

- \*Svolgere e riportare su questo foglio l'analisi cinematica.
- \*Riportare le reazioni vincolari finali in forma grafica e analitica.
- \*Riportare i diagrammi quotati delle azioni interne.
- \*Indicare chiaramente i sistemi di riferimento adottati per le espressioni della linea elastica
- \*Allegare l'elaborato.

Carichi e deformazioni date hanno verso efficace in disegno.  
Calcolare reazioni vincolari della struttura e delle aste.  
Tracciare i diagrammi quotati delle azioni interne nelle aste.  
Esprimere la linea elastica delle aste. AB CD BC  
 $J_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Indicare il verso del riferimento locale AB oppure BA

AB BA  $y(x)EI=$

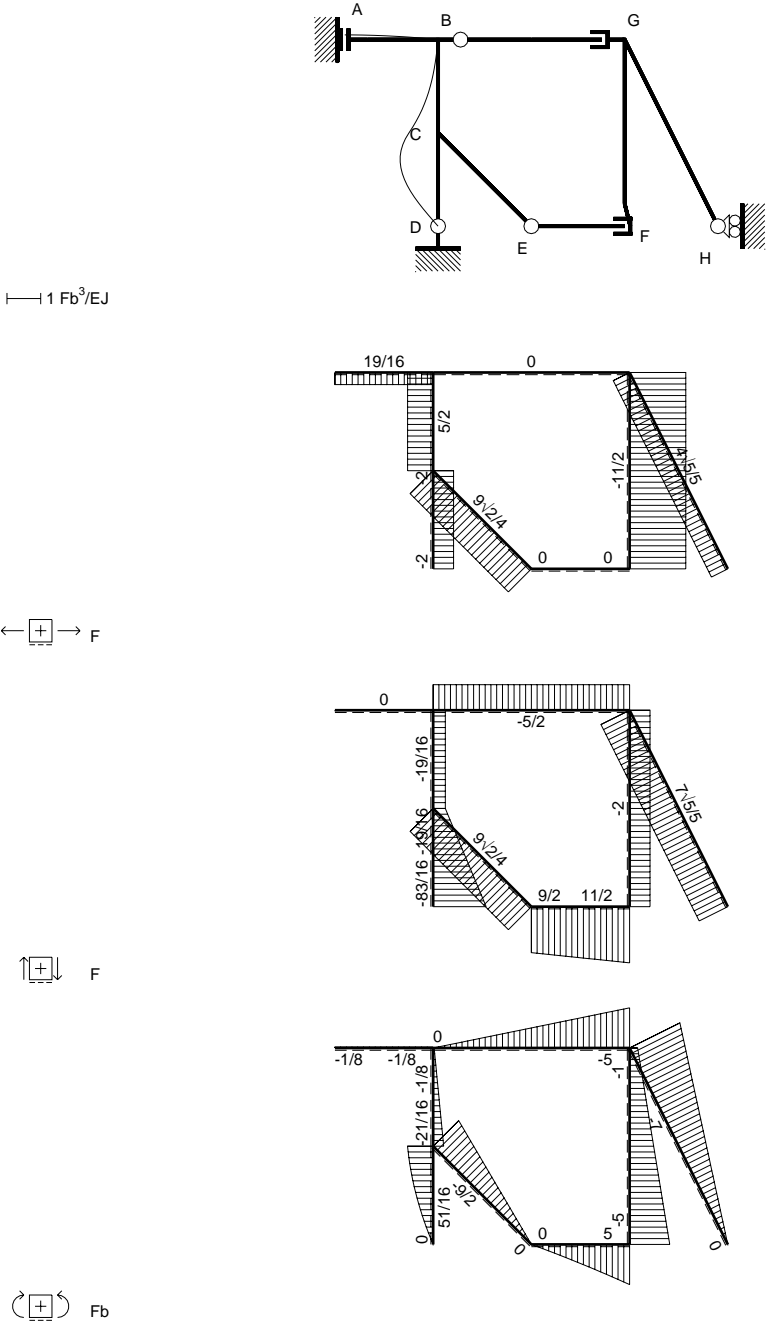
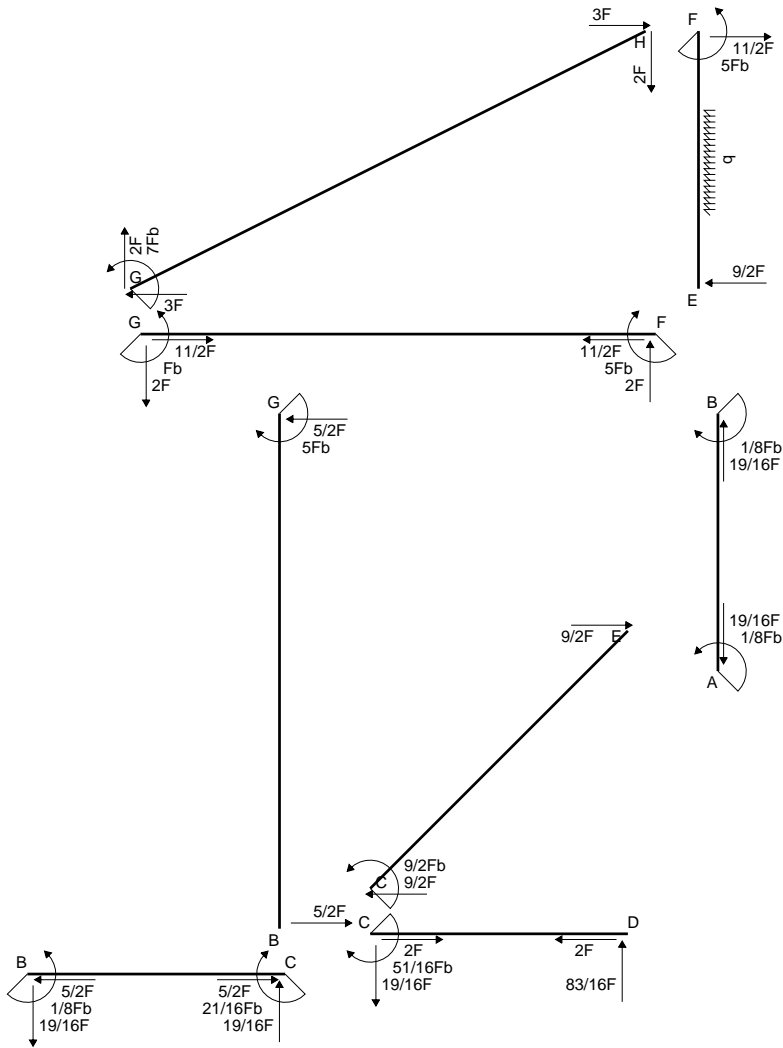
CD DC  $y(x)EI=$

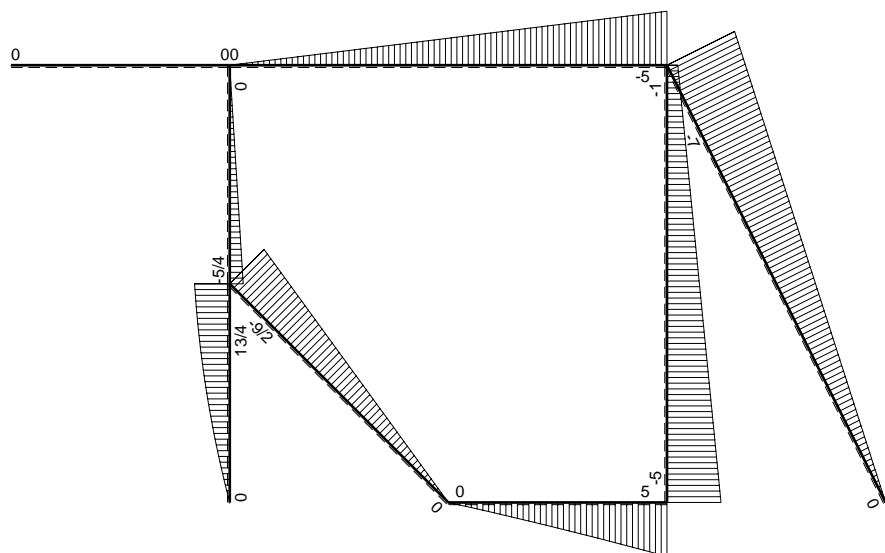
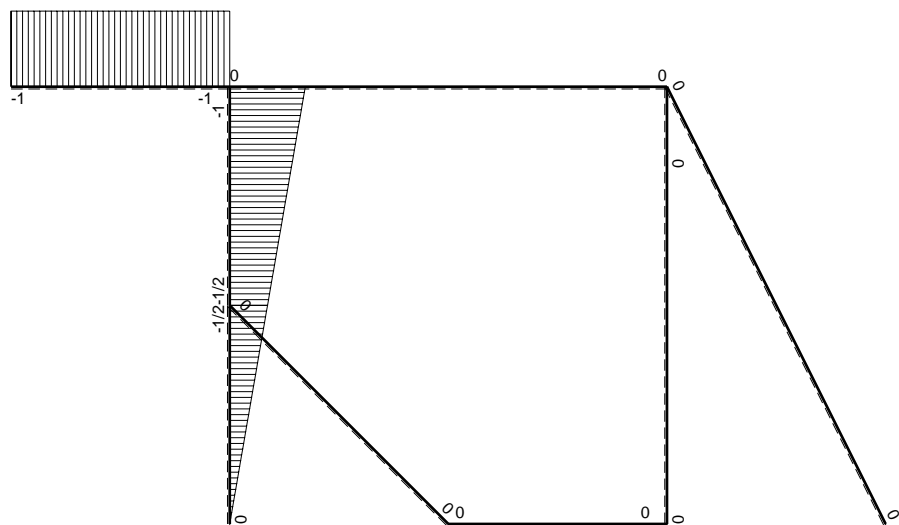
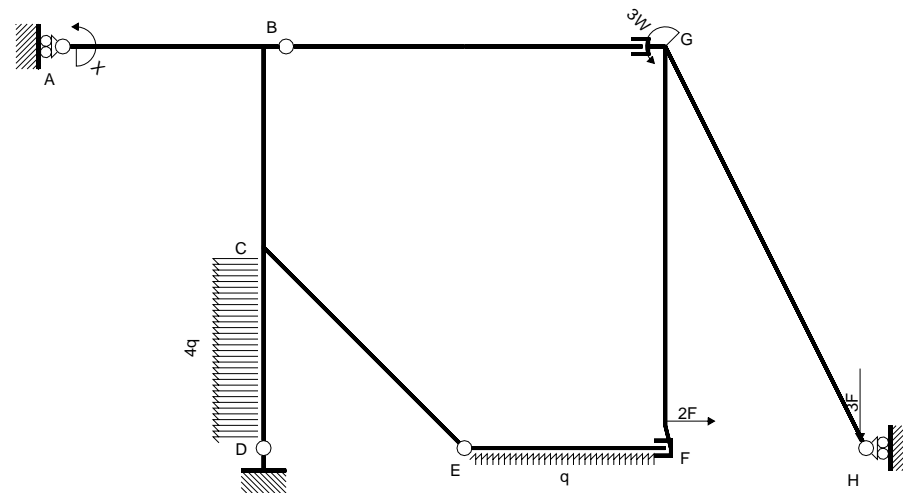
BC CB  $y(x)EI=$

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Azione flettente  $M_0$ Azione flettente  $M_x$ 

Calcolo iperstatico

REAZIONI IPERSTATICHE

$$X = W_{AB}$$

DETERMINAZIONE DELLA DEFORMATA ELASTICA

Costanti di integrazione:  $\varphi_{AB}$   $K_{AB}$   $\varphi_{CD}$   $K_{CD}$   $\varphi_{BC}$   $K_{BC}$ 

Relazioni di congruenza

$$y'_{AB}(0) = 0$$

$$y'_{AB}(b) - y'_{BC}(0) = 0$$

$$y'_{CD}(0) - y'_{BC}(b) = 0$$

$$y_{AB}(b) = 0$$

$$y_{CD}(b) = 0$$

$$y_{BC}(0) = 0$$

$$y_{BC}(b) - y_{CD}(0) = 0$$

$$M_{AB} = -X$$

$$EJy''_{AB} = -X$$

$$EJy'_{AB} = -Xx + EJ\varphi_{AB}$$

$$EJy_{AB} = -1/2Xx^2 + EJ\varphi_{AB}x + EJK_{AB}$$

$$M_{BA} = X$$

$$EJy''_{BA} = X$$

$$EJy'_{BA} = Xx + EJ\varphi_{BA}$$

$$EJy_{BA} = 1/2Xx^2 + EJ\varphi_{BA}x + EJK_{BA}$$

$$\begin{aligned}
 M_{CD} &= -5/4Fx + 13/4Fb - 2qx^2 + 1/2Xx/b - 1/2X \\
 EJy''_{CD} &= -5/4Fx + 13/4Fb - 2qx^2 + 1/2Xx/b - 1/2X \\
 EJy'_{CD} &= -5/8Fx^2 + 13/4Fbx - 2/3qx^3 + 1/4Xx^2/b - 1/2Xx + EJ\varphi_{CD} \\
 EJy_{CD} &= -5/24Fx^3 + 13/8Fbx^2 - 1/6qx^4 + 1/12Xx^3/b - 1/4Xx^2 + EJ\varphi_{CD}x + EJK_{CD}
 \end{aligned}$$

$$\begin{aligned}
 M_{DC} &= -21/4Fx + 2qx^2 + 1/2Xx/b \\
 EJy''_{DC} &= -21/4Fx + 2qx^2 + 1/2Xx/b \\
 EJy'_{DC} &= -21/8Fx^2 + 2/3qx^3 + 1/4Xx^2/b + EJ\varphi_{DC} \\
 EJy_{DC} &= -7/8Fx^3 + 1/6qx^4 + 1/12Xx^3/b + EJ\varphi_{DC}x + EJK_{DC}
 \end{aligned}$$

$$\begin{aligned}
 M_{BC} &= -5/4Fx + 1/2Xx/b - X \\
 EJy''_{BC} &= -5/4Fx + 1/2Xx/b - X \\
 EJy'_{BC} &= -5/8Fx^2 + 1/4Xx^2/b - Xx + EJ\varphi_{BC} \\
 EJy_{BC} &= -5/24Fx^3 + 1/12Xx^3/b - 1/2Xx^2 + EJ\varphi_{BC}x + EJK_{BC}
 \end{aligned}$$

$$\begin{aligned}
 M_{CB} &= -5/4Fx + 5/4Fb + 1/2Xx/b + 1/2X \\
 EJy''_{CB} &= -5/4Fx + 5/4Fb + 1/2Xx/b + 1/2X \\
 EJy'_{CB} &= -5/8Fx^2 + 5/4Fbx + 1/4Xx^2/b + 1/2Xx + EJ\varphi_{CB} \\
 EJy_{CB} &= -5/24Fx^3 + 5/8Fbx^2 + 1/12Xx^3/b + 1/4Xx^2 + EJ\varphi_{CB}x + EJK_{CB}
 \end{aligned}$$

Condizioni al contorno

$$\begin{aligned}
 & \begin{bmatrix} \varphi_{AB}b & K_{AB} & \varphi_{CD}b & K_{CD} & \varphi_{BC}b & K_{BC} & Xb^2/EJ \end{bmatrix} \begin{bmatrix} Fb^3/EJ \end{bmatrix} \\
 y'_{AB} & \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \\
 y'_{BA} & \begin{bmatrix} 1 & 0 & 0 & 0 & -1 & 0 & -1 \end{bmatrix} \\
 y'_{CD} & \begin{bmatrix} 0 & 0 & 1 & 0 & -1 & 0 & 3/4 \end{bmatrix} \\
 y_{BA} & \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & -1/2 \end{bmatrix} \\
 y_{DC} & \begin{bmatrix} 0 & 0 & 1 & 1 & 0 & 0 & -1/6 \end{bmatrix} \\
 y_{BC} & \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} \\
 y_{CB} & \begin{bmatrix} 0 & 0 & 0 & -1 & 1 & 1 & -5/12 \end{bmatrix}
 \end{aligned} = \begin{bmatrix} 0 \\ 0 \\ -5/8 \\ 0 \\ -5/4 \\ 0 \\ 5/24 \end{bmatrix}$$

Soluzione

$$\begin{aligned}
 & \begin{bmatrix} \varphi_{AB}b \\ \varphi_{BC}b \\ \varphi_{CD}b \\ K_{AB} \\ K_{CD} \\ K_{BC} \\ Xb^2/EJ \end{bmatrix} = \begin{bmatrix} 0 \\ -1/8 \\ -27/32 \\ 1/16 \\ -37/96 \\ 0 \\ 1/8 \end{bmatrix}
 \end{aligned}$$

$$\begin{aligned}
 K_{BA} &= 0 & \varphi_{BA} &= -1/8Fb^2/EJ \\
 K_{DC} &= 0 & \varphi_{DC} &= 13/12Fb^2/EJ \\
 K_{CB} &= 37/96Fb^3/EJ & \varphi_{CB} &= -27/32Fb^2/EJ
 \end{aligned}$$

DEFORMATA (coordinate locali)

$$\begin{aligned}
 AB \ y(x)EJ &= 1/16Fb^3 - 1/16x^2Fb \\
 BA \ y(x)EJ &= 1/8xFb^2 - 1/16x^2Fb \\
 CD \ y(x)EJ &= -37/96Fb^3 - 27/32xFb^2 + 51/32x^2Fb - 19/96x^3F - 1/6x^4q \\
 DC \ y(x)EJ &= -13/12xFb^2 + 83/96x^3F - 1/6x^4q
 \end{aligned}$$

$$\begin{aligned}
 BC \ y(x)EJ &= -1/8xFb^2 - 1/16x^2Fb - 19/96x^3F \\
 CB \ y(x)EJ &= -37/96Fb^3 + 27/32xFb^2 - 21/32x^2Fb + 19/96x^3F
 \end{aligned}$$