 contestants (which you may wish to share with your committee on graduate students), an announcement of winners, and a list of participating schools. Some tables are given below. Your contributions to the Competition are greatly appreciated.

Leonard F. Klosinski, Director Gerald L. Alexanderson, Associate Director Mark Krusemeyer, Associate Director

| Score | Rank | Score | Rank | Score | Rank | Score | Rank | Score | Rank | Score | Rank |
|-------|------|-------|------|-------|-------|-------|-------|-------|-------|-------|--------|
| 114 | 1 | 78 | 24.5 | 58 | 79 | 41.8 | 182.5 | 27 | 530.5 | 10 | 1313.5 |
| 103 | 2 | 77 | 26 | 57 | 88.5 | 41.7 | 185 | 26 | 552.5 | 9 | 1499.5 |
| 102 | 3 | 76 | 28 | 56 | 99 | 41.6 | 186.5 | 25 | 566 | 8 | 1602 |
| 100 | 4 | 75 | 30 | 55 | 106.5 | 41 | 198.5 | 24 | 575 | 7 | 1634.5 |
| 97 | 5 | 72 | 32 | 54 | 109.5 | 40 | 221.5 | 23 | 585.5 | 6 | 1637.5 |
| 96 | 6 | 71 | 35 | 53 | 111 | 39 | 248 | 22 | 608 | 5 | 1644.5 |
| 95 | 7 | 70 | 37.5 | 52 | 113 | 38 | 269.5 | 21 | 658.5 | 4 | 1670.5 |
| 93 | 8 | 69 | 39 | 51 | 118 | 37 | 284.5 | 20 | 733 | 3 | 1720 |
| 92 | 9 | 68 | 42 | 50 | 126 | 36 | 298 | 19 | 813 | 2 | 1866 |
| 90 | 11 | 67 | 45.5 | 49 | 135.5 | 35 | 305.5 | 18 | 881 | 1 | 2123.5 |
| 87 | 13 | 66 | 47.5 | 48 | 147.5 | 34 | 310 | 17 | 926.5 | 0 | 3214 |
| 86 | 14 | 65 | 52 | 47 | 161 | 33 | 318 | 16 | 947.5 | | |
| 85 | 16 | 64 | 57.5 | 46 | 170.5 | 32 | 337 | 15 | 958.5 | 1 | |
| 84 | 18 | 63 | 60.5 | 45 | 174.5 | 31 | 365.5 | 14 | 975.5 | | |
| 83 | 19 | 61 | 65 | 44 | 176 | 30 | 408.5 | 13 | 1006 | | |
| 82 | 21 | 60 | 69.5 | 42 | 177 | 29 | 460.5 | 12 | 1064 | | |
| 79 | 23 | 59 | 72.5 | 41.9 | 179 | 28 | 501 | 11 | 1150 | | |

FREQUENCY DISTRIBUTION OF PROBLEM SCORES OF THE TOP 187 CONTESTANTS

| | A1 | A2 | A3 | A4 | A5 | A6 | B1 | B2 | В3 | B4 | B5 | B6 | total |
|-------|-----|----------------|------|----------------|-----|------|-----|----|------|----------|----------------|-----|-------|
| 10 | 123 | 49 | 15 | 45 | 28 | 2 | 110 | 94 | 28 | 62 | 21 | 20 | 597 |
| 9 | 55 | 66 | 6 | 16 | 4 | 0 | 18 | 18 | 124 | 32 | 12 | 11 | 362 |
| 8 | 1 | 49 | 47 | 4 | 1 | 0 | 22 | 39 | 13 | 16 | 5 | 7 | 204 |
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0. | 0 | 0 | 0 | 0 | 0 |
| 6 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 3 | 13 | 12 | 12 | 10 | 1 | 17 | 23 | 3 | 3 | 6 | 4 | 107 |
| 1- | -0- | 7 - | -37- | 5- | 8- | 1-1- | 8- | 8- | 1-1- | <u> </u> | 5- | 2- | —91— |
| 0 | 5 | 3 | 45 | 31 | 27 | 69 | 10 | 5 | 6 | 27 | 62 | 35 | 325 |
| blank | 0 | 0 | 25 | 74 | 109 | 114 | 2 | 0 | 12 | 38 | 76 | 108 | 558 |