

$$\left[\begin{array}{ccc|c} 1 & -2 & 1 & 1 \\ 2 & -6 & 6 & 4 \\ -3 & 5 & -1 & -2 \end{array} \right] \xrightarrow{\text{R2} - 2\text{R1}, \text{R3} + 3\text{R1}} \left[\begin{array}{ccc|c} 1 & -2 & 1 & 1 \\ 0 & -2 & 4 & 0 \\ 0 & -1 & 2 & 1 \end{array} \right]$$

$$(-1) + (-10)x = 0 \Rightarrow -10x = 1 \Rightarrow x = -\frac{1}{10}$$

$$\left[\begin{array}{ccc|c} 1 & -2 & 1 & 1 \\ 0 & -10 & 4 & 2 \\ 0 & -1 & 2 & 1 \end{array} \right] \xrightarrow{\text{R2} - 4\text{R1}, \text{R3} - \frac{1}{10}\text{R1}} \left[\begin{array}{ccc|c} 1 & -2 & 1 & 1 \\ 0 & 1 & -\frac{2}{5} & -\frac{1}{5} \\ 0 & 0 & \frac{8}{5} & \frac{4}{5} \end{array} \right]$$

$$4\left(\frac{-1}{10}\right) = \frac{-4}{10} = \frac{-2}{5}$$

$$2 + 4\left(-\frac{1}{10}\right) = 2 - \frac{4}{10} = \frac{20}{10} - \frac{4}{10} = \frac{16}{10} = \frac{8}{5}$$

$$\left[\begin{array}{ccc|c} 1 & -2 & 1 & 1 \\ 0 & 1 & -\frac{2}{5} & -\frac{1}{5} \\ 0 & 0 & \frac{8}{5} & \frac{4}{5} \end{array} \right] \xrightarrow{\text{R3} \cdot \frac{5}{8}}$$

$$1 + 2\left(-\frac{1}{10}\right) = 1 - \frac{2}{10} = 1 - \frac{1}{5} = \frac{4}{5}$$

$$\left[\begin{array}{ccc|c} 1 & -2 & 1 & 1 \\ 0 & 1 & -\frac{2}{5} & -\frac{1}{5} \\ 0 & 0 & 1 & \frac{1}{2} \end{array} \right]$$

$$\frac{4}{5} \cdot \frac{5}{8} = \frac{4}{8} = \frac{1}{2}$$