

CSE3506 Essentials of Data Analytics

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Lab Exercise: 9: Gradient Descent Optimization

Objective: To perform Gradient Descent Optimization

Question:

Gradient Descent - Optimization

```
rm(list=ls())
```

Create a sequence of elements in a Vector to generate sequences when plotting the axes of figures or simulating data.

```
xs <- seq(0,4,len=20)
xs

## [1] 0.0000000 0.2105263 0.4210526 0.6315789 0.8421053 1.0526316 1.26315
79

## [8] 1.4736842 1.6842105 1.8947368 2.1052632 2.3157895 2.5263158 2.73684
21

## [15] 2.9473684 3.1578947 3.3684211 3.5789474 3.7894737 4.0000000</pre>
```

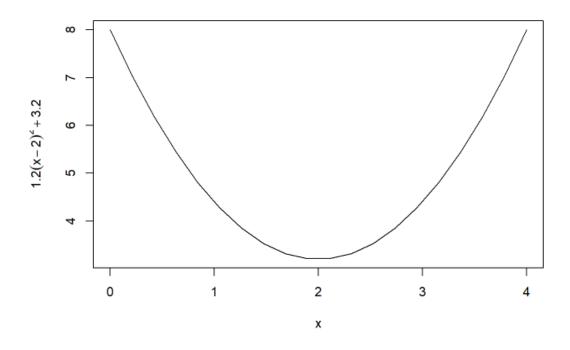
Define the function we want to optimize

```
f \leftarrow function(x) \{1.2 * (x-2)^2 + 3.2\}
```

Plot the function

```
plot(xs , f (xs), type="l",xlab="x",ylab=expression(1.2(x-2)^2 +3.2))
```





calculate the gradient df/dx

```
grad <- function(x) {
   1.2*2*(x-2)
}</pre>
```

$$df/dx = 2.4(x-2)$$
, if $x = 2$ then $2.4(2-2) = 0$

The actual solution we will approximate with gradient descent

is x = 2 as depicted in the plot below

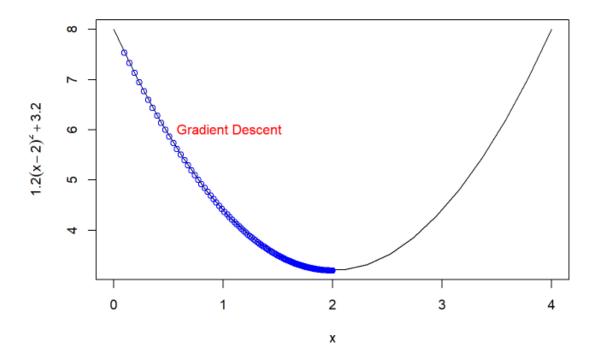
 $\# lines \ (c\ (2,2),\ c\ (3,8),\ col="red",lty=2)\ \# text\ (2.1,7,\ "Closed form\ solution",col="red",pos=4)$

gradient descent implementation

```
x <- 0.1 # initialize the first guess for x-value
xtrace <- x # store x -values for graphing purposes (initial)
ftrace <- f(x) # store y-values (function evaluated at x) for graphing purp
oses (initial)
stepFactor <- 0.01 # learning rate 'alpha'</pre>
```



```
for (step in 1:5000) {
    x <- x - stepFactor*grad(x) # gradient descent update
    xtrace <- c(xtrace,x) # update for graph
    ftrace <- c(ftrace,f(x)) # update for graph
}
plot(xs , f (xs), type="l",xlab="x",ylab=expression(1.2(x-2)^2 +3.2))
lines ( xtrace , ftrace , type="b",col="blue") # type=b (both points & line s)
text (0.5,6, "Gradient Descent",col="red",pos= 4)</pre>
```



print final value of x

```
print(x) # x converges to 2.0
## [1] 2
plot(xs , f (xs), type="l",xlab="x",ylab=expression(1.2(x-2)^2 +3.2))
text(2,4,"x=2",col="red",pos=1)
text(2,4,"(Global minimum)",col="red",pos=3)
```



