

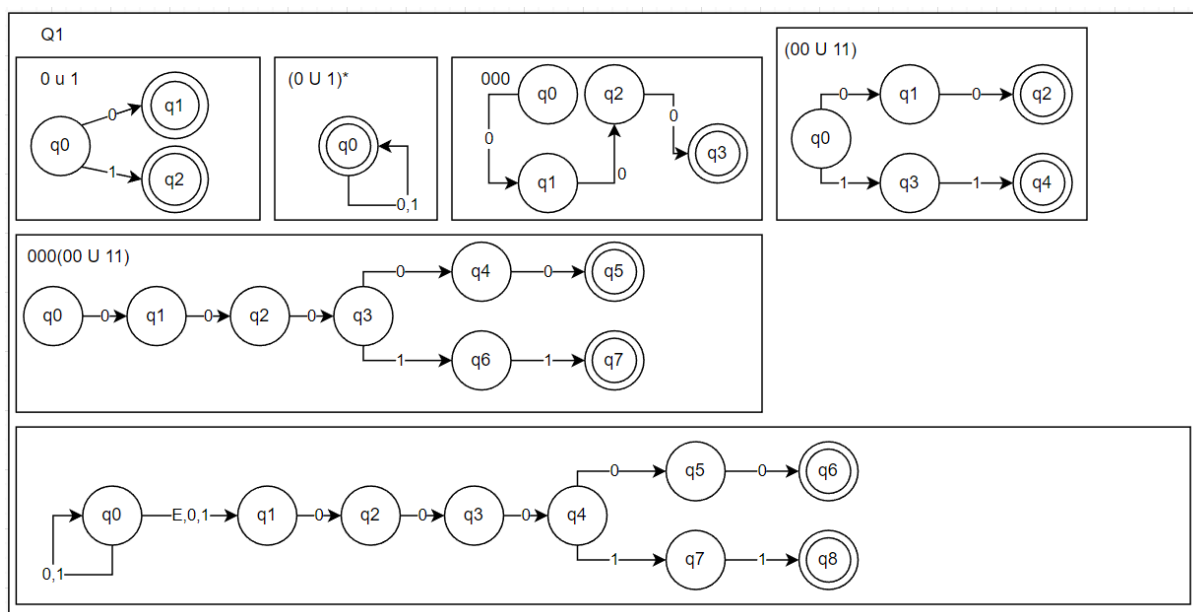
Scott Bebington

U21546216

COS 210

Worksheet 5

### Question 1



### Question 2

$$L_r = \bigcup_{a \in \Sigma} a \cdot L_{\delta(r,a)} \text{ if } r \notin F$$

$$L_r = \epsilon \cup \left( \bigcup_{a \in \Sigma} a \cdot L_{\delta(r,a)} \right) \text{ if } r \in F$$

We have the following functions

	a	b
q0	q0	q0

And:

$$L_{q0} = a.L_{q0} \cup b.L_{q0}$$

This is equivalent to:

$$L_{q0} = (a \cup b).L_{q0}$$

Using Lemma:

$$L_{q0} = (a \cup b)^*$$

### Question 3

Since the DFA does not accept any strings using the language  $\{a,b\}$ , the regular expression for this is the empty set.

$$L(M) = \emptyset$$

### Question 4

$$L_r = \bigcup_{a \in \Sigma} a \cdot L_{\delta(r,a)} \text{ if } r \notin F$$

$$L_r = \epsilon \cup \left( \bigcup_{a \in \Sigma} a \cdot L_{\delta(r,a)} \right) \text{ if } r \in F$$

	a	b
q	q	r
r	r	r

And:

$$L_q = a.L_q \cup b.L_r$$

$$L_r = a.L_r \cup b.L_r$$

This is equivalent to:

$$L_r = (a \cup b).L_r$$

Using Lemma:

$$L_r = (a \cup b)^*$$

Substituting into  $L_q$ :

$$L_q = a.L_q \cup b(a \cup b)^*$$

Using Lemma:

$$L(M) = a^* b (a \cup b)^*$$

