

1. Given the points  $P(-1, 5, 7)$ ,  $Q(2, 1, 4)$ ,  $R(1, 1, 1)$  and the vectors  $\vec{v} = \overrightarrow{PQ}$  and  $\vec{w} = \overrightarrow{PR}$ , find:

a)  $3\vec{v} - 2\vec{w}$

b)  $\|\vec{v}\|$

c) the angle  $\theta$  between  $\vec{v}$  and  $\vec{w}$ . Give answer exactly (using  $\cos^{-1}$ ), and to the nearest 0.1 degree

d)  $\text{proj}_{\vec{v}} \vec{w}$

e)  $\text{scal}_{\vec{w}} \vec{v}$

f) a unit vector that is orthogonal to both  $\vec{v}$  and  $\vec{w}$

1. (continued)

g) the area of triangle  $PQR$

h) the equation (in  $x,y,z$ ) of the sphere centered at  $P$  and containing  $R$

i) a parametric vector equation of the line through  $Q$  and perpendicular to triangle  $PQR$

2. In  $\mathbb{R}^3$ , graph the curve  $\vec{\mathbf{r}}(t) = \langle \sin(\pi t), t/2, \cos(\pi t) \rangle$ ,  $0 \leq t \leq 4$ . Trying different points of view might help your sketch.