

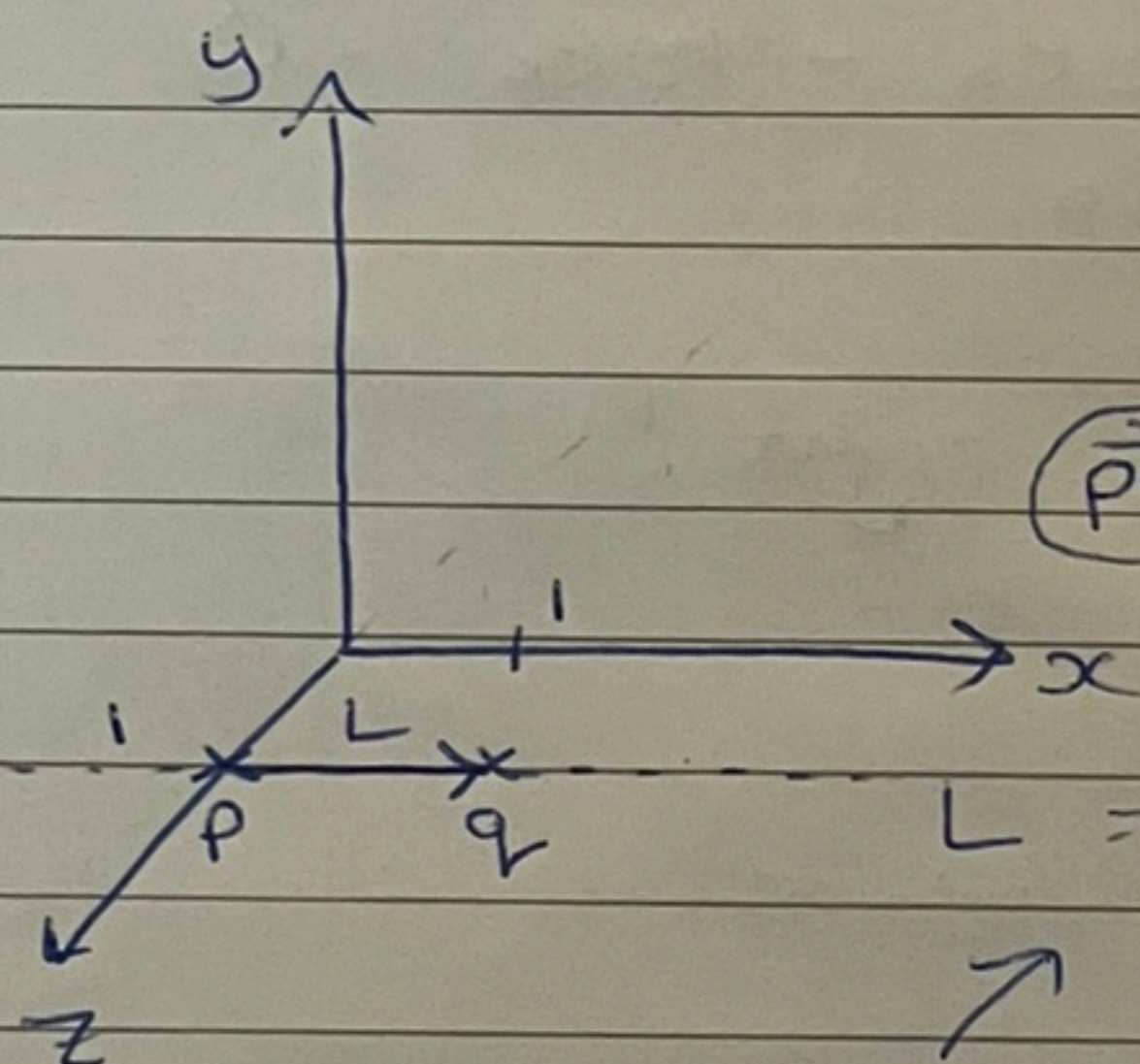
2024-02-15 - UN

What is a line? Apparently a plucker coords looks like this

$$\{\underbrace{-\vec{p} + \vec{q}}_{\text{vector from } \vec{p} \text{ to } \vec{q}}, \vec{p} \times \vec{q}\}$$

Where  $\vec{p}$  &  $\vec{q}$  are two points on a line. Apparently this is how a line is defined in PGA. Let's see...

How about the line below.



$$\vec{p} = [0, 0, 1]$$

$$\vec{q} = [1, 0, 0]$$

$$\{\underbrace{-\vec{p} + \vec{q}}_{\vec{p}-\vec{q}}, \vec{p} \times \vec{q}\}$$

$$L = ([+1, 0, 0], [0, 1, 0])$$

Plucker coords representation of a line

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{vmatrix} = \hat{i}(0) - \hat{j}(-1) + \hat{k}(0) = \hat{j}$$

What about PGA?

The line is the meet of the x-z plane going through the origin and the x-y plane going one unit away from origin.

$$\text{Plane}_1 = e_2$$

$$\text{Plane}_2 = e_3 - e_0$$

$$\leftarrow \text{use } ax + by + cz - d = 0$$

$$ae_1 + be_2 + ce_3 - de_0 = 0$$

$$L = \text{Plane}_1 \wedge \text{Plane}_2$$

$$= e_2 \wedge (e_3 - e_0)$$

$$= e_{23} - e_{20}$$

$$= e_{23} + e_{02}$$

$$\text{erase } e_{32} \text{ and } e_{02}$$

$$\text{or } \text{Plane}_2 \wedge \text{Plane}_1$$

$$= (e_3 - e_0) \wedge e_2$$

$$= e_{32} - e_{02}$$

$$= -e_{23} - e_{02}$$

$$L = ([1, 0, 0], [0, 1, 0]) \text{ or } = ([-1, 0, 0], [0, -1, 0])$$

$e_{23} \ e_{31} \ e_{12}$

$e_{01} \ e_{02} \ e_{03}$

Exactly the same as Plucker coords