

```
1 (defn third [list]
2   (second (next list)))
3
4 ;; True if the form is a variable (symbol).
5 (defn variable? [form]
6   (symbol? form))
7
8 ;; True if the two forms are the same variable.
9 (defn same-variable? [form1 form2]
10  (and (variable? form1) (variable? form2) (= form1 form2)))
11
12 ;; True if the form represents a sum.
13 (defn sum? [form]
14  (and (list? form) (= '+ (first form))))
15
16 ;; Constructs a sum of a and b.
17 (defn make-sum [a b]
18  (list '+ a b))
19  ;(cond
20    ;(= a 0) b
21    ;(= b 0) a
22    ;:else (+ a b)))
23
24 ;; Selects the addend (first value) of a sum.
25 (defn addend [sum]
26  (second sum))
27
28 ;; Selects the augend (second value) of a sum.
29 (defn augend [sum]
30  (third sum))
31
32 ;; True if the form represents a difference.
33 (defn diff? [form]
34  (and (list? form) (= '- (first form))))
35
36 ;; Constructs a difference of a and b.
37 (defn make-diff [a b]
38  (list '- a b))
39  ;(cond
40    ;(= a 0) (list - b)
41    ;(= b 0) a
42    ;:else (- a b)))
43
44 ;; Selects the minuend (first value) of a difference.
45 (defn minuend [diff]
46  (second diff))
47
48 ;; Selects the minuend (second value) of a difference.
49 (defn subtrahend [diff]
50  (third diff))
51
52 ;; True if the form represents a product.
53 (defn prod? [form]
54  (and (list? form) (= '* (first form))))
55
56 ;; Constructs a product of a and b.
57 (defn make-prod [a b]
58  (list '* a b))
59  ;(cond
60    ;(= a 0) 0
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61      ;(= a 1) b
62      ;(= b 0) 0
63      ;(= b 1) a
64      ;:else (* a b)))
65
66 ;; Selects the multiplier (first value) of a product.
67 (defn multiplier [prod]
68   (second prod))
69
70 ;; Selects the multiplicand (second value) of a product.
71 (defn multiplicand [prod]
72   (third prod))
73
74 ;; True if the form represents a quotient.
75 (defn quot? [form]
76   (and (list? form) (= '/ (first form))))
77
78 ;; Constructs a quotient of a and b.
79 (defn make-quot [a b]
80   (list '/ a b))
81   ;(cond
82     ;(= a 0) 0
83     ;(= b 1) a
84     ;:else (/ a b)))
85
86 ;; Selects the dividend (top value) of a quotient.
87 (defn dividend [quotient]
88   (second quotient))
89
90 ;; Selects the divisor (bottom value) of a quotient.
91 (defn divisor [quotient]
92   (third quotient))
93
94 ;; True if the form represents a power.
95 (defn power? [form]
96   (and (list? form) (= '** (first form))))
97
98 ;; Constructs a power of a and b.
99 (defn make-power [a b]
100   (list '** a b))
101   ;(cond
102     ;(= b 0) 1
103     ;(= b 1) a
104     ;:else (Math/pow a b)))
105
106 ;; Selects the base value of the power.
107 (defn base-power [power]
108   (second power))
109
110 ;; Selects the exponent of the power.
111 (defn exponent-power [power]
112   (third power))
113
114 ;; True if the form represents a power.
115 (defn ln? [form]
116   (and (list? form) (= 'ln (first form))))
117
118 ;; Constructs a power of a and b.
119 (defn log-of [form]
120   (second form))
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121
122 ;; Returns the derivative of a function expressed in Clojure notation, where
    variables are quoted.
123 ;; The second parameter is the variable which the derivative is calculated
    with respect to.
124 (defn derivative [form var]
125   (cond ; The derivative of a constant is 0
126         (number? form) 0
127         ; The derivative of a variable is 0 if the variable is not the one
    being derived; or 1, if it is.
128         (variable? form) (if (same-variable? form var) 1 0)
129         ; Sum rule
130         (sum? form) (make-sum (derivative (addend form) var)
131                                (derivative (augend form) var))
132         ; Difference rule
133         (diff? form) (make-diff (derivative (minuend form) var)
134                                  (derivative (subtrahend form) var))
135         ; Quotient rule
136         (quot? form) (make-quot (make-diff (make-prod (divisor form)
137                                                         (derivative (dividend form)
138                                                         (divisor form) var))
139                                     (divisor form) var)
140                                  (make-prod (divisor form)
141                                                (dividend form)))
142         ; Power rule
143         (power? form) (make-prod (make-prod (exponent-power form)
144                                                (make-power (base-power form) (-
145                                                                (exponent-power form) 1)))
146                                   (derivative (base-power form) var))
147         ; Natural Log rule
148         (ln? form) (make-quot (derivative (log-of form) var)
149                                (log-of form))
150         ; Product rule
151         (prod? form) (make-sum (make-prod (multiplier form)
152                                              (derivative (multiplicand form)
153                                              var))
154                                (make-prod (derivative (multiplier form) var)
155                                              (multiplicand form))))
152
153

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