

Svolgere l'analisi cinematica.

Determinare matrice di congruenza e di equilibrio.

Determinare le reazioni vincolari a terra col PLV ( $Le=0$ ).

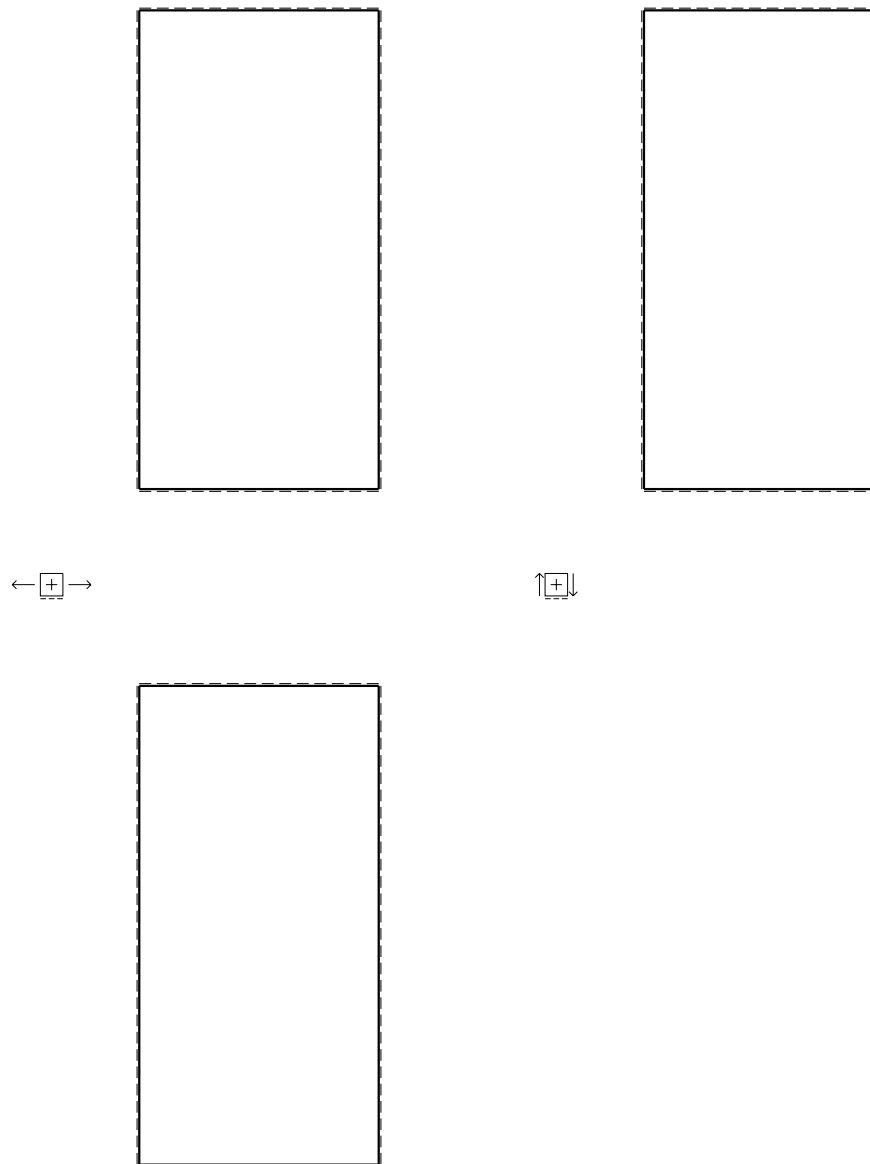
Determinare le azioni interne in C col PLV ( $Le=0$ ).

Carichi e deformazioni date hanno verso efficace in disegno.

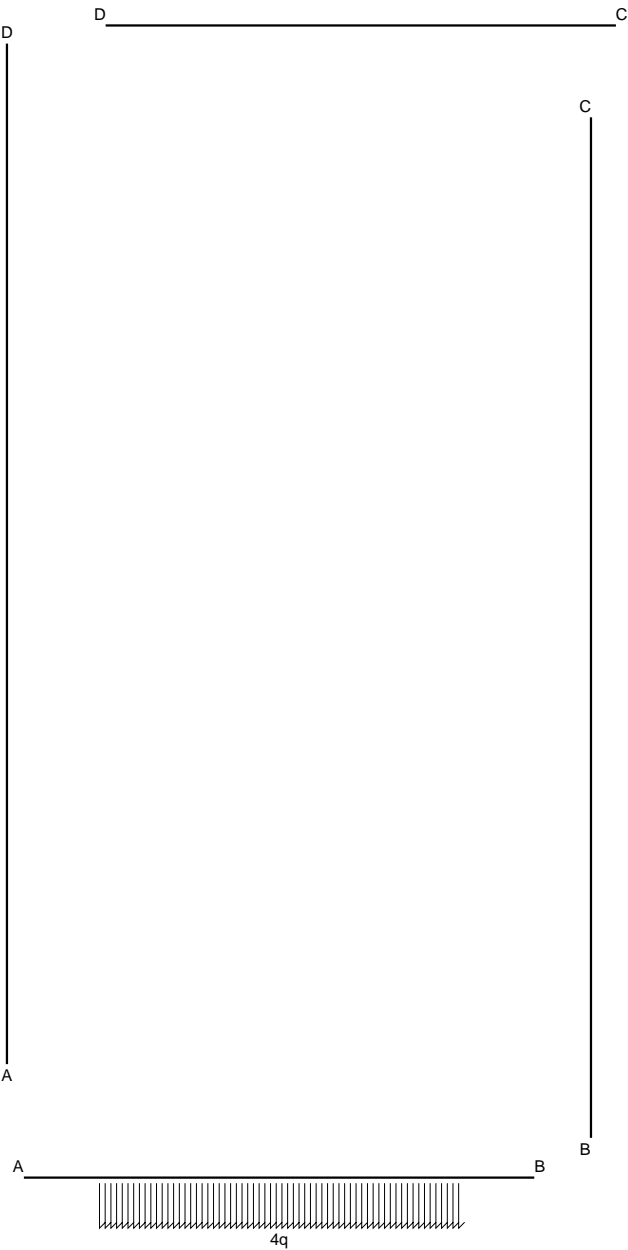
Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

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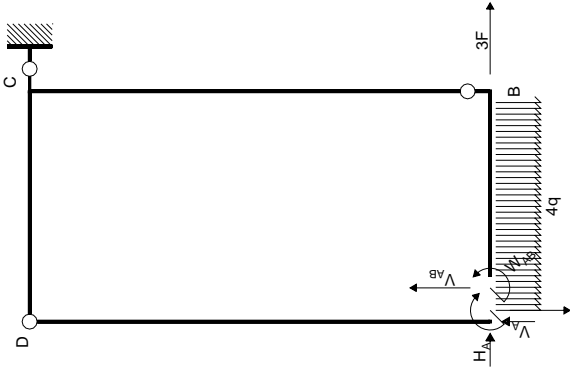


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REAZIONI

$H_A =$	$V_A =$	$H_C =$	$V_C =$
$N_{DA} =$			
$H_{AB} =$	$H_{BC} =$	$H_{CD} =$	
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$	
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$	
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$	
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$	
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$	



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$2H_A b - V_A b = -6Fb - 2qb^2$

Rotazione intorno a B: aste BA

$-V_{AB} b + W_{AB} = -2qb^2$

Rotazione intorno a D: aste DA

$2H_A b - W_{AB} = 0$

Rapporto tra componenti nodo ZA

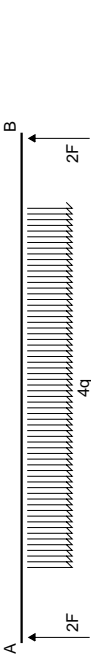
$-W_{AB} = 0$

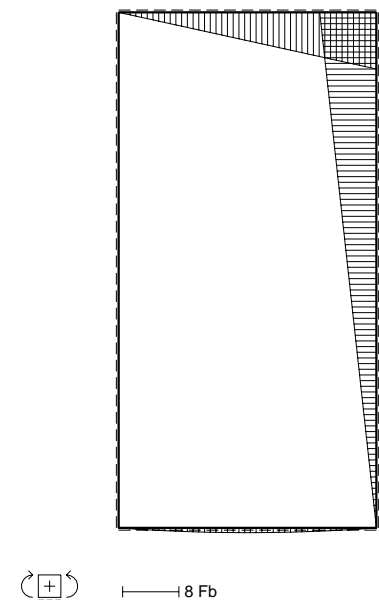
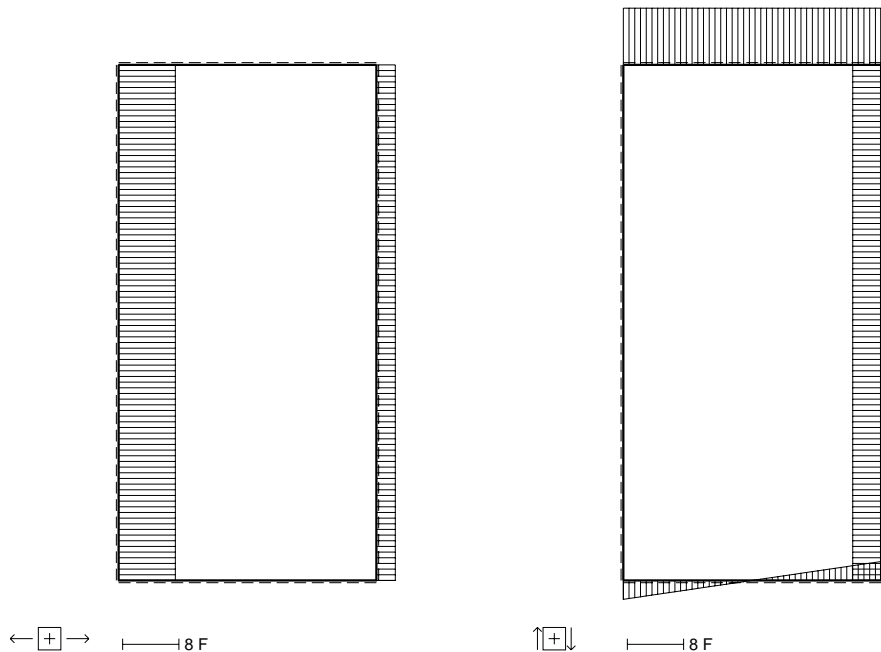
Matrice di equilibrio

$$\begin{bmatrix} H_A b & V_A b & V_{AB} b & W_{AB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\varphi_C \begin{bmatrix} 2 & -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -6 & -2 \end{bmatrix}$$
$$\varphi_{BC} \begin{bmatrix} 0 & 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} 0 & -2 \end{bmatrix}$$
$$\varphi_{DA} \begin{bmatrix} 2 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 0 & 0 \end{bmatrix}$$
$$\varphi_{AD} \begin{bmatrix} 0 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_{AB} b \\ V_A b \\ W_{AB} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 2 \\ 6 & 2 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$





## REAZIONI

$H_A = 0$

$V_A = 6F + 2qb = 8F$

$H_C = -3F = -3F$

$V_C = -6F + 2qb = -4F$

$N_{DA} = -6F = -6F$

$H_{AB} = 0$

$V_{AB} = 2qb = 2F$

$W_{AB} = 0$

$H_{BA} = 0$

$V_{BA} = 2qb = 2F$

$W_{BA} = 0$

$H_{BC} = 3F = 3F$

$V_{BC} = -2qb = -2F$

$W_{BC} = 0$

$H_{CB} = -3F = -3F$

$V_{CB} = 2qb = 2F$

$W_{CB} = -6Fb = -6Fb$

$H_{CD} = 0$

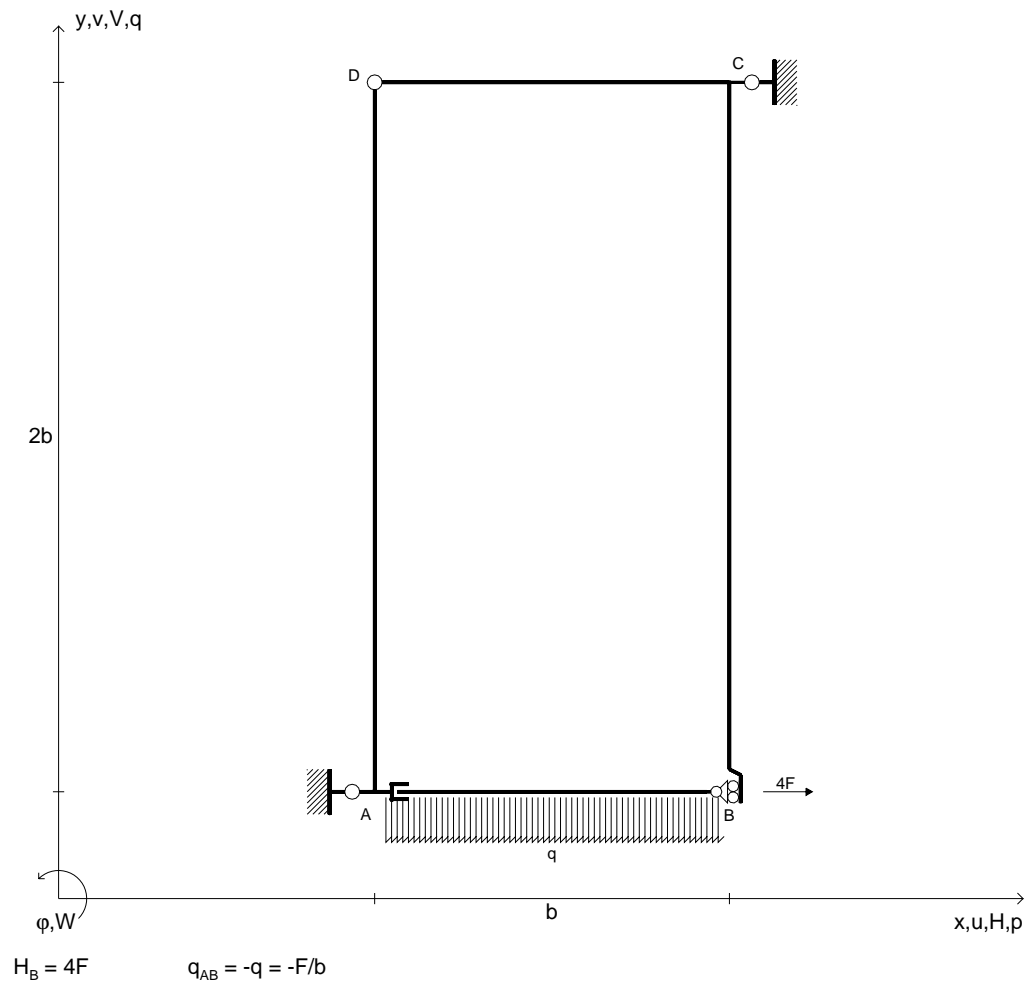
$V_{CD} = -6F = -6F$

$W_{CD} = 6Fb = 6Fb$

$H_{DC} = 0$

$V_{DC} = 6F = 6F$

$W_{DC} = 0$



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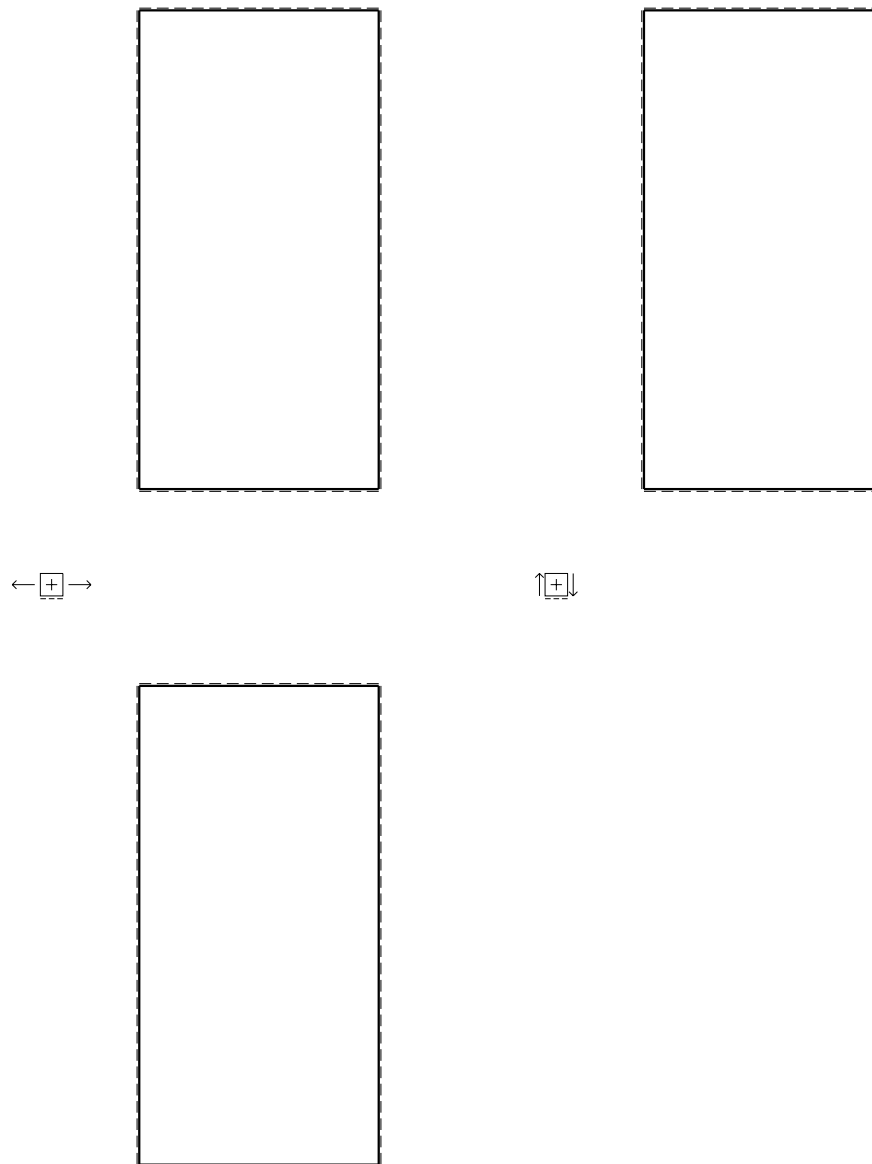
Determinare le azioni interne in C col PLV ( $Le=0$ ).

Carichi e deformazioni date hanno verso efficace in disegno.

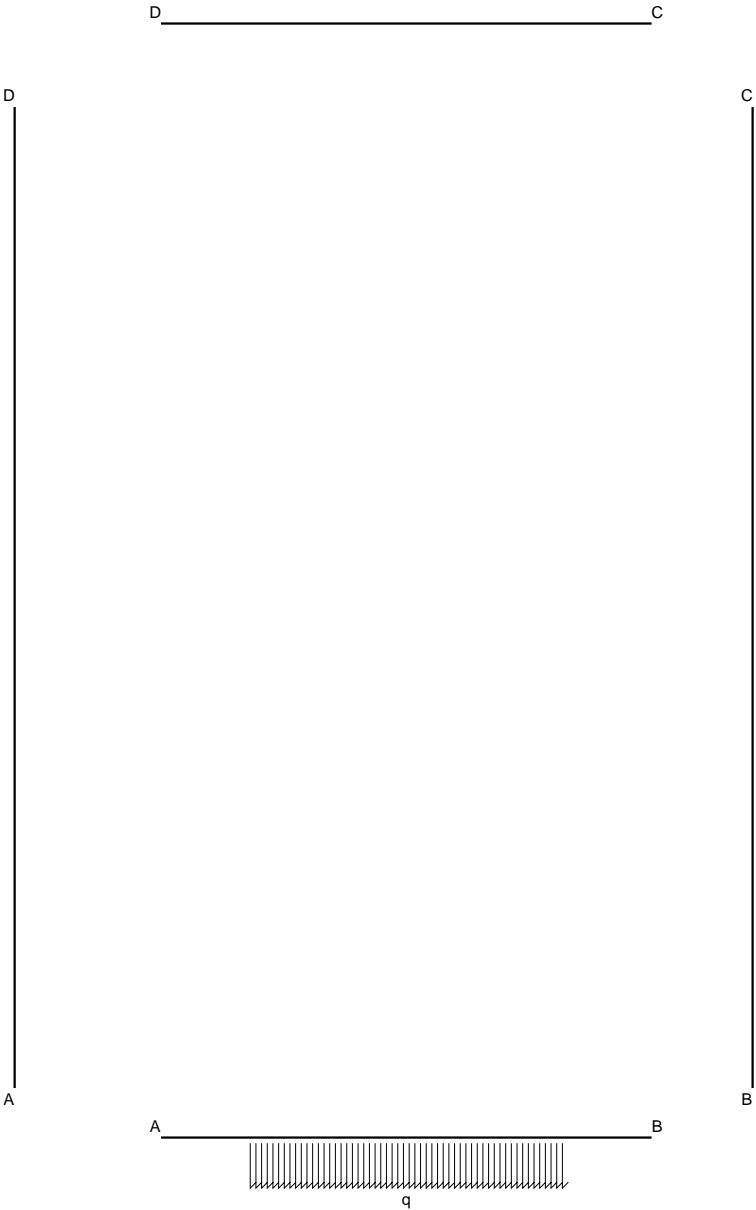
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Tracciare i diagrammi delle azioni interne nelle aste.

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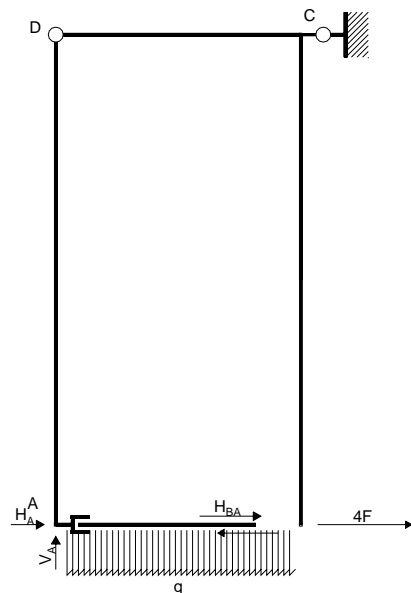


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REAZIONI

$H_A =$	$H_C =$		
$V_A =$	$V_C =$		
$H_{AB} =$	$H_{BC} =$	$H_{CD} =$	$H_{DA} =$
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$	$V_{DA} =$
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$	$W_{DA} =$
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$	$H_{AD} =$
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$	$V_{AD} =$
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$	$W_{AD} =$



## EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_A b - V_A b = -8Fb - 1/2qb^2$$

Rotazione intorno a D: aste DA AB

$$2H_A b + 2H_{BA} b = 1/2qb^2$$

Traslazione orizzontale: aste AB

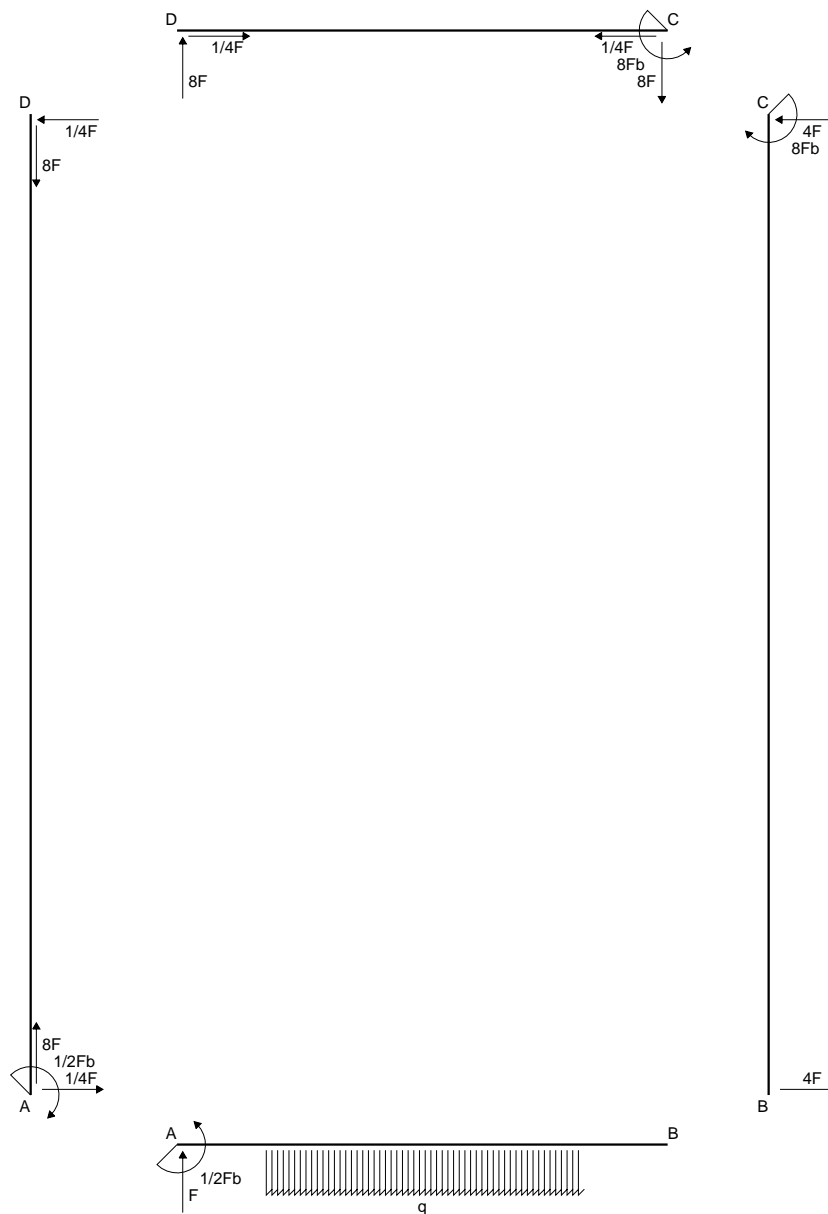
$$H_{BA} = 0$$

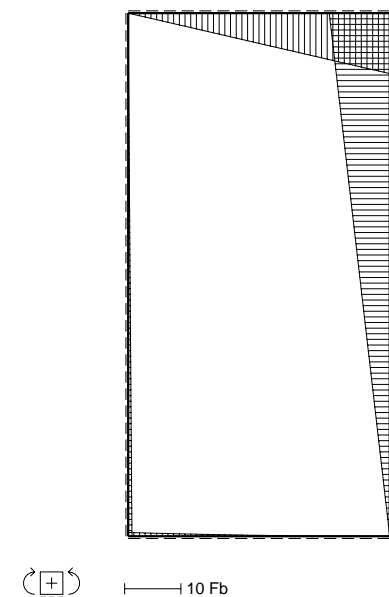
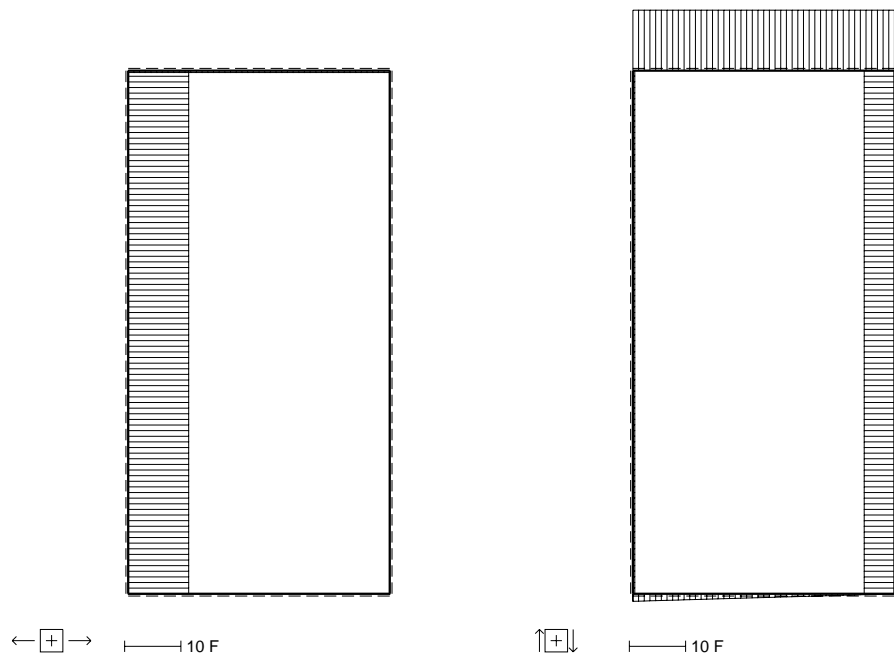
Matrice di equilibrio

$$\begin{bmatrix} \varphi_C \\ \varphi_{DA} \\ u_{AB} \end{bmatrix} \begin{bmatrix} H_A b & V_A b & H_{BA} b \\ 2 & -1 & 0 \\ 2 & 0 & 2 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -8 & -1/2 \\ 0 & 1/2 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 1/4 \\ 8 & 1 \\ 0 & 0 \end{bmatrix}$$





## REAZIONI

$$H_A = 1/4qb = 1/4F$$

$$V_A = 8F + qb = 9F$$

$$H_{AB} = 0$$

$$V_{AB} = qb = F$$

$$W_{AB} = 1/2qb^2 = 1/2Fb$$

$$H_{BA} = 0$$

$$V_{BA} = 0$$

$$W_{BA} = 0$$

$$H_C = -4F - 1/4qb = -17/4F$$

$$V_C = -8F = -8F$$

$$H_{BC} = 4F = 4F$$

$$V_{BC} = 0$$

$$W_{BC} = 0$$

$$H_{CB} = -4F = -4F$$

$$V_{CB} = 0$$

$$W_{CB} = -8Fb = -8Fb$$

$$H_{CD} = -1/4qb = -1/4F$$

$$V_{CD} = -8F = -8F$$

$$W_{CD} = 8Fb = 8Fb$$

$$H_{DC} = 1/4qb = 1/4F$$

$$V_{DC} = 8F = 8F$$

$$W_{DC} = 0$$

$$H_{DA} = -1/4qb = -1/4F$$

$$V_{DA} = -8F = -8F$$

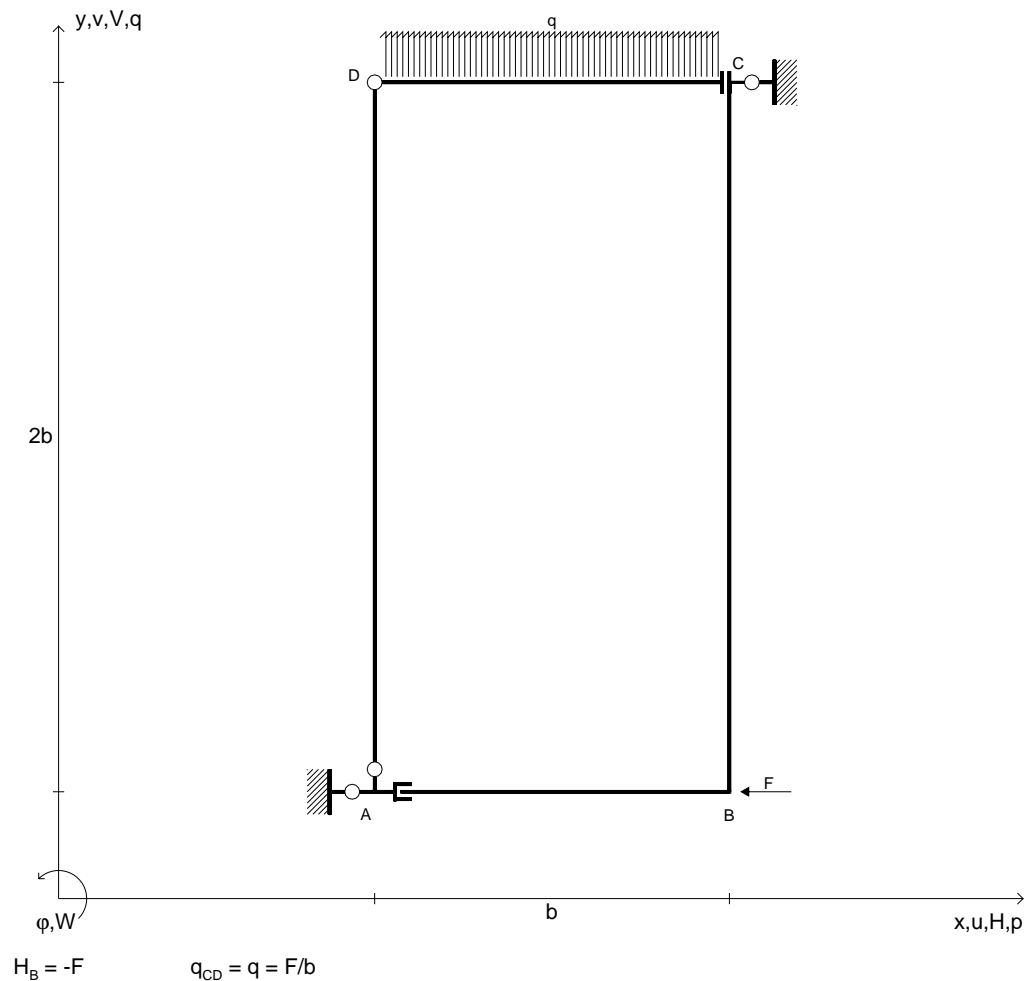
$$W_{DA} = 0$$

$$H_{AD} = 1/4qb = 1/4F$$

$$V_{AD} = 8F = 8F$$

$$W_{AD} = -1/2qb^2 = -1/2Fb$$





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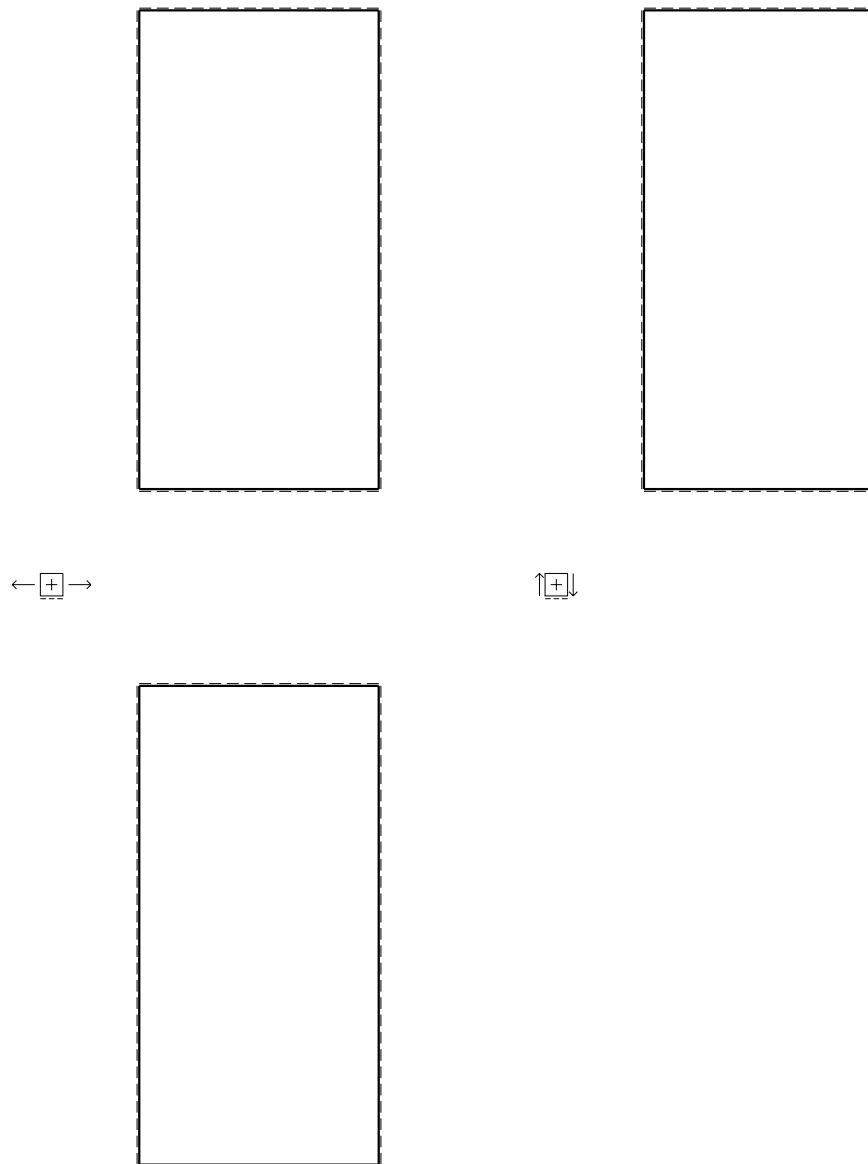
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Carichi e deformazioni date hanno verso efficace in disegno.

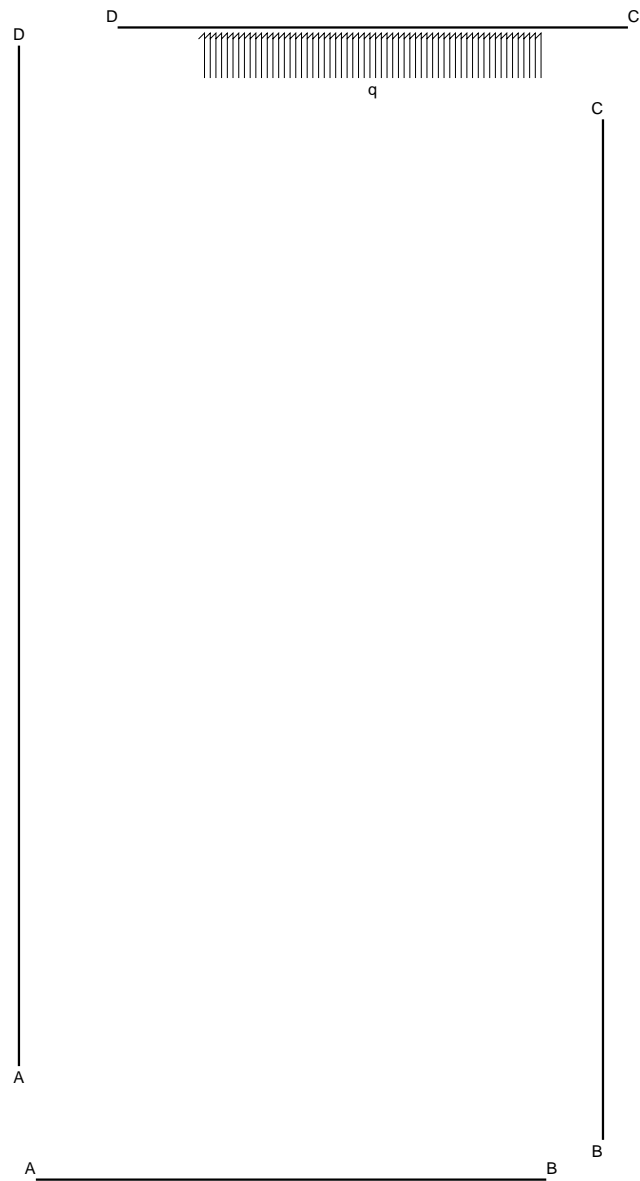
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Tracciare i diagrammi delle azioni interne nelle aste.

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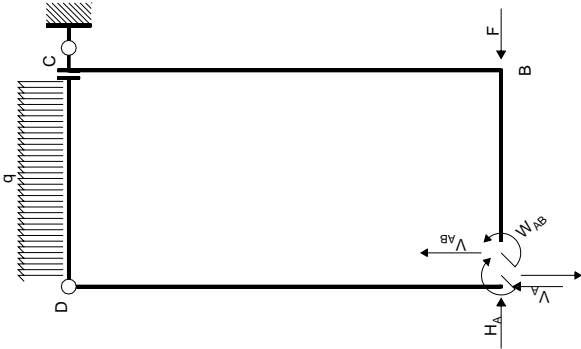


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REAZIONI

$H_A =$	$V_A =$	$H_C =$	$V_C =$
$N_{DA} =$			
$H_{AB} =$	$H_{BC} =$	$H_{CD} =$	
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$	
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$	
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$	
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$	
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$	



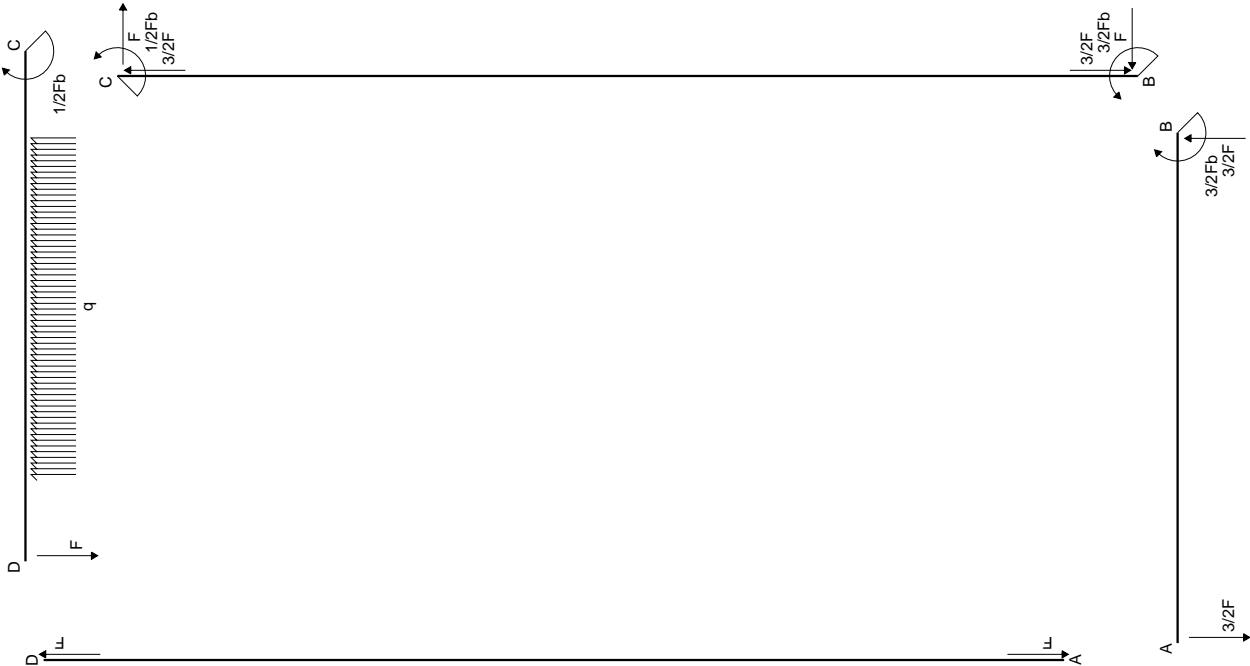
EQUAZIONI DI EQUILIBRIO  
Rotazione globale intorno a C  
 $2H_A b - V_A b = 2Fb + 1/2qb^2$   
Traslazione verticale: aste CD DA  
 $V_A - V_{AB} = -qb$   
Rotazione intorno a D: aste DA  
 $2H_A b - W_{AB} = 0$   
Rapporto tra componenti nodo ZA  
 $-W_{AB} = 0$

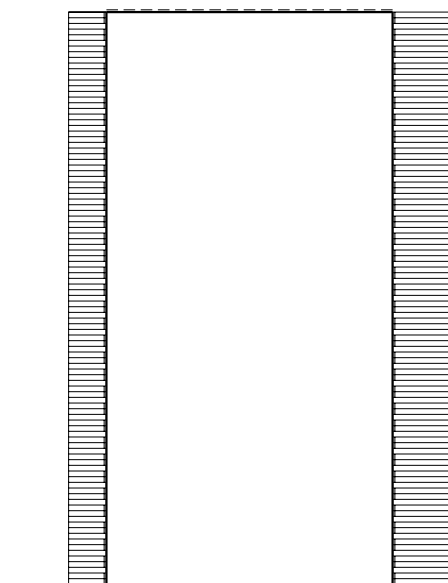
Matrice di equilibrio

$$\begin{bmatrix} H_A b & V_A b & V_{AB} b & W_{AB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\varphi_C \begin{bmatrix} 2 & -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 2 & 1/2 \end{bmatrix}$$
$$\varphi_{CD} \begin{bmatrix} 0 & 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} 0 & -1 \end{bmatrix}$$
$$\varphi_{DA} \begin{bmatrix} 2 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 0 & 0 \end{bmatrix}$$
$$\varphi_{AD} \begin{bmatrix} 0 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 0 & 0 \end{bmatrix}$$

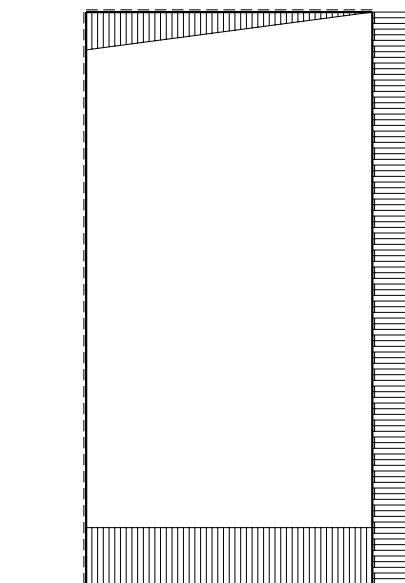
Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \\ V_{AB} b \\ W_{AB} \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\begin{bmatrix} 0 & 0 \\ -2 & -1/2 \\ -2 & 1/2 \\ 0 & 0 \end{bmatrix}$$

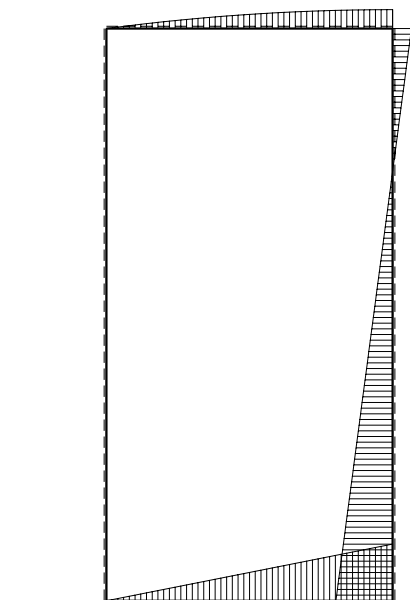




← ⊕ → | 2 F



↑ ⊕ ↓ | 2 F



⊕ ↺ | 2 Fb

## REAZIONI

$$H_A = 0$$

$$V_A = -2F - 1/2qb = -5/2F \quad H_C = F = F$$

$$V_C = 2F - 1/2qb = 3/2F$$

$$N_{DA} = qb = F$$

$$H_{AB} = 0$$

$$V_{AB} = -2F + 1/2qb = -3/2F$$

$$W_{AB} = 0$$

$$H_{BA} = 0$$

$$V_{BA} = 2F - 1/2qb = 3/2F$$

$$W_{BA} = -2Fb + 1/2qb^2 = -3/2Fb$$

$$H_{BC} = -F = -F$$

$$V_{BC} = -2F + 1/2qb = -3/2F$$

$$W_{BC} = 2Fb - 1/2qb^2 = 3/2Fb$$

$$H_{CB} = F = F$$

$$V_{CB} = 2F - 1/2qb = 3/2F$$

$$W_{CB} = 1/2qb^2 = 1/2Fb$$

$$H_{CD} = 0$$

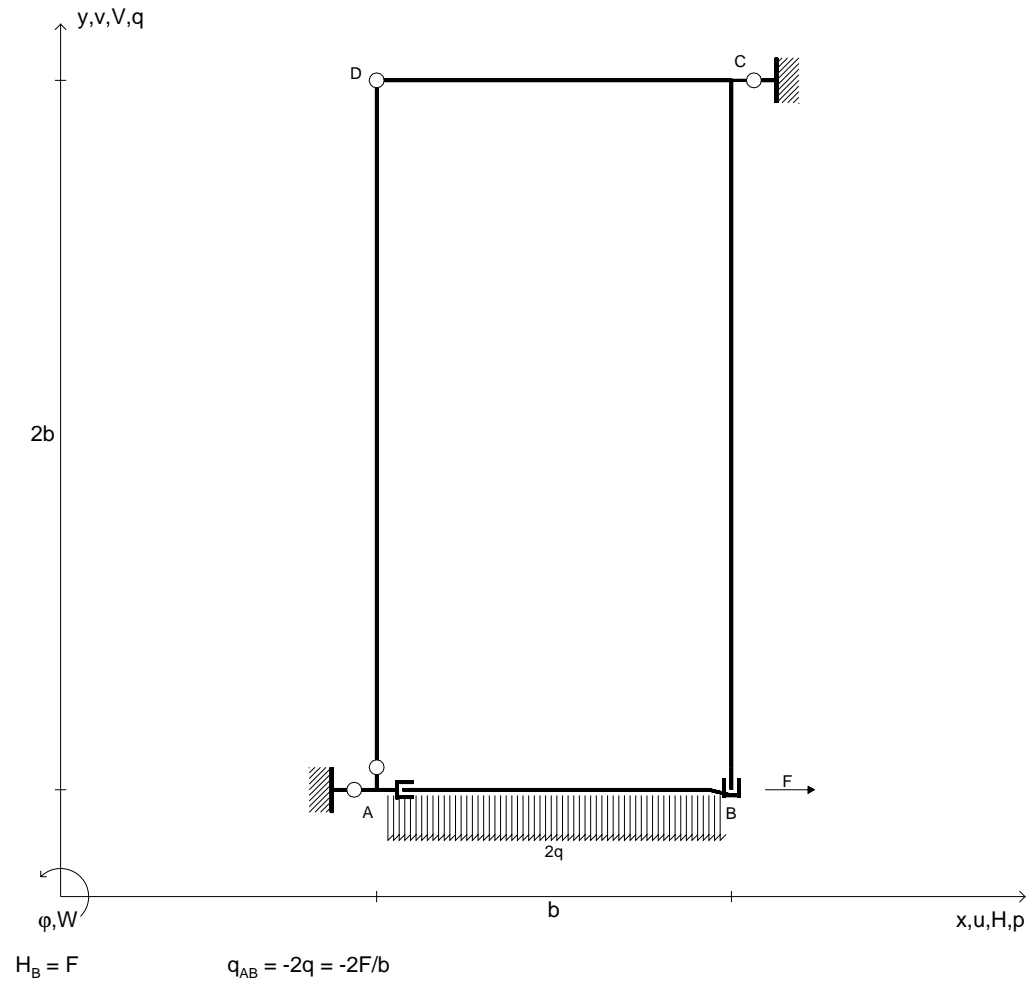
$$V_{CD} = 0$$

$$W_{CD} = -1/2qb^2 = -1/2Fb$$

$$H_{DC} = 0$$

$$V_{DC} = -qb = -F$$

$$W_{DC} = 0$$



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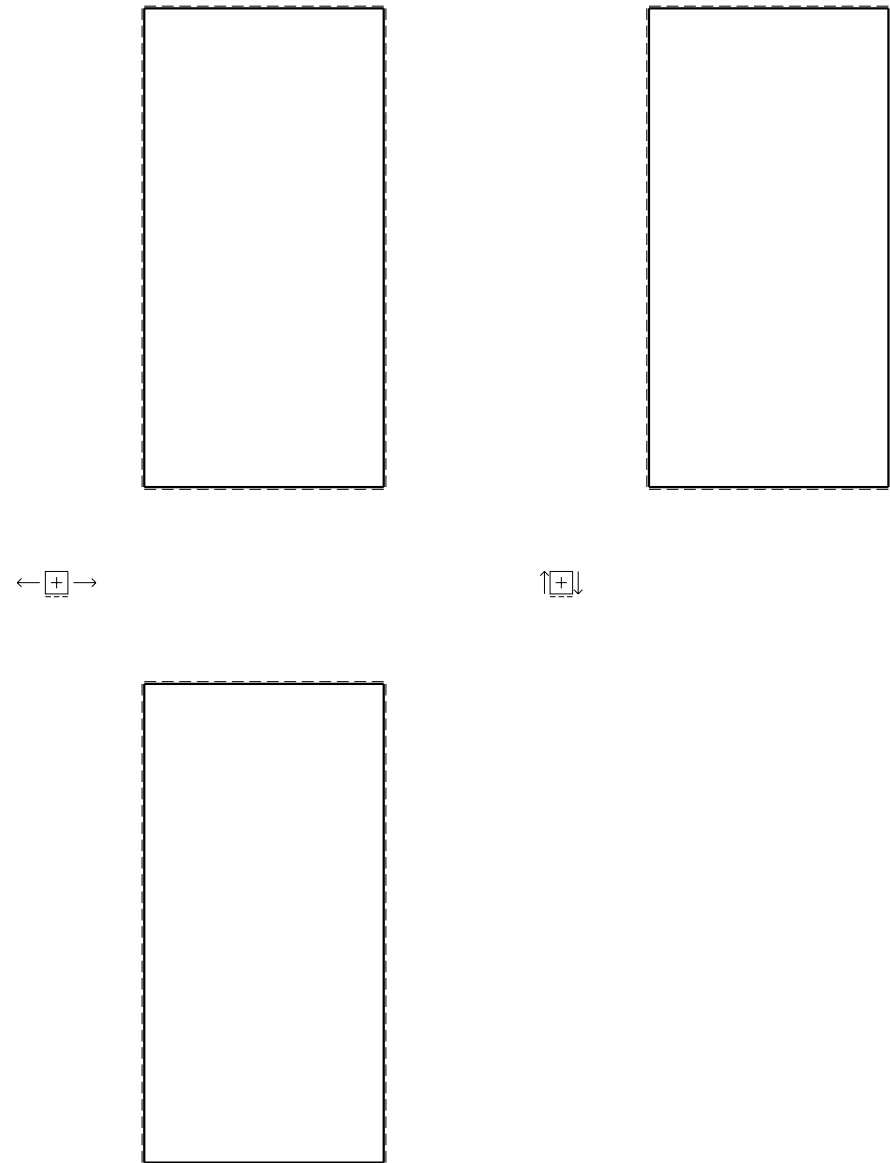
Determinare le azioni interne in C col PLV ( $Le=0$ ).

Carichi e deformazioni date hanno verso efficace in disegno.

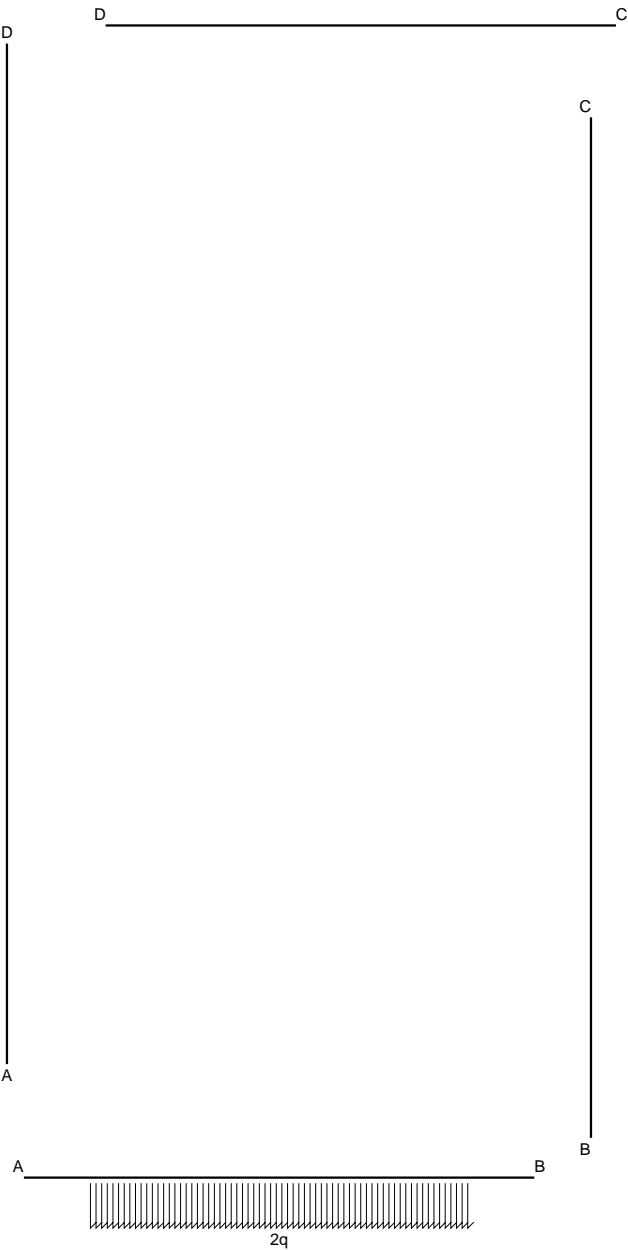
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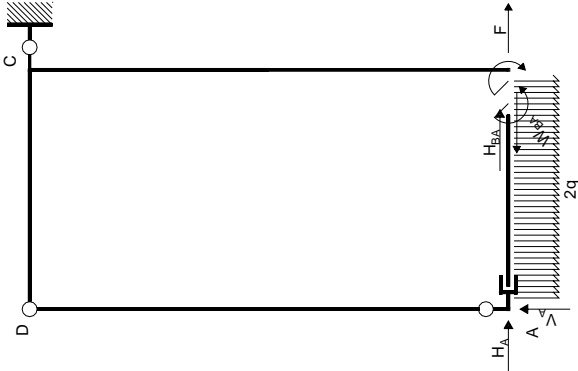


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REAZIONI

$H_A =$	$V_A =$	$H_C =$	$V_C =$
$N_{DA} =$			
$H_{AB} =$	$H_{BC} =$	$H_{CD} =$	
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$	
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$	
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$	
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$	
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$	



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$2H_A b - V_A b = -2Fb - qb^2$

Rotazione intorno a D: aste DA AB

$2H_A b + 2H_{BA} b + W_{BA} = qb^2$

Rotazione intorno a A: aste AB

$W_{BA} = qb^2$

Traslazione orizzontale: aste AB

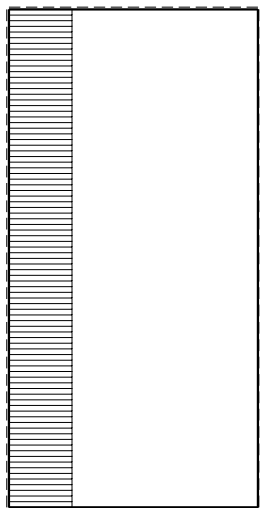
$H_{BA} = 0$

Matrice di equilibrio

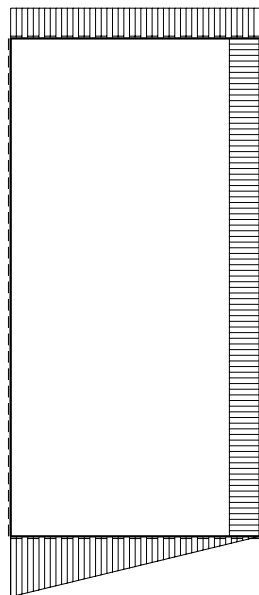
$$\begin{bmatrix} H_A b & V_A b & H_{BA} b & W_{BA} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\varphi_C \begin{bmatrix} 2 & -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -2 & -1 \end{bmatrix}$$
$$\varphi_{DA} \begin{bmatrix} 2 & 0 & 2 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 1 \end{bmatrix}$$
$$\varphi_{AD} \begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 1 \end{bmatrix}$$
$$U_{AB} \begin{bmatrix} 0 & 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 \end{bmatrix}$$

Soluzione del sistema

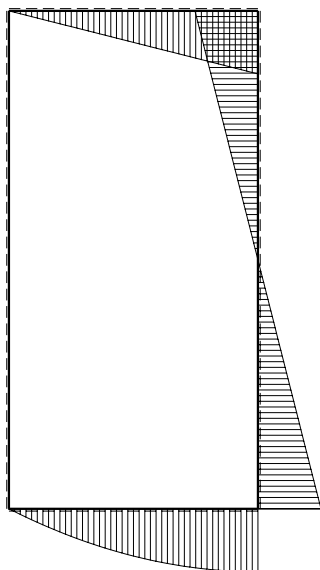
$$\begin{bmatrix} H_A b \\ V_A b \\ W_{BA} \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\begin{bmatrix} 0 & 0 \\ 2 & 1 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$$



← ⊕ → | 1.2 F



↑ ⊕ ↓ | 2.5 F



↺ ⊕ ↻ | 1.2 Fb

## REAZIONI

$$H_A = 0 \quad V_A = 2F + qb = 3F \quad H_C = -F = -F \quad V_C = -2F + qb = -F$$

$$N_{DA} = -2F + qb = -F$$

$$H_{AB} = 0$$

$$V_{AB} = 2qb = 2F$$

$$W_{AB} = 0$$

$$H_{BA} = 0$$

$$V_{BA} = 0$$

$$W_{BA} = qb^2 = Fb$$

$$H_{BC} = F = F$$

$$V_{BC} = 0$$

$$W_{BC} = -qb^2 = -Fb$$

$$H_{CB} = -F = -F$$

$$V_{CB} = 0$$

$$W_{CB} = -2Fb + qb^2 = -Fb$$

$$H_{CD} = 0$$

$$V_{CD} = -2F + qb = -F$$

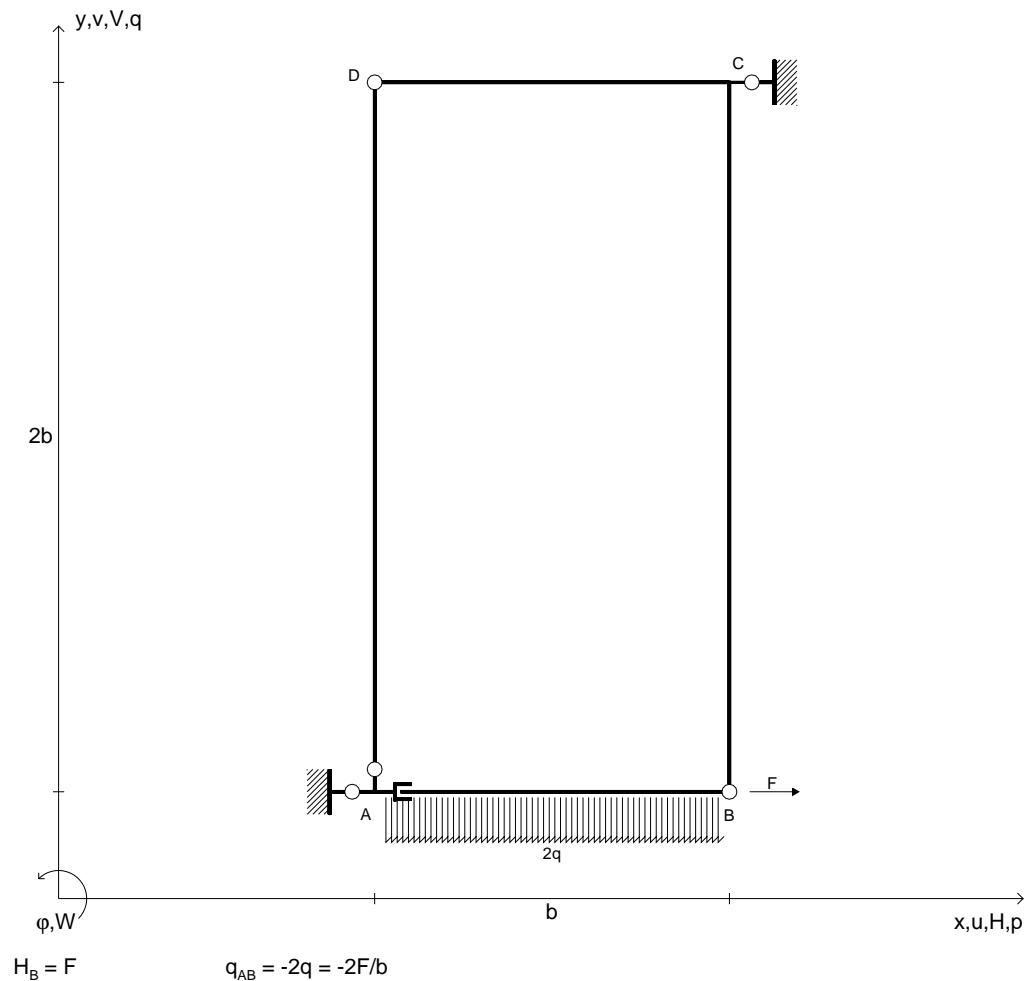
$$W_{CD} = 2Fb - qb^2 = Fb$$

$$H_{DC} = 0$$

$$V_{DC} = 2F - qb = F$$

$$W_{DC} = 0$$





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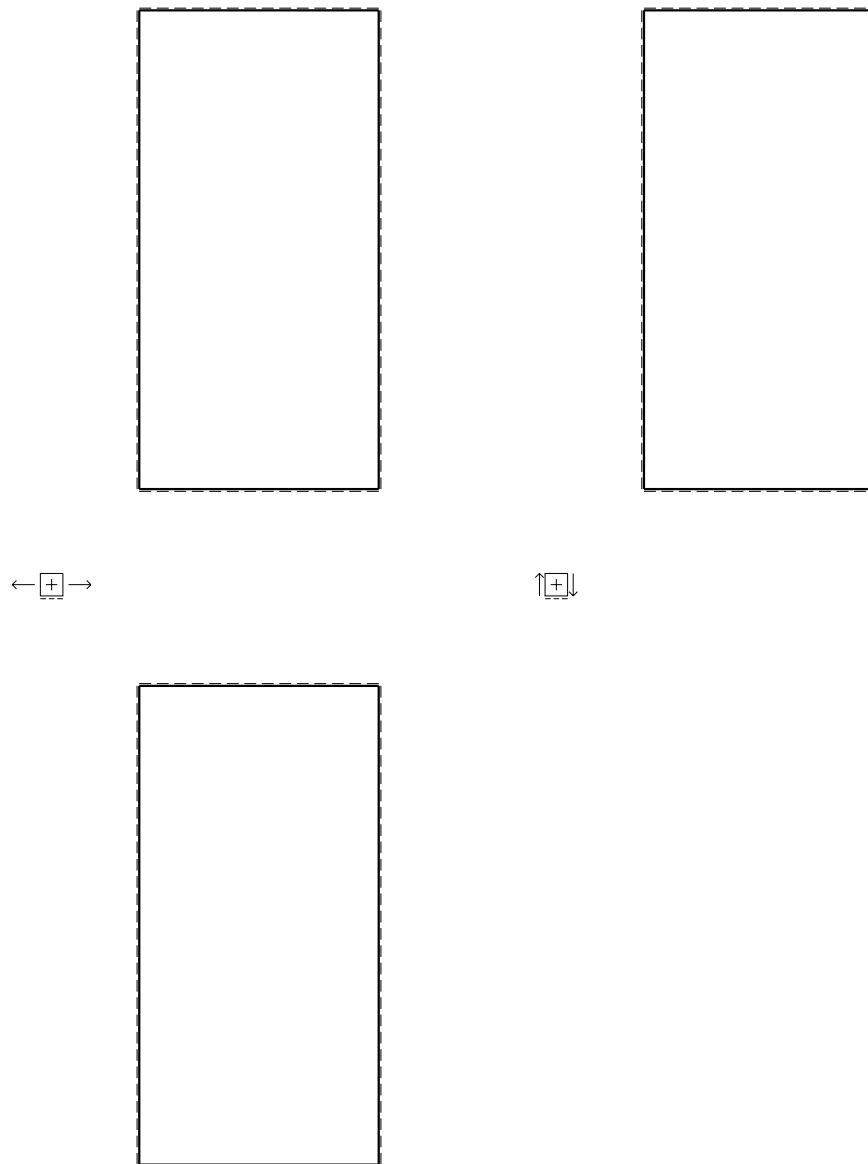
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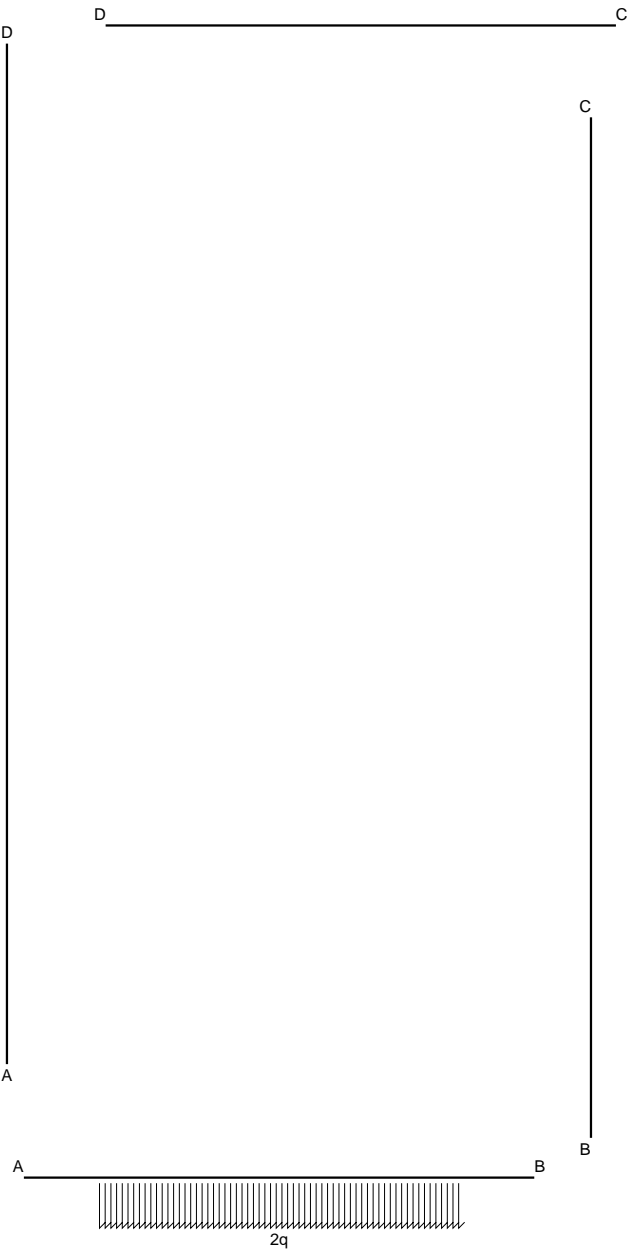
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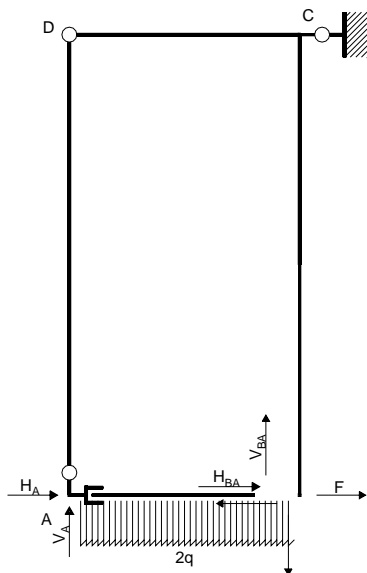
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REAZIONI			
$H_A =$	$V_A =$	$H_C =$	$V_C =$
$N_{DA} =$			
$H_{AB} =$	$H_{BC} =$	$H_{CD} =$	
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$	
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$	
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$	
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$	
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$	



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Rotazione globale intorno a C

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Rotazione intorno a D: aste DA AB

$$2H_A b + 2H_{BA} b + V_{BA} b = qb^2$$

Rotazione intorno a A: aste AB

$$V_{BA} b = qb^2$$

Traslazione orizzontale: aste AB

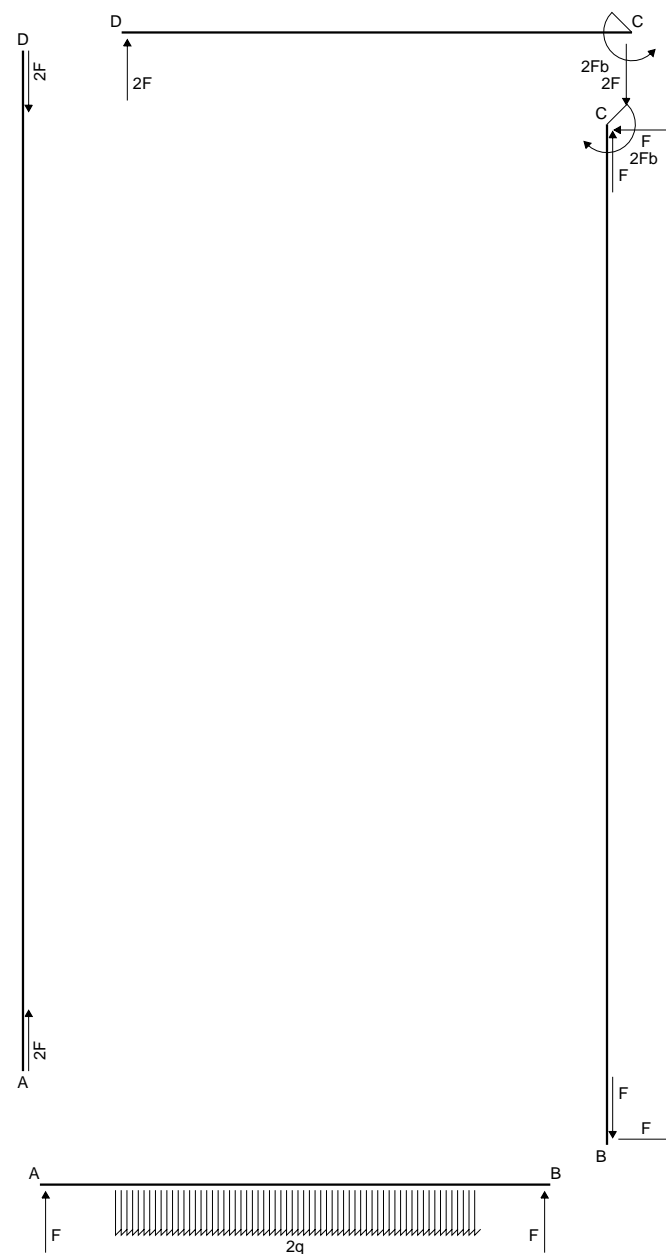
$$H_{BA} = 0$$

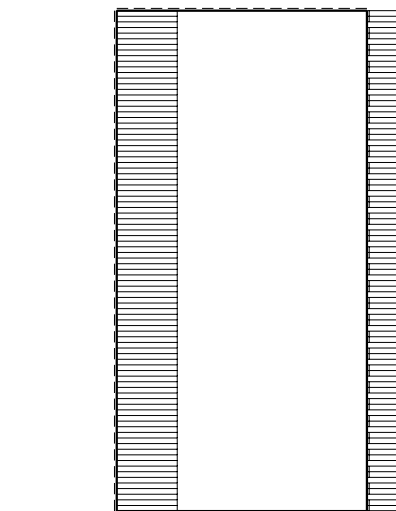
## Matrice di equilibrio

$$\begin{bmatrix} \varphi_C \\ \varphi_{DA} \\ \varphi_{AD} \\ u_{AB} \end{bmatrix} \begin{bmatrix} H_A b & V_A b & H_{BA} b & V_{BA} b \\ 2 & -1 & 0 & 0 \\ 2 & 0 & 2 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & -1 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$$

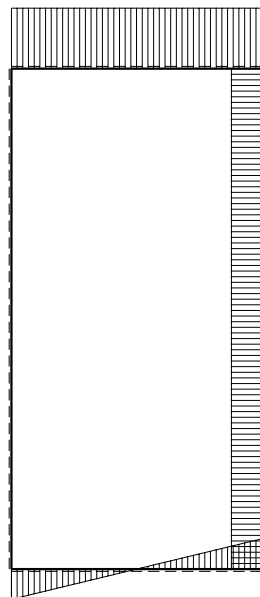
## Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \\ V_{BA} b \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 0 \\ 2 & 1 \\ 0 & 0 \end{bmatrix}$$

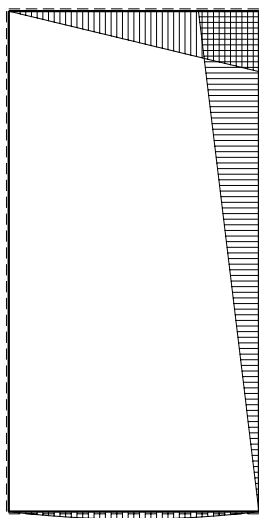




← ⊕ → | 2.5 F



↑ ⊕ ↓ | 2.5 F



↺ ⊕ ↻ | 2.5 Fb

## REAZIONI

$$H_A = 0$$

$$V_A = 2F + qb = 3F$$

$$H_C = -F = -F$$

$$V_C = -2F + qb = -F$$

$$N_{DA} = -2F = -2F$$

$$H_{AB} = 0$$

$$V_{AB} = qb = F$$

$$W_{AB} = 0$$

$$H_{BA} = 0$$

$$V_{BA} = qb = F$$

$$W_{BA} = 0$$

$$H_{BC} = F = F$$

$$V_{BC} = -qb = -F$$

$$W_{BC} = 0$$

$$H_{CB} = -F = -F$$

$$V_{CB} = qb = F$$

$$W_{CB} = -2Fb = -2Fb$$

$$H_{CD} = 0$$

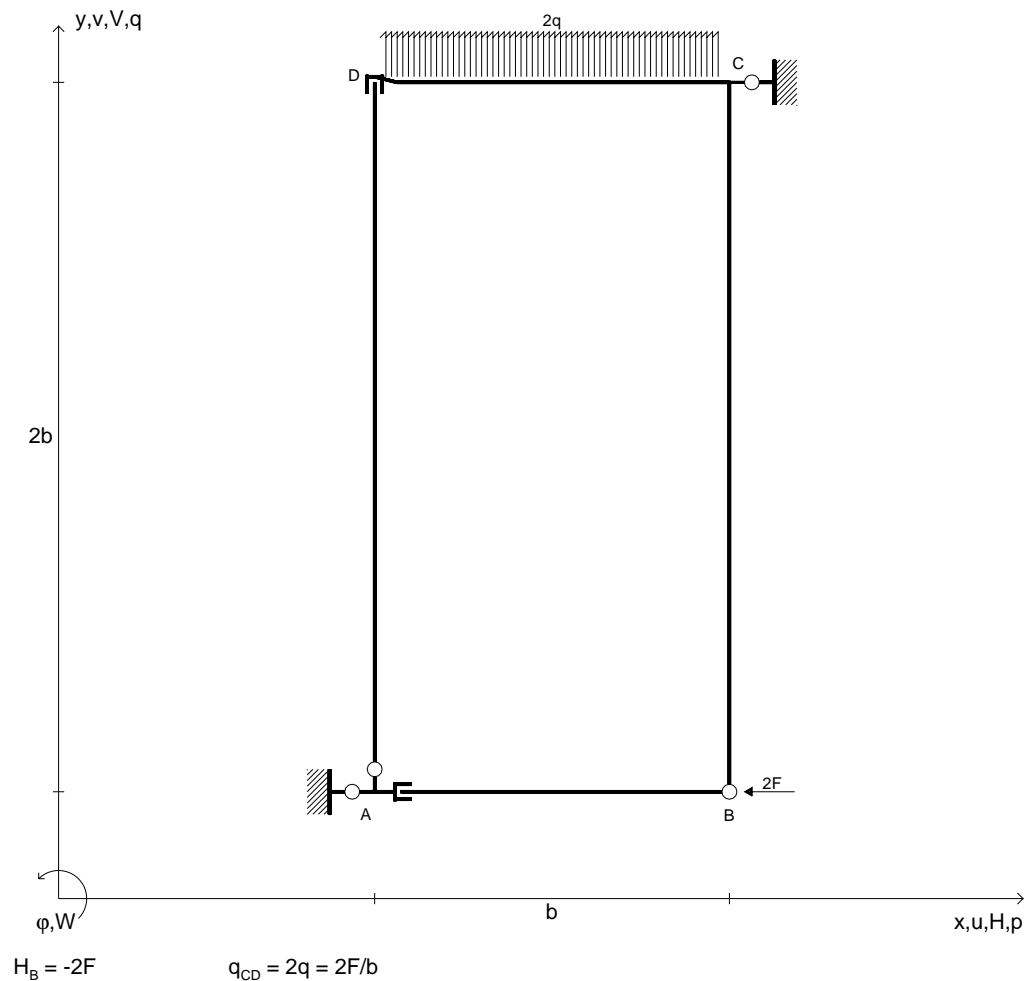
$$V_{CD} = -2F = -2F$$

$$W_{CD} = 2Fb = 2Fb$$

$$H_{DC} = 0$$

$$V_{DC} = 2F = 2F$$

$$W_{DC} = 0$$



Svolgere l'analisi cinematica.

Determinare matrice di congruenza e di equilibrio.

Determinare le reazioni vincolari a terra col PLV ( $Le=0$ ).

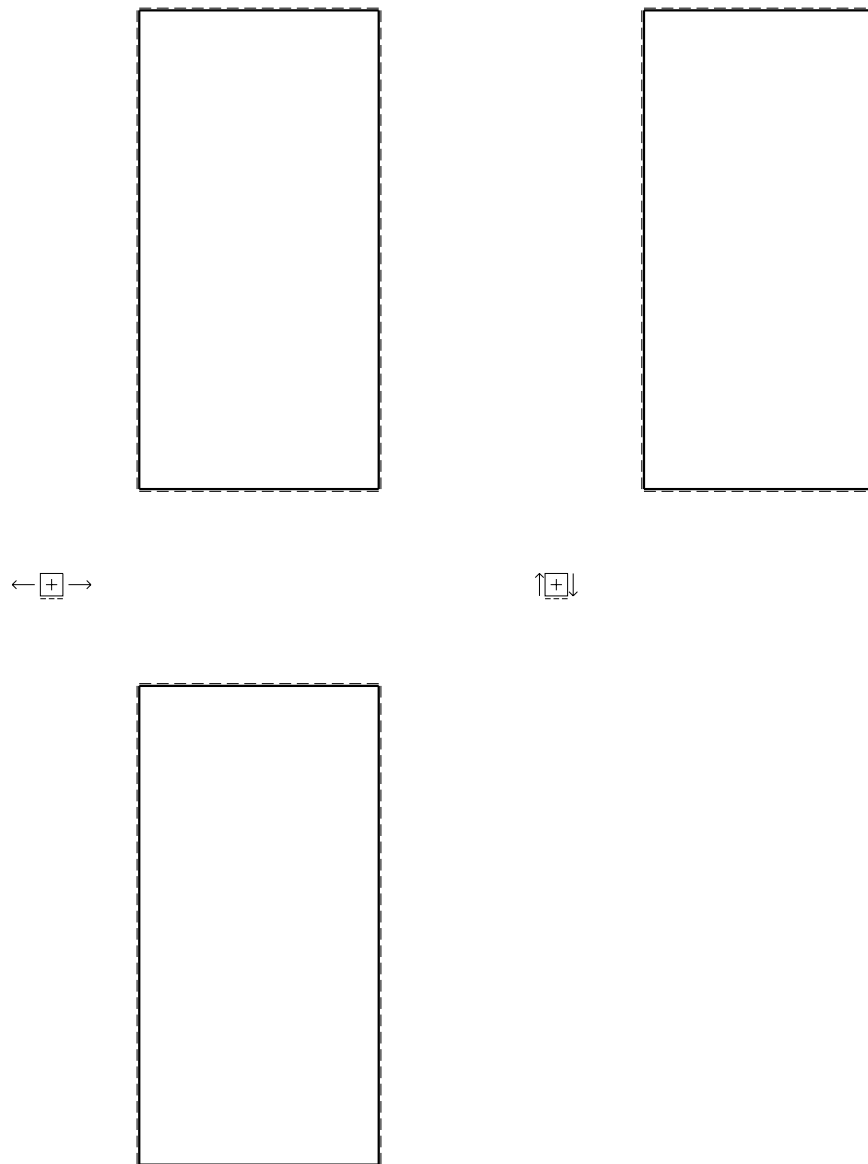
Determinare le azioni interne in C col PLV ( $Le=0$ ).

Carichi e deformazioni date hanno verso efficace in disegno.

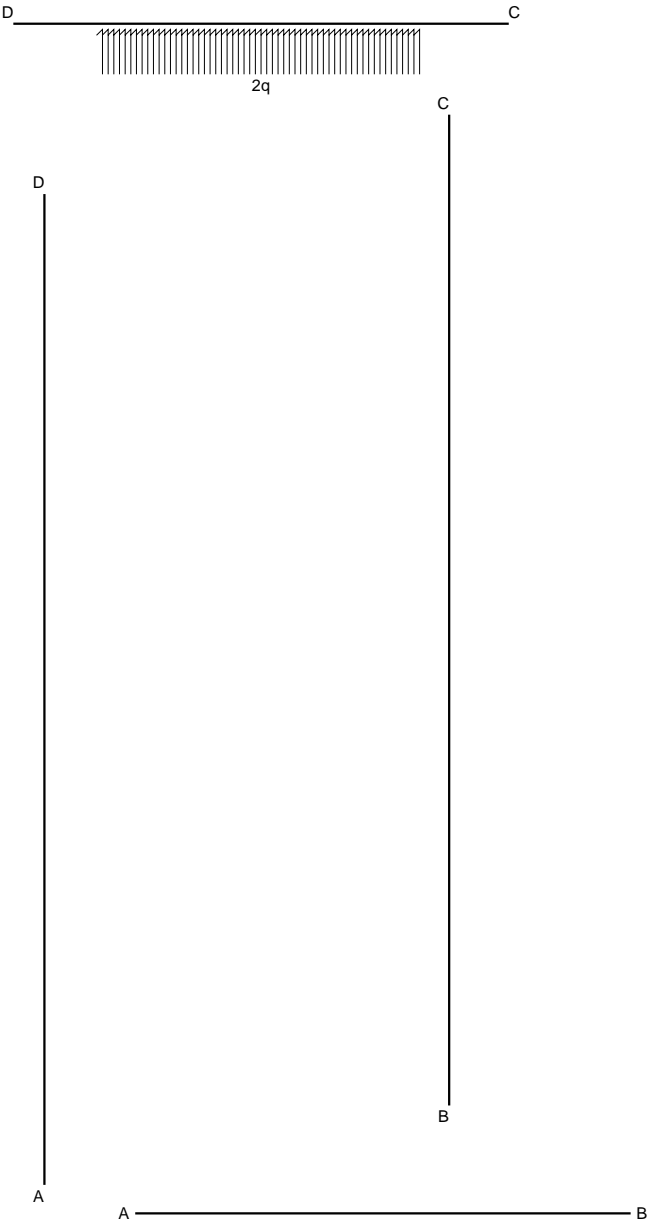
Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

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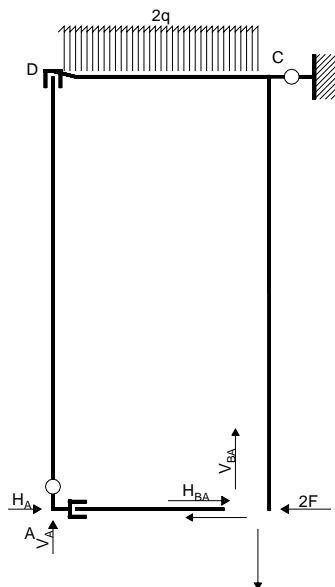


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REAZIONI

$H_A =$	$V_A =$	$H_C =$	$V_C =$
$H_{AB} =$	$H_{BC} =$	$H_{CD} =$	
$V_{AB} =$	$V_{BC} =$	$V_{CD} =$	
$W_{AB} =$	$W_{BC} =$	$W_{CD} =$	
$H_{BA} =$	$H_{CB} =$	$H_{DC} =$	
$V_{BA} =$	$V_{CB} =$	$V_{DC} =$	
$W_{BA} =$	$W_{CB} =$	$W_{DC} =$	
$H_{DA} =$			
$V_{DA} =$			
$W_{DA} =$			
$H_{AD} =$			
$V_{AD} =$			
$W_{AD} =$			



## EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a C

$$2H_A b - V_A b = 4Fb + qb^2$$

Traslazione verticale: aste DA AB

$$V_A + V_{BA} = 0$$

Rotazione intorno a A: aste AB

$$V_{BA} b = 0$$

Traslazione orizzontale: aste AB

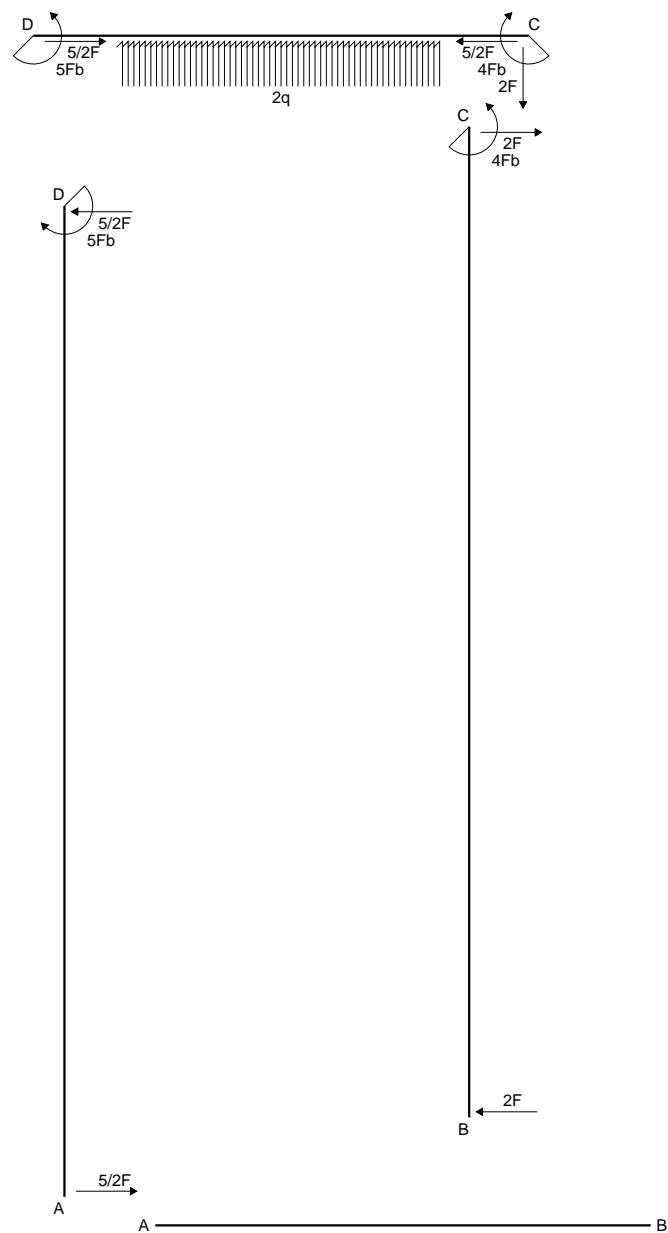
$$H_{BA} = 0$$

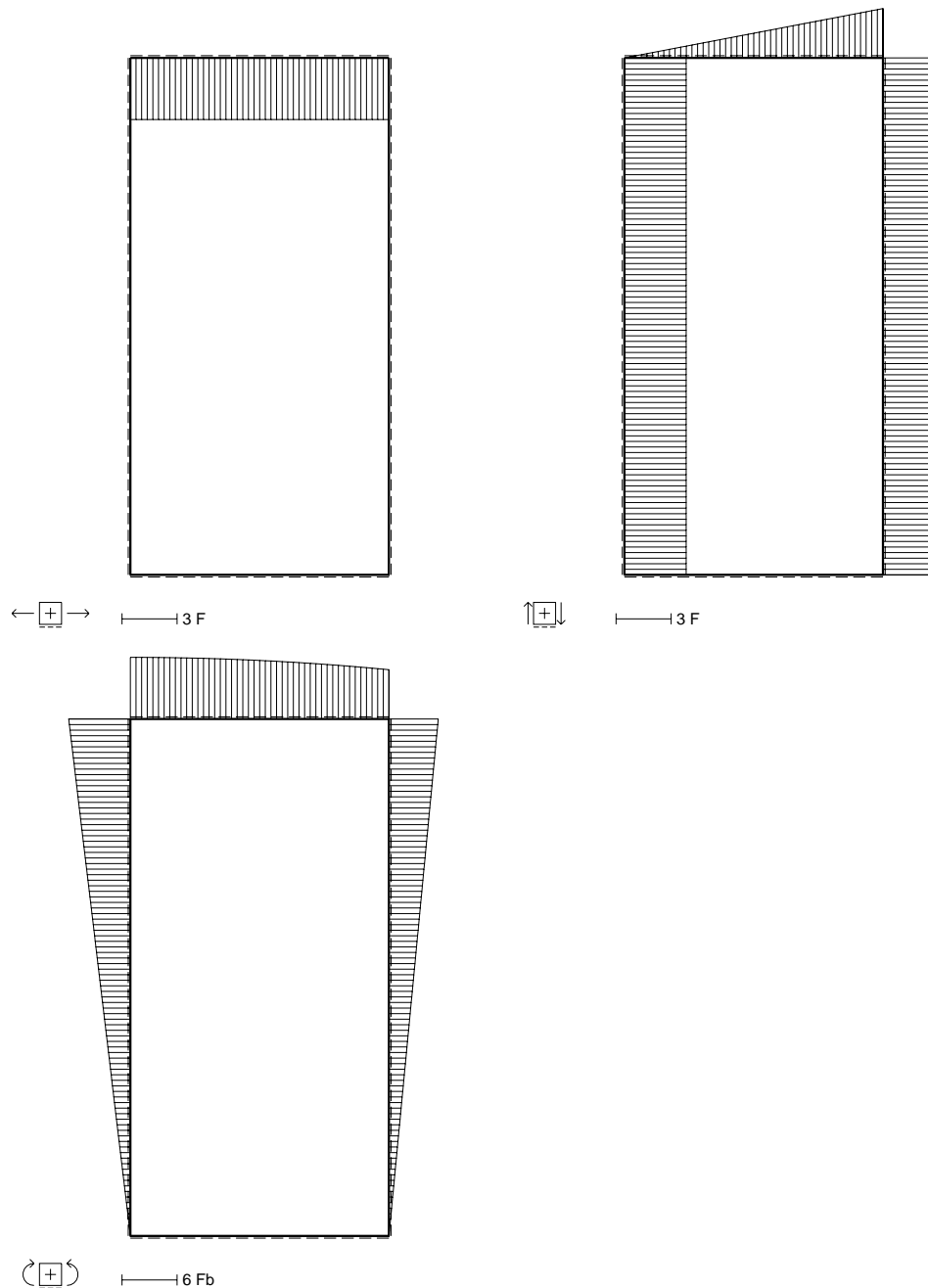
## Matrice di equilibrio

$$\begin{bmatrix} \varphi_C \\ V_{DC} \\ \varphi_{AD} \\ u_{AB} \end{bmatrix} \begin{bmatrix} H_A b & V_A b & H_{BA} b & V_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

## Soluzione del sistema

$$\begin{bmatrix} H_A b \\ V_A b \\ V_{BA} b \\ H_{BA} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & 1/2 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$





## REAZIONI

$$H_A = 2F + 1/2qb = 5/2F \quad V_A = 0$$

$$H_C = -1/2qb = -1/2F \quad V_C = -2qb = -2F$$

$$H_{AB} = 0$$

$$H_{BC} = -2F = -2F$$

$$H_{CD} = -2F - 1/2qb = -5/2F$$

$$V_{AB} = 0$$

$$V_{BC} = 0$$

$$V_{CD} = -2qb = -2F$$

$$W_{AB} = 0$$

$$W_{BC} = 0$$

$$W_{CD} = -4Fb = -4Fb$$

$$H_{BA} = 0$$

$$H_{CB} = 2F = 2F$$

$$H_{DC} = 2F + 1/2qb = 5/2F$$

$$V_{BA} = 0$$

$$V_{CB} = 0$$

$$V_{DC} = 0$$

$$W_{BA} = 0$$

$$W_{CB} = 4Fb = 4Fb$$

$$W_{DC} = 4Fb + qb^2 = 5Fb$$

$$H_{DA} = -2F - 1/2qb = -5/2F$$

$$V_{DA} = 0$$

$$W_{DA} = -4Fb - qb^2 = -5Fb$$

$$H_{AD} = 2F + 1/2qb = 5/2F$$

$$V_{AD} = 0$$

$$W_{AD} = 0$$