

Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

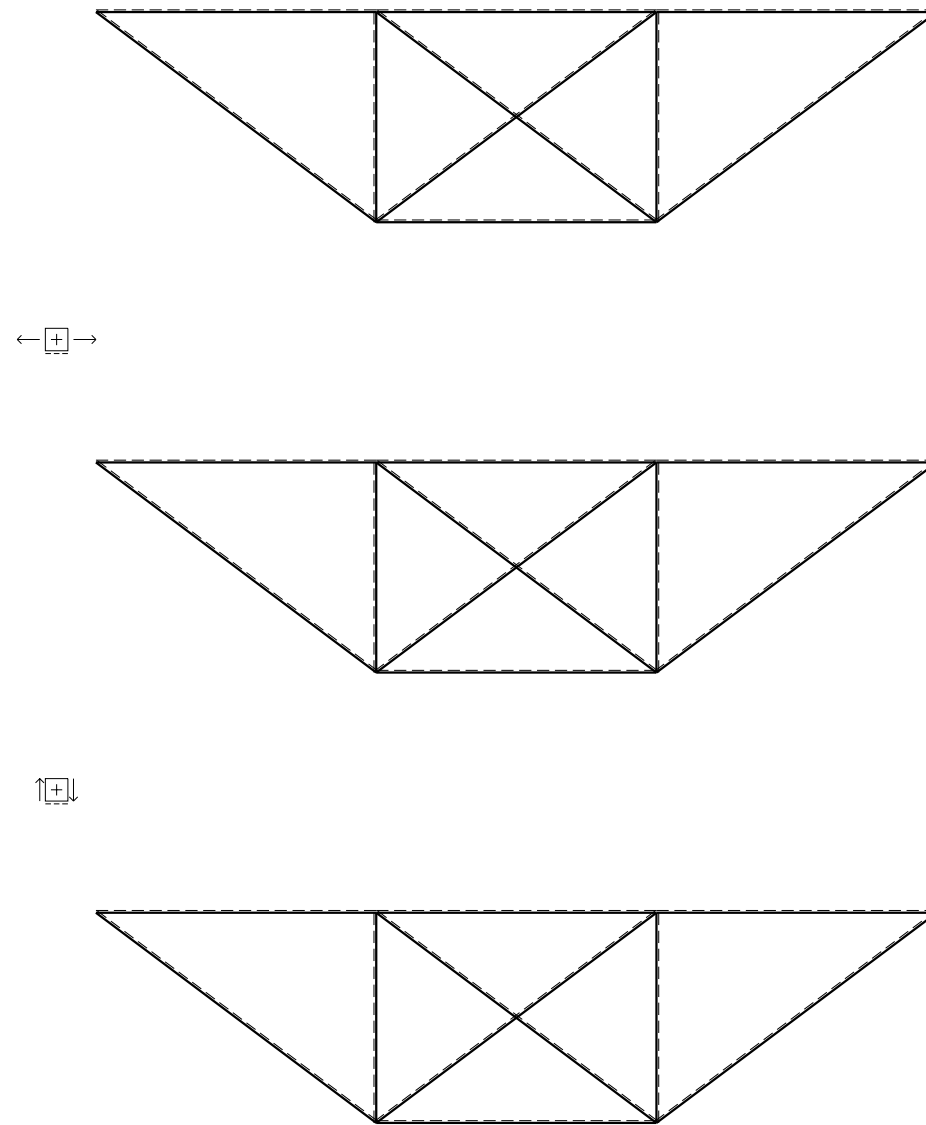
Tracciare i diagrammi delle azioni interne nelle aste.

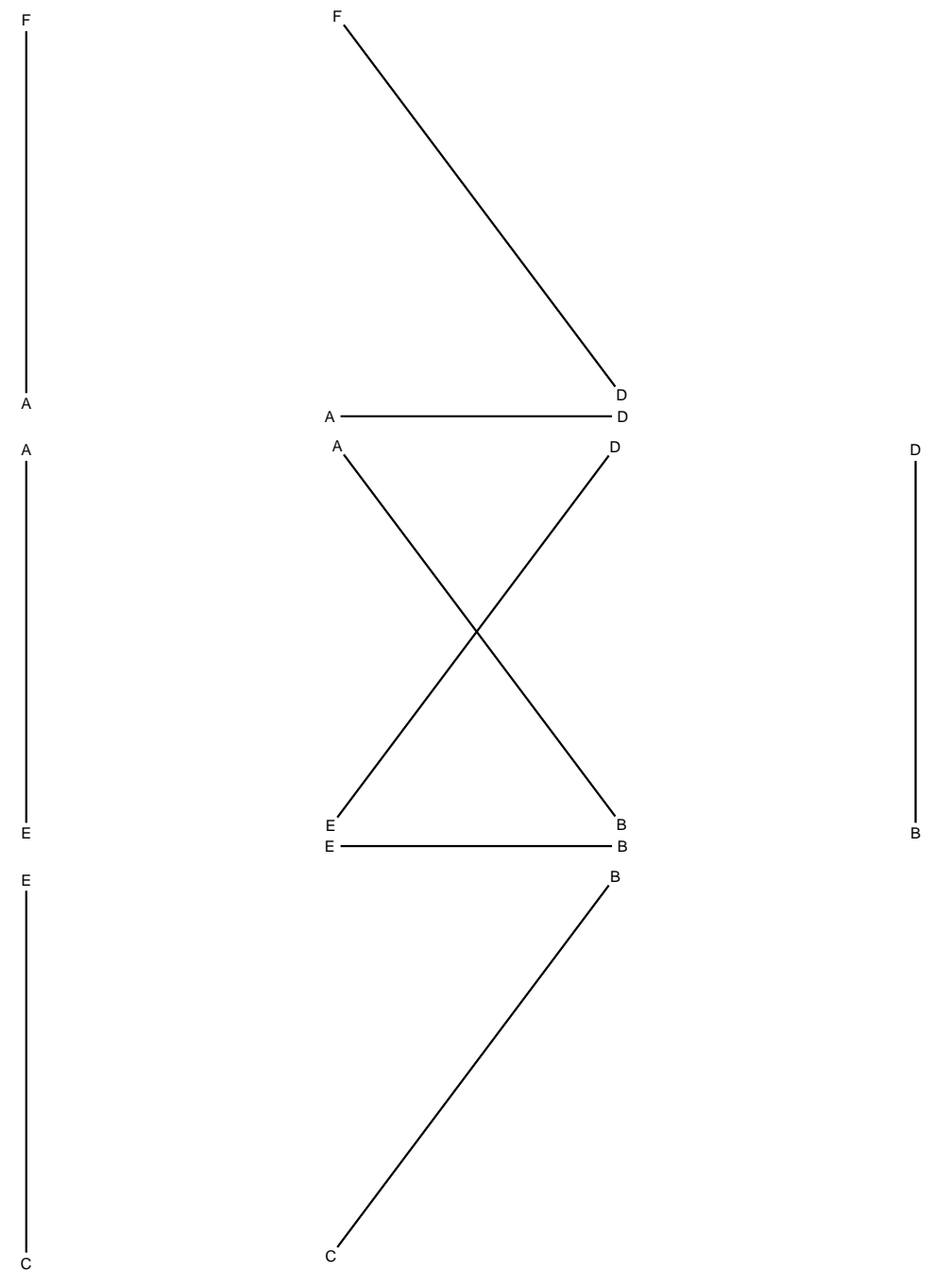
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo E

Calcolare lo spostamento verticale del nodo E

@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_C =$        $V_C =$        $H_F =$        $V_F =$

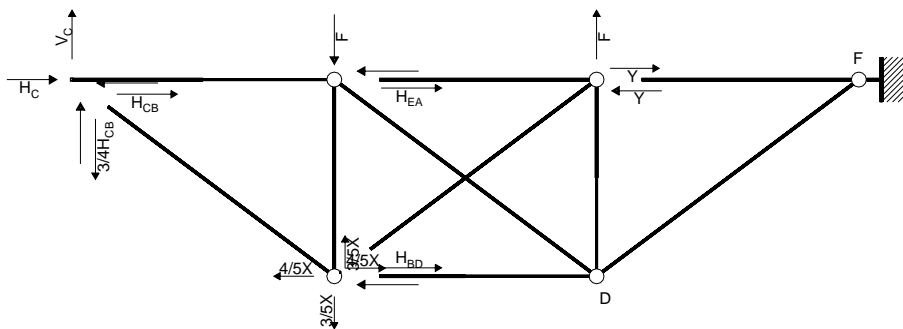
$N_{AB} =$        $N_{BC} =$        $N_{DB} =$        $N_{DA} =$        $N_{EB} =$        $N_{FA} =$        $N_{AE} =$

$N_{EC} =$        $N_{FD} =$        $N_{DE} =$

SPOSTAMENTI ASSOLUTI

$u_E =$

$v_E =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DB DA DE AB EB AE EC BC

$$-12V_C b = -4Fb$$

Rotazione intorno a D: aste DA AB AE

$$-3H_{EA} b = 12/5 X b - 3Y b$$

Rotazione intorno a D: aste DE EB EC BC

$$-3H_C b - 8V_C b + 3H_{EA} b = -12/5 X b - 4Fb$$

Rotazione intorno a E: aste EB BC

$$3H_{CB} b - 3H_{BD} b = 12/5 X b$$

Rotazione intorno a E: aste EC

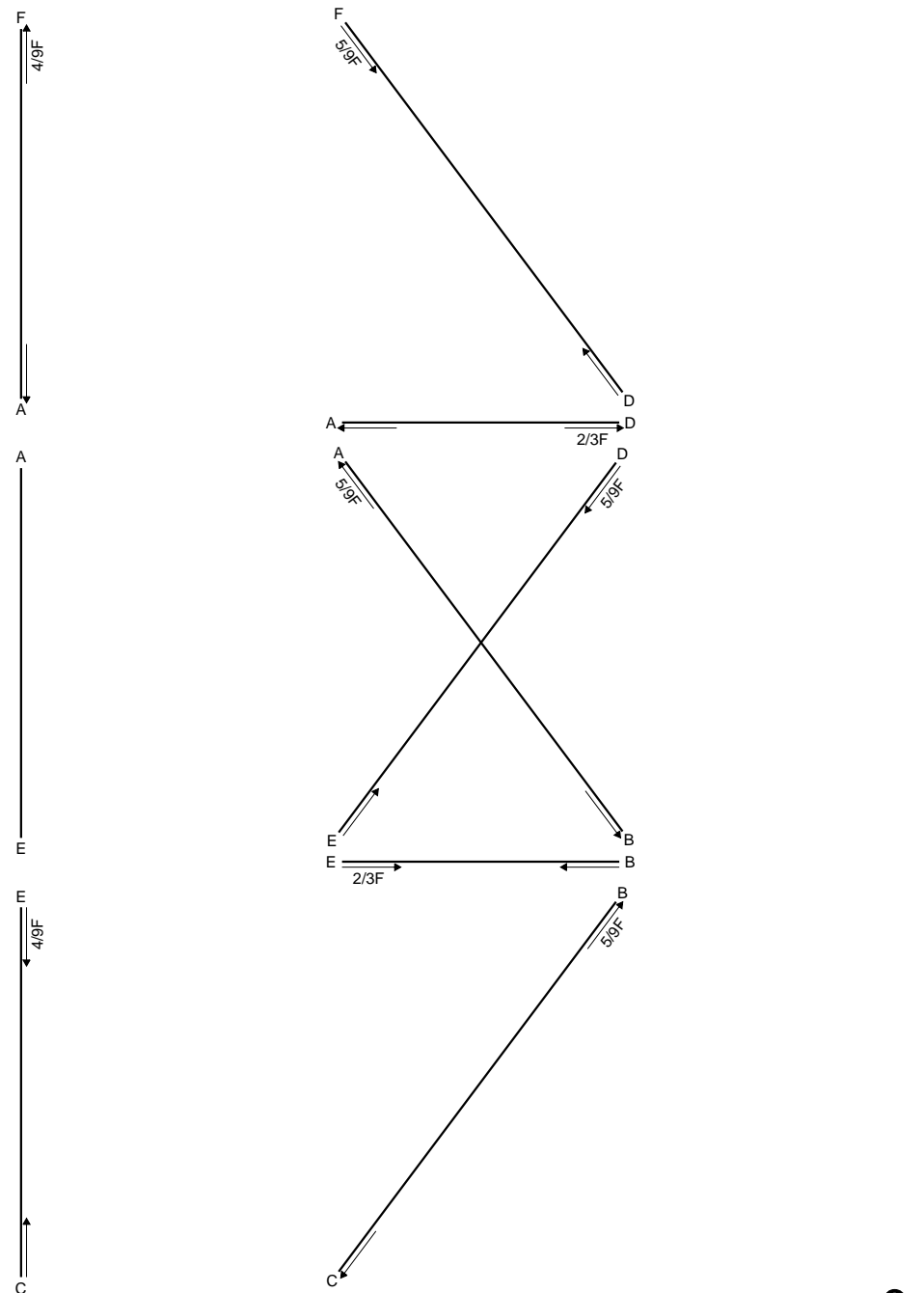
$$-4V_C b - 3H_{CB} b = 0$$

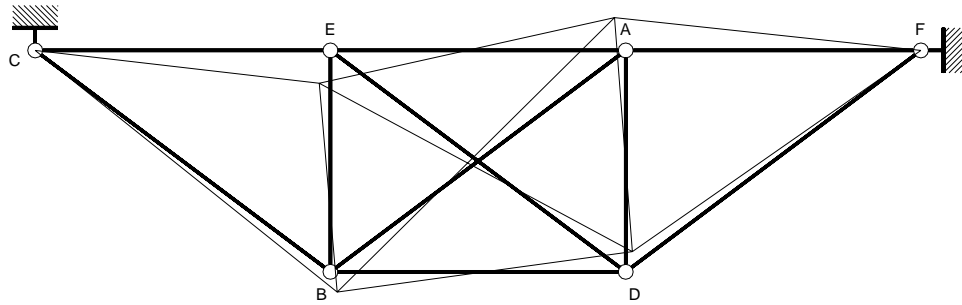
Matrice di equilibrio

$$\begin{bmatrix} H_C b & V_C b & H_{CB} b & H_{BD} b & H_{EA} b \\ \phi_{FD} & 0 & -12 & 0 & 0 & 0 \\ \phi_{DA} & 0 & 0 & 0 & 0 & -3 \\ \phi_{DE} & -3 & -8 & 0 & 0 & 3 \\ \phi_{EB} & 0 & 0 & 3 & -3 & 0 \\ \phi_{EC} & 0 & -4 & -3 & 0 & 0 \end{bmatrix} = \begin{bmatrix} X b & Y b & F b \\ 0 & 0 & -4 \\ 12/5 & -3 & 0 \\ -12/5 & 0 & -4 \\ 12/5 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

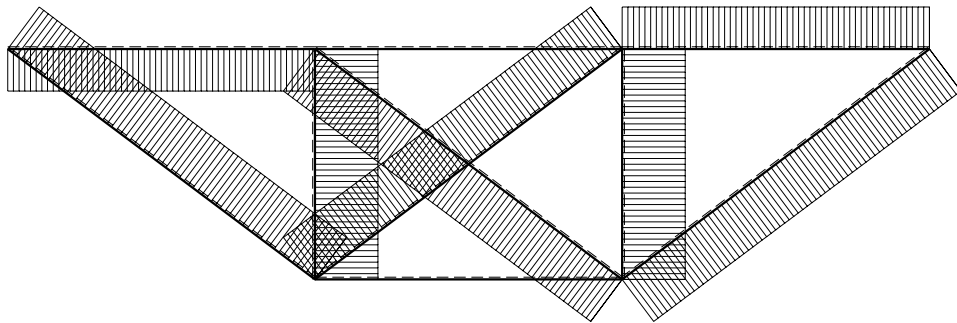
Soluzione del sistema

$$\begin{bmatrix} V_C b \\ H_{EA} b \\ H_C b \\ H_{BD} b \\ H_{CB} b \end{bmatrix} = \begin{bmatrix} X b & Y b & F b \\ 0 & 0 & 1/3 \\ -4/5 & 1 & 0 \\ 0 & 1 & 4/9 \\ -4/5 & 0 & -4/9 \\ 0 & 0 & -4/9 \end{bmatrix}$$





12 Fb/EA



← ⊕ → 0.8 F

## REAZIONI

$$H_C = 0 \quad V_C = 1/3F \quad H_F = 0 \quad V_F = -1/3F$$

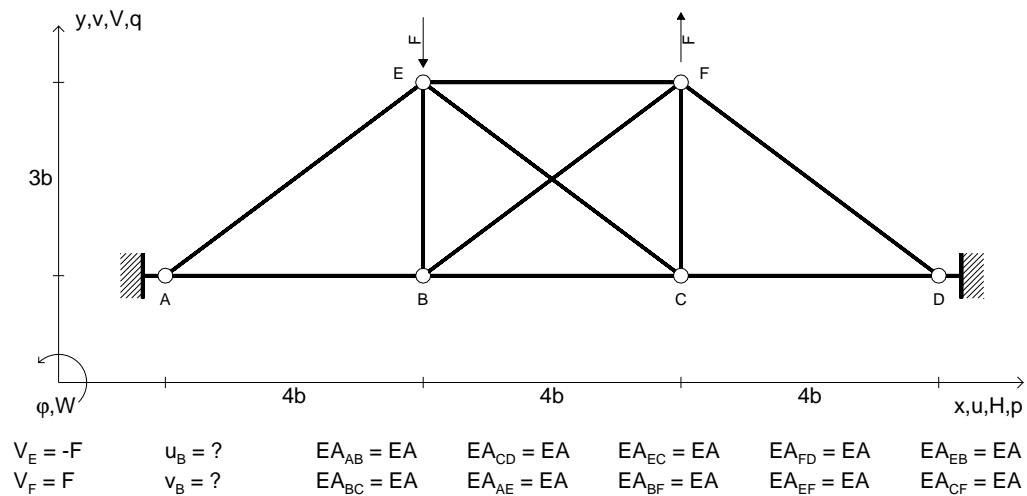
$$N_{AB} = 5/9F \quad N_{BC} = 5/9F \quad N_{DB} = 0 \quad N_{DA} = 2/3F \quad N_{EB} = -2/3F \quad N_{FA} = 4/9F \quad N_{AE} = 0$$

$$N_{EC} = -4/9F \quad N_{FD} = -5/9F \quad N_{DE} = -5/9F$$

## SPOSTAMENTI ASSOLUTI

$$u_E = -16/9(Fb/EA)$$

$$v_E = -422/81(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

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Calcolare reazioni vincolari della struttura e delle aste.

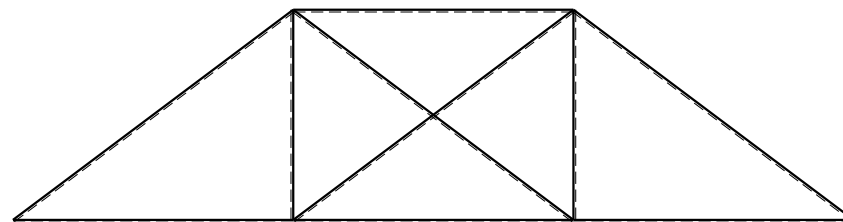
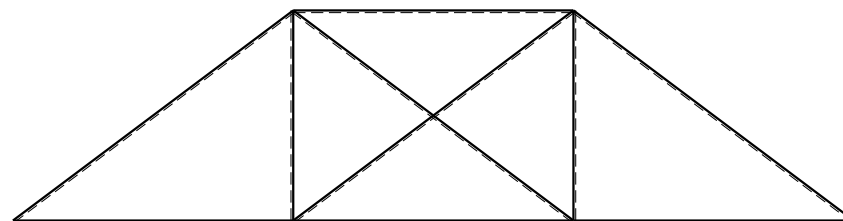
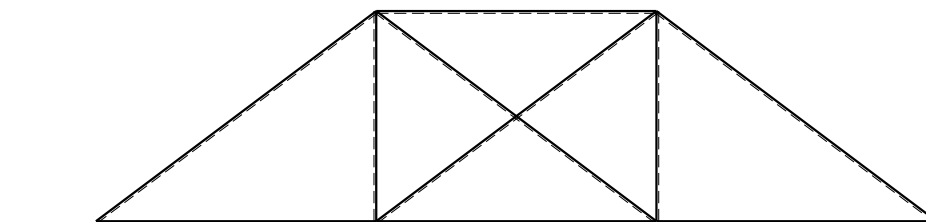
Tracciare i diagrammi delle azioni interne nelle aste.

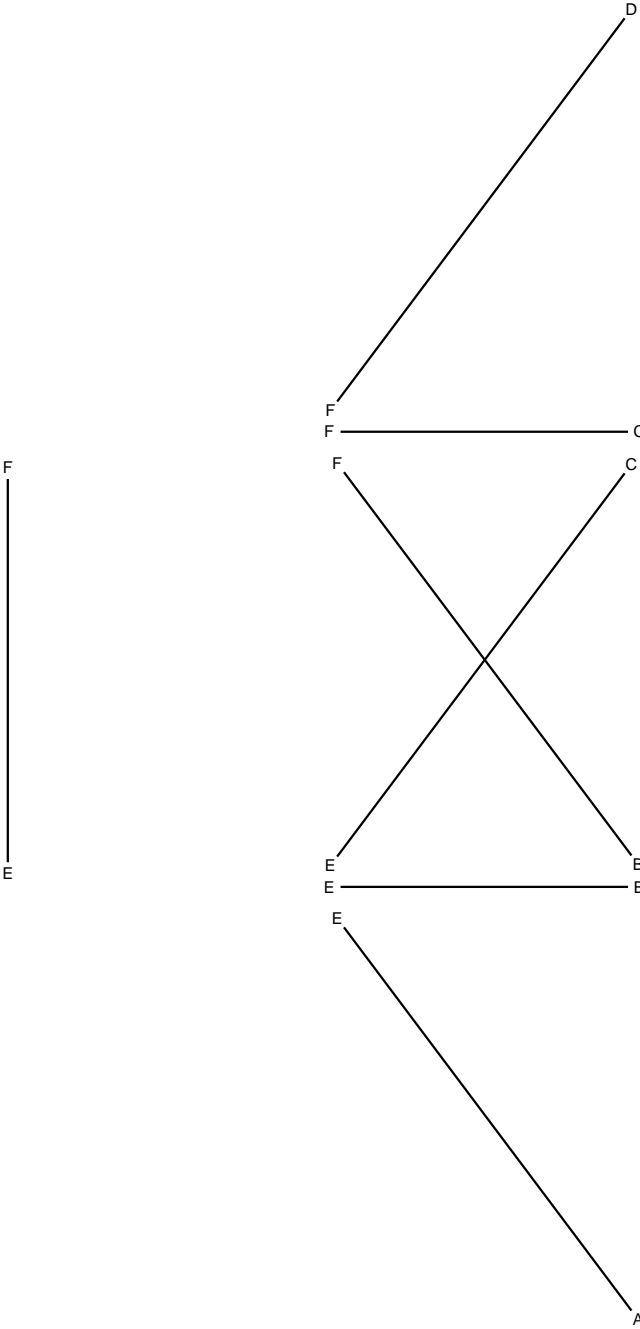
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo B

Calcolare lo spostamento verticale del nodo B

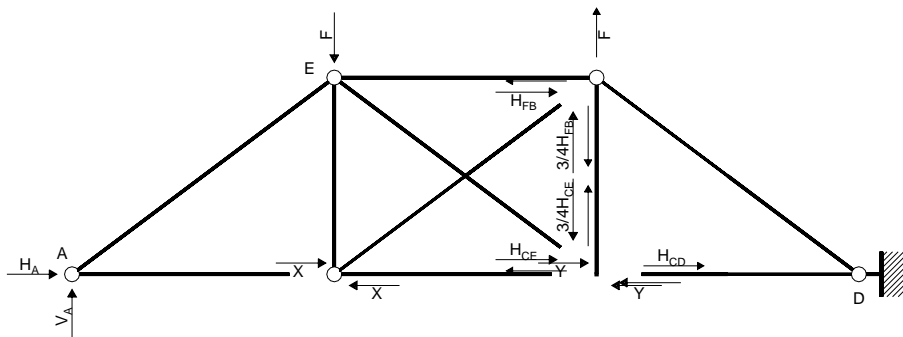
@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI  
 $H_A =$        $V_A =$        $H_D =$        $V_D =$   
 $N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{AE} =$        $N_{EC} =$        $N_{BF} =$        $N_{FD} =$   
 $N_{EF} =$        $N_{EB} =$        $N_{CF} =$

SPOSTAMENTI ASSOLUTI  
 $u_B =$   
 $v_B =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a D: aste DF FE FC EA EC EB AB BC BF

$$-12V_A b = -4Fb$$

Rotazione intorno a F: aste FE EA EC EB AB BC BF

$$3H_A b - 8V_A b + 3H_{CE} b = -3Yb - 4Fb$$

Rotazione intorno a F: aste FC

$$-3H_{CD} b - 3H_{CE} b = 3Yb$$

Rotazione intorno a E: aste EA AB

$$3H_A b - 4V_A b = -3Xb$$

Rotazione intorno a E: aste EB BC BF

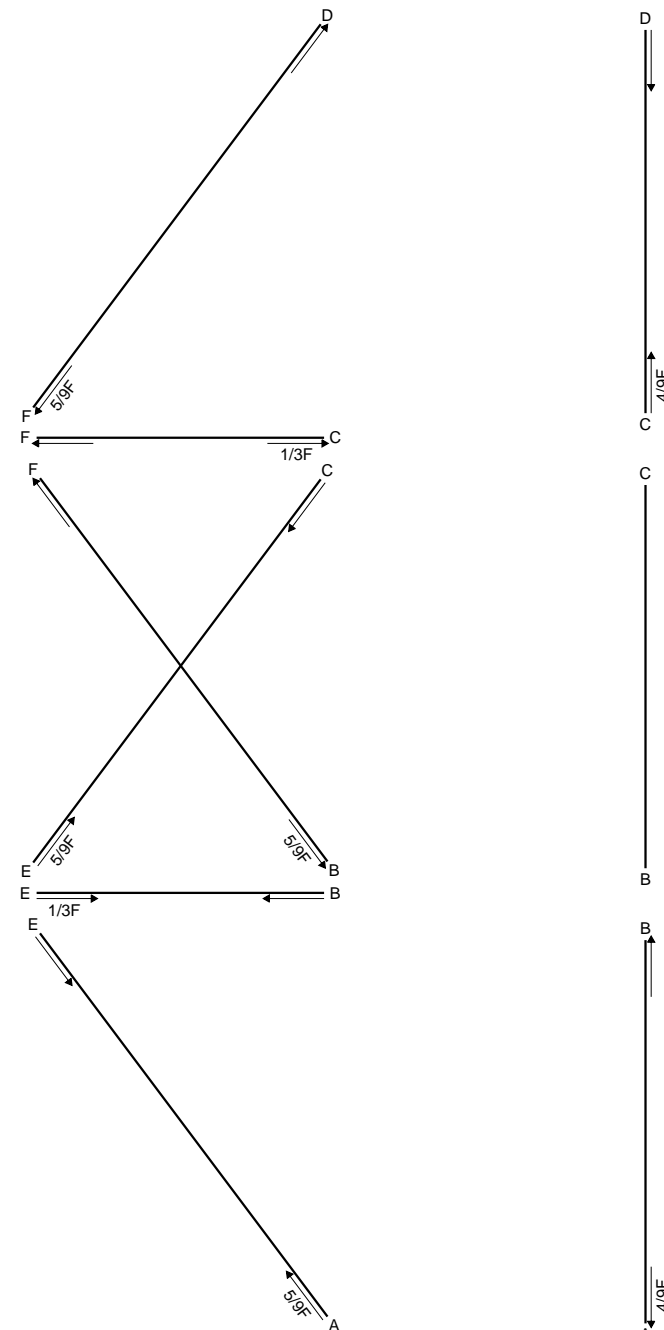
$$3H_{FB} b = 3Xb - 3Yb$$

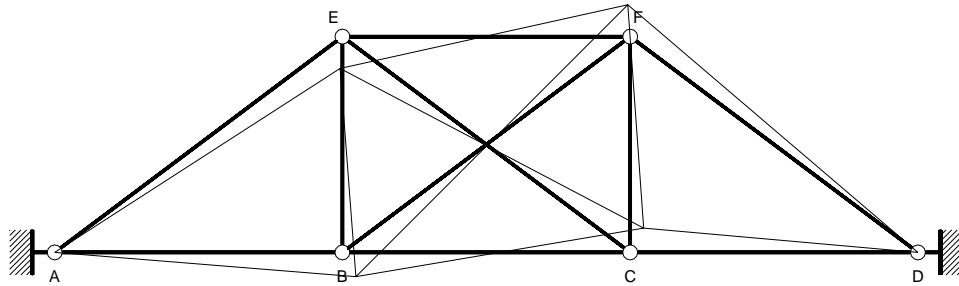
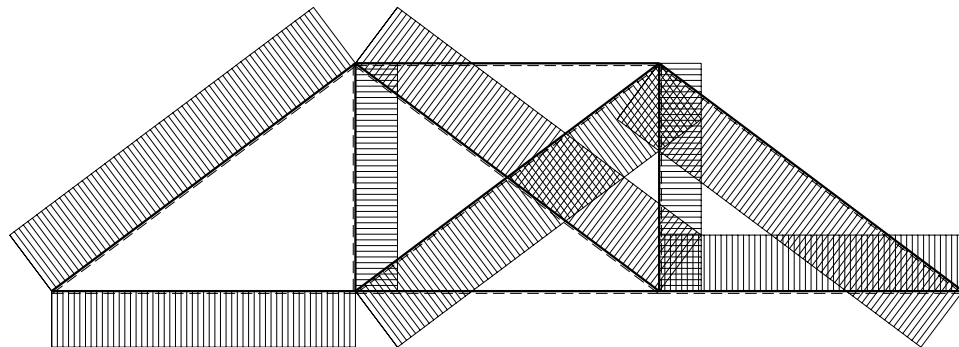
Matrice di equilibrio

$$\begin{bmatrix} H_A b & V_A b & H_{CD} b & H_{CE} b & H_{FB} b \\ \phi_{DF} & 0 & -12 & 0 & 0 & 0 \\ \phi_{FE} & 3 & -8 & 0 & 3 & 0 \\ \phi_{FC} & 0 & 0 & -3 & -3 & 0 \\ \phi_{EA} & 3 & -4 & 0 & 0 & 0 \\ \phi_{EB} & 0 & 0 & 0 & 0 & 3 \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & -4 \\ 0 & -3 & -4 \\ 0 & 3 & 0 \\ -3 & 0 & 0 \\ 3 & -3 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_A b \\ H_A b \\ H_{CD} b \\ H_{CE} b \\ H_{FB} b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & 1/3 \\ -1 & 0 & 4/9 \\ -1 & 0 & 8/9 \\ 1 & -1 & -8/9 \\ 1 & -1 & 0 \end{bmatrix}$$




 $\longrightarrow 10 Fb/EA$ 

 $\leftarrow \boxed{+} \rightarrow \quad \longrightarrow 0.6 F$ 

## REAZIONI

$$H_A = 0 \quad V_A = 1/3F \quad H_D = 0 \quad V_D = -1/3F$$

$$N_{AB} = 4/9F \quad N_{BC} = 0 \quad N_{CD} = -4/9F \quad N_{AE} = -5/9F \quad N_{EC} = -5/9F \quad N_{BF} = 5/9F \quad N_{FD} = 5/9F$$

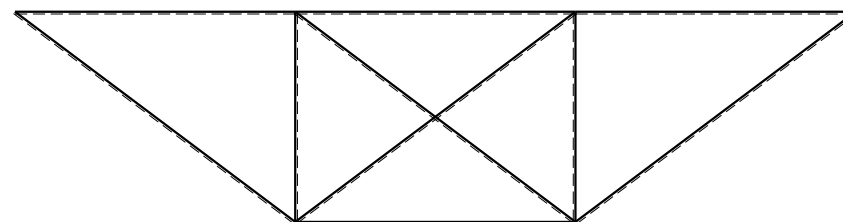
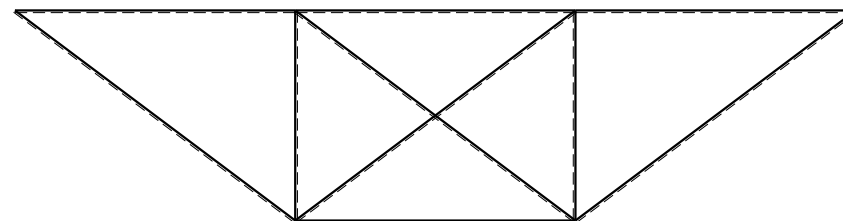
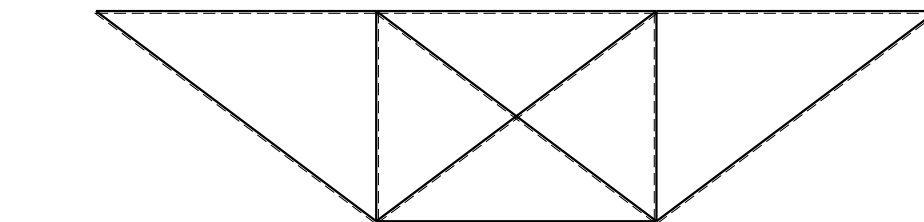
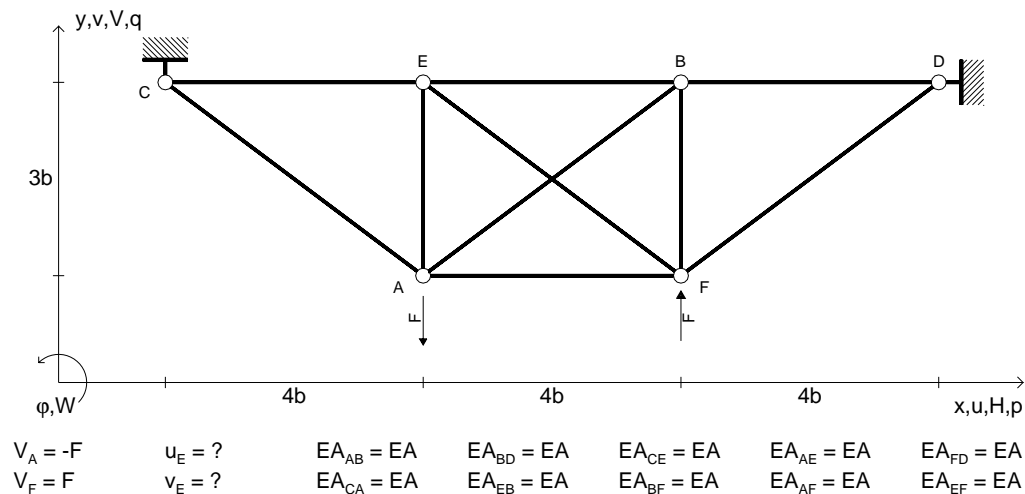
$$N_{EF} = 0 \quad N_{EB} = -1/3F \quad N_{CF} = 1/3F$$

## SPOSTAMENTI ASSOLUTI

$$u_B = 16/9(Fb/EA)$$

$$v_B = -260/81(Fb/EA)$$





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Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

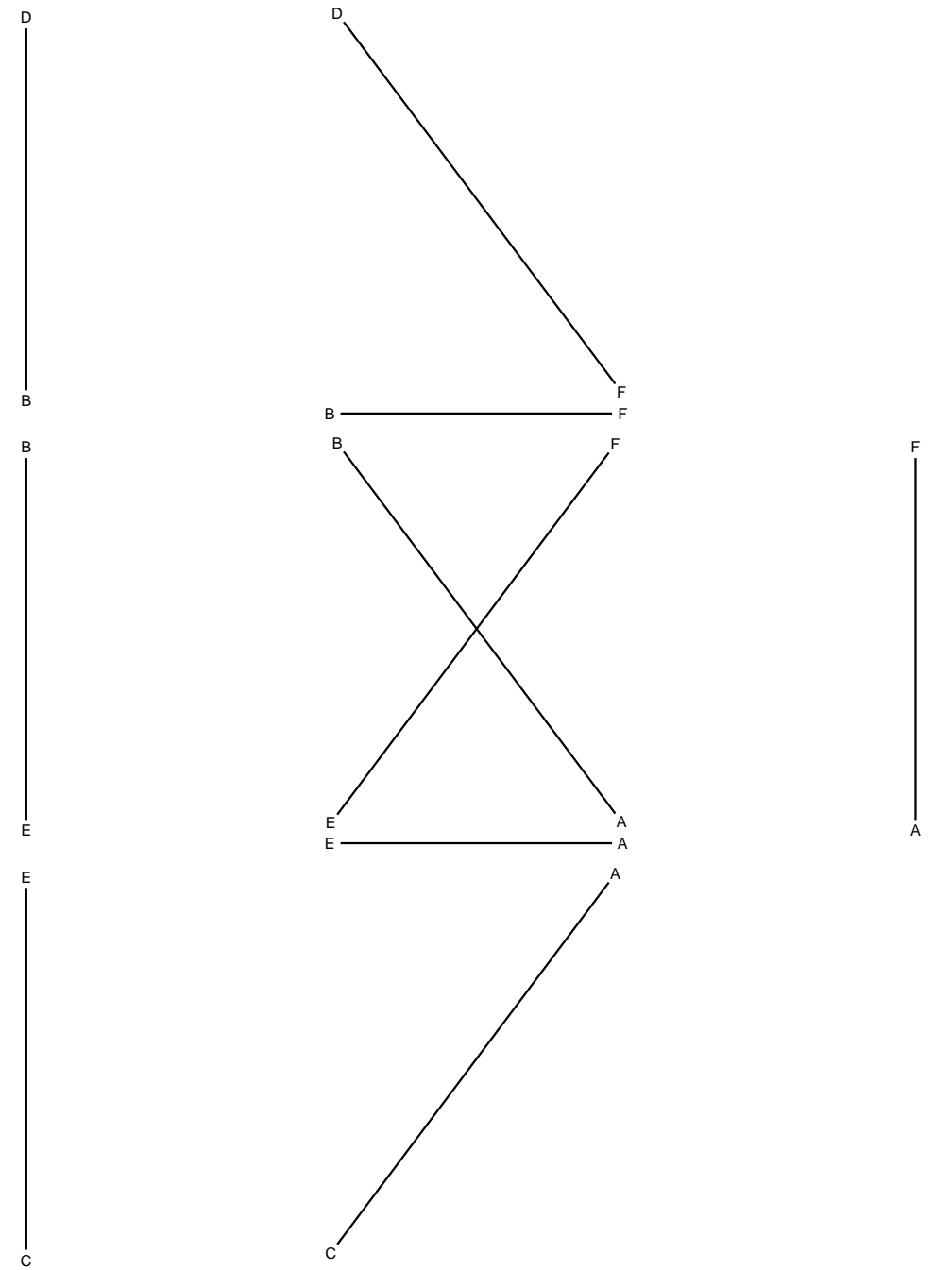
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo E

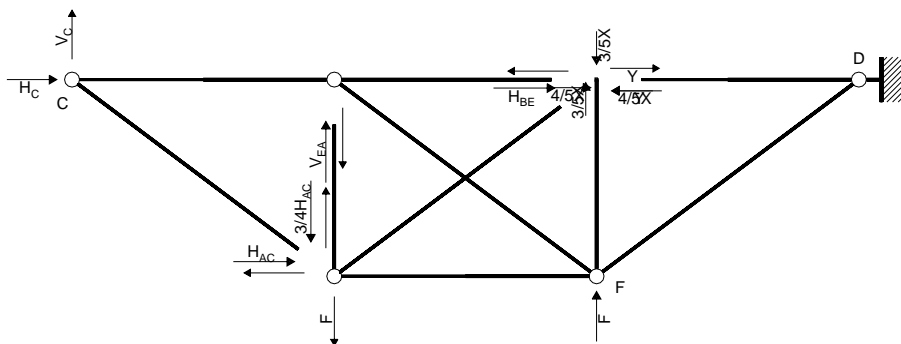
Calcolare lo spostamento verticale del nodo E

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REAZIONI  
 $H_C =$        $V_C =$        $H_D =$        $V_D =$   
 $N_{AB} =$        $N_{CA} =$        $N_{BD} =$        $N_{EB} =$        $N_{CE} =$        $N_{BF} =$        $N_{AE} =$   
 $N_{AF} =$        $N_{FD} =$        $N_{EF} =$   
SPOSTAMENTI ASSOLUTI  
 $u_E =$   
 $v_E =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a D: aste DF FB FA FE AB EB EC AE CA

$$-12V_Cb = -4Fb$$

Rotazione intorno a F: aste FB

$$3H_{BE}b = -12/5Xb - 3Yb$$

Rotazione intorno a F: aste FA AB AE

$$-3H_{AC}b - 4V_{EA}b = 12/5Xb - 4Fb$$

Rotazione intorno a F: aste FE EB EC CA

$$-3H_Cb - 8V_Cb + 3H_{AC}b - 3H_{BE}b + 4V_{EA}b = 0$$

Rotazione intorno a E: aste EC CA

$$-4V_Cb + 3H_{AC}b = 0$$

Matrice di equilibrio

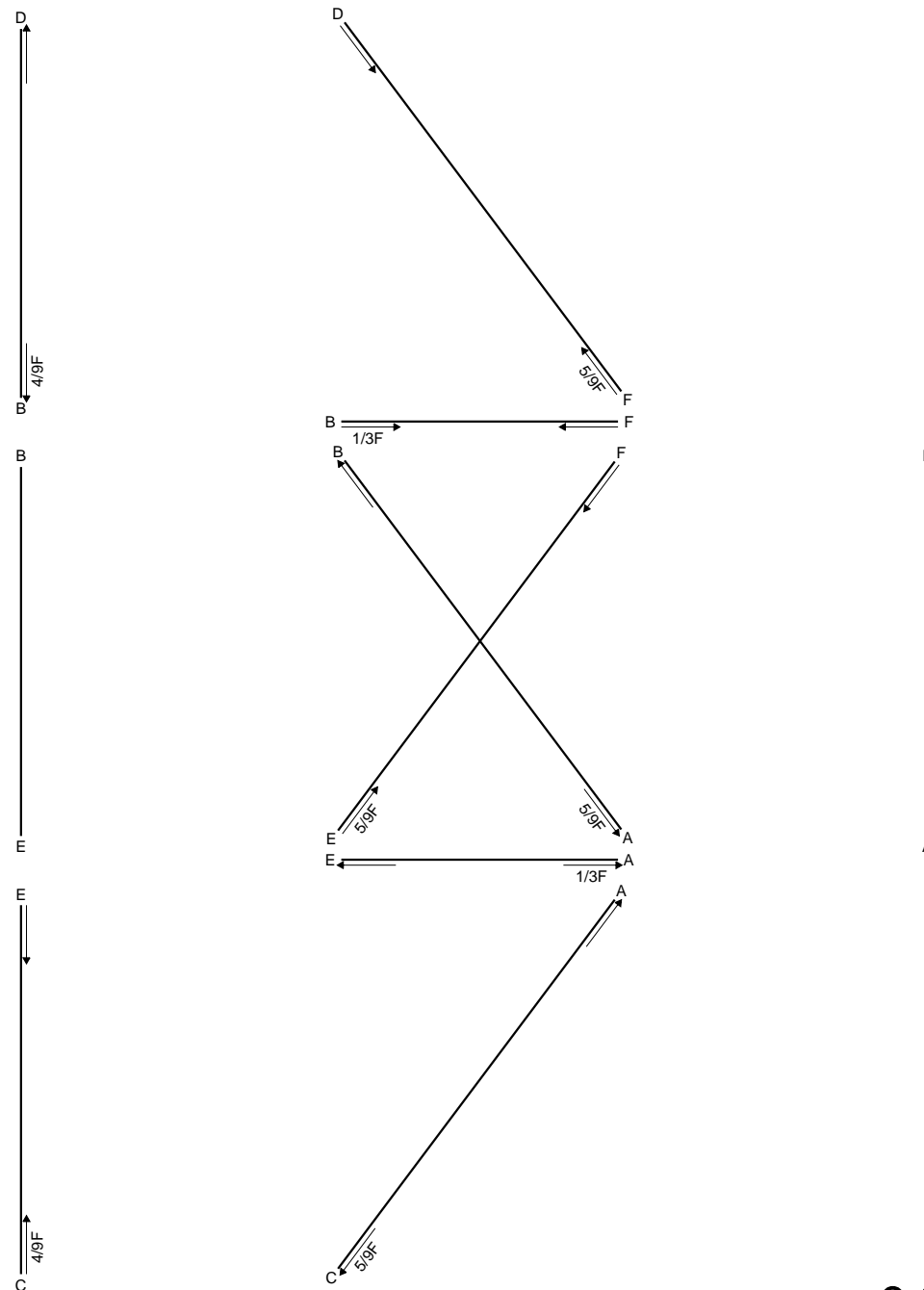
$$\begin{bmatrix} \phi_{DF} \\ \phi_{FB} \\ \phi_{FA} \\ \phi_{FE} \\ \phi_{EC} \end{bmatrix} \begin{bmatrix} H_Cb & V_Cb & H_{AC}b & H_{BE}b & V_{EA}b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \end{bmatrix}$$

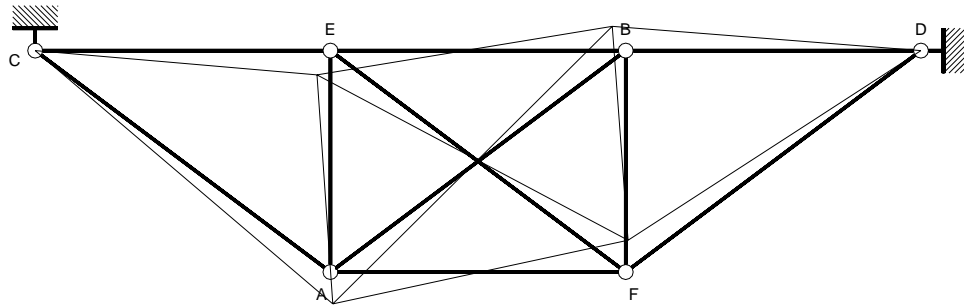
$$\begin{bmatrix} 0 & -12 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & -3 & 0 & -4 \\ -3 & -8 & 3 & -3 & 4 \\ 0 & -4 & 3 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & -4 \\ -12/5 & -3 & 0 \\ 12/5 & 0 & -4 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Soluzione del sistema

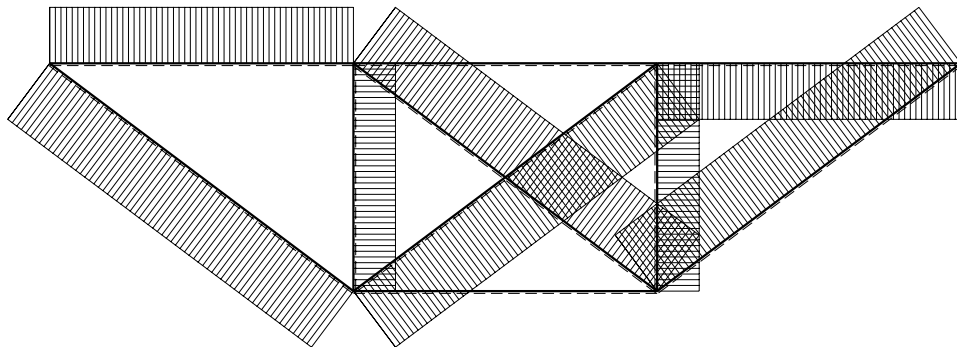
$$\begin{bmatrix} V_Cb \\ H_{BE}b \\ H_{AC}b \\ H_Cb \\ V_{EA}b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 1/3 \\ -4/5 & -1 & 0 \\ 0 & 0 & 4/9 \\ 0 & 1 & 4/9 \\ -3/5 & 0 & 2/3 \end{bmatrix}$$





10 Fb/EA



← ⊕ → 0.6 F

## REAZIONI

$$H_C = 0 \quad V_C = 1/3F \quad H_D = 0 \quad V_D = -1/3F$$

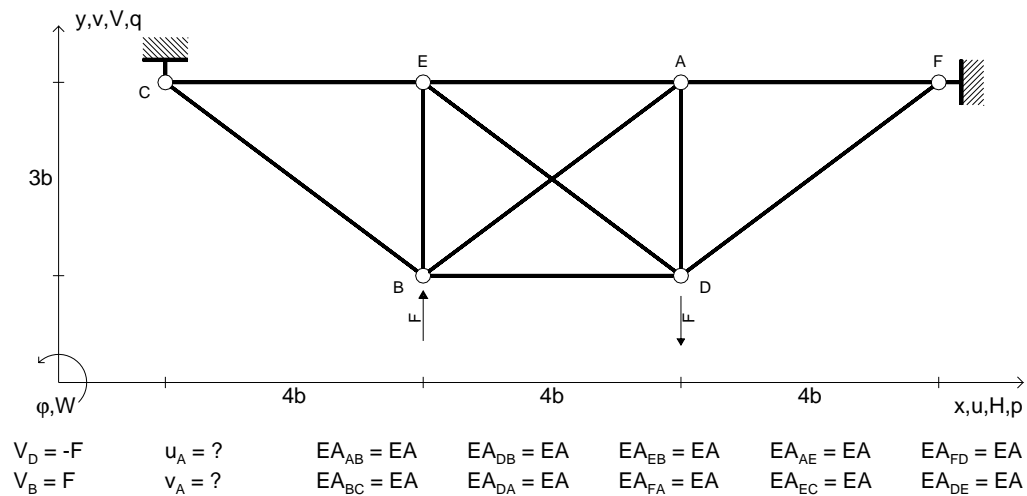
$$N_{AB} = 5/9F \quad N_{CA} = 5/9F \quad N_{BD} = 4/9F \quad N_{EB} = 0 \quad N_{CE} = -4/9F \quad N_{BF} = -1/3F \quad N_{AE} = 1/3F$$

$$N_{AF} = 0 \quad N_{FD} = -5/9F \quad N_{EF} = -5/9F$$

## SPOSTAMENTI ASSOLUTI

$$u_E = -16/9(Fb/EA)$$

$$v_E = -260/81(Fb/EA)$$



Svolgere l'analisi cinematica.

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Calcolare reazioni vincolari della struttura e delle aste.

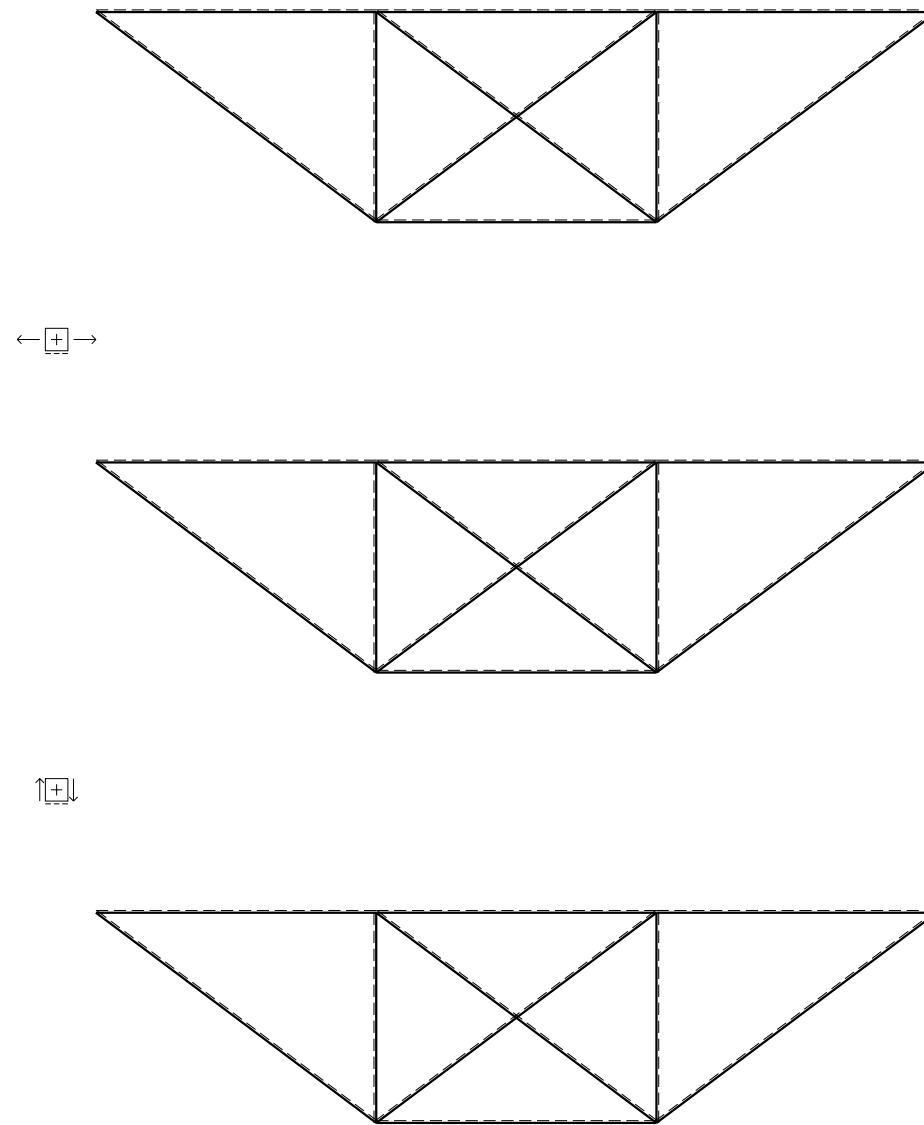
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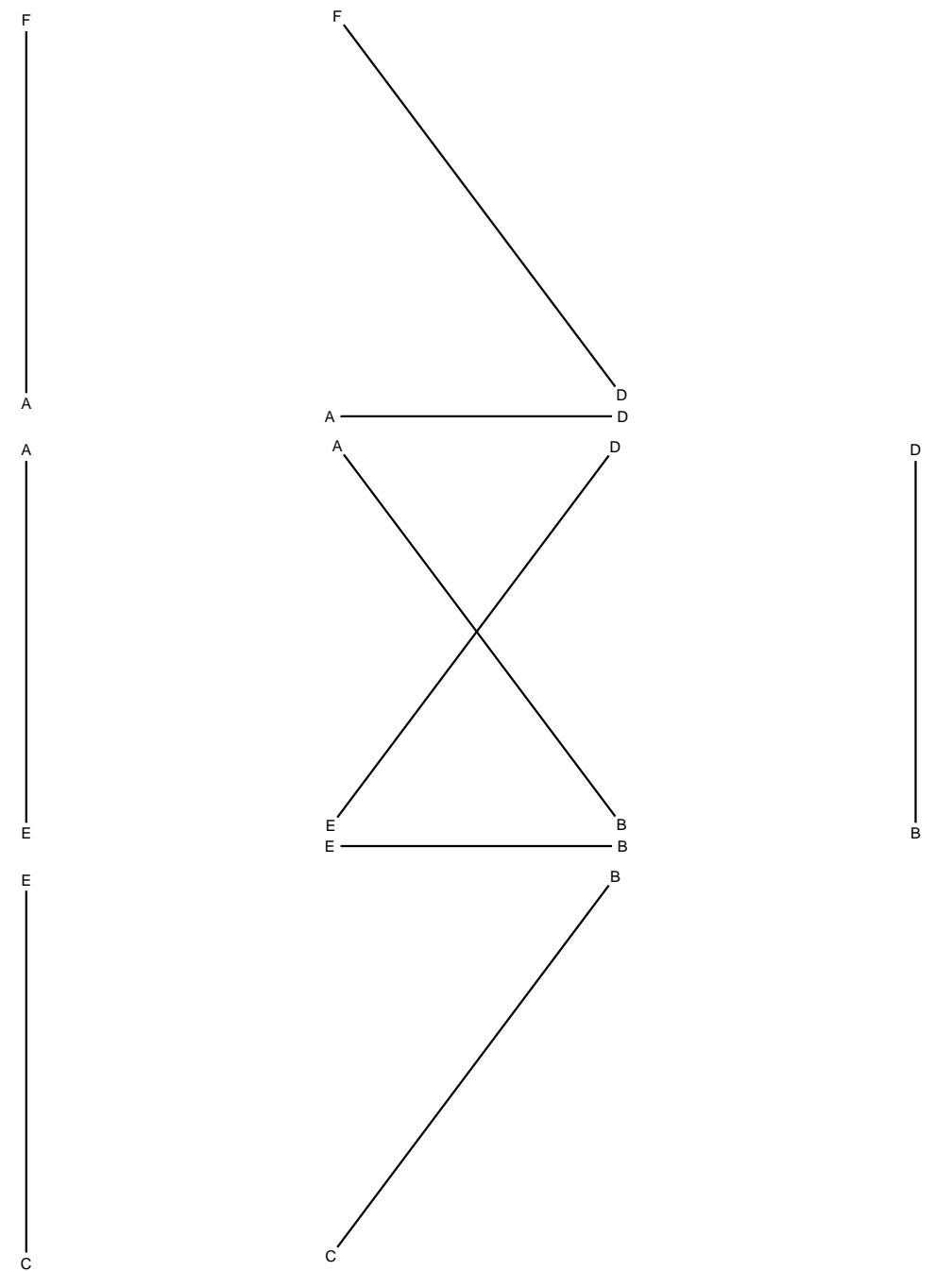
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo A

Calcolare lo spostamento verticale del nodo A

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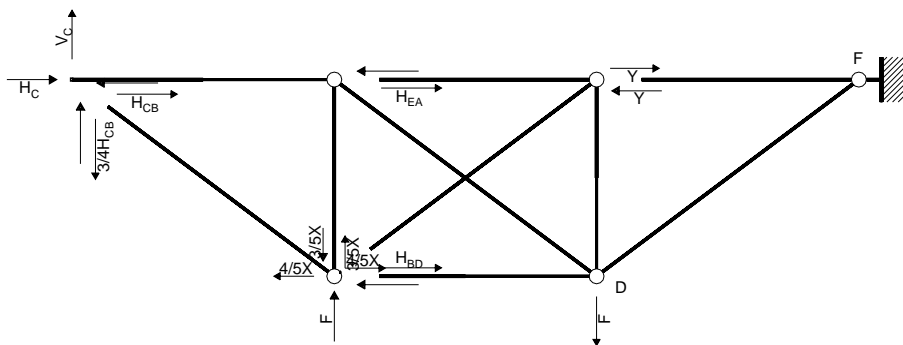
REAZIONI

|            |            |            |            |            |            |            |
|------------|------------|------------|------------|------------|------------|------------|
| $H_C =$    | $V_C =$    | $H_F =$    | $V_F =$    |            |            |            |
| $N_{AB} =$ | $N_{BC} =$ | $N_{DB} =$ | $N_{DA} =$ | $N_{EB} =$ | $N_{FA} =$ | $N_{AE} =$ |
| $N_{EC} =$ | $N_{FD} =$ | $N_{DE} =$ |            |            |            |            |

SPOSTAMENTI ASSOLUTI

$u_A =$

$v_A =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DB DA DE AB EB AE EC BC

$$-12V_C b = 4Fb$$

Rotazione intorno a D: aste DA AB AE

$$-3H_{EA} b = 12/5 X b - 3Y b$$

Rotazione intorno a D: aste DE EB EC BC

$$-3H_C b - 8V_C b + 3H_{EA} b = -12/5 X b + 4Fb$$

Rotazione intorno a E: aste EB BC

$$3H_{CB} b - 3H_{BD} b = 12/5 X b$$

Rotazione intorno a E: aste EC

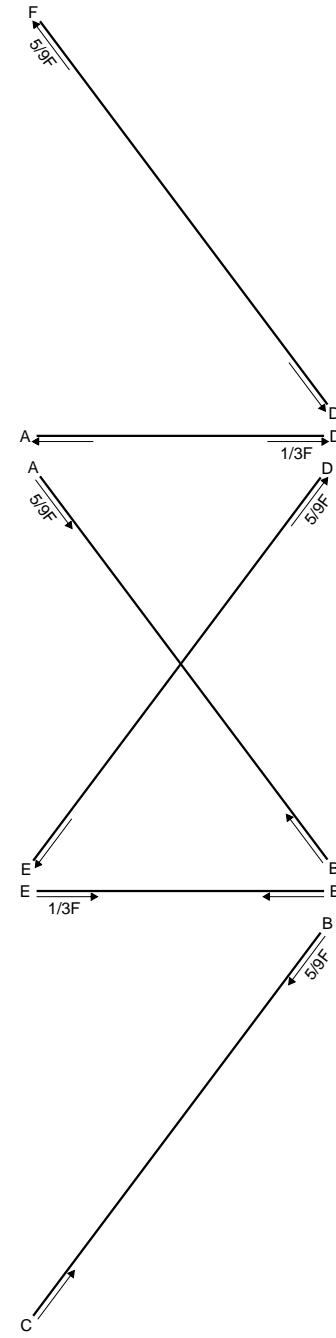
$$-4V_C b - 3H_{CB} b = 0$$

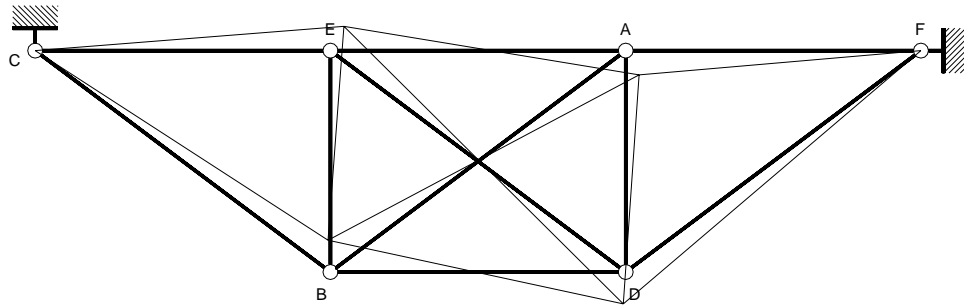
## Matrice di equilibrio

$$\begin{bmatrix} H_C b & V_C b & H_{CB} b & H_{BD} b & H_{EA} b \\ \phi_{FD} & 0 & -12 & 0 & 0 & 0 \\ \phi_{DA} & 0 & 0 & 0 & 0 & -3 \\ \phi_{DE} & -3 & -8 & 0 & 0 & 3 \\ \phi_{EB} & 0 & 0 & 3 & -3 & 0 \\ \phi_{EC} & 0 & -4 & -3 & 0 & 0 \end{bmatrix} = \begin{bmatrix} X b & Y b & F b \\ 0 & 0 & 4 \\ 12/5 & -3 & 0 \\ -12/5 & 0 & 4 \\ 12/5 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

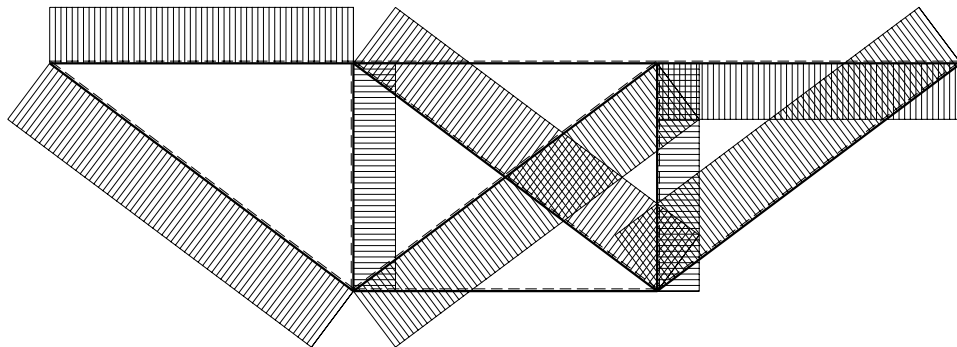
## Soluzione del sistema

$$\begin{bmatrix} V_C b \\ H_{EA} b \\ H_C b \\ H_{BD} b \\ H_{CB} b \end{bmatrix} = \begin{bmatrix} X b & Y b & F b \\ 0 & 0 & -1/3 \\ -4/5 & 1 & 0 \\ 0 & 1 & -4/9 \\ -4/5 & 0 & 4/9 \\ 0 & 0 & 4/9 \end{bmatrix}$$





10 Fb/EA



← ⊕ → 0.6 F

## REAZIONI

$$H_C = 0 \quad V_C = -1/3F \quad H_F = 0 \quad V_F = 1/3F$$

$$N_{AB} = -5/9F \quad N_{BC} = -5/9F \quad N_{DB} = 0 \quad N_{DA} = 1/3F \quad N_{EB} = -1/3F \quad N_{FA} = -4/9F \quad N_{AE} = 0$$

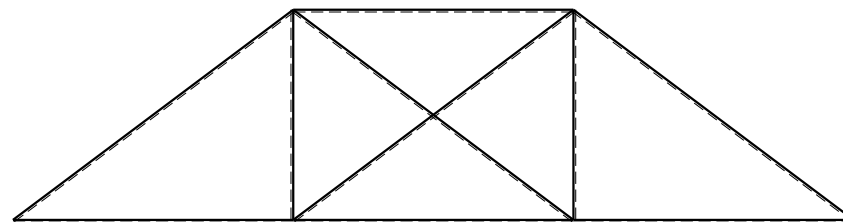
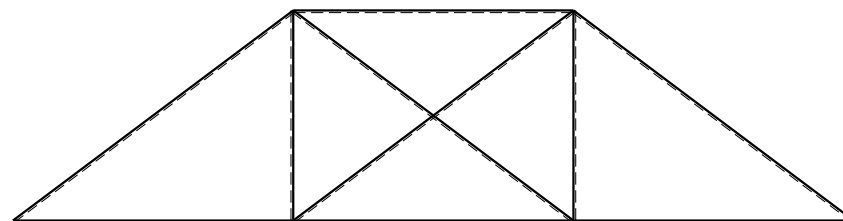
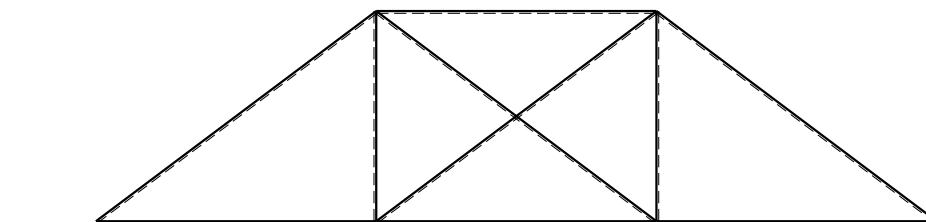
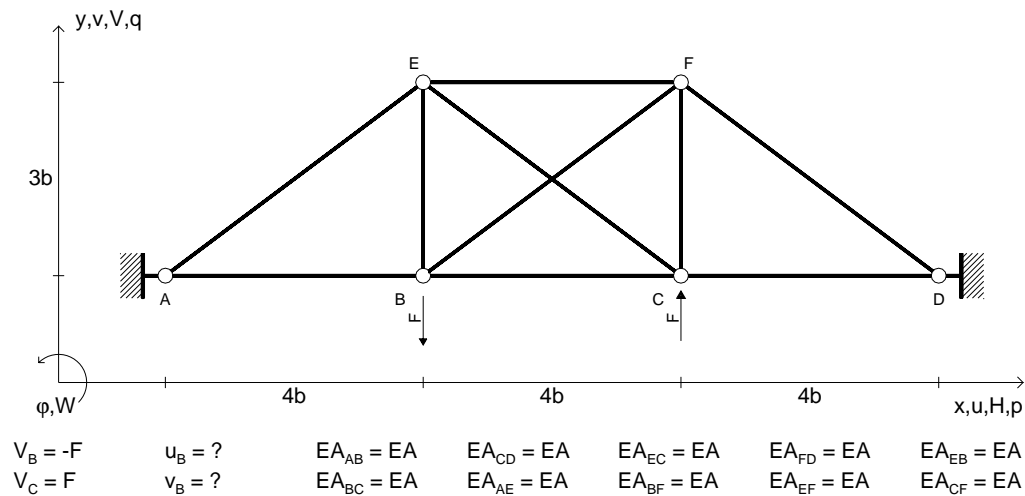
$$N_{EC} = 4/9F \quad N_{FD} = 5/9F \quad N_{DE} = 5/9F$$

## SPOSTAMENTI ASSOLUTI

$$u_A = 16/9(Fb/EA)$$

$$v_A = -260/81(Fb/EA)$$





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Calcolare reazioni vincolari della struttura e delle aste.

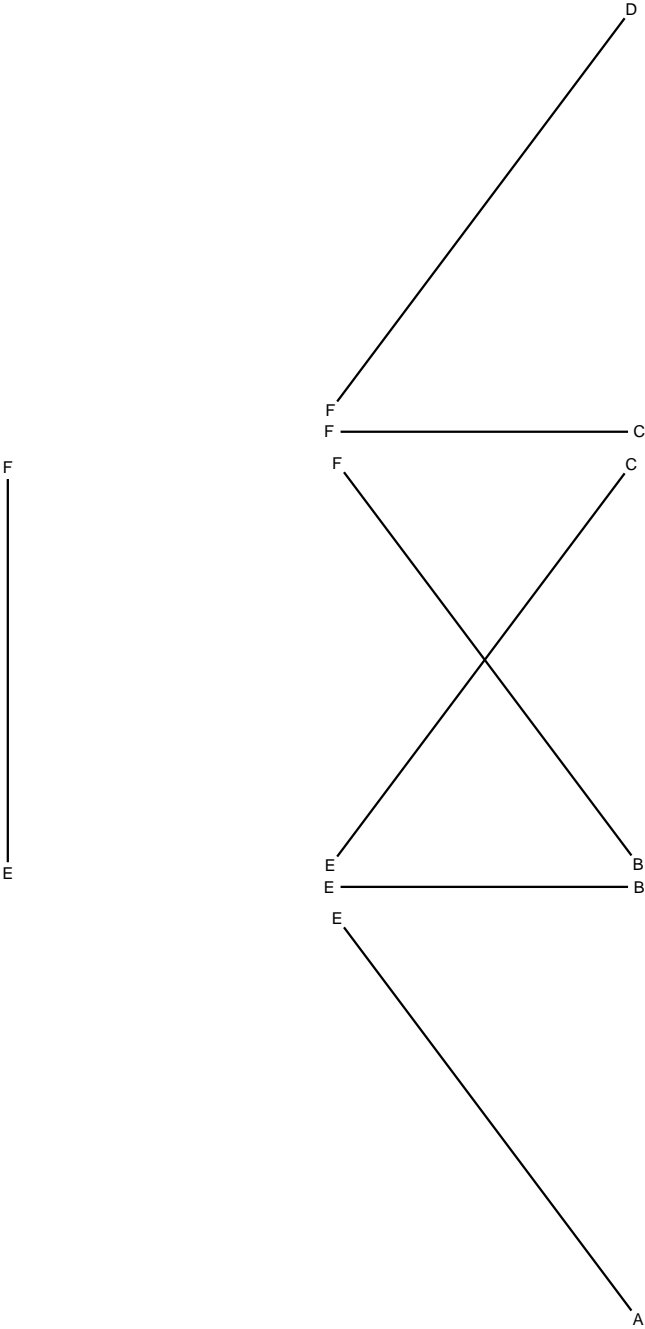
Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo B

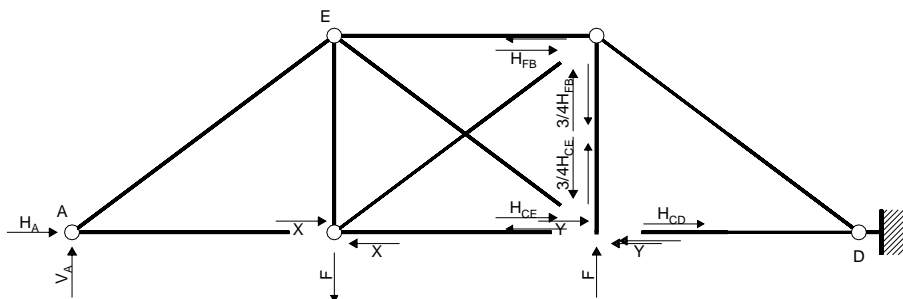
Calcolare lo spostamento verticale del nodo B

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REAZIONI  
 $H_A =$        $V_A =$        $H_D =$        $V_D =$   
 $N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{AE} =$        $N_{EC} =$        $N_{BF} =$        $N_{FD} =$   
 $N_{EF} =$        $N_{EB} =$        $N_{CF} =$

SPOSTAMENTI ASSOLUTI  
 $u_B =$   
 $v_B =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a D: aste DF FE FC EA EC EB AB BC BF

$$-12V_A b = -4Fb$$

Rotazione intorno a F: aste FE EA EC EB AB BC BF

$$3H_A b - 8V_A b + 3H_{CF} b = -3Yb - 4Fb$$

Rotazione intorno a F: aste FC

$$-3H_{CD}b - 3H_{CE}b = 3Yb$$

Rotazione intorno a E: aste EA AB

$$3H_A b - 4V_A b = -3Xb$$

Rotazione intorno a E: aste EB BC BF

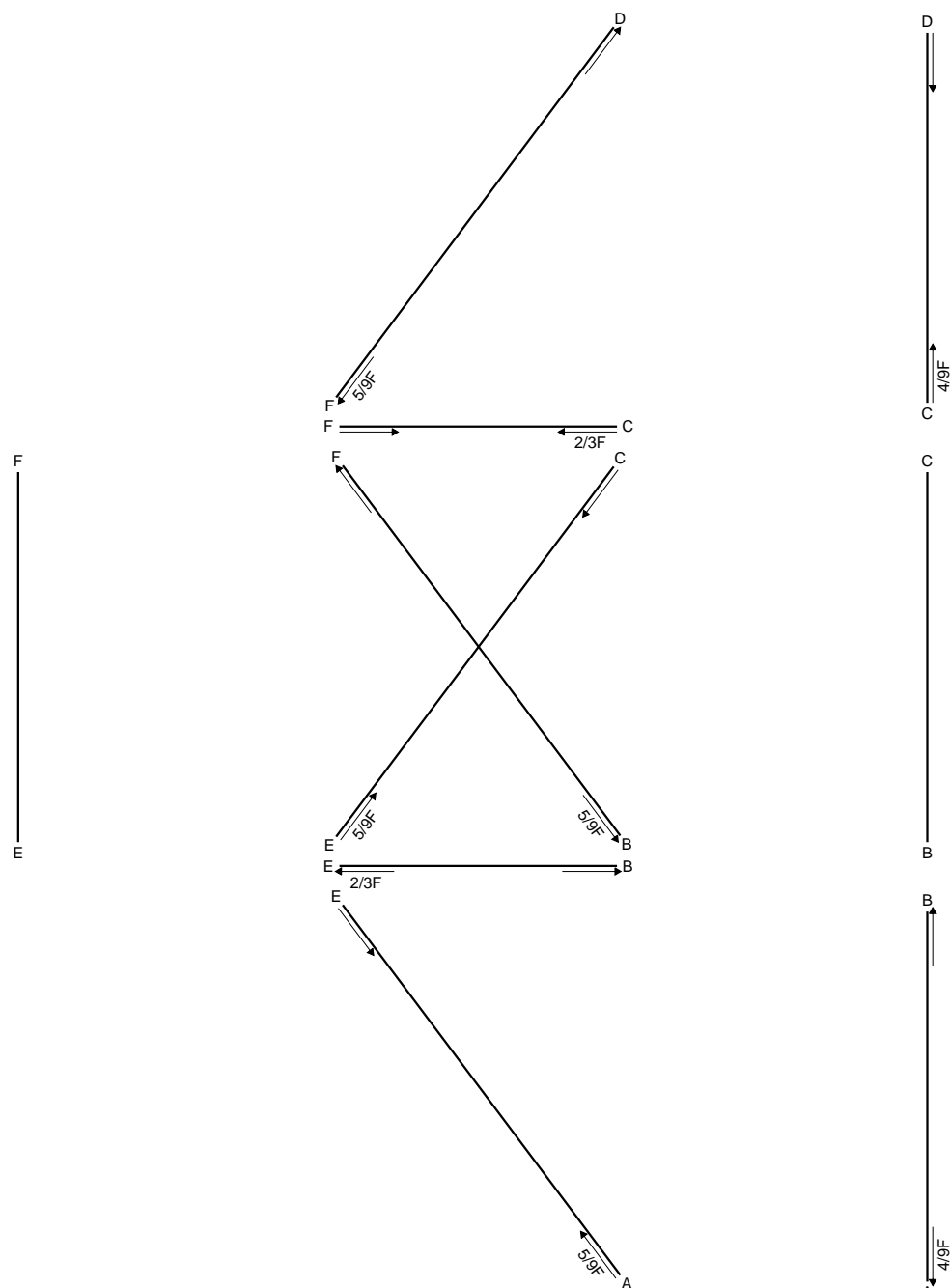
$$3H_{FB}b = 3Xb - 3Yb$$

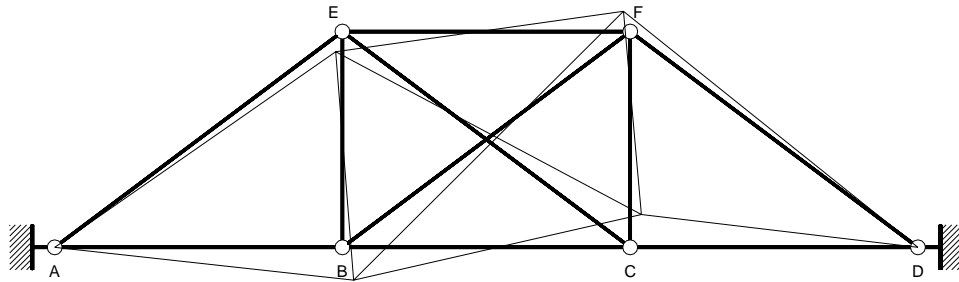
### Matrice di equilibrio

$$\begin{bmatrix} H_{Ab} & V_{Ab} & H_{CDb} & H_{CEb} & H_{FBb} \\ \Phi_{DF} & 0 & -12 & 0 & 0 \\ \Phi_{FE} & 3 & -8 & 0 & 0 \\ \Phi_{FC} & 0 & 0 & -3 & 0 \\ \Phi_{EA} & 3 & -4 & 0 & 0 \\ \Phi_{EB} & 0 & 0 & 0 & 3 \end{bmatrix} = \begin{bmatrix} X_b & Y_b & F_b \\ 0 & 0 & -4 \\ 0 & -3 & -4 \\ 0 & 3 & 0 \\ -3 & 0 & 0 \\ 3 & -3 & 0 \end{bmatrix}$$

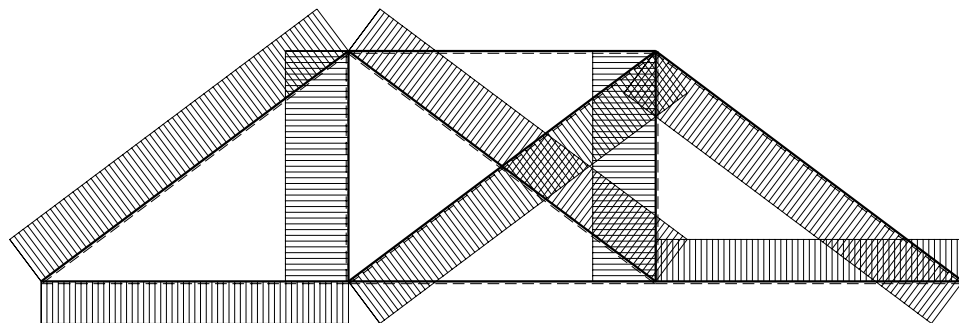
### Soluzione del sistema

$$\begin{bmatrix} V_A b \\ H_A b \\ H_{CD} b \\ H_{CE} b \\ H_{FB} b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & 1/3 \\ -1 & 0 & 4/9 \\ -1 & 0 & 8/9 \\ 1 & -1 & -8/9 \\ 1 & -1 & 0 \end{bmatrix}$$





$\longrightarrow 12 Fb/EA$



$\leftarrow \boxed{+} \rightarrow$   $\longrightarrow 0.8 F$

REAZIONI

$$H_A = 0 \quad V_A = 1/3F \quad H_D = 0 \quad V_D = -1/3F$$

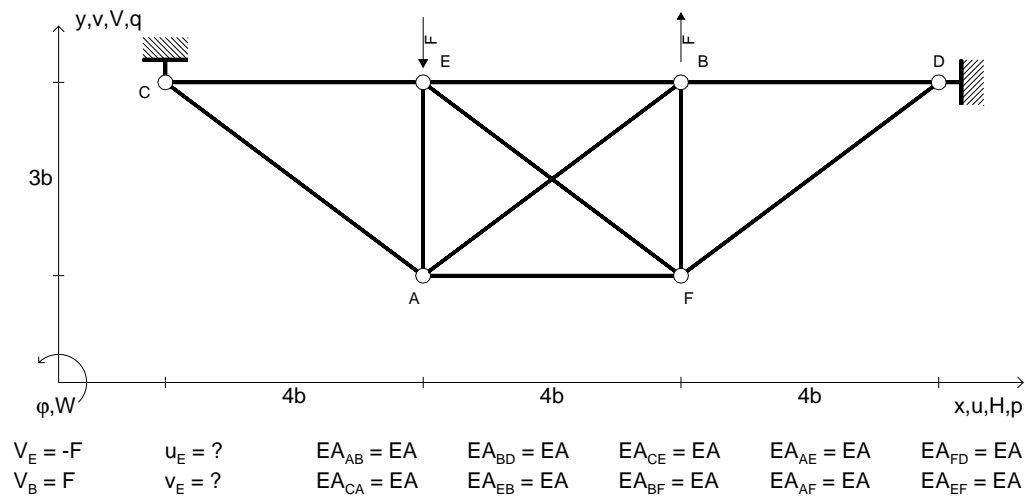
$$N_{AB} = 4/9F \quad N_{BC} = 0 \quad N_{CD} = -4/9F \quad N_{AE} = -5/9F \quad N_{EC} = -5/9F \quad N_{BF} = 5/9F \quad N_{FD} = 5/9F$$

$$N_{EF} = 0 \quad N_{EB} = 2/3F \quad N_{CF} = -2/3F$$

SPOSTAMENTI ASSOLUTI

$$u_B = 16/9(Fb/EA)$$

$$v_B = -422/81(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

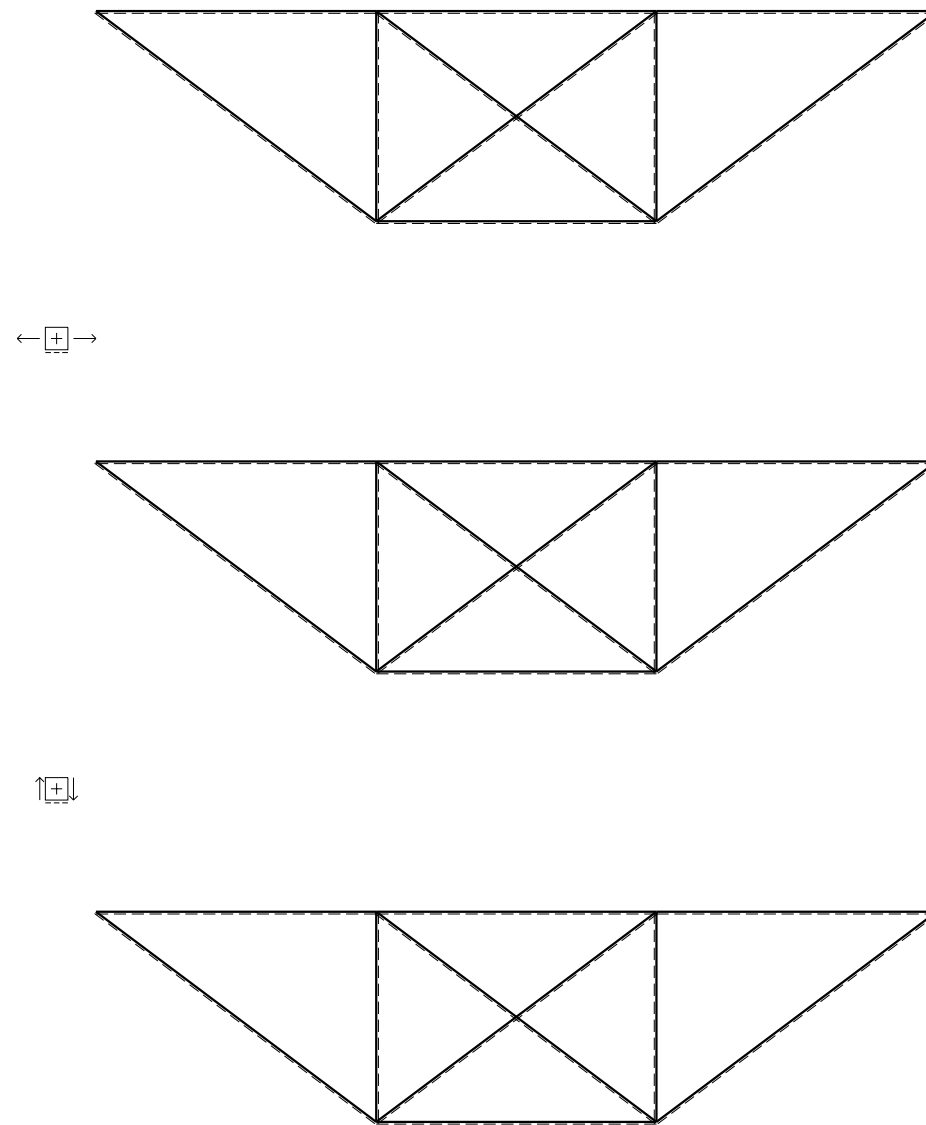
Tracciare i diagrammi delle azioni interne nelle aste.

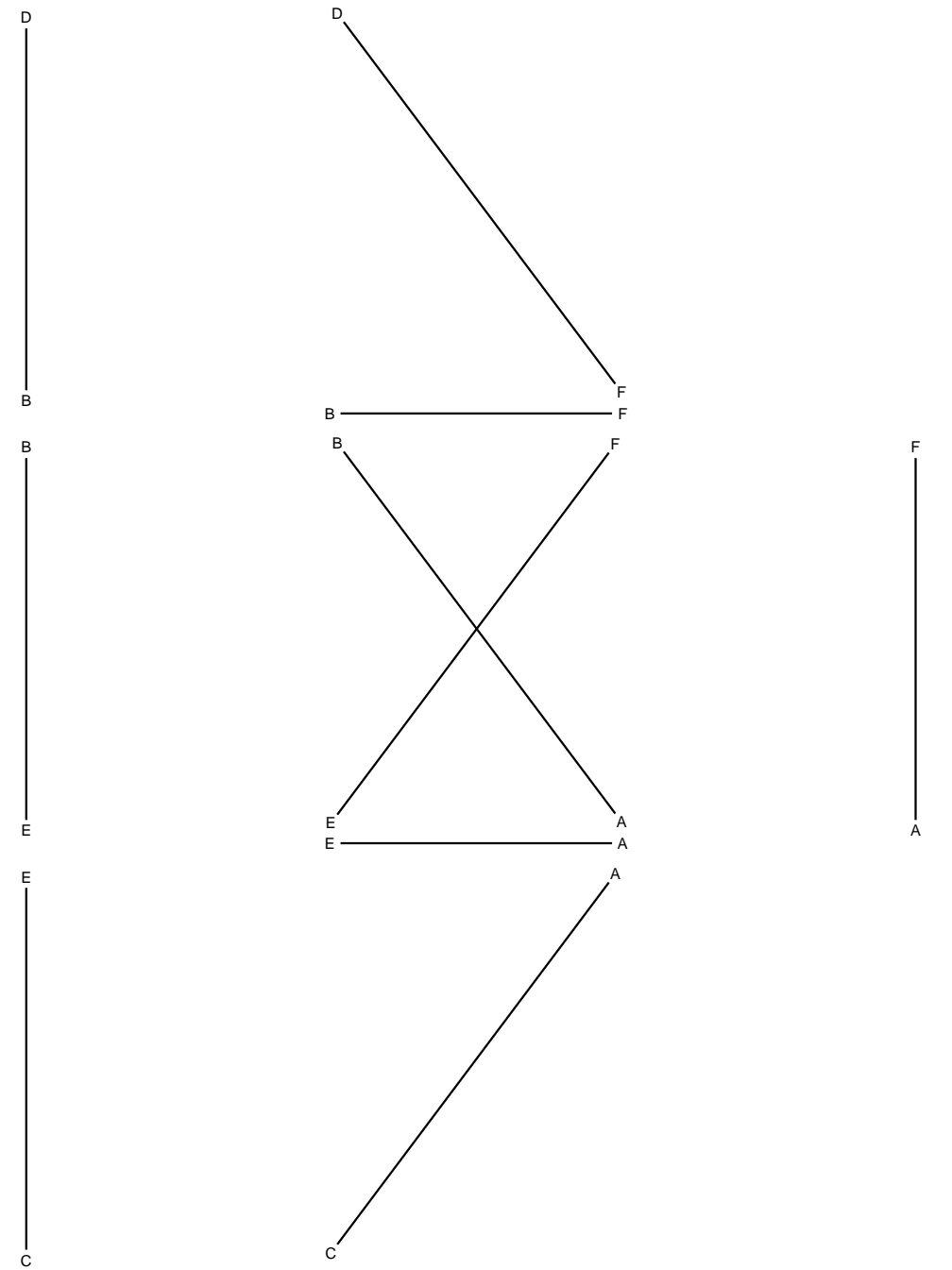
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo E

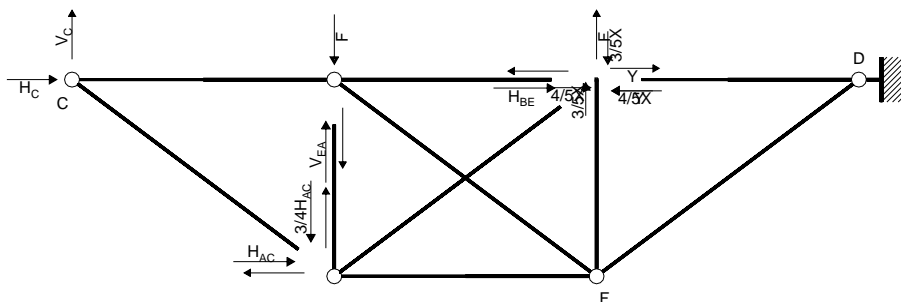
Calcolare lo spostamento verticale del nodo E

@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI  
 $H_C =$        $V_C =$        $H_D =$        $V_D =$   
 $N_{AB} =$        $N_{CA} =$        $N_{BD} =$        $N_{EB} =$        $N_{CE} =$        $N_{BF} =$        $N_{AE} =$   
 $N_{AF} =$        $N_{FD} =$        $N_{EF} =$   
SPOSTAMENTI ASSOLUTI  
 $u_E =$   
 $v_E =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a D: aste DF FB FA FE AB EB EC AE CA

$$-12V_C b = -4Fb$$

Rotazione intorno a F: aste FB

$$3H_{BF}b = -12/5Xb - 3Yb$$

Rotazione intorno a F: aste FA AB AE

$$-3H_{AC}b - 4V_{FA}b = 12/5Xb$$

Rotazione intorno a F: aste FE EB EC CA

$$-3H_G b - 8V_G b + 3H_{AG} b - 3H_{BF} b + 4V_{FA} b = -4Fb$$

Rotazione intorno a E: aste EC CA

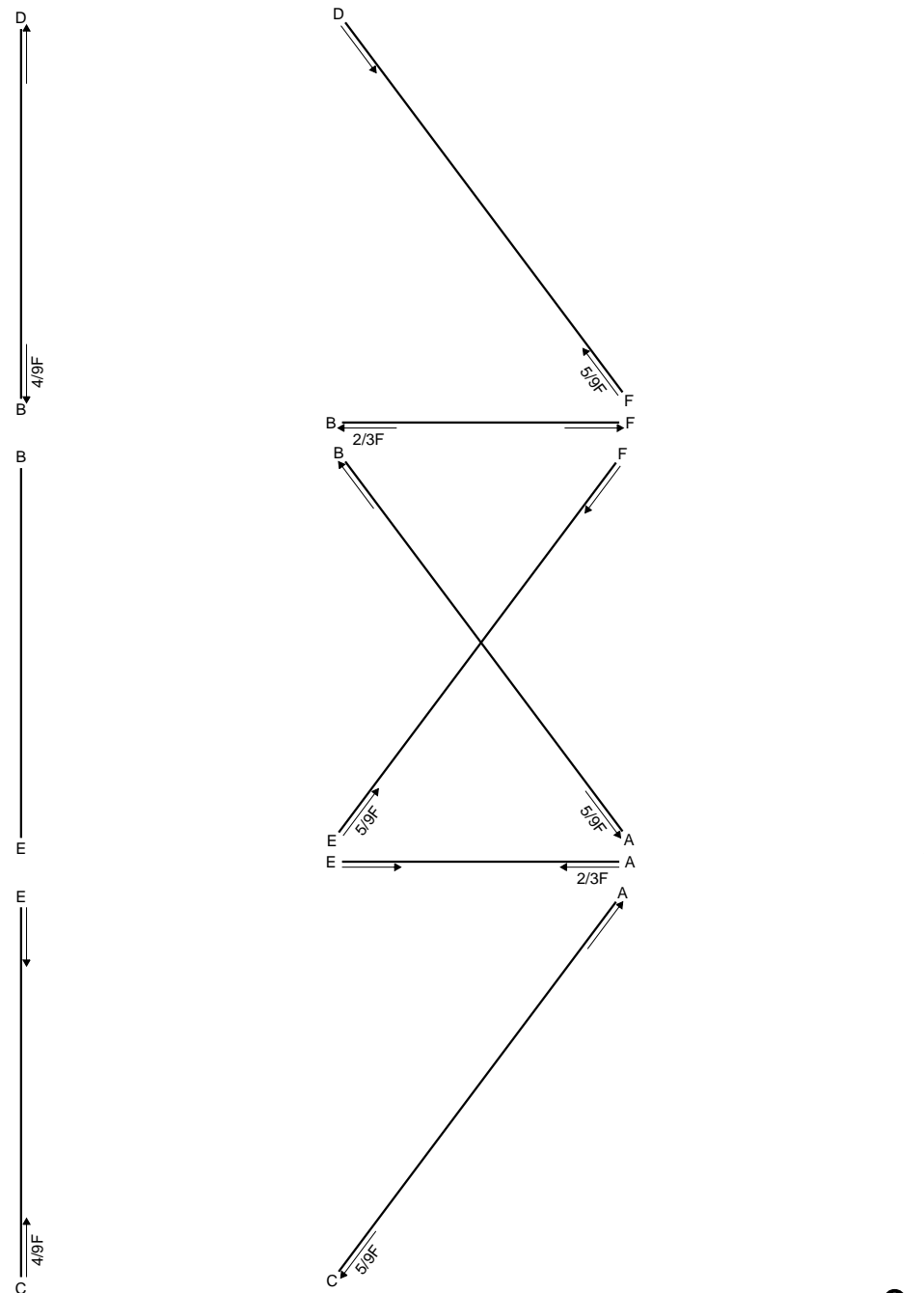
$$-4V_{Cb} + 3H_{AC}b = 0$$

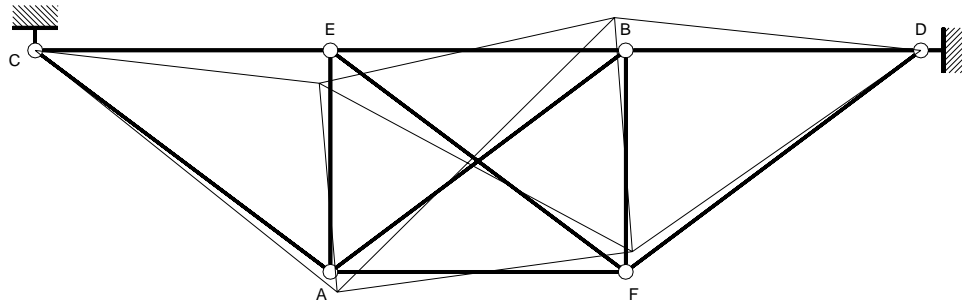
### Matrice di equilibrio

$$\begin{bmatrix} \text{H}_{\text{C}^{\text{b}}} & \text{V}_{\text{C}^{\text{b}}} & \text{H}_{\text{A}^{\text{b}}} & \text{H}_{\text{BE}^{\text{b}}} & \text{V}_{\text{EA}^{\text{b}}} \end{bmatrix} = \begin{bmatrix} \text{Xb} & \text{Yb} & \text{Fb} \end{bmatrix}$$

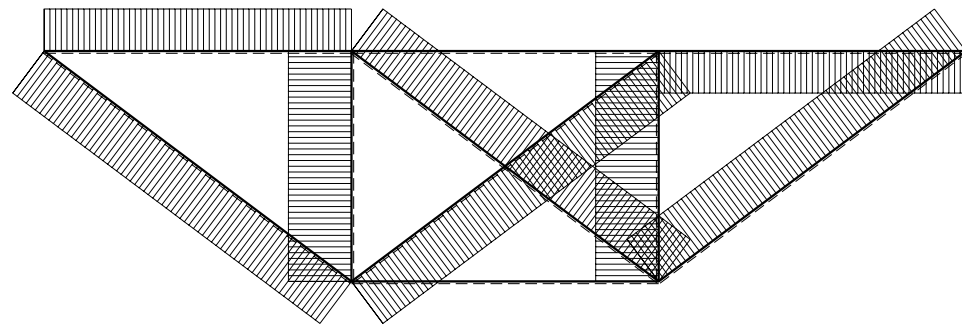
### Soluzione del sistema

$$\begin{bmatrix} V_{Cb} \\ H_{BE}b \\ H_{AC}b \\ H_Cb \\ V_{FA}b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & 1/3 \\ -4/5 & -1 & 0 \\ 0 & 0 & 4/9 \\ 0 & 1 & 4/9 \\ -3/5 & 0 & -1/3 \end{bmatrix}$$





12 Fb/EA



← ⊕ → 0.8 F

## REAZIONI

$$H_C = 0 \quad V_C = 1/3F \quad H_D = 0 \quad V_D = -1/3F$$

$$N_{AB} = 5/9F \quad N_{CA} = 5/9F \quad N_{BD} = 4/9F \quad N_{EB} = 0 \quad N_{CE} = -4/9F \quad N_{BF} = 2/3F \quad N_{AE} = -2/3F$$

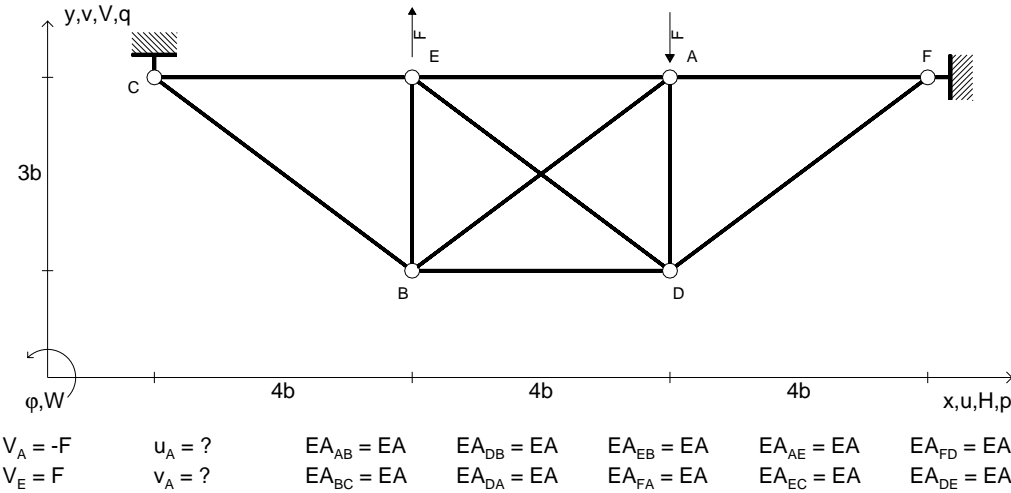
$$N_{AF} = 0 \quad N_{FD} = -5/9F \quad N_{EF} = -5/9F$$

## SPOSTAMENTI ASSOLUTI

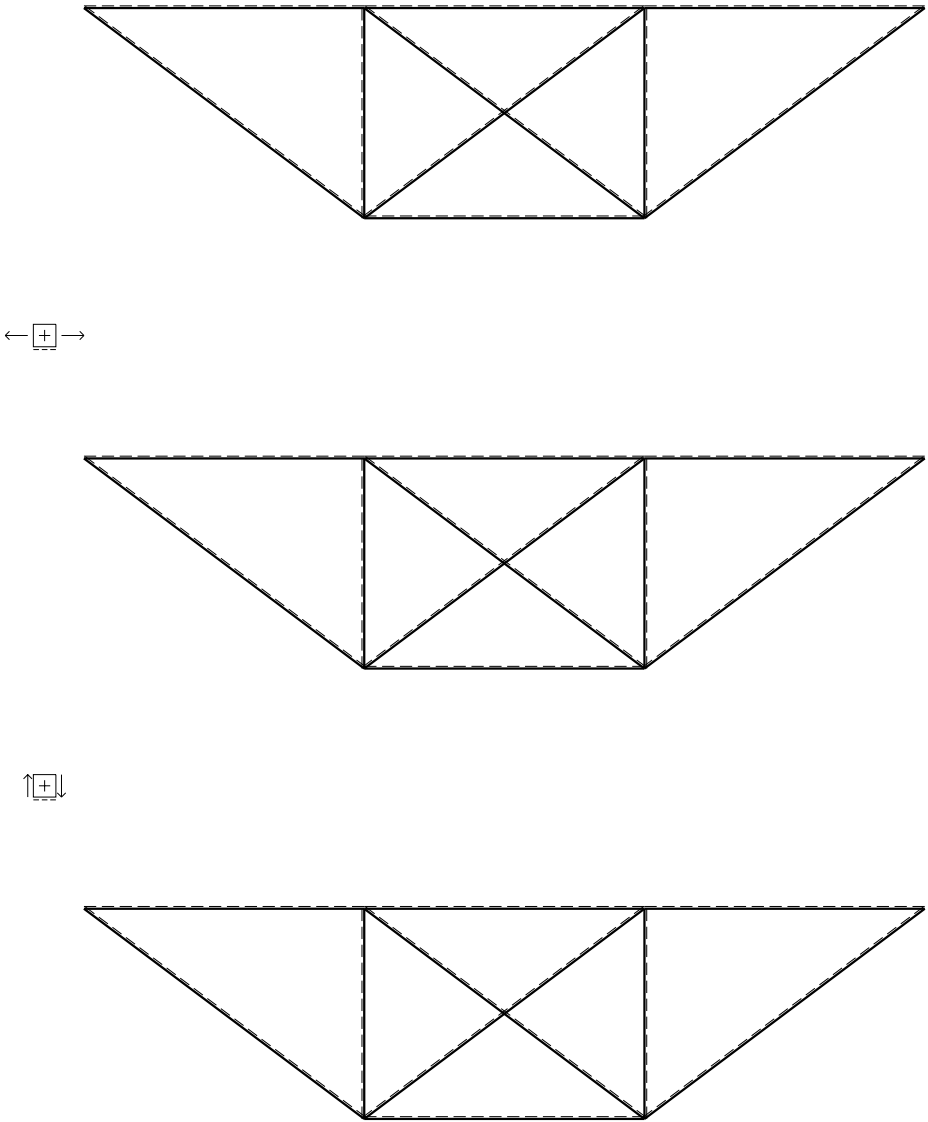
$$u_E = -16/9(Fb/EA)$$

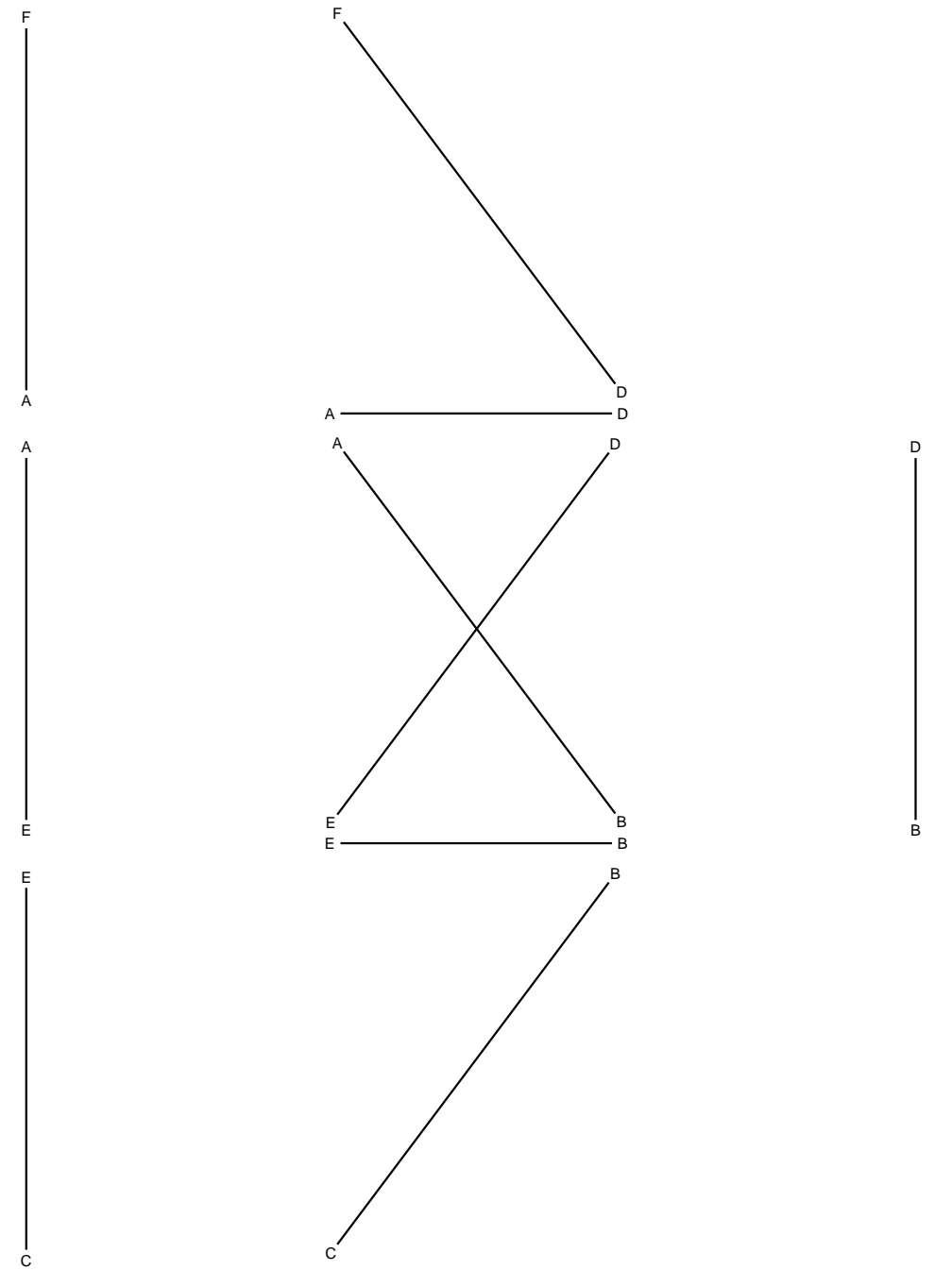
$$v_E = -422/81(Fb/EA)$$



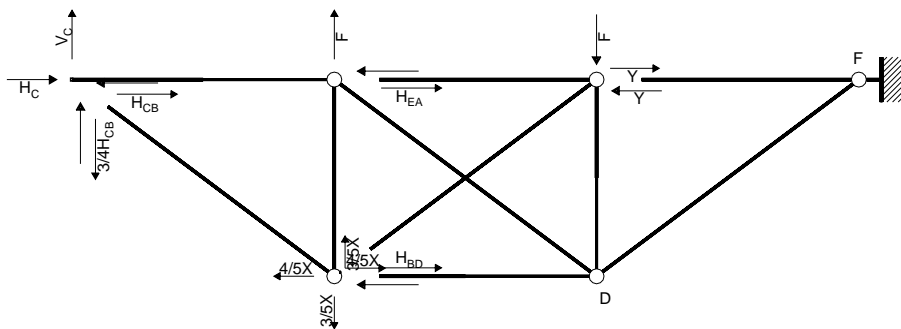


Svolgere l'analisi cinematica.  
Riportare la soluzione su questo foglio.  
Carichi e deformazioni date hanno verso efficace in disegno.  
Calcolare reazioni vincolari della struttura e delle aste.  
Tracciare i diagrammi delle azioni interne nelle aste.  
 $A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.  
Calcolare lo spostamento orizzont. del nodo A  
Calcolare lo spostamento verticale del nodo A  
@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI  
 $H_C =$        $V_C =$        $H_F =$        $V_F =$   
 $N_{AB} =$        $N_{BC} =$        $N_{DB} =$        $N_{DA} =$        $N_{EB} =$        $N_{FA} =$        $N_{AE} =$   
 $N_{EC} =$        $N_{FD} =$        $N_{DE} =$   
SPOSTAMENTI ASSOLUTI  
 $u_A =$   
 $v_A =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DB DA DE AB EB AE EC BC

$$-12V_C b = 4Fb$$

Rotazione intorno a D: aste DA AB AE

$$-3H_{FA}b = 12/5Xb - 3Yb$$

Rotazione intorno a D: aste DE EB EC BC

$$-3H_C b - 8V_C b + 3H_{EA} b = -12/5 X b + 4F b$$

Rotazione intorno a E: aste EB BC

$$3H_{CB}b - 3H_{BD}b = 12/5Xb$$

Rotazione intorno a E: aste EC

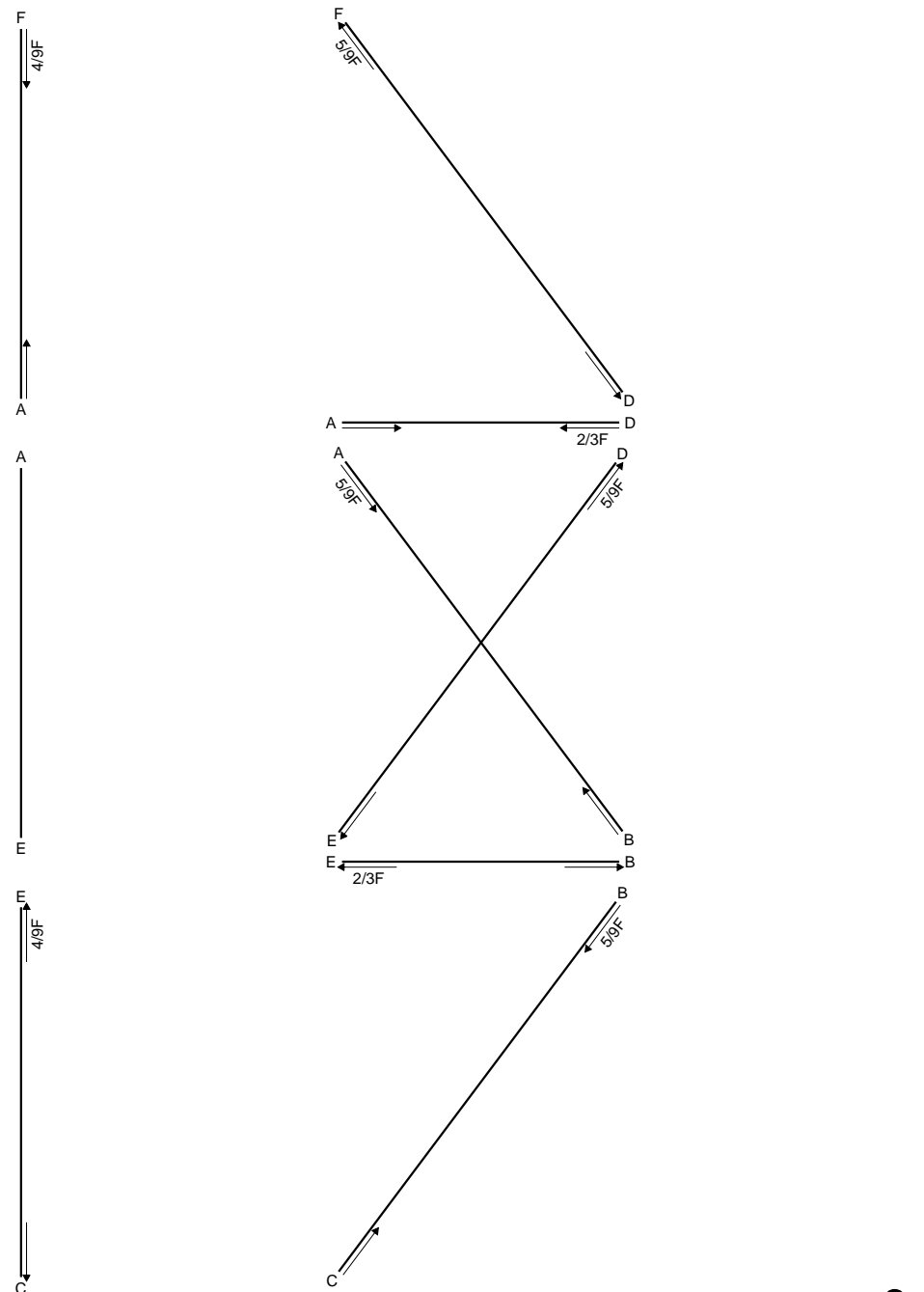
$$-4V_{Cb} - 3H_{CB}b = 0$$

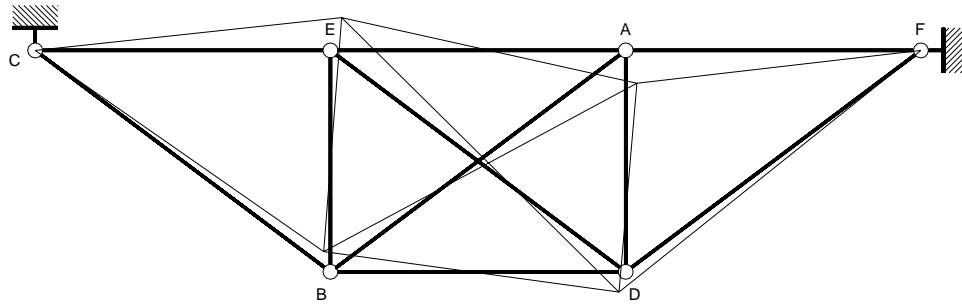
### Matrice di equilibrio

$$\begin{bmatrix} H_{Cb} & V_{Cb} & H_{CBb} & H_{BDb} & H_{EAb} \\ \varphi_{FD} & 0 & -12 & 0 & 0 \\ \varphi_{DA} & 0 & 0 & 0 & -3 \\ \varphi_{DE} & -3 & -8 & 0 & 3 \\ \varphi_{EB} & 0 & 0 & 3 & -3 \\ \varphi_{EC} & 0 & -4 & -3 & 0 \end{bmatrix} = \begin{bmatrix} X_b & Y_b & F_b \\ 0 & 0 & 4 \\ 12/5 & -3 & 0 \\ -12/5 & 0 & 4 \\ 12/5 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

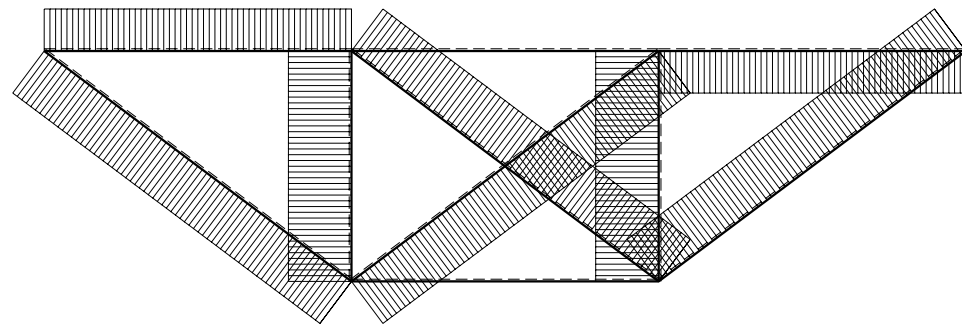
### Soluzione del sistema

$$\begin{bmatrix} V_{Cb} \\ H_{EA}b \\ H_{Cb} \\ H_{BD}b \\ H_{CB}b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & -1/3 \\ -4/5 & 1 & 0 \\ 0 & 1 & -4/9 \\ -4/5 & 0 & 4/9 \\ 0 & 0 & 4/9 \end{bmatrix}$$





12 Fb/EA



← ⊕ → 0.8 F

REAZIONI

$$H_C = 0 \quad V_C = -1/3F \quad H_F = 0 \quad V_F = 1/3F$$

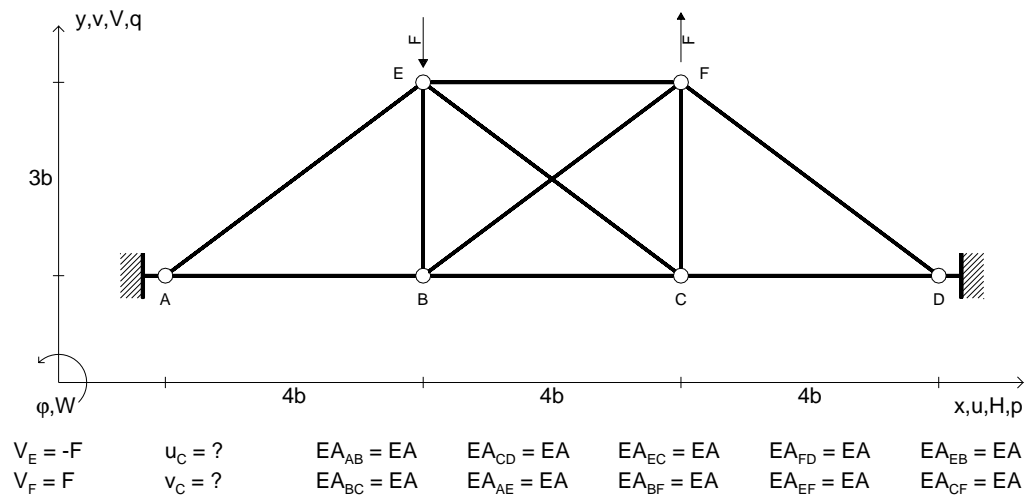
$$N_{AB} = -5/9F \quad N_{BC} = -5/9F \quad N_{DB} = 0 \quad N_{DA} = -2/3F \quad N_{EB} = 2/3F \quad N_{FA} = -4/9F \quad N_{AE} = 0$$

$$N_{EC} = 4/9F \quad N_{FD} = 5/9F \quad N_{DE} = 5/9F$$

SPOSTAMENTI ASSOLUTI

$$u_A = 16/9(Fb/EA)$$

$$v_A = -422/81(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

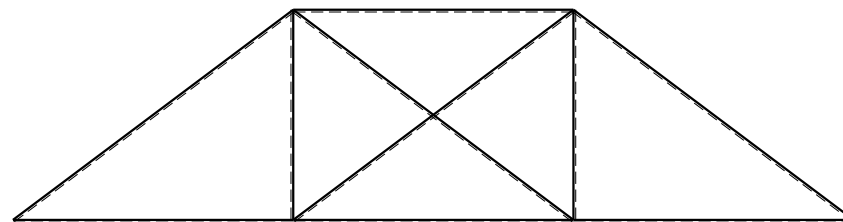
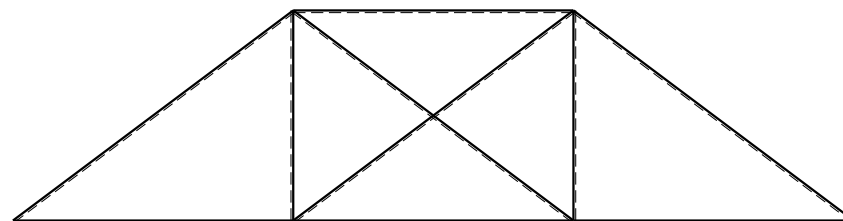
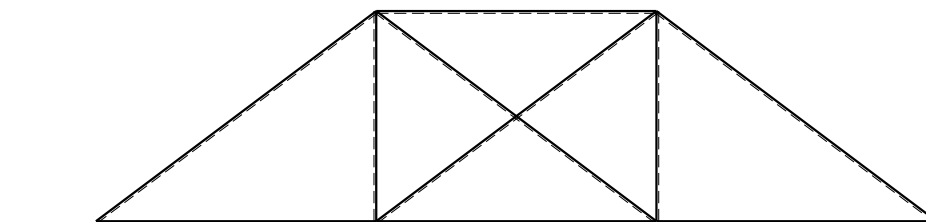
Tracciare i diagrammi delle azioni interne nelle aste.

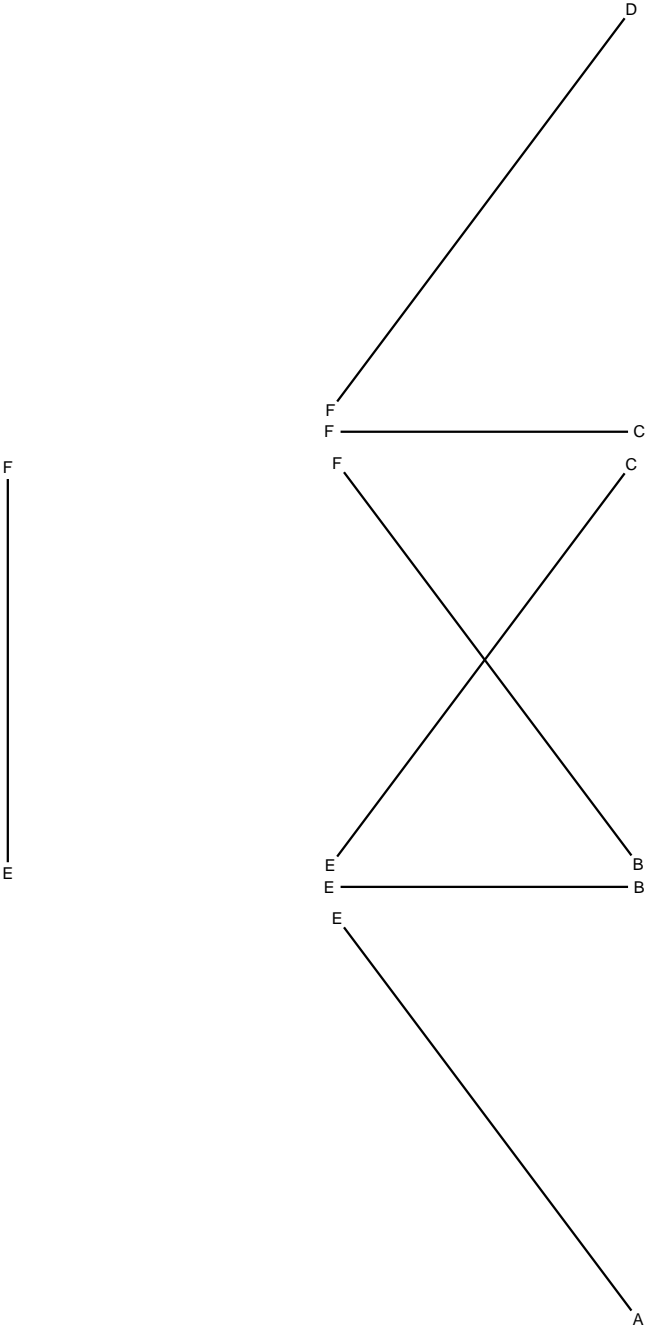
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo C

Calcolare lo spostamento verticale del nodo C

@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$        $V_A =$        $H_D =$        $V_D =$

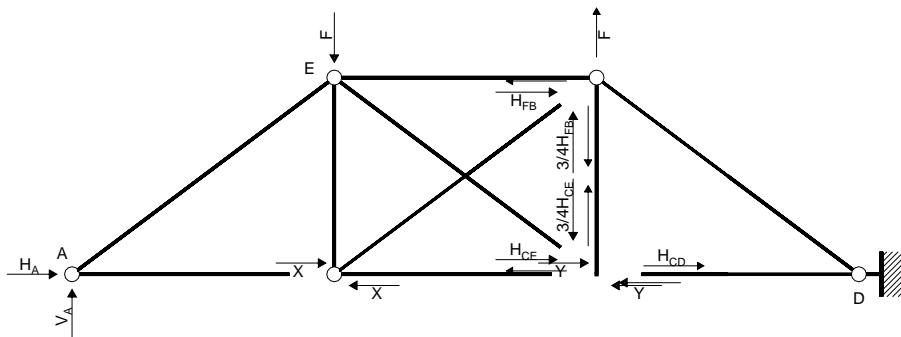
$N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{AE} =$        $N_{EC} =$        $N_{BF} =$        $N_{FD} =$

$N_{EF} =$        $N_{EB} =$        $N_{CF} =$

SPOSTAMENTI ASSOLUTI

$u_C =$

$v_C =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a D: aste DF FE FC EA EC EB AB BC BF

$$-12V_A b = -4Fb$$

Rotazione intorno a F: aste FE EA EC EB AB BC BF

$$3H_A b - 8V_A b + 3H_{CE} b = -3Yb - 4Fb$$

Rotazione intorno a F: aste FC

$$-3H_{CD} b - 3H_{CE} b = 3Yb$$

Rotazione intorno a E: aste EA AB

$$3H_A b - 4V_A b = -3Xb$$

Rotazione intorno a E: aste EB BC BF

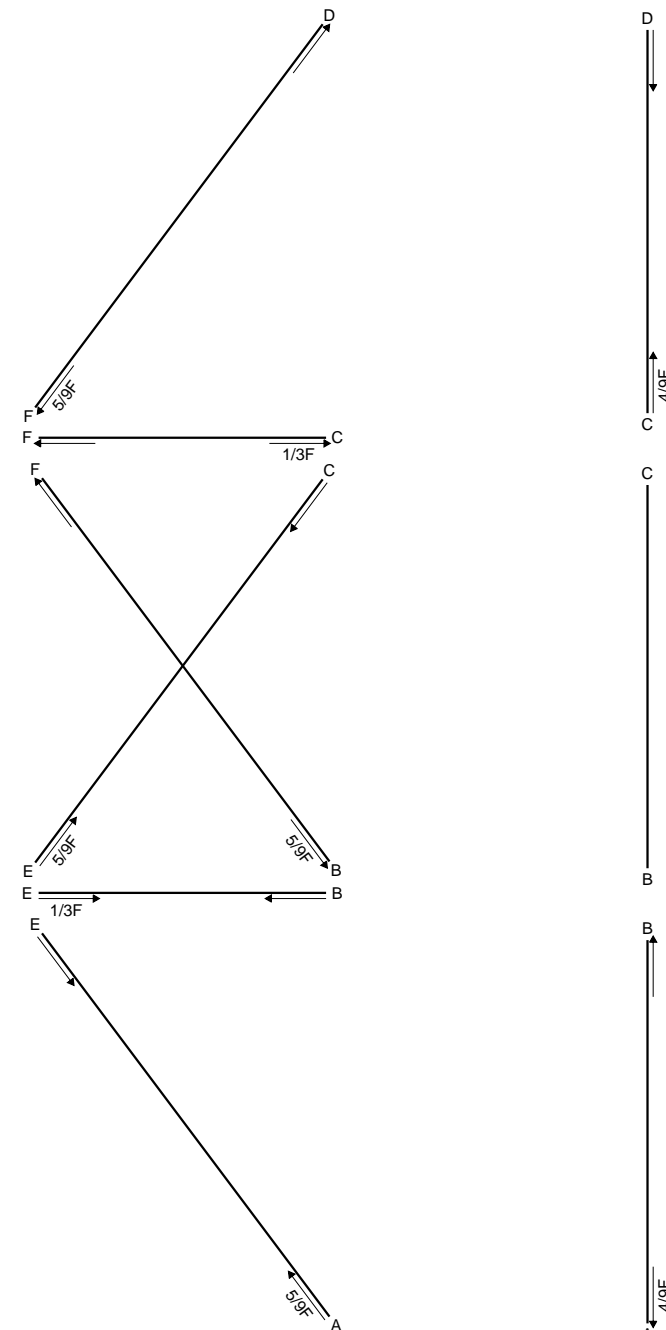
$$3H_{FB} b = 3Xb - 3Yb$$

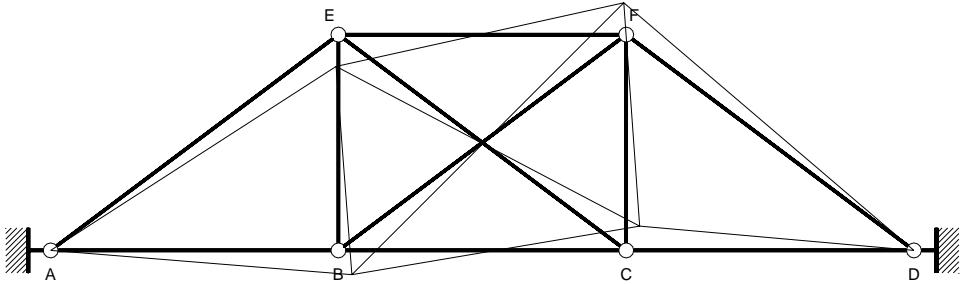
Matrice di equilibrio

$$\begin{bmatrix} H_A b & V_A b & H_{CD} b & H_{CE} b & H_{FB} b \\ \phi_{DF} & 0 & -12 & 0 & 0 & 0 \\ \phi_{FE} & 3 & -8 & 0 & 3 & 0 \\ \phi_{FC} & 0 & 0 & -3 & -3 & 0 \\ \phi_{EA} & 3 & -4 & 0 & 0 & 0 \\ \phi_{EB} & 0 & 0 & 0 & 0 & 3 \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & -4 \\ 0 & -3 & -4 \\ 0 & 3 & 0 \\ -3 & 0 & 0 \\ 3 & -3 & 0 \end{bmatrix}$$

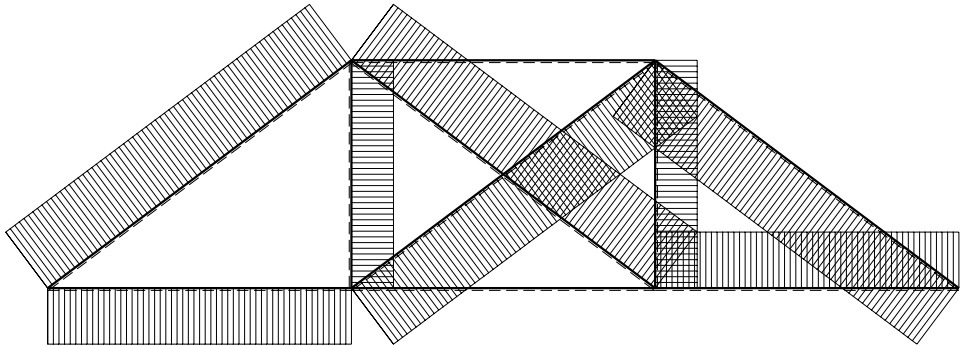
Soluzione del sistema

$$\begin{bmatrix} V_A b \\ H_A b \\ H_{CD} b \\ H_{CE} b \\ H_{FB} b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \\ 0 & 0 & 1/3 \\ -1 & 0 & 4/9 \\ -1 & 0 & 8/9 \\ 1 & -1 & -8/9 \\ 1 & -1 & 0 \end{bmatrix}$$





10 Fb/EA



← + → 0.6 F

REAZIONI

$H_A = 0$        $V_A = 1/3F$        $H_D = 0$        $V_D = -1/3F$

$N_{AB} = 4/9F$      $N_{BC} = 0$        $N_{CD} = -4/9F$      $N_{AE} = -5/9F$      $N_{EC} = -5/9F$      $N_{BF} = 5/9F$      $N_{FD} = 5/9F$

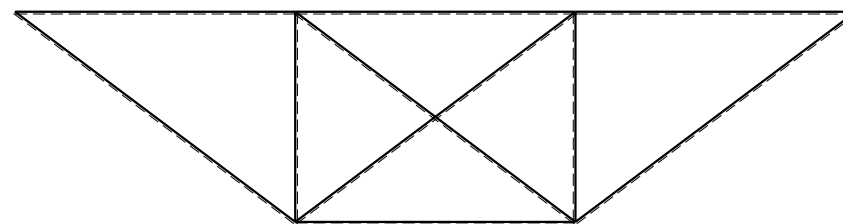
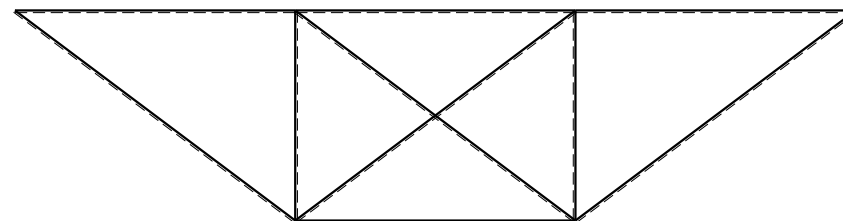
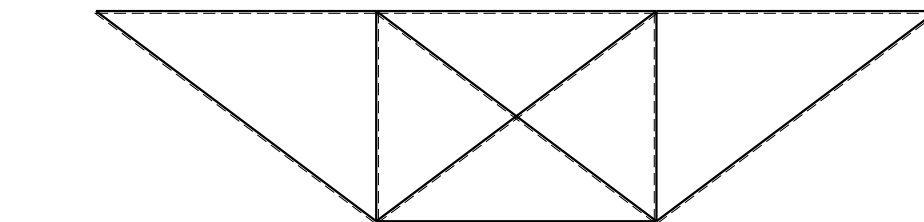
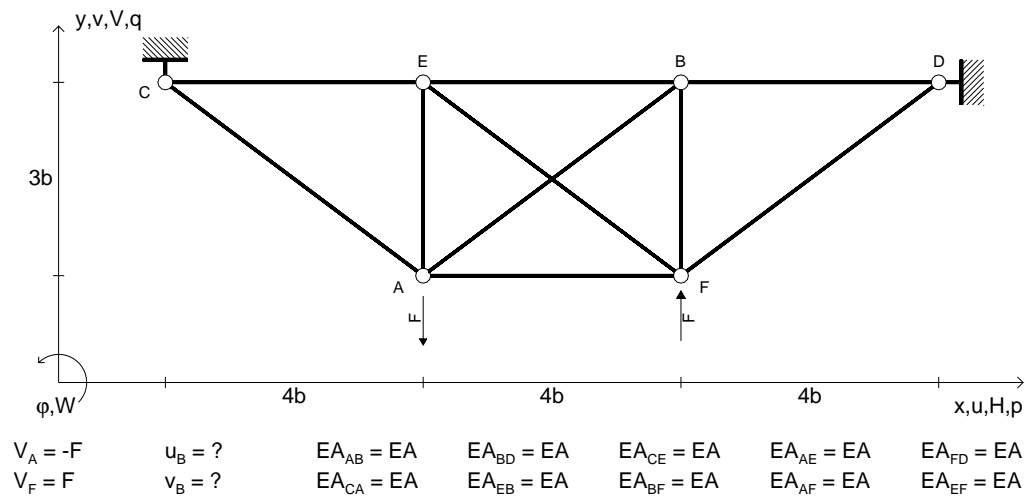
$N_{EF} = 0$        $N_{EB} = -1/3F$      $N_{CF} = 1/3F$

SPOSTAMENTI ASSOLUTI

$u_C = 16/9(Fb/EA)$

$v_C = 260/81(Fb/EA)$





Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

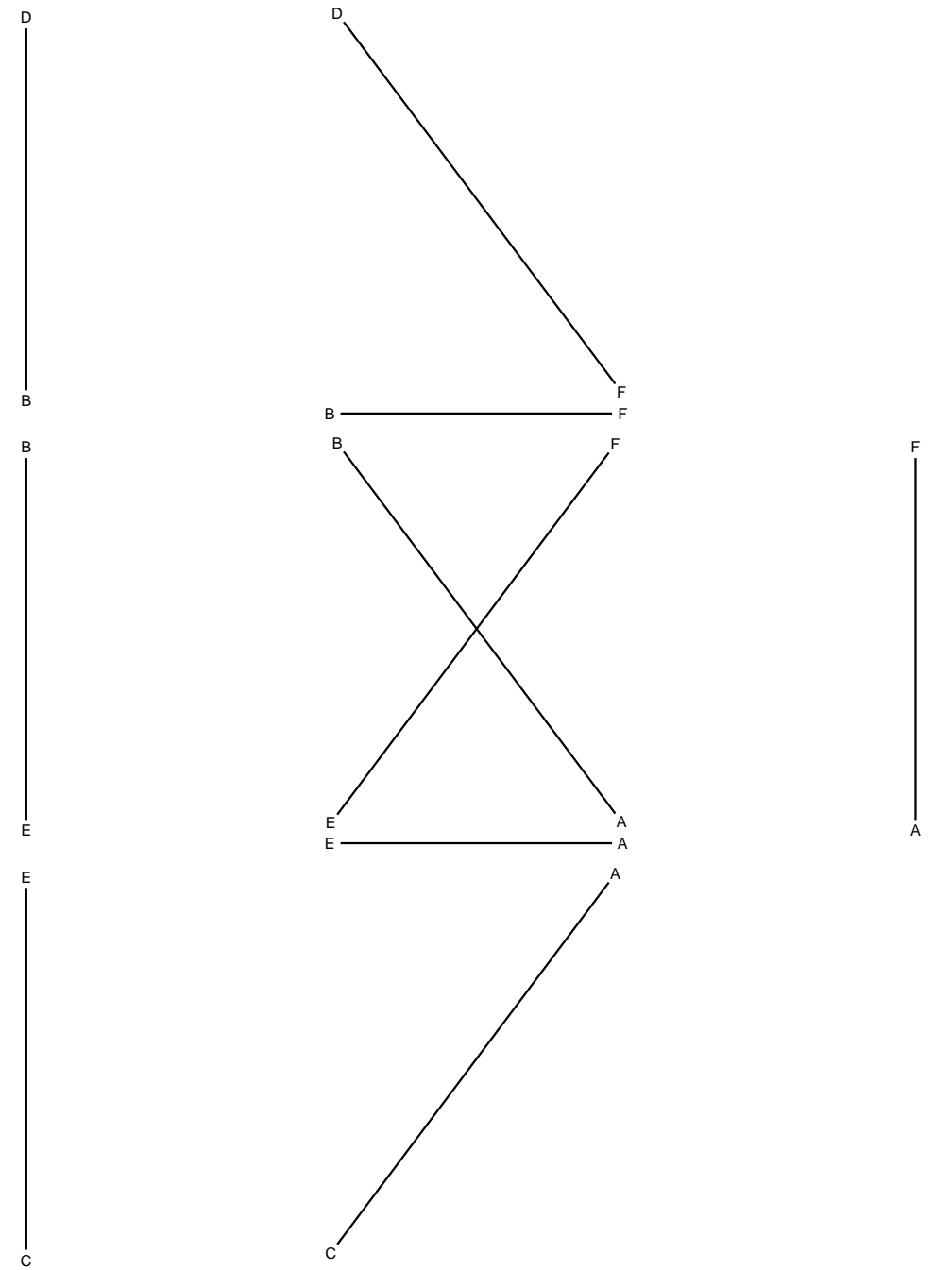
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo B

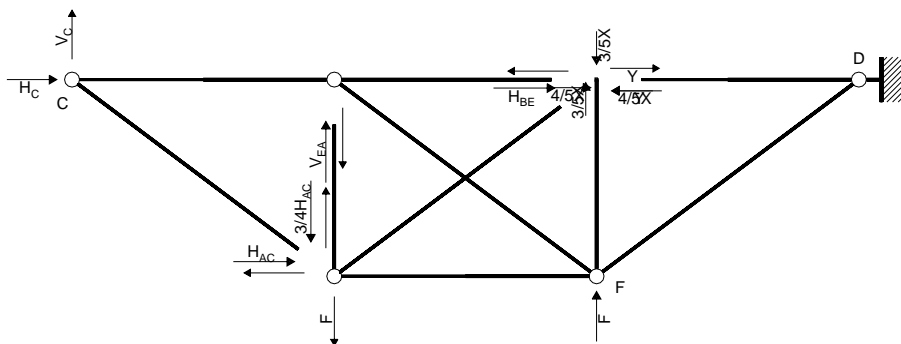
Calcolare lo spostamento verticale del nodo B

@ Adolfo Zavelani Rossi, Politecnico di Milano

@ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI  
 $H_C =$        $V_C =$        $H_D =$        $V_D =$   
 $N_{AB} =$        $N_{CA} =$        $N_{BD} =$        $N_{EB} =$        $N_{CE} =$        $N_{BF} =$        $N_{AE} =$   
 $N_{AF} =$        $N_{FD} =$        $N_{EF} =$   
SPOSTAMENTI ASSOLUTI  
 $u_B =$   
 $v_B =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a D: aste DF FB FA FE AB EB EC AE CA

$$-12V_Cb = -4Fb$$

Rotazione intorno a F: aste FB

$$3H_{BE}b = -12/5Xb - 3Yb$$

Rotazione intorno a F: aste FA AB AE

$$-3H_{AC}b - 4V_{EA}b = 12/5Xb - 4Fb$$

Rotazione intorno a F: aste FE EB EC CA

$$-3H_Cb - 8V_Cb + 3H_{AC}b - 3H_{BE}b + 4V_{EA}b = 0$$

Rotazione intorno a E: aste EC CA

$$-4V_Cb + 3H_{AC}b = 0$$

Matrice di equilibrio

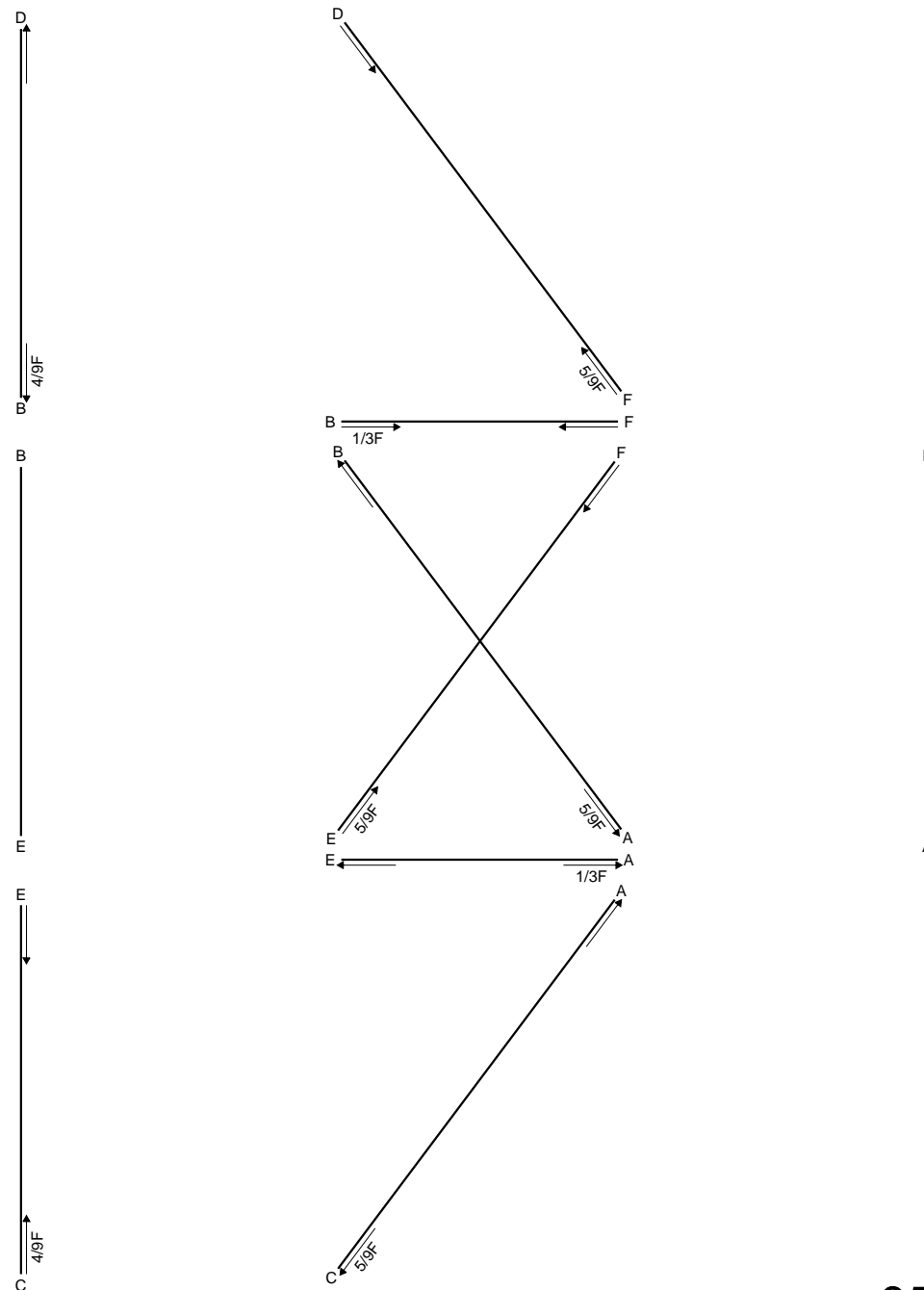
$$\begin{bmatrix} \phi_{DF} \\ \phi_{FB} \\ \phi_{FA} \\ \phi_{FE} \\ \phi_{EC} \end{bmatrix} \begin{bmatrix} H_Cb & V_Cb & H_{AC}b & H_{BE}b & V_{EA}b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \end{bmatrix}$$

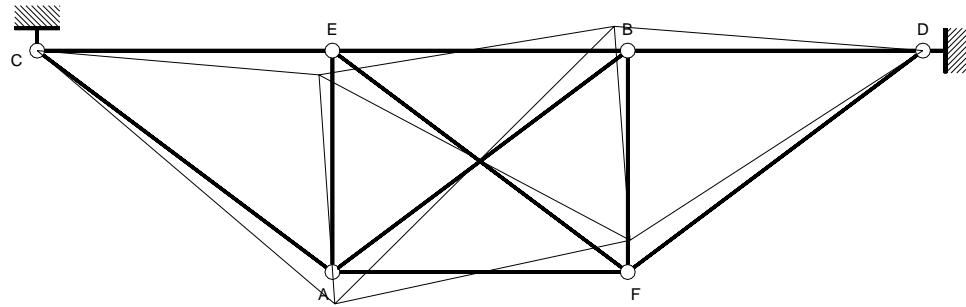
$$\begin{bmatrix} 0 & -12 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & -3 & 0 & -4 \\ -3 & -8 & 3 & -3 & 4 \\ 0 & -4 & 3 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & -4 \\ -12/5 & -3 & 0 \\ 12/5 & 0 & -4 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Soluzione del sistema

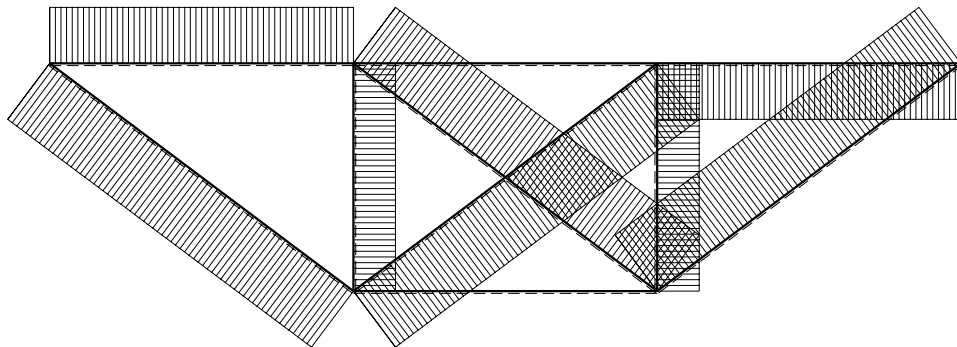
$$\begin{bmatrix} V_Cb \\ H_{BE}b \\ H_{AC}b \\ H_Cb \\ V_{EA}b \end{bmatrix} = \begin{bmatrix} Xb & Yb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 1/3 \\ -4/5 & -1 & 0 \\ 0 & 0 & 4/9 \\ 0 & 1 & 4/9 \\ -3/5 & 0 & 2/3 \end{bmatrix}$$





10 Fb/EA



← ⊕ → 0.6 F

## REAZIONI

$$H_C = 0 \quad V_C = 1/3F \quad H_D = 0 \quad V_D = -1/3F$$

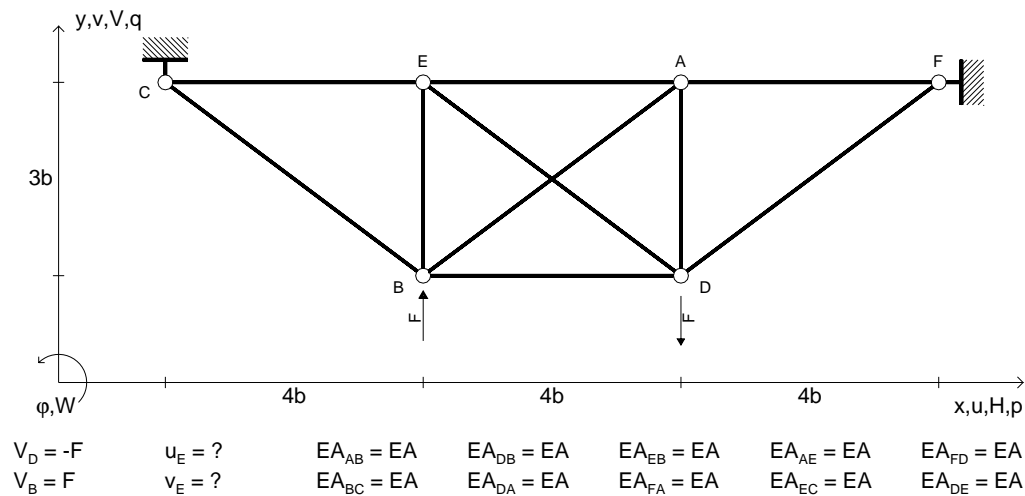
$$N_{AB} = 5/9F \quad N_{CA} = 5/9F \quad N_{BD} = 4/9F \quad N_{EB} = 0 \quad N_{CE} = -4/9F \quad N_{BF} = -1/3F \quad N_{AE} = 1/3F$$

$$N_{AF} = 0 \quad N_{FD} = -5/9F \quad N_{EF} = -5/9F$$

## SPOSTAMENTI ASSOLUTI

$$u_B = -16/9(Fb/EA)$$

$$v_B = 260/81(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

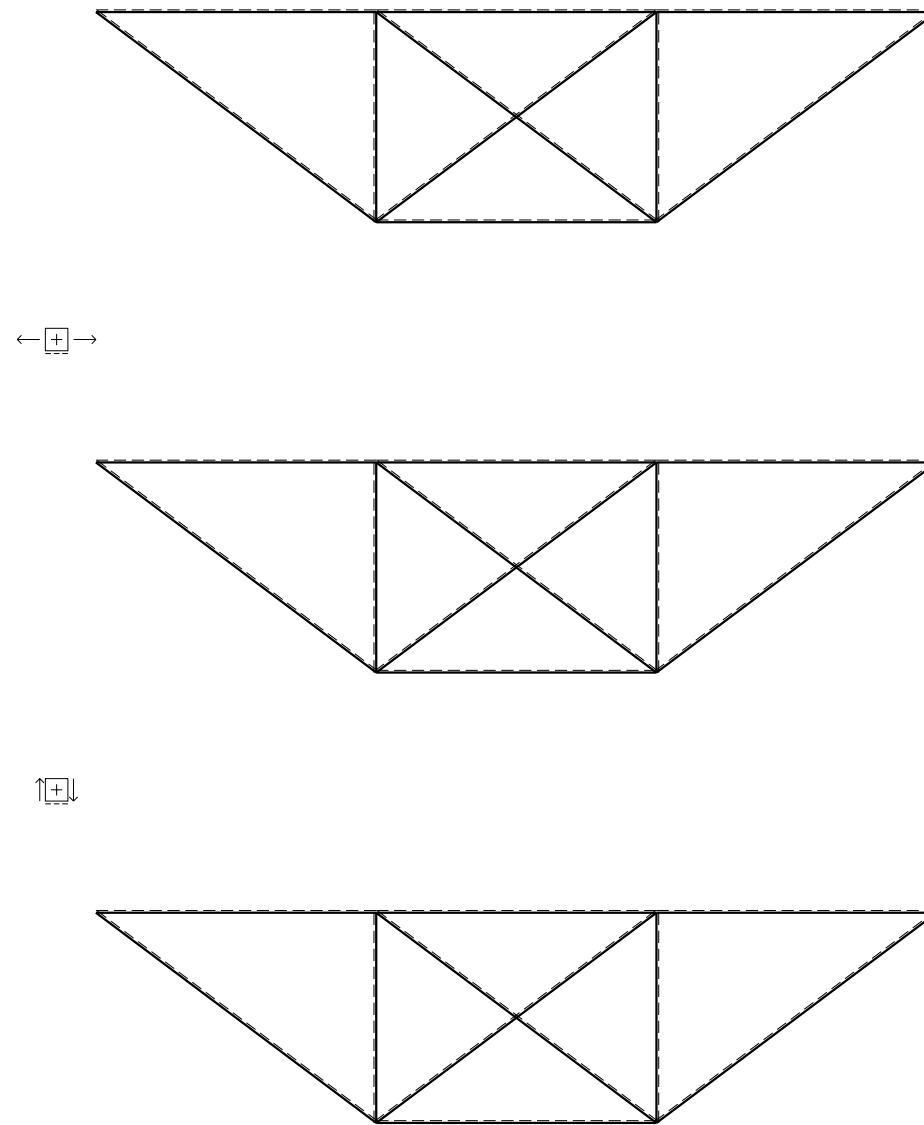
Tracciare i diagrammi delle azioni interne nelle aste.

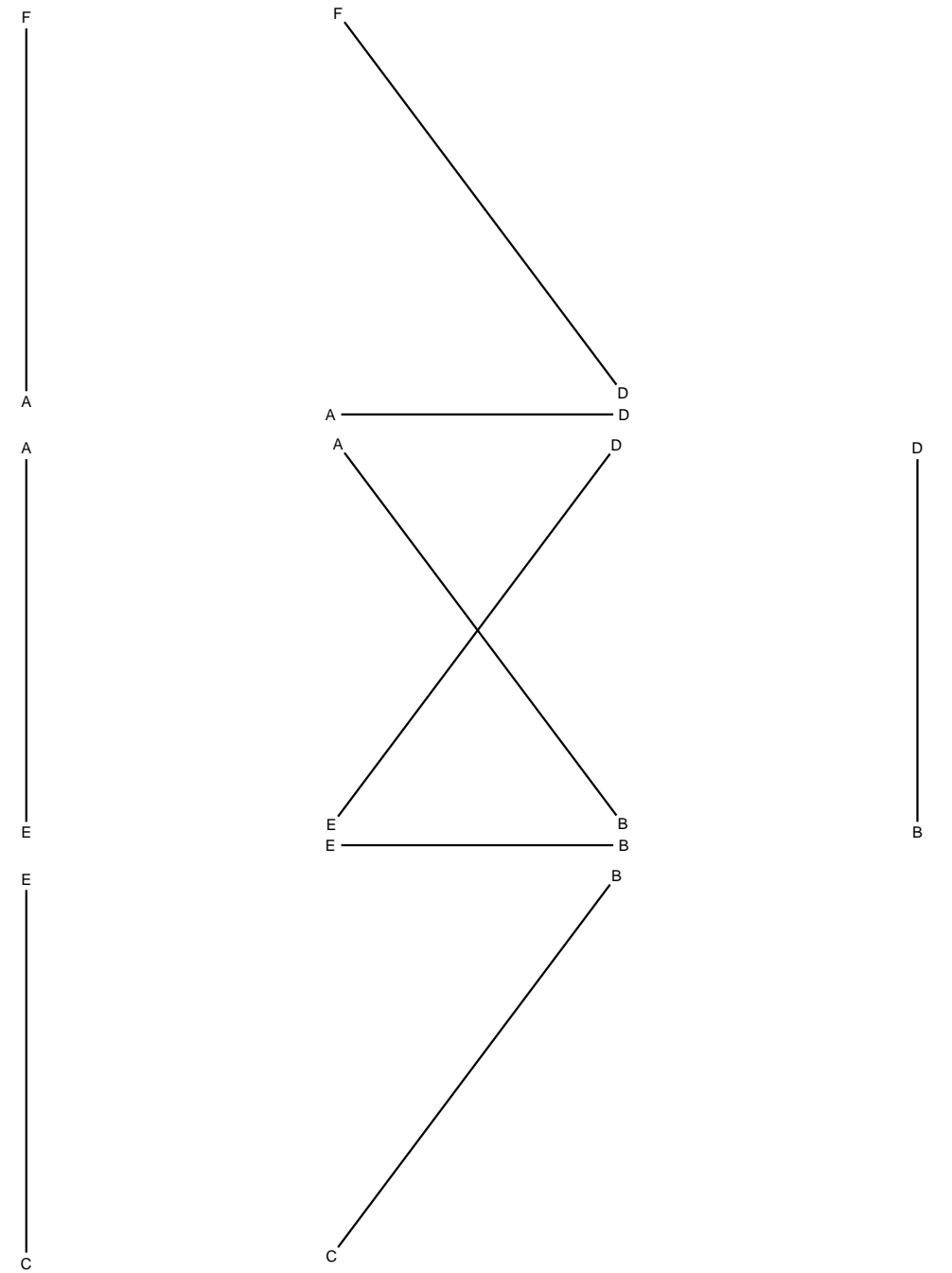
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo E

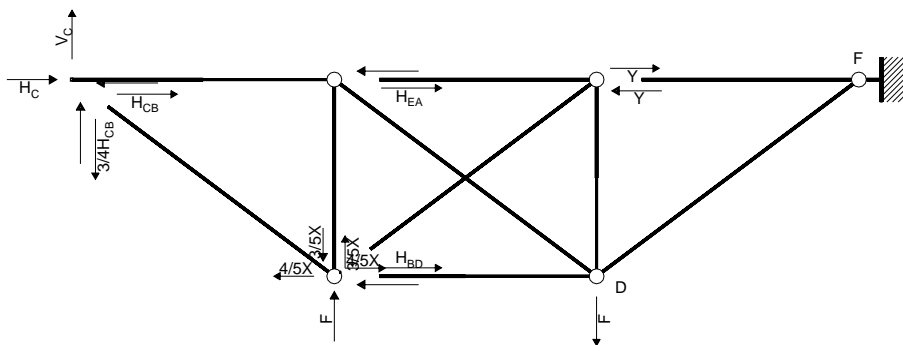
Calcolare lo spostamento verticale del nodo E

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REAZIONI  
 $H_C =$        $V_C =$        $H_F =$        $V_F =$   
 $N_{AB} =$        $N_{BC} =$        $N_{DB} =$        $N_{DA} =$        $N_{EB} =$        $N_{FA} =$        $N_{AE} =$   
 $N_{EC} =$        $N_{FD} =$        $N_{DE} =$   
SPOSTAMENTI ASSOLUTI  
 $u_E =$   
 $v_E =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DB DA DE AB EB AE EC BC

$$-12V_C b = 4Fb$$

Rotazione intorno a D: aste DA AB AE

$$-3H_{EA} b = 12/5 Xb - 3Yb$$

Rotazione intorno a D: aste DE EB EC BC

$$-3H_C b - 8V_C b + 3H_{EA} b = -12/5 Xb + 4Fb$$

Rotazione intorno a E: aste EB BC

$$3H_{CB} b - 3H_{BD} b = 12/5 Xb$$

Rotazione intorno a E: aste EC

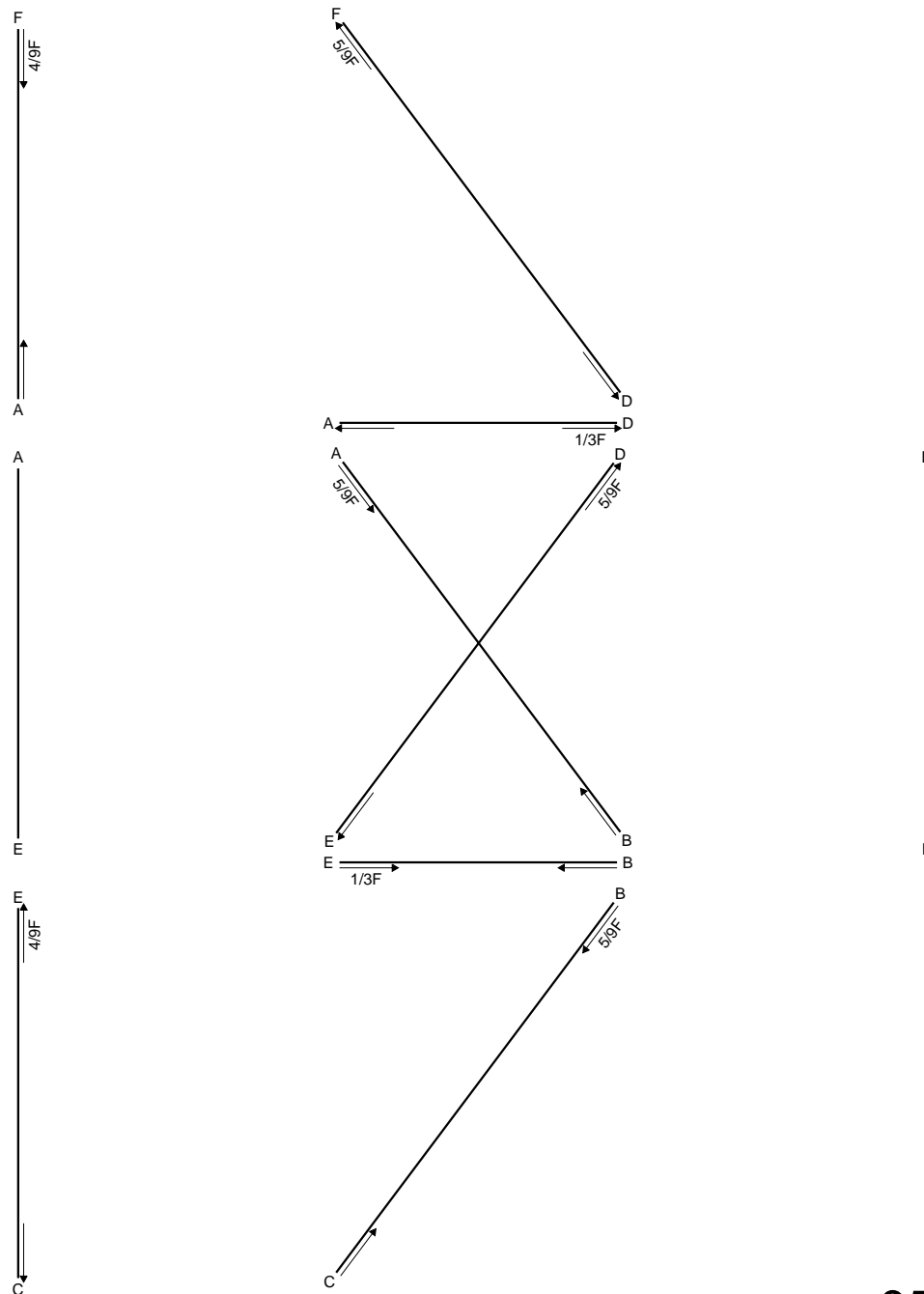
$$-4V_C b - 3H_{CB} b = 0$$

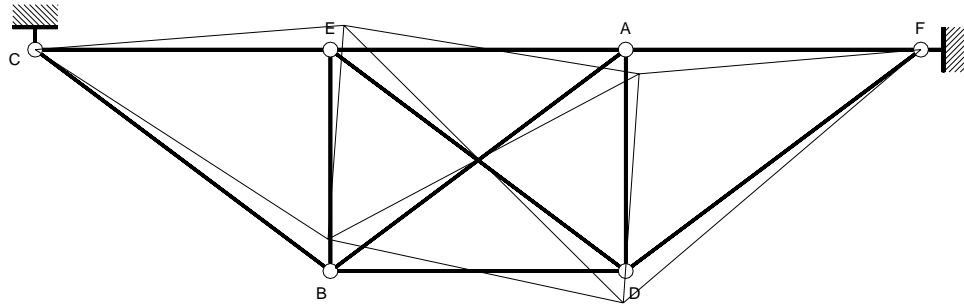
## Matrice di equilibrio

$$\begin{bmatrix} H_C b & V_C b & H_{CB} b & H_{BD} b & H_{EA} b \\ \phi_{FD} & 0 & -12 & 0 & 0 \\ \phi_{DA} & 0 & 0 & 0 & -3 \\ \phi_{DE} & -3 & -8 & 0 & 3 \\ \phi_{EB} & 0 & 0 & 3 & -3 \\ \phi_{EC} & 0 & -4 & -3 & 0 \end{bmatrix} \begin{bmatrix} Xb \\ Yb \\ Fb \end{bmatrix} = \begin{bmatrix} 0 \\ 12/5 \\ -12/5 \\ 12/5 \\ 0 \end{bmatrix}$$

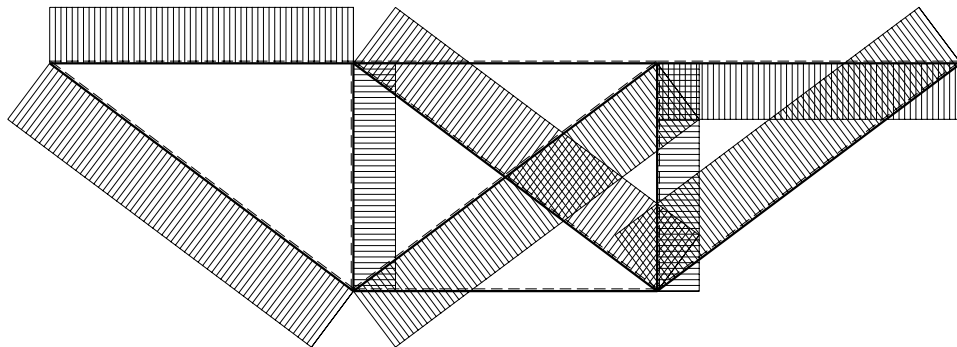
## Soluzione del sistema

$$\begin{bmatrix} V_C b \\ H_{EA} b \\ H_C b \\ H_{BD} b \\ H_{CB} b \end{bmatrix} = \begin{bmatrix} 0 & 0 & -1/3 \\ -4/5 & 1 & 0 \\ 0 & 1 & -4/9 \\ -4/5 & 0 & 4/9 \\ 0 & 0 & 4/9 \end{bmatrix} \begin{bmatrix} Xb \\ Yb \\ Fb \end{bmatrix}$$





10 Fb/EA



0.6 F

## REAZIONI

$$H_C = 0 \quad V_C = -1/3F \quad H_F = 0 \quad V_F = 1/3F$$

$$N_{AB} = -5/9F \quad N_{BC} = -5/9F \quad N_{DB} = 0 \quad N_{DA} = 1/3F \quad N_{EB} = -1/3F \quad N_{FA} = -4/9F \quad N_{AE} = 0$$

$$N_{EC} = 4/9F \quad N_{FD} = 5/9F \quad N_{DE} = 5/9F$$

## SPOSTAMENTI ASSOLUTI

$$u_E = 16/9(Fb/EA)$$

$$v_E = 260/81(Fb/EA)$$