

Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

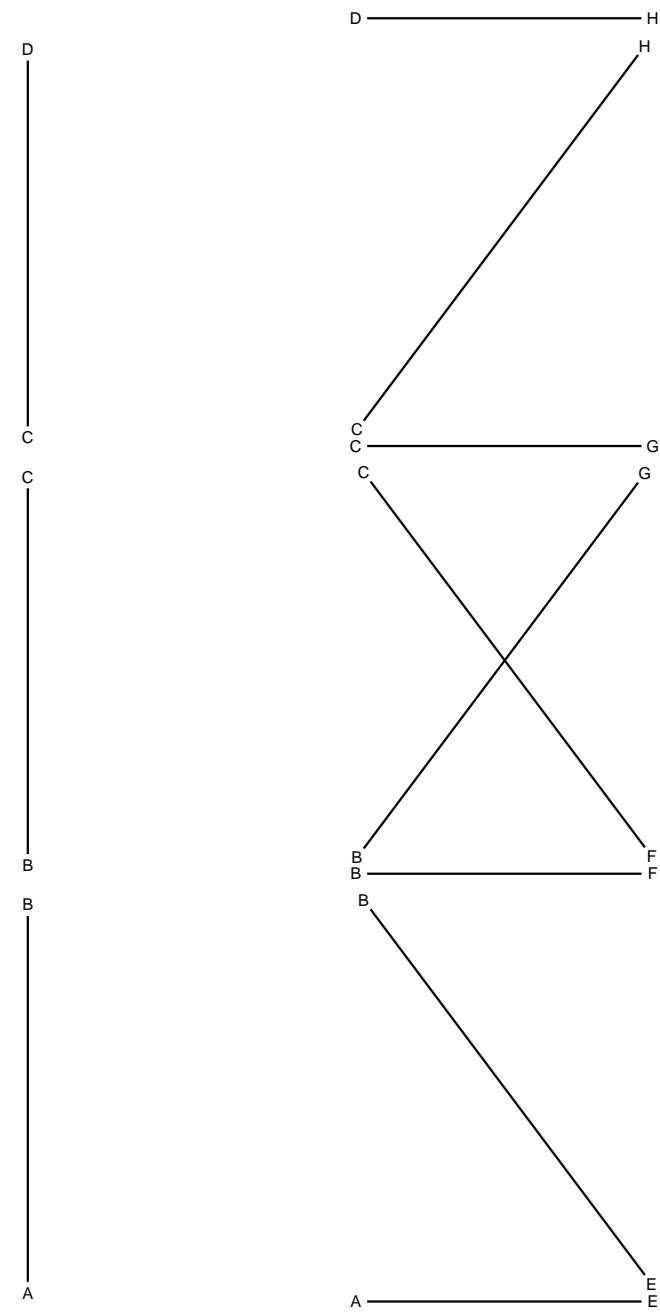
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

@ Adolfo Zavelani Rossi, Politecnico di Milano

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REAZIONI

$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{EB} =$        $N_{FC} =$        $N_{BG} =$

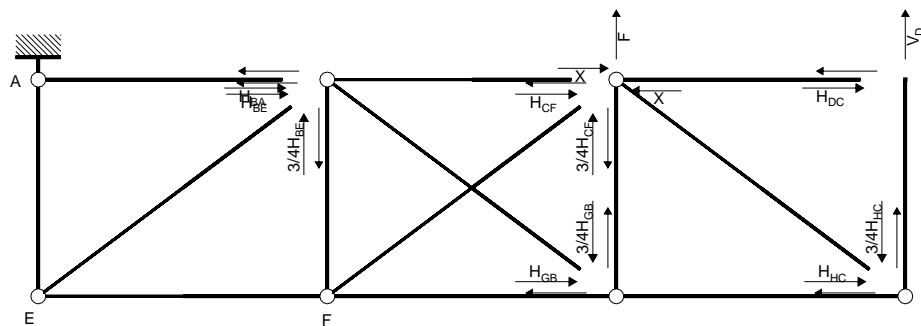
$N_{CH} =$        $N_{EF} =$        $N_{FG} =$        $N_{GH} =$        $N_{EA} =$        $N_{FB} =$

$N_{CG} =$        $N_{DH} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b = -8Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b + 3H_{BA} b = -8Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$8V_{D_b} + 3H_{GB_b} = -3X_b - 4F_b$$

Rotazione intorno a F: aste FB BC BG

$$3H_{BA}b + 3H_{BF}b - 3H_{GB}b = 3Xb$$

Rotazione intorno a G: aste GH HD

$$4V_{Db} + 3H_{DGb} + 3H_{HGb} = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC}b + 3H_{CF}b - 3H_{HC}b = -3Xb$$

Rotazione intorno a H: aste HD

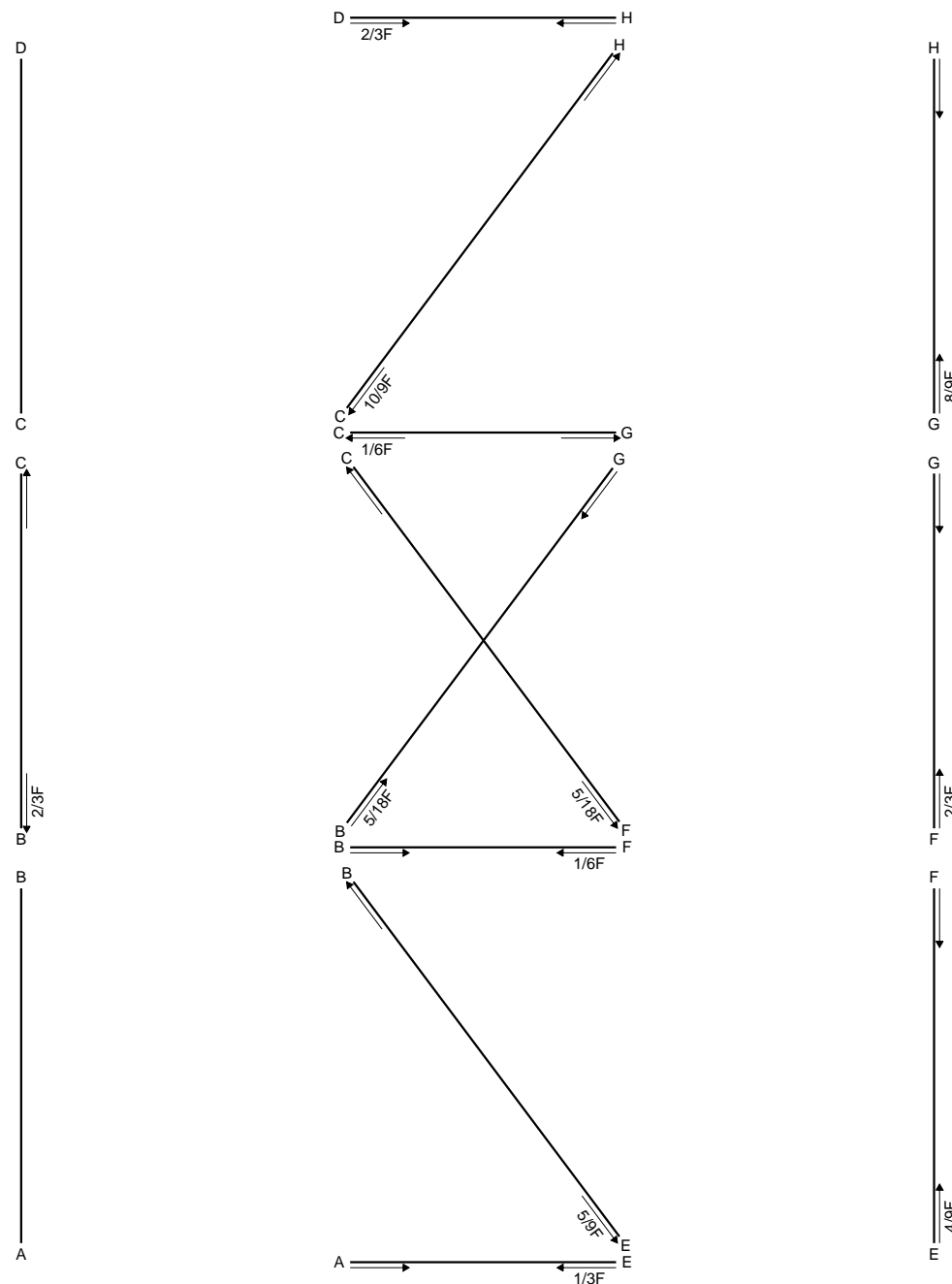
$$3H_{DC}b = 0$$

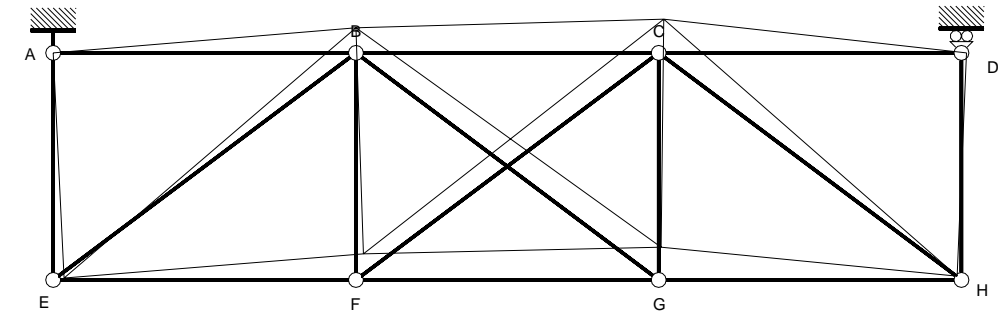
### Matrice di equilibrio

$$\begin{bmatrix} \Phi_{AE} & \Phi_{EF} & \Phi_{FG} & \Phi_{FB} & \Phi_{GH} & \Phi_{GC} & \Phi_{HD} \end{bmatrix} \begin{bmatrix} V_D & H_{BA} & H_{DC} & H_{BE} & H_{CF} & H_{GB} & H_{HC} \end{bmatrix} = \begin{bmatrix} X_B & F_B \end{bmatrix}$$

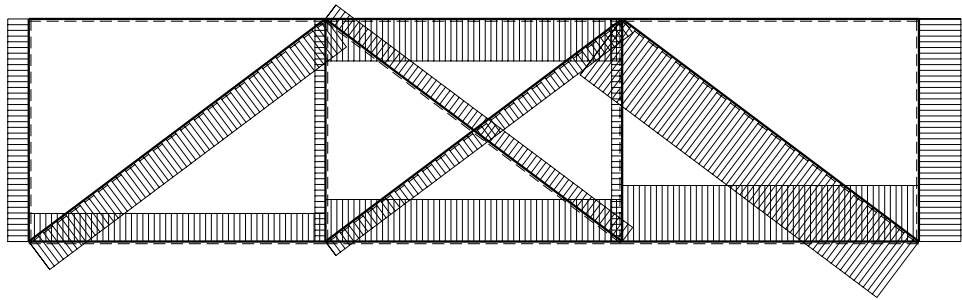
### Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} \text{Xb} & \text{Fb} \\ 0 & -2/3 \\ 0 & 0 \\ -1 & 4/9 \\ 0 & 4/9 \\ 0 & 0 \\ -1 & 8/9 \\ 0 & 8/9 \end{bmatrix}$$





1 40 Fb/EA



← ⊕ → 1 1.2 F

REAZIONI

$H_A = 0$        $V_A = -1/3F$        $V_D = -2/3F$

$N_{AB} = 0$        $N_{BC} = 2/3F$        $N_{CD} = 0$        $N_{EB} = 5/9F$        $N_{FC} = 5/18F$        $N_{BG} = -5/18F$

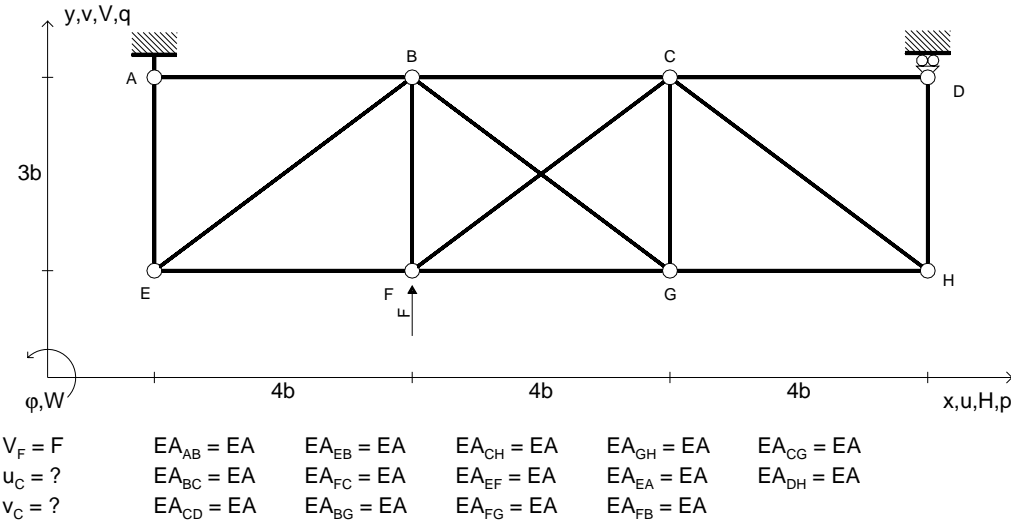
$N_{CH} = 10/9F$        $N_{EF} = -4/9F$        $N_{FG} = -2/3F$        $N_{GH} = -8/9F$        $N_{EA} = -1/3F$        $N_{FB} = -1/6F$

$N_{CG} = 1/6F$        $N_{DH} = -2/3F$

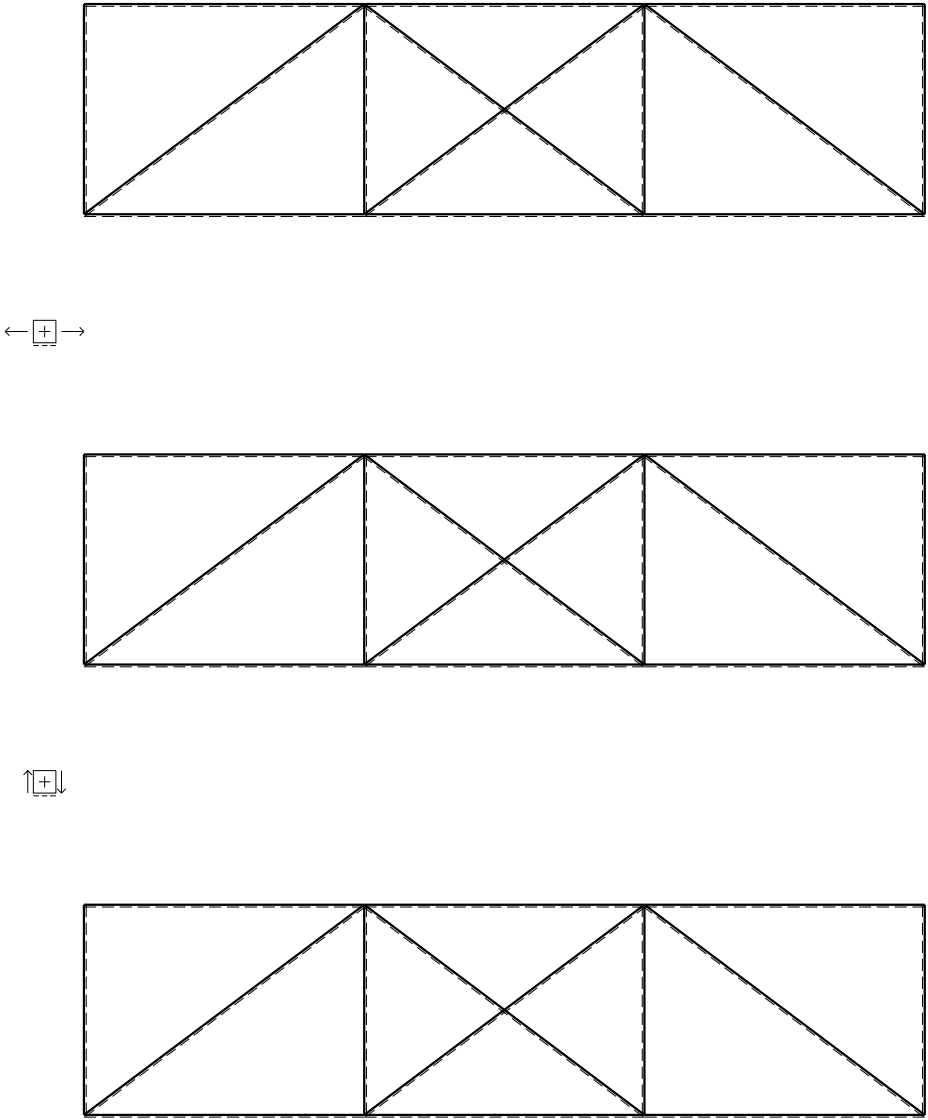
SPOSTAMENTI ASSOLUTI

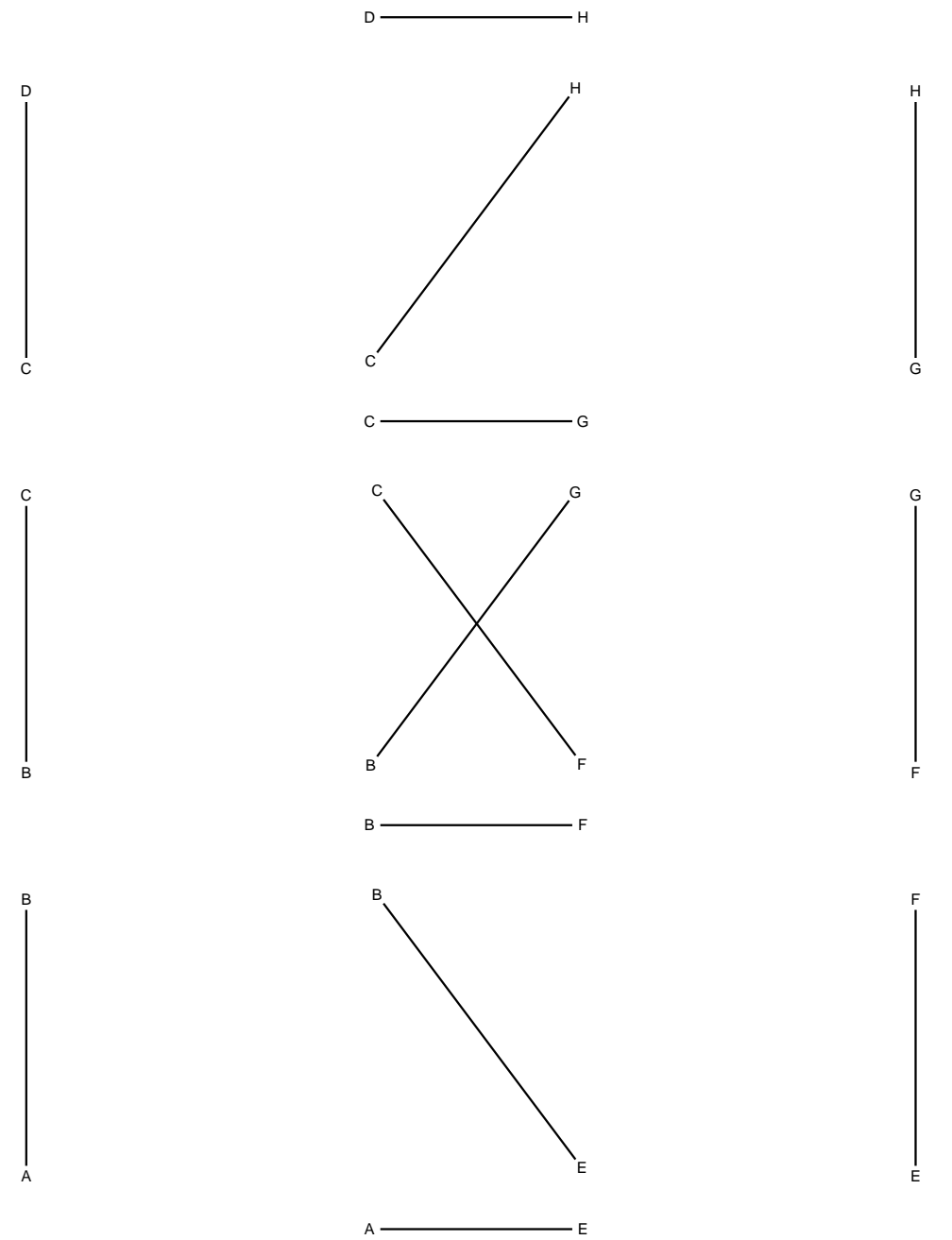
$u_F = 107/27(Fb/EA)$

$v_F = 2233/162(Fb/EA)$



Svolgere l'analisi cinematica.  
Riportare la soluzione su questo foglio.  
Carichi e deformazioni date hanno verso efficace in disegno.  
Calcolare reazioni vincolari della struttura e delle aste.  
Tracciare i diagrammi delle azioni interne nelle aste.  
 $A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.  
Calcolare lo spostamento orizzont. del nodo C  
Calcolare lo spostamento verticale del nodo C  
@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

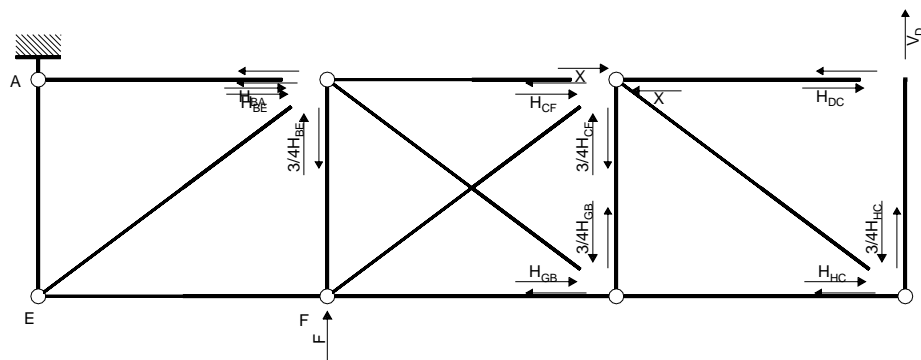
$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EB} =$	$N_{FC} =$
$N_{BG} =$	$N_{CH} =$	$N_{EF} =$	$N_{FG} =$	$N_{GH} =$
$N_{EA} =$	$N_{FB} =$	$N_{CG} =$	$N_{DH} =$	

SPOSTAMENTI ASSOLUTI

$u_C =$

$v_C =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b = -4Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b + 3H_{BA} b = -4Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$8V_D b + 3H_{GB} b = -3Xb$$

Rotazione intorno a G: aste FB BC BG

$$3H_{BA} b + 3H_{BE} b - 3H_{GB} b = 3Xb$$

Rotazione intorno a H: aste GH HD

$$4V_D b + 3H_{DC} b + 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC} b + 3H_{CF} b - 3H_{HC} b = -3Xb$$

Rotazione intorno a H: aste HD

$$3H_{DC} b = 0$$

## Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EF} \\ \phi_{FG} \\ \phi_{FB} \\ \phi_{GH} \\ \phi_{GC} \\ \phi_{HD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{DC} b & H_{BE} b & H_{CF} b & H_{GB} b & H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

## Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

D

C

B

A

D

H

C

G

B

F

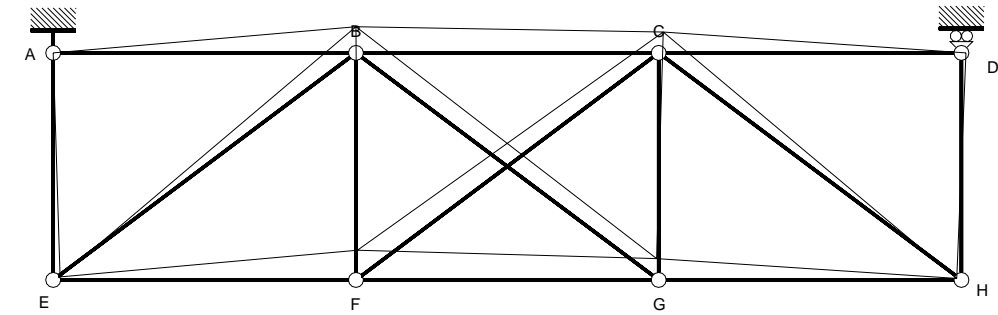
A

H

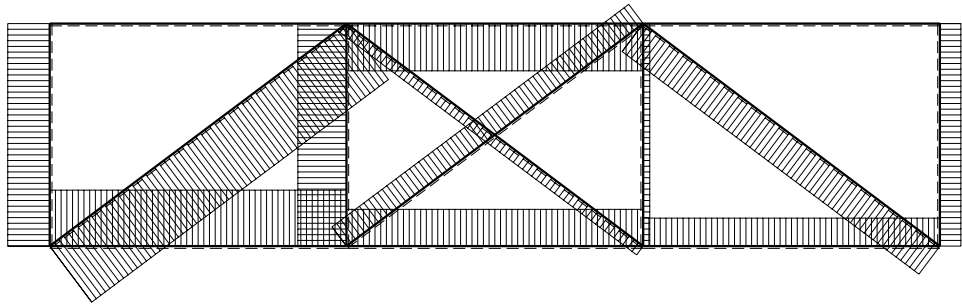
G

F

E



50 Fb/EA



1.2 F

REAZIONI

$H_A = 0$        $V_A = -2/3F$        $V_D = -1/3F$

$N_{AB} = 0$        $N_{BC} = 3/4F$        $N_{CD} = 0$        $N_{EB} = 10/9F$        $N_{FC} = -55/144F$

$N_{BG} = 25/144F$        $N_{CH} = 5/9F$        $N_{EF} = -8/9F$        $N_{FG} = -7/12F$        $N_{GH} = -4/9F$

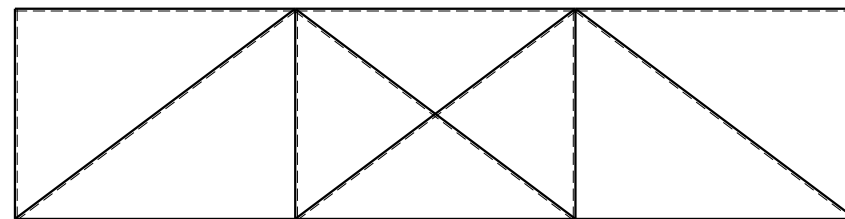
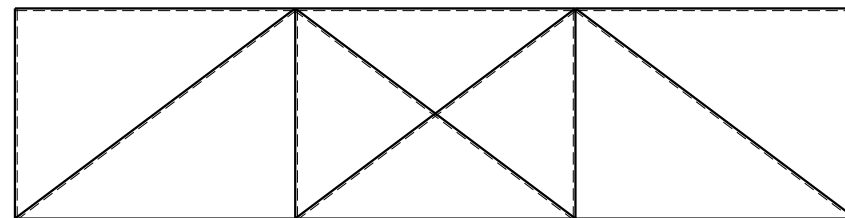
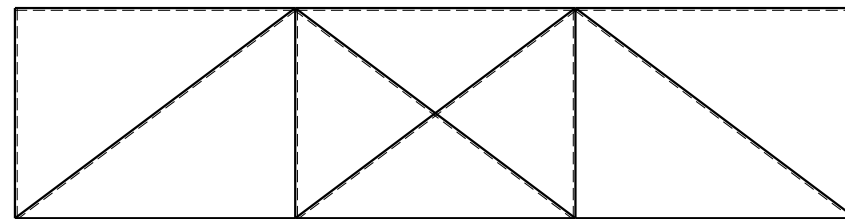
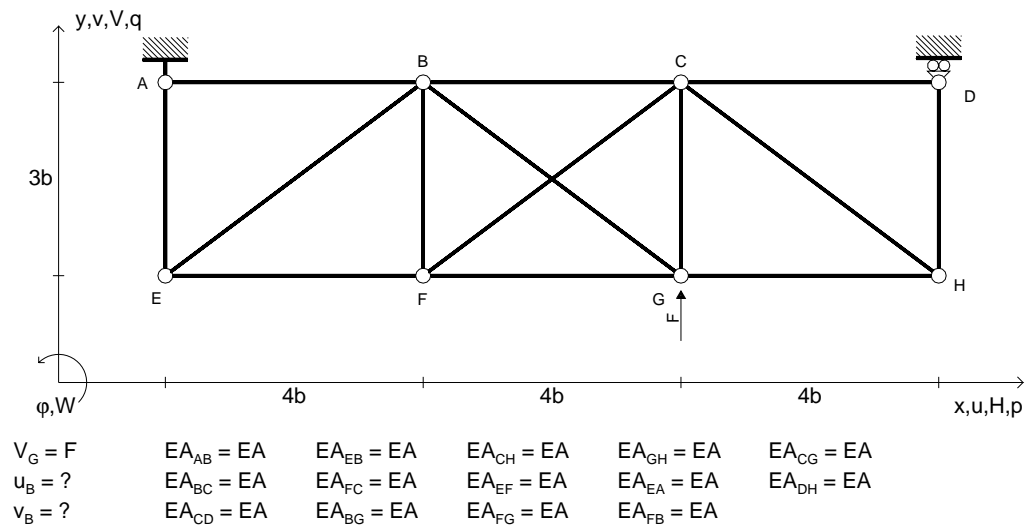
$N_{EA} = -2/3F$        $N_{FB} = -37/48F$        $N_{CG} = -5/48F$        $N_{DH} = -1/3F$

SPOSTAMENTI ASSOLUTI

$u_C = 3(Fb/EA)$

$v_C = 2233/162(Fb/EA)$





Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

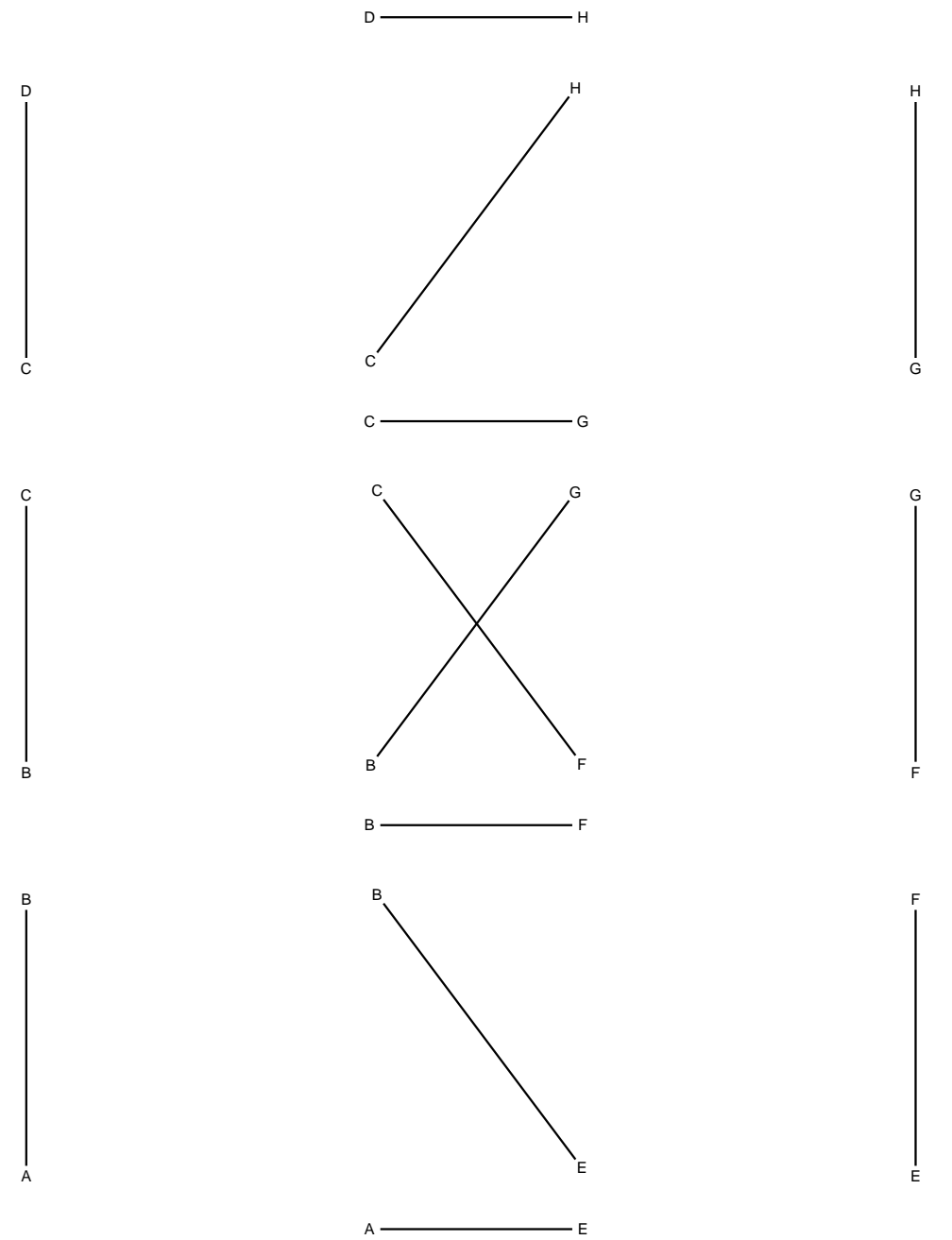
Calcolare lo spostamento orizzont. del nodo B

Calcolare lo spostamento verticale del nodo B

@ Adolfo Zavelani Rossi, Politecnico di Milano



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REAZIONI

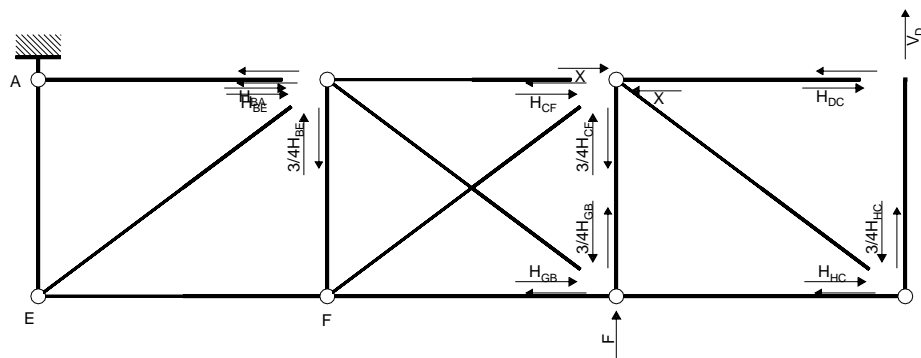
$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EB} =$	$N_{FC} =$
$N_{BG} =$	$N_{CH} =$	$N_{EF} =$	$N_{FG} =$	$N_{GH} =$
$N_{EA} =$	$N_{FB} =$	$N_{CG} =$	$N_{DH} =$	

SPOSTAMENTI ASSOLUTI

$u_B =$

$v_B =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b = -8Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b + 3H_{BA} b = -8Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$8V_D b + 3H_{GB} b = -3Xb - 4Fb$$

Rotazione intorno a F: aste FB BC BG

$$3H_{BA} b + 3H_{BE} b - 3H_{GB} b = 3Xb$$

Rotazione intorno a G: aste GH HD

$$4V_D b + 3H_{DC} b + 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC} b + 3H_{CF} b - 3H_{HC} b = -3Xb$$

Rotazione intorno a H: aste HD

$$3H_{DC} b = 0$$

## Matrice di equilibrio

$$\begin{bmatrix} \varphi_{AE} \\ \varphi_{EF} \\ \varphi_{FG} \\ \varphi_{FB} \\ \varphi_{GH} \\ \varphi_{GC} \\ \varphi_{HD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{DC} b & H_{BE} b & H_{CF} b & H_{GB} b & H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

## Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

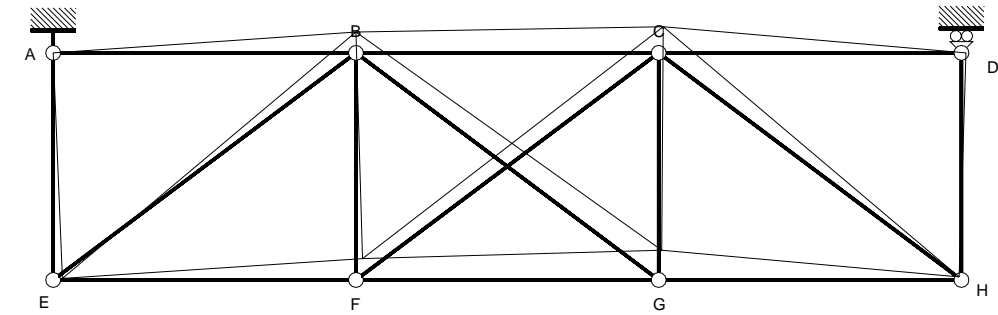
D

C

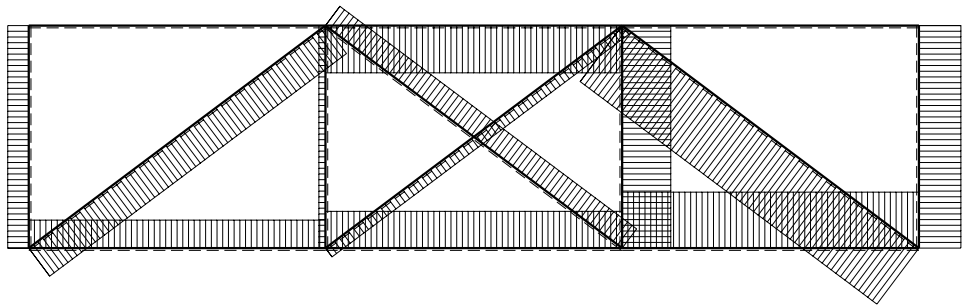
B

A

D  $\frac{2}{3}F$  HC  $\frac{10}{9}F$  HC  $\frac{37}{48}F$  GB  $\frac{55}{144}F$  F  $\frac{25}{144}F$ B  $\frac{5}{48}F$  FB  $\frac{5}{9}F$  EA  $\frac{1}{3}F$  EH  $\frac{8}{9}F$  GG  $\frac{7}{12}F$  FF  $\frac{4}{9}F$  E



50 Fb/EA



← ⊕ → 1.2 F

REAZIONI

$H_A = 0$        $V_A = -1/3F$        $V_D = -2/3F$

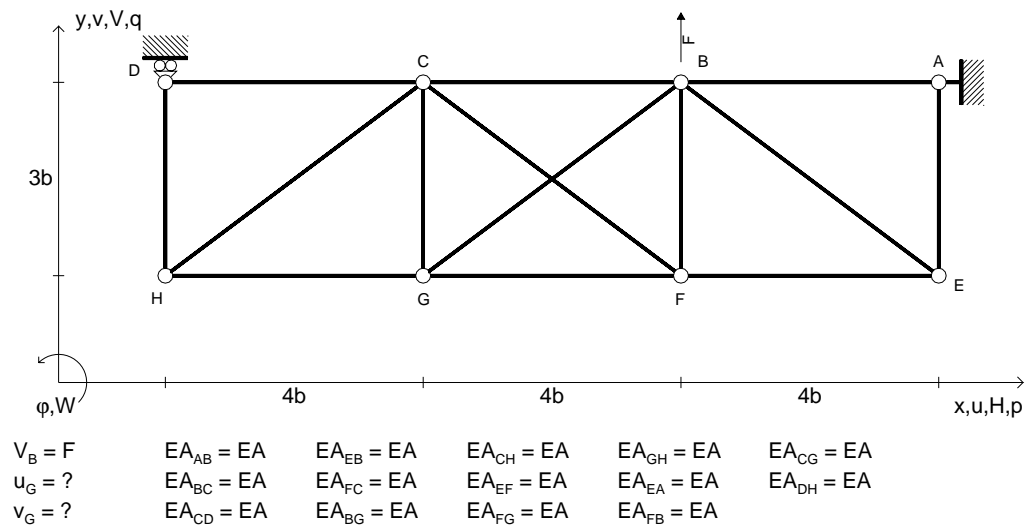
$N_{AB} = 0$        $N_{BC} = 3/4F$        $N_{CD} = 0$        $N_{EB} = 5/9F$        $N_{FC} = 25/144F$

$N_{BG} = -55/144F$        $N_{CH} = 10/9F$        $N_{EF} = -4/9F$        $N_{FG} = -7/12F$        $N_{GH} = -8/9F$

$N_{EA} = -1/3F$        $N_{FB} = -5/48F$        $N_{CG} = -37/48F$        $N_{DH} = -2/3F$

SPOSTAMENTI ASSOLUTI

$u_B = 0$   
 $v_B = 2233/162(Fb/EA)$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

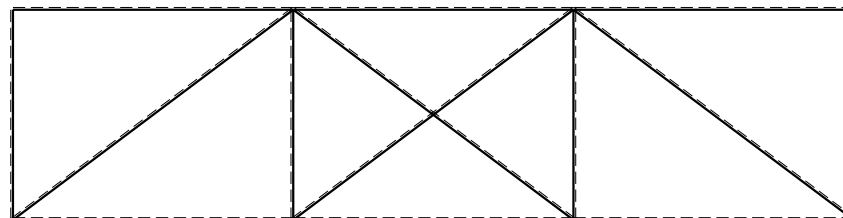
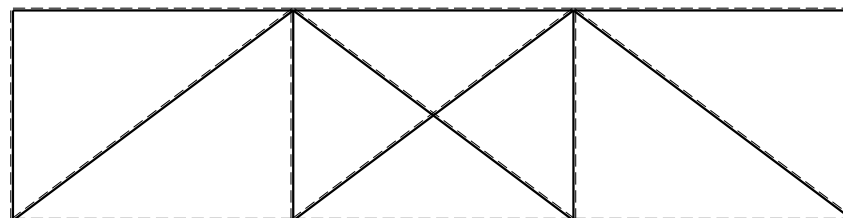
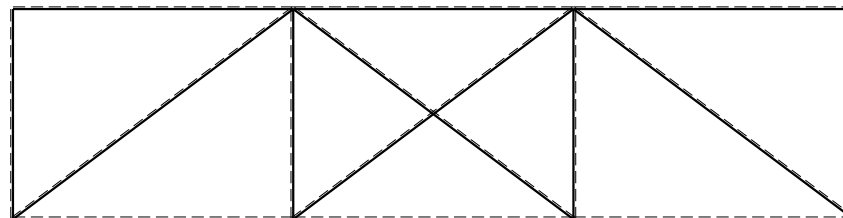
Tracciare i diagrammi delle azioni interne nelle aste.

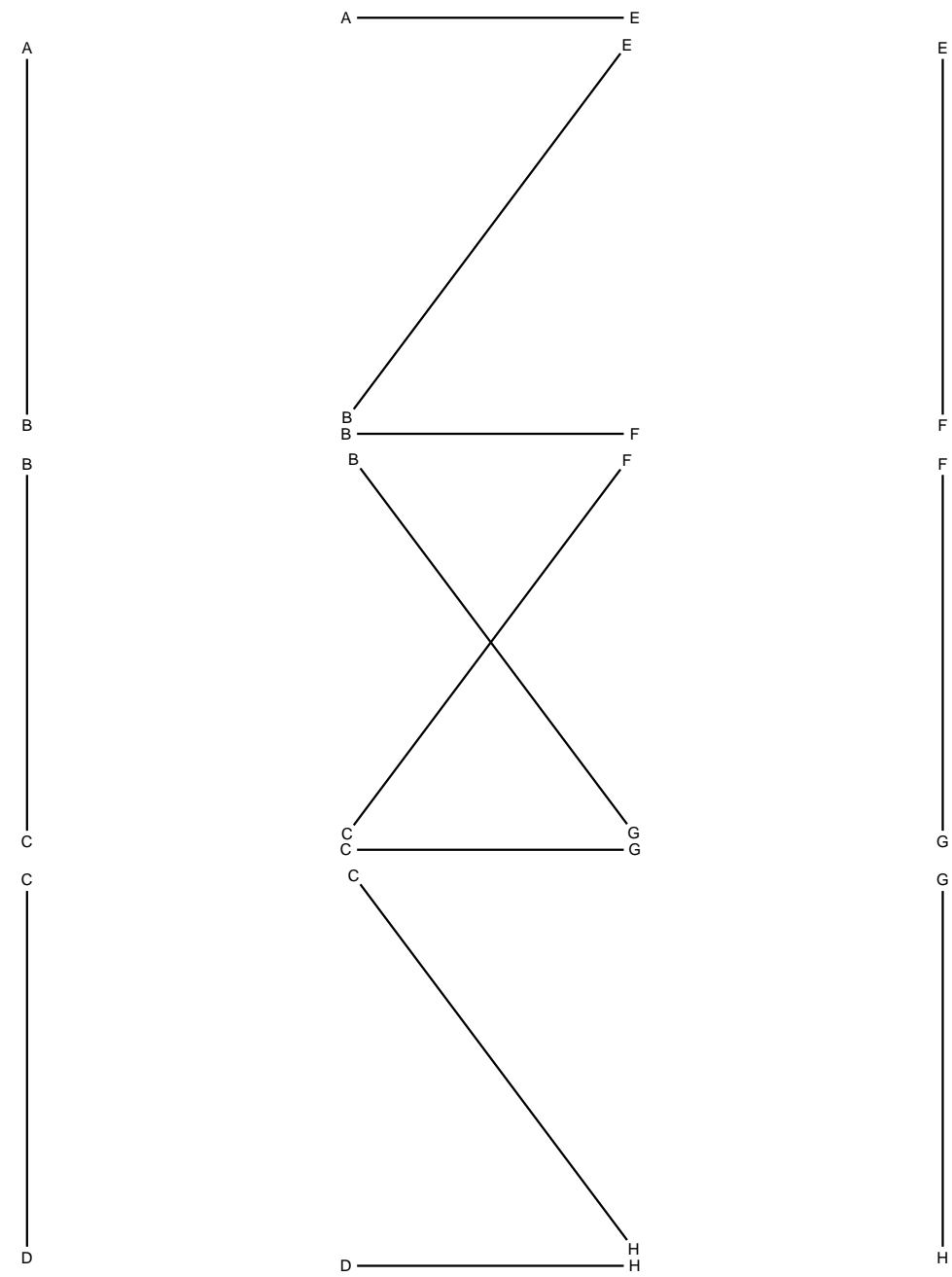
$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo G

Calcolare lo spostamento verticale del nodo G

@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{EB} =$        $N_{FC} =$        $N_{BG} =$

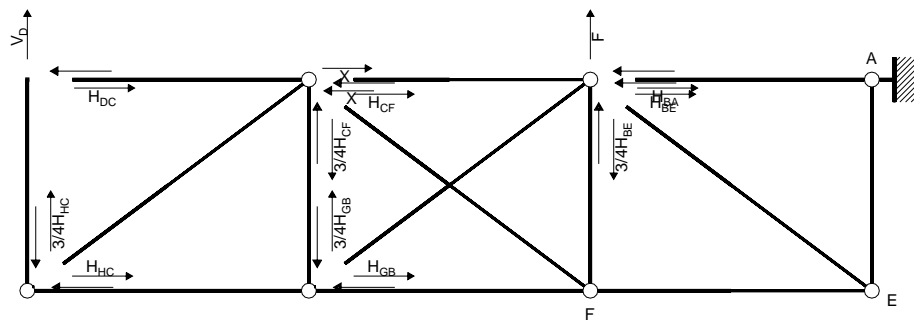
$N_{CH} =$        $N_{EF} =$        $N_{FG} =$        $N_{GH} =$        $N_{EA} =$        $N_{FB} =$

$N_{CG} =$        $N_{DH} =$

SPOSTAMENTI ASSOLUTI

$u_G =$

$v_G =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b = 4Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b + 3H_{BA} b = 4Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$-8V_D b + 3H_{GB} b = -3Xb$$

Rotazione intorno a F: aste FB BC BG

$$3H_{BA} b + 3H_{BE} b - 3H_{GB} b = 3Xb$$

Rotazione intorno a G: aste GH HD

$$-4V_D b + 3H_{DC} b + 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC} b + 3H_{CF} b - 3H_{HC} b = -3Xb$$

Rotazione intorno a H: aste HD

$$3H_{DC} b = 0$$

Matrice di equilibrio

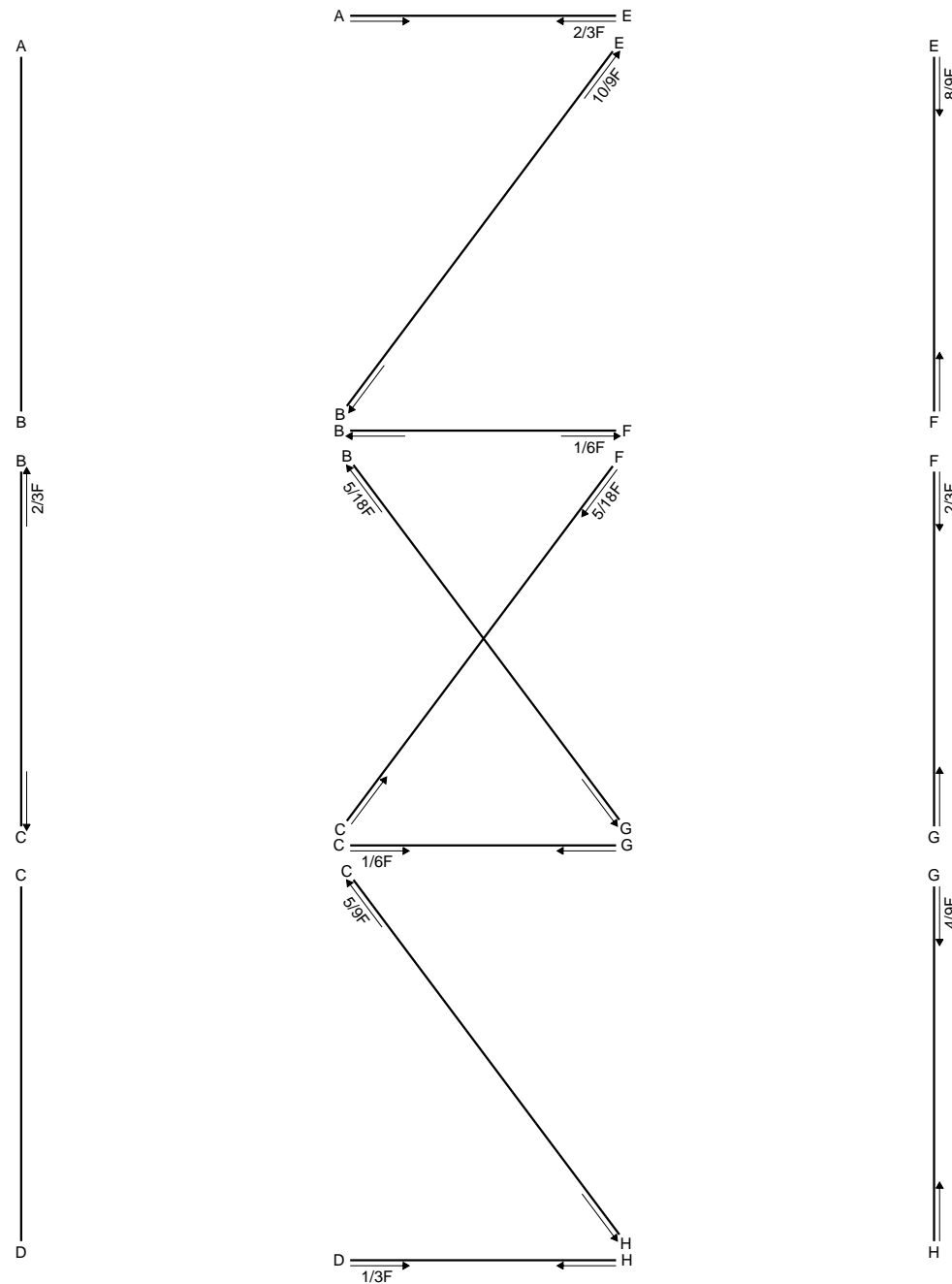
$$\begin{bmatrix} \phi_{AE} \\ \phi_{EF} \\ \phi_{FG} \\ \phi_{FB} \\ \phi_{GH} \\ \phi_{GC} \\ \phi_{HD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{DC} b & H_{BE} b & H_{CF} b & H_{GB} b & H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

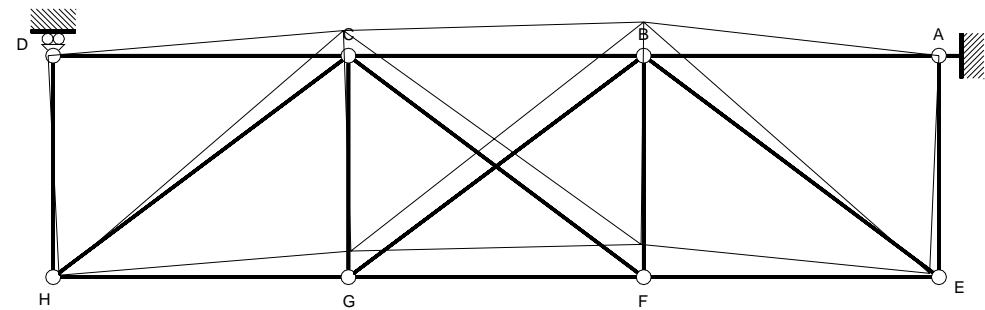
$$\begin{bmatrix} -12 & 0 & 0 & 0 & 0 & 0 & 0 \\ -12 & 3 & 0 & 0 & 0 & 0 & 0 \\ -8 & 0 & 0 & 0 & 0 & 3 & 0 \\ 0 & 3 & 0 & 3 & 0 & -3 & 0 \\ -4 & 0 & 3 & 0 & 0 & 0 & 3 \\ 0 & 0 & -3 & 0 & 3 & 0 & -3 \\ 0 & 0 & 3 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 4 \\ 0 & 4 \\ -3 & 0 \\ 3 & 0 \\ 0 & 0 \\ -3 & 0 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

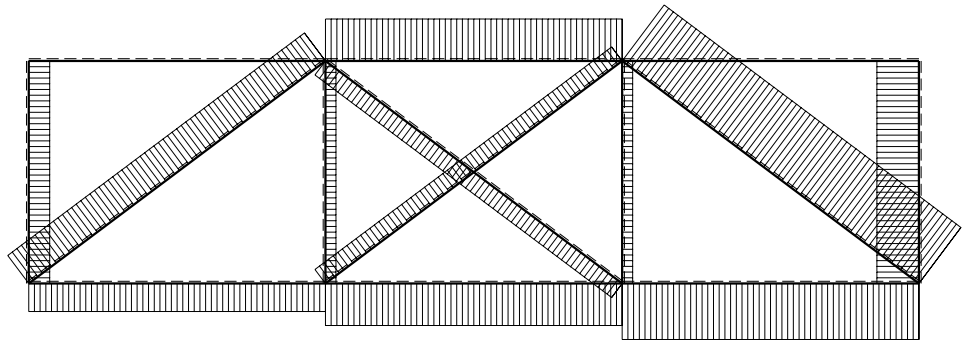
$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1/3 \\ 0 & 0 \\ -1 & -8/9 \\ 0 & -8/9 \\ 0 & 0 \\ -1 & -4/9 \\ 0 & -4/9 \end{bmatrix}$$





1 40 Fb/EA



1 1.2 F

REAZIONI

$H_A = 0$        $V_A = -2/3F$        $V_D = -1/3F$

$N_{AB} = 0$        $N_{BC} = 2/3F$        $N_{CD} = 0$        $N_{EB} = 10/9F$        $N_{FC} = -5/18F$        $N_{BG} = 5/18F$

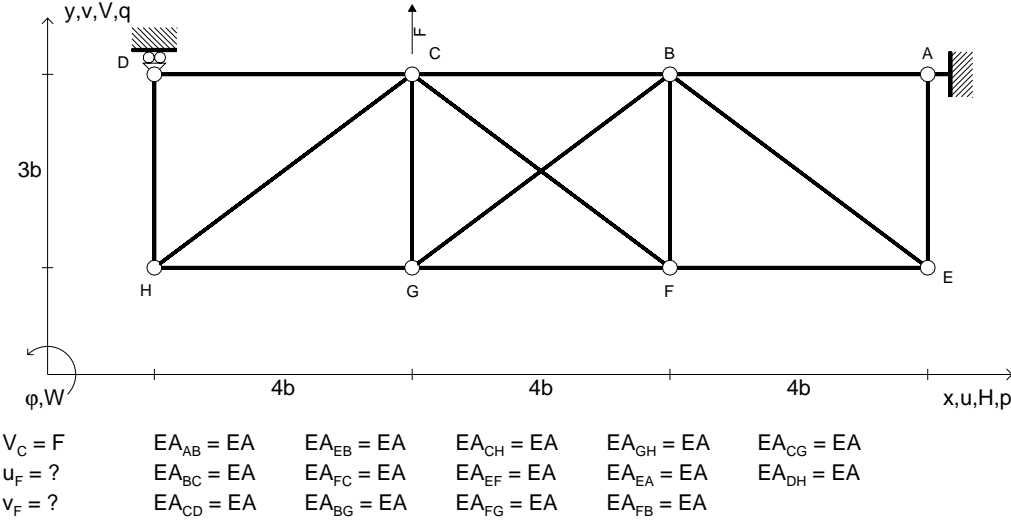
$N_{CH} = 5/9F$        $N_{EF} = -8/9F$        $N_{FG} = -2/3F$        $N_{GH} = -4/9F$        $N_{EA} = -2/3F$        $N_{FB} = 1/6F$

$N_{CG} = -1/6F$        $N_{DH} = -1/3F$

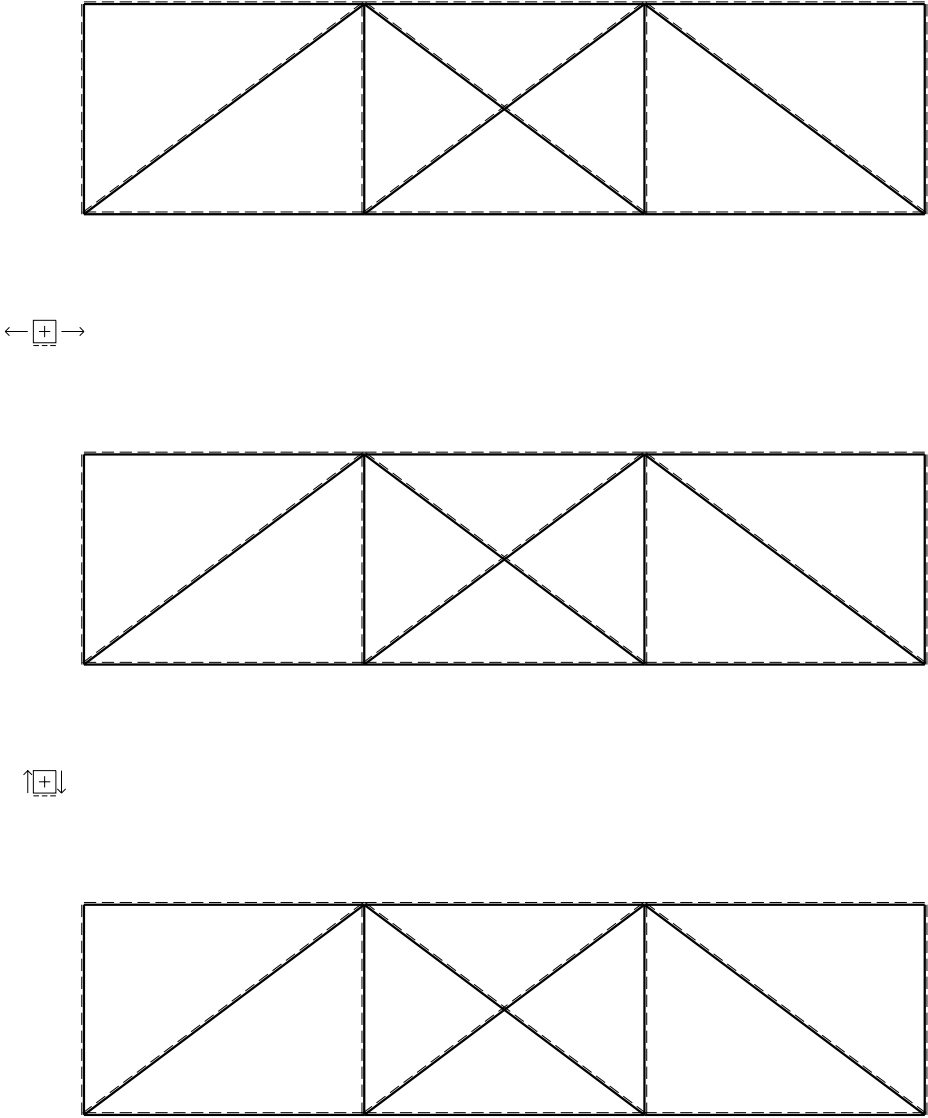
SPOSTAMENTI ASSOLUTI

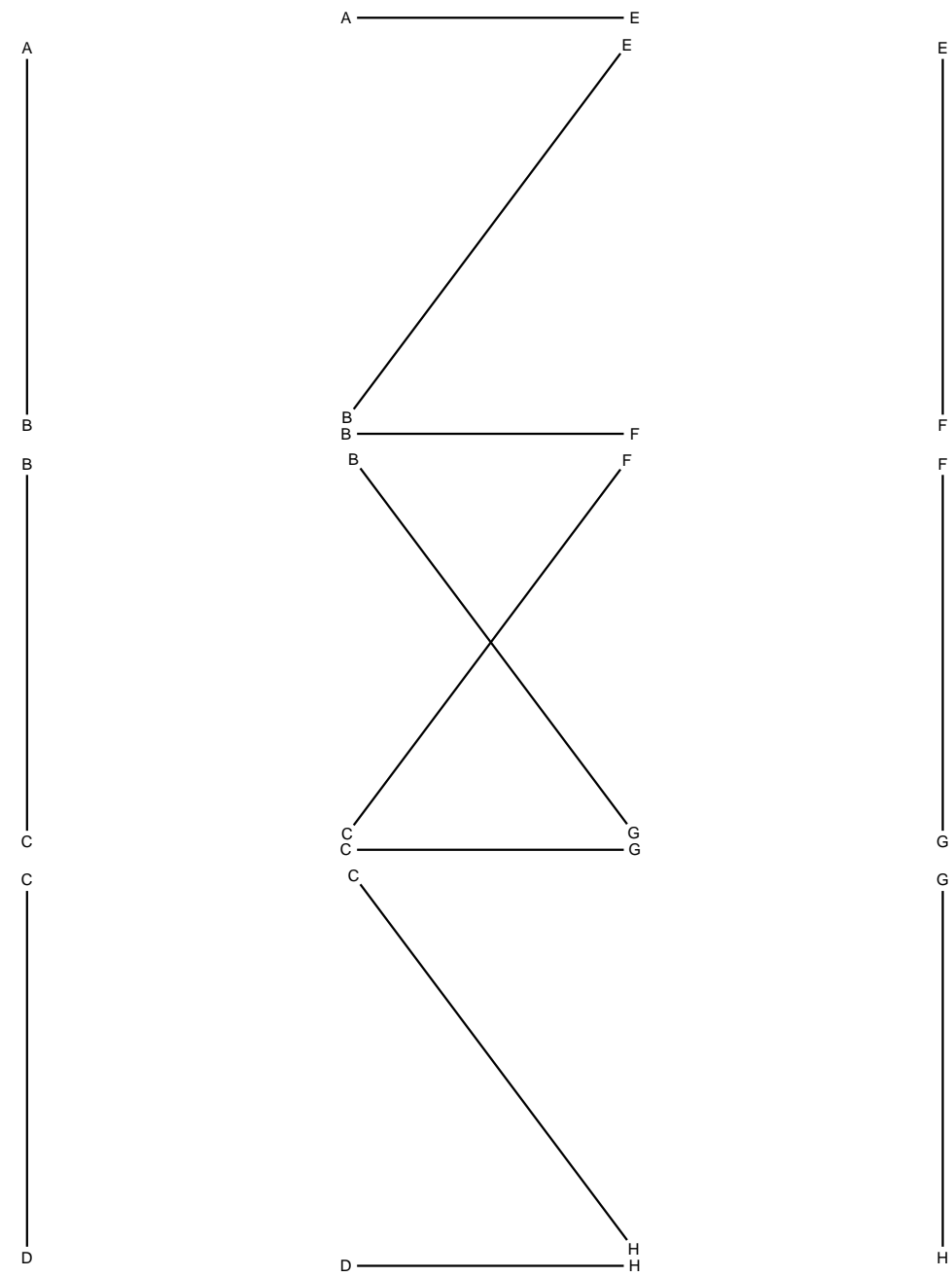
$u_G = 35/27(Fb/EA)$   
 $v_G = 2233/162(Fb/EA)$





Svolgere l'analisi cinematica.  
Riportare la soluzione su questo foglio.  
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Tracciare i diagrammi delle azioni interne nelle aste.  
 $A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.  
Calcolare lo spostamento orizzont. del nodo F  
Calcolare lo spostamento verticale del nodo F  
@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{EB} =$        $N_{FC} =$        $N_{BG} =$

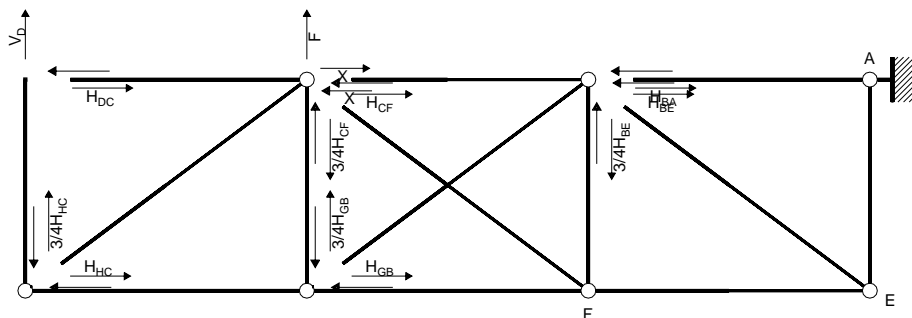
$N_{CH} =$        $N_{EF} =$        $N_{FG} =$        $N_{GH} =$        $N_{EA} =$        $N_{FB} =$

$N_{CG} =$        $N_{DH} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b = 8Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b + 3H_{BA} b = 8Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$-8V_D b + 3H_{GB} b = -3Xb + 4Fb$$

Rotazione intorno a F: aste FB BC BG

$$3H_{BA}b + 3H_{BF}b - 3H_{GB}b = 3Xb$$

Rotazione intorno a G: aste GH HD

$$-4V_D b + 3H_{DC} b + 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC}b + 3H_{CF}b - 3H_{HC}b = -3Xb$$

Rotazione intorno a H: aste HD

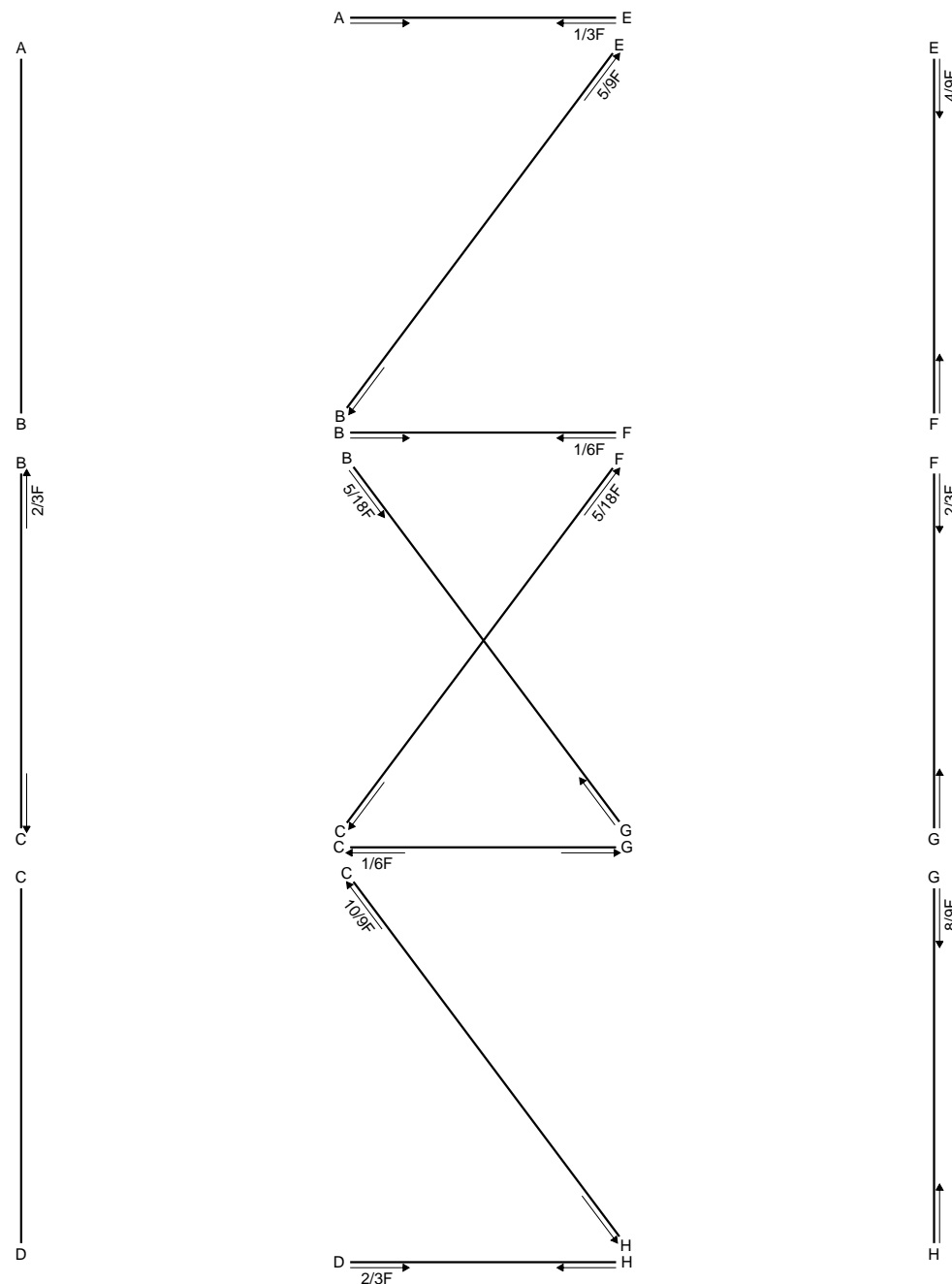
$$3H_{DC}b = 0$$

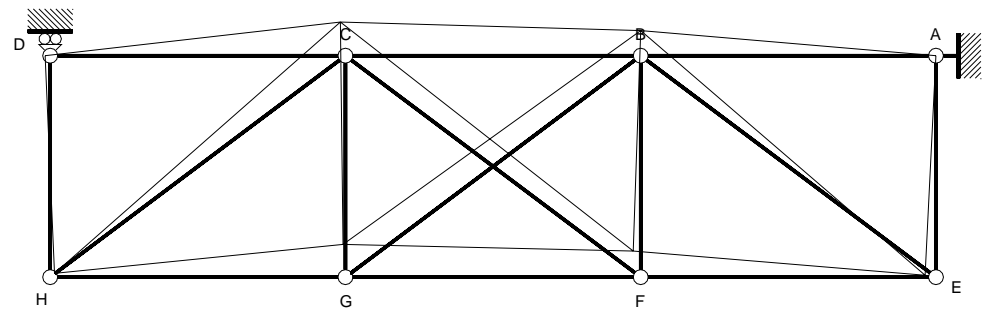
### Matrice di equilibrio

$$\begin{bmatrix} \Phi_{AE} & \Phi_{EF} & \Phi_{FG} & \Phi_{FB} & \Phi_{GH} & \Phi_{GC} & \Phi_{HD} \end{bmatrix} \begin{bmatrix} V_D^b & H_{BA}^b & H_{DC}^b & H_{BE}^b & H_{CF}^b & H_{GB}^b & H_{HC}^b \end{bmatrix} = \begin{bmatrix} X_B & F_B \end{bmatrix}$$

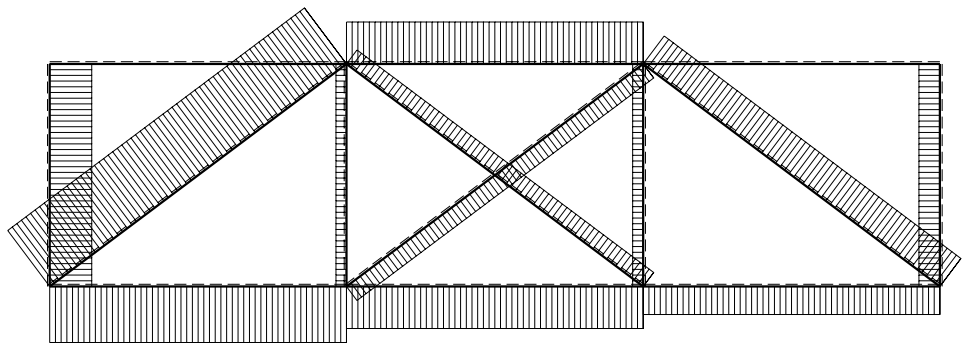
### Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} \text{Xb} & \text{Fb} \\ 0 & -2/3 \\ 0 & 0 \\ -1 & -4/9 \\ 0 & -4/9 \\ 0 & 0 \\ -1 & -8/9 \\ 0 & -8/9 \end{bmatrix}$$





1 40 Fb/EA



1 1.2 F

REAZIONI

$H_A = 0$        $V_A = -1/3F$        $V_D = -2/3F$

$N_{AB} = 0$        $N_{BC} = 2/3F$        $N_{CD} = 0$        $N_{EB} = 5/9F$        $N_{FC} = 5/18F$        $N_{BG} = -5/18F$

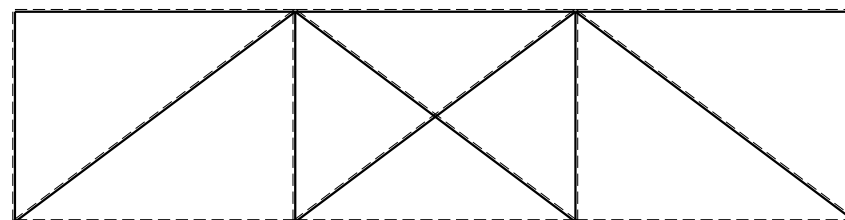
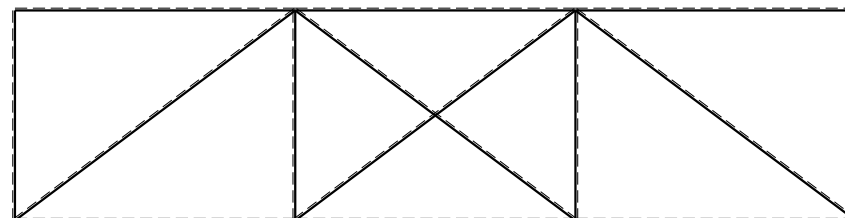
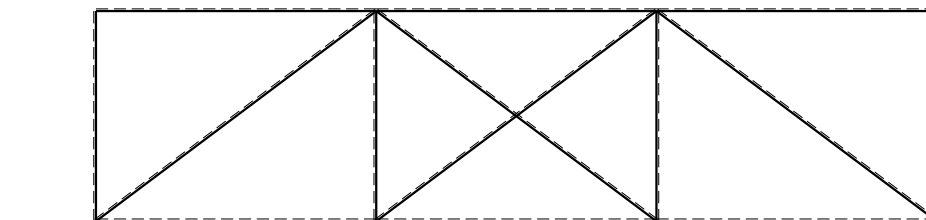
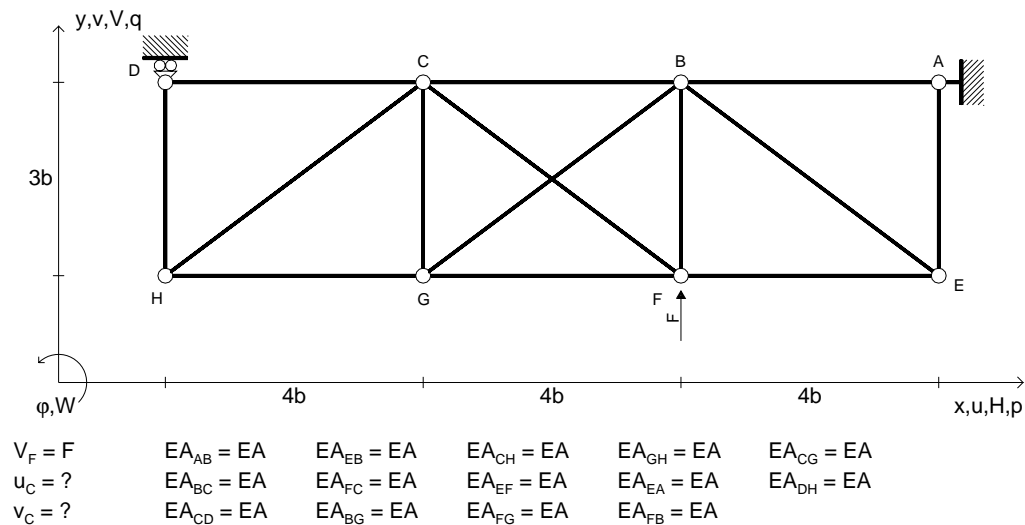
$N_{CH} = 10/9F$        $N_{EF} = -4/9F$        $N_{FG} = -2/3F$        $N_{GH} = -8/9F$        $N_{EA} = -1/3F$        $N_{FB} = -1/6F$

$N_{CG} = 1/6F$        $N_{DH} = -2/3F$

SPOSTAMENTI ASSOLUTI

$u_F = -107/27(Fb/EA)$

$v_F = 2233/162(Fb/EA)$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

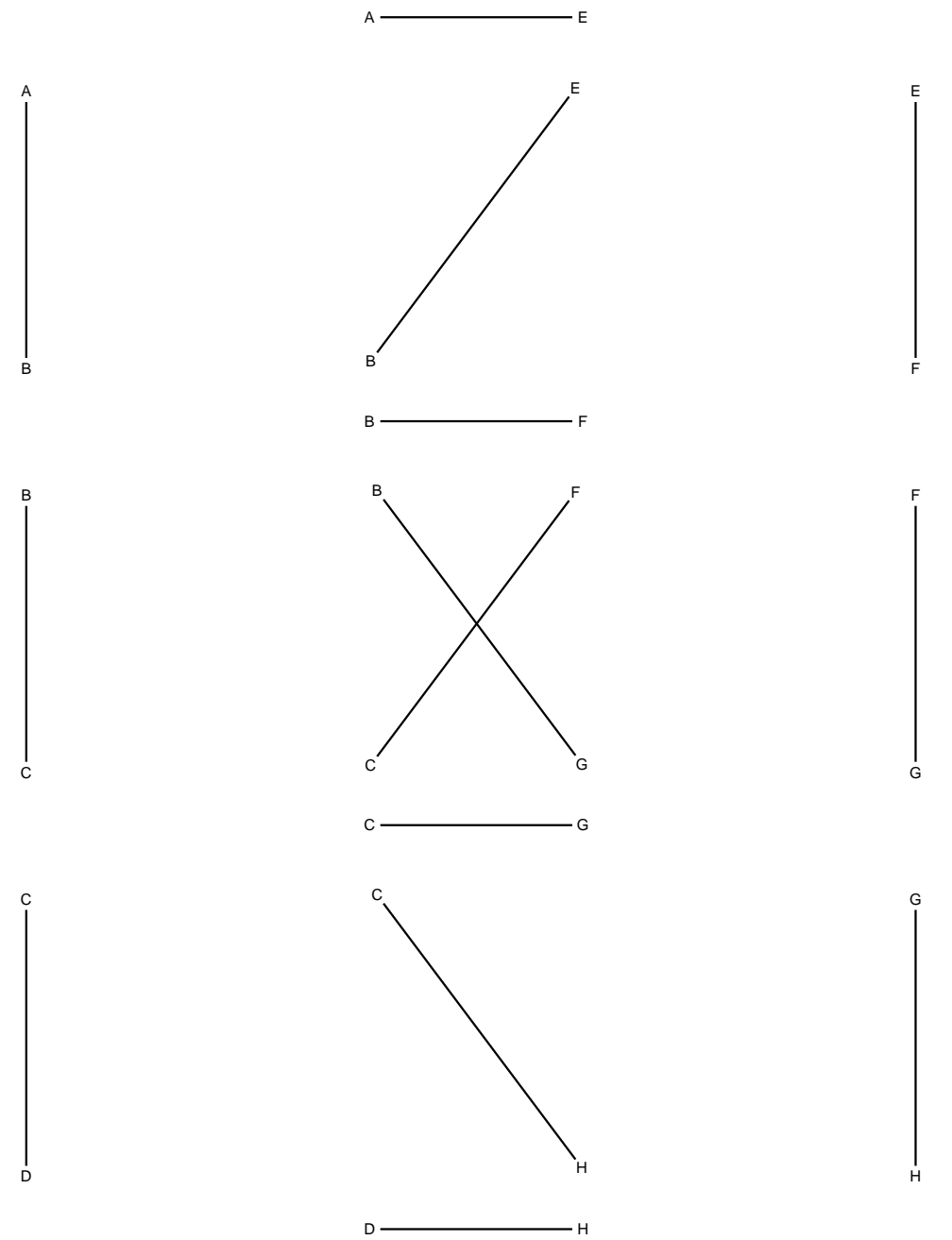
Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.

Calcolare lo spostamento orizzont. del nodo C

Calcolare lo spostamento verticale del nodo C

@ Adolfo Zavelani Rossi, Politecnico di Milano

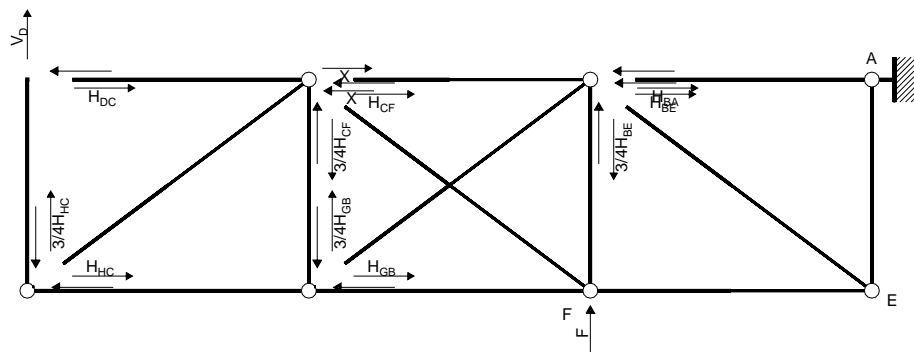


REAZIONI

$H_A =$	$V_A =$	$V_D =$			
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EB} =$	$N_{FC} =$	
$N_{BG} =$	$N_{CH} =$	$N_{EF} =$	$N_{FG} =$	$N_{GH} =$	
$N_{EA} =$	$N_{FB} =$	$N_{CG} =$	$N_{DH} =$		

SPOSTAMENTI ASSOLUTI

$u_C =$	
$v_C =$	



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b = 4Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b + 3H_{BA} b = 4Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$-8V_D b + 3H_{GB} b = -3Xb$$

Rotazione intorno a G: aste FB BC BG

$$3H_{BA} b + 3H_{BE} b - 3H_{GB} b = 3Xb$$

Rotazione intorno a H: aste GH HD

$$-4V_D b + 3H_{DC} b + 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC} b + 3H_{CF} b - 3H_{HC} b = -3Xb$$

Rotazione intorno a H: aste HD

$$3H_{DC} b = 0$$

Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EF} \\ \phi_{FG} \\ \phi_{FB} \\ \phi_{GH} \\ \phi_{GC} \\ \phi_{HD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{DC} b & H_{BE} b & H_{CF} b & H_{GB} b & H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

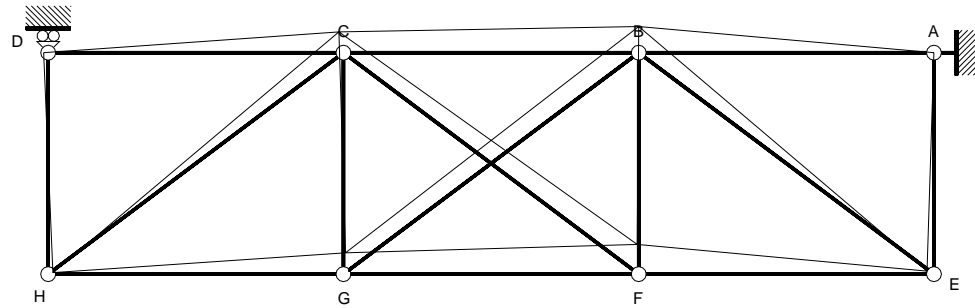
$$\begin{bmatrix} -12 & 0 & 0 & 0 & 0 & 0 & 0 \\ -12 & 3 & 0 & 0 & 0 & 0 & 0 \\ -8 & 0 & 0 & 0 & 0 & 3 & 0 \\ 0 & 3 & 0 & 3 & 0 & -3 & 0 \\ -4 & 0 & 3 & 0 & 0 & 0 & 3 \\ 0 & 0 & -3 & 0 & 3 & 0 & -3 \\ 0 & 0 & 3 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 4 \\ 0 & 4 \\ -3 & 0 \\ 3 & 0 \\ 0 & 0 \\ -3 & 0 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

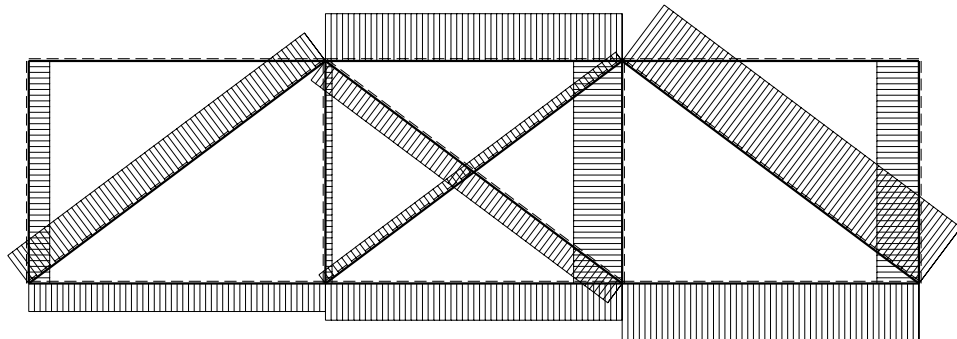
$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1/3 \\ 0 & 0 \\ -1 & -8/9 \\ 0 & -8/9 \\ 0 & 0 \\ -1 & -4/9 \\ 0 & -4/9 \end{bmatrix}$$

A  
BA  $\xrightarrow{\quad} \xleftarrow{2/3F} E$ B  $\xrightarrow{\quad} \xleftarrow{10/9F} E$ B  $\xrightarrow{\quad} \xleftarrow{37/48F} F$ B  $\xrightarrow{25/144F} \xleftarrow{55/144F} F$ C  $\xrightarrow{\quad} \xleftarrow{5/48F} G$ C  $\xrightarrow{5/9F} \xleftarrow{4/9F} H$ D  $\xrightarrow{\quad} \xleftarrow{1/3F} H$ C  
DE  $\xrightarrow{\quad} \xleftarrow{8/9F} F$ F  $\xrightarrow{\quad} \xleftarrow{7/12F} G$ G  $\xrightarrow{\quad} \xleftarrow{4/9F} H$



1 — 50 Fb/EA



← ⊕ → 1 — 1.2 F

## REAZIONI

$$H_A = 0 \quad V_A = -2/3F \quad V_D = -1/3F$$

$$N_{AB} = 0 \quad N_{BC} = 3/4F \quad N_{CD} = 0 \quad N_{EB} = 10/9F \quad N_{FC} = -55/144F$$

$$N_{BG} = 25/144F \quad N_{CH} = 5/9F \quad N_{EF} = -8/9F \quad N_{FG} = -7/12F \quad N_{GH} = -4/9F$$

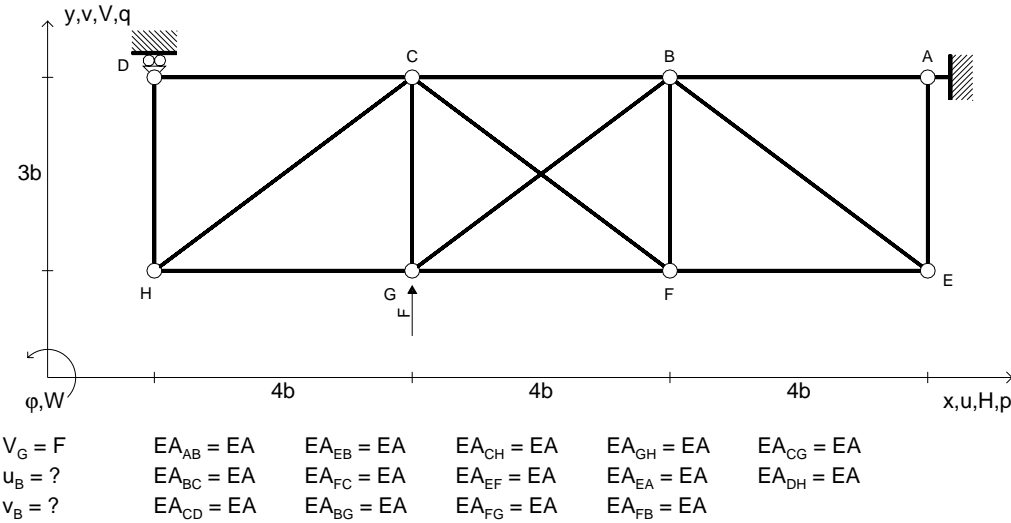
$$N_{EA} = -2/3F \quad N_{FB} = -37/48F \quad N_{CG} = -5/48F \quad N_{DH} = -1/3F$$

## SPOSTAMENTI ASSOLUTI

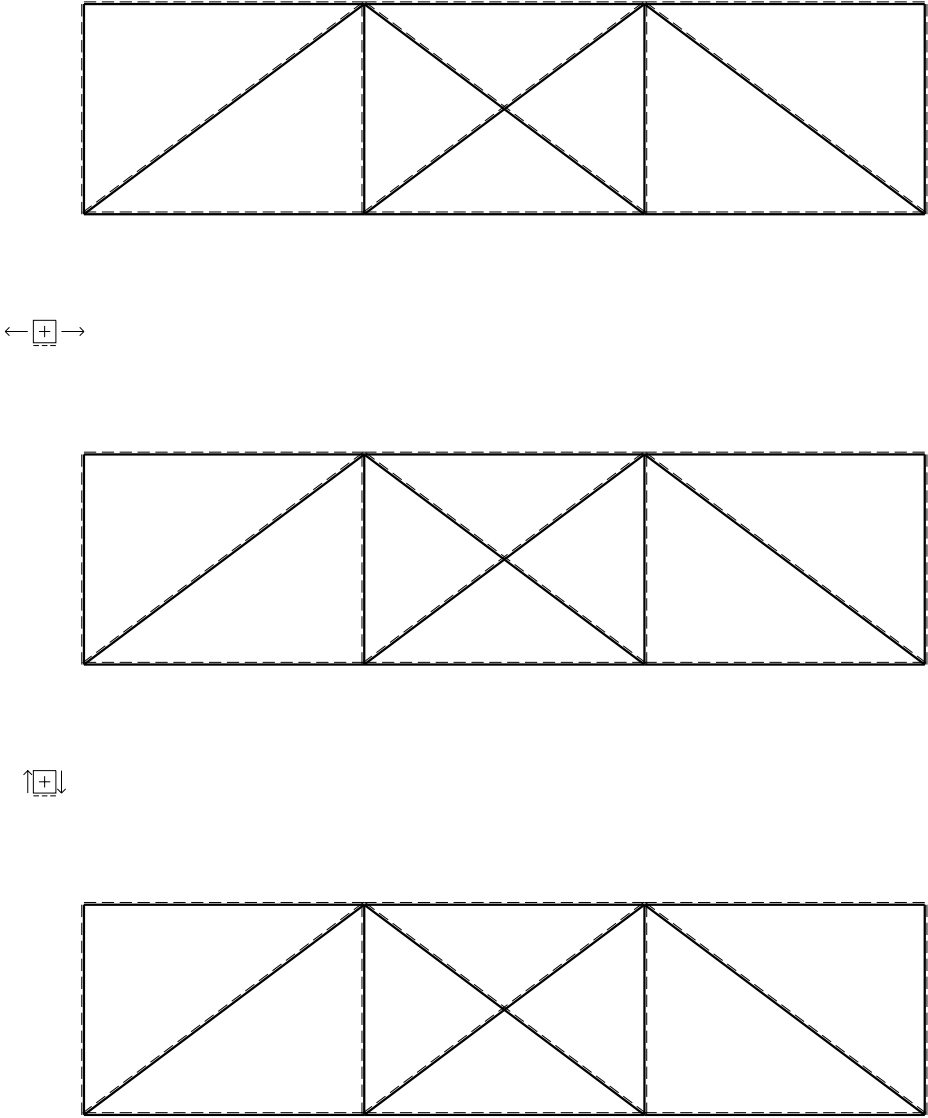
$$u_C = -3(Fb/EA)$$

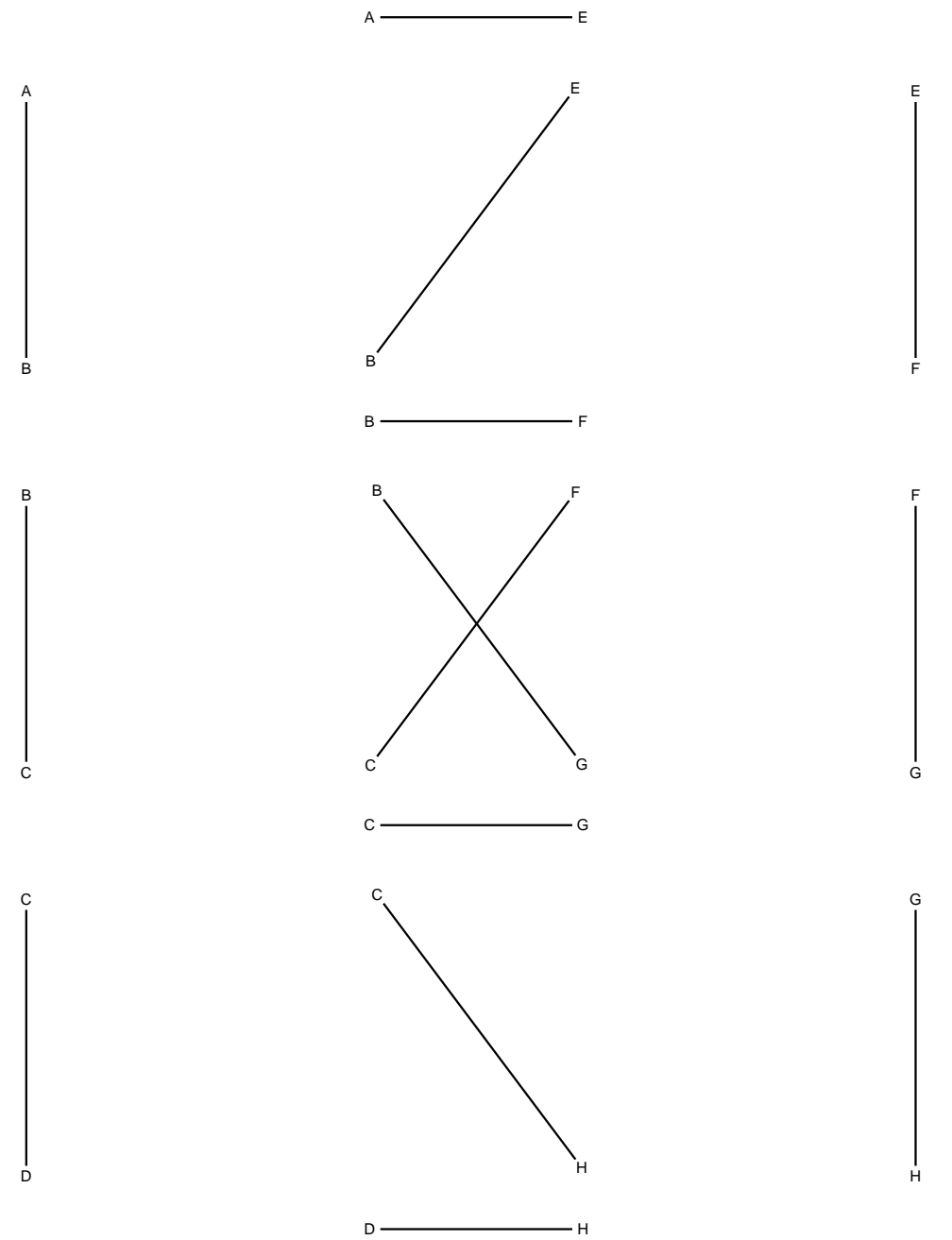
$$v_C = 2233/162(Fb/EA)$$





Svolgere l'analisi cinematica.  
Riportare la soluzione su questo foglio.  
Carichi e deformazioni date hanno verso efficace in disegno.  
Calcolare reazioni vincolari della struttura e delle aste.  
Tracciare i diagrammi delle azioni interne nelle aste.  
 $A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.  
Calcolare lo spostamento orizzont. del nodo B  
Calcolare lo spostamento verticale del nodo B  
@ Adolfo Zavelani Rossi, Politecnico di Milano



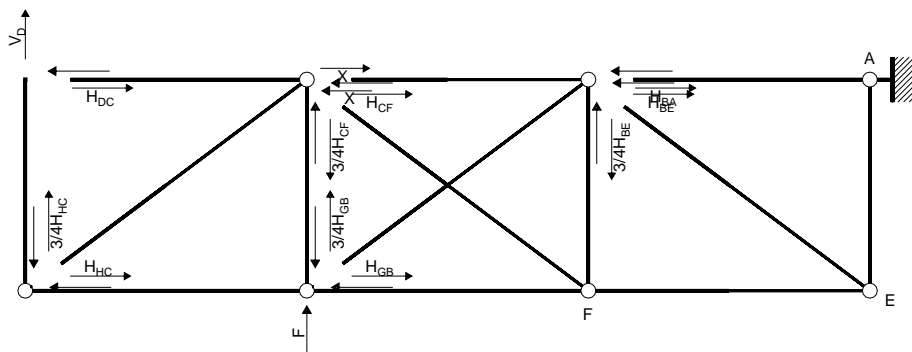


REAZIONI

$H_A =$	$V_A =$	$V_D =$			
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EB} =$	$N_{FC} =$	
$N_{BG} =$	$N_{CH} =$	$N_{EF} =$	$N_{FG} =$	$N_{GH} =$	
$N_{EA} =$	$N_{FB} =$	$N_{CG} =$	$N_{DH} =$		

SPOSTAMENTI ASSOLUTI

$u_B =$	
$v_B =$	



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$-12V_{nb} = 8Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$-12V_D b + 3H_{BA} b = 8Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$-8V_D b + 3H_{GB} b = -3Xb + 4Fb$$

Rotazione intorno a F: aste FB BC BG

$$3H_{BA}b + 3H_{BF}b - 3H_{GB}b = 3Xb$$

Rotazione intorno a G: aste GH HD

$$-4V_D b + 3H_{DC} b + 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$-3H_{DC}b + 3H_{CF}b - 3H_{HC}b = -3Xb$$

Rotazione intorno a H: aste HD

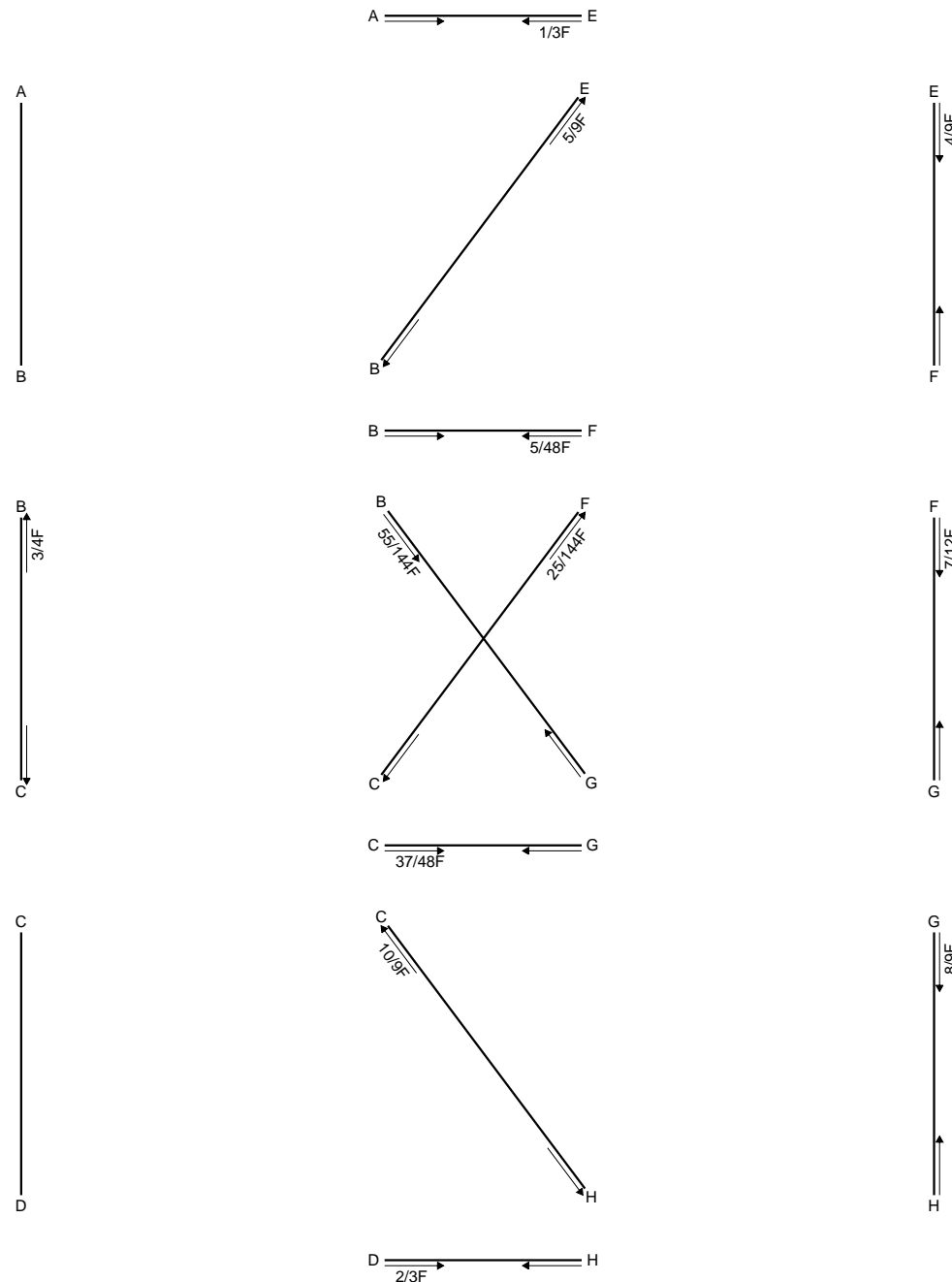
$$3H_{DC}b = 0$$

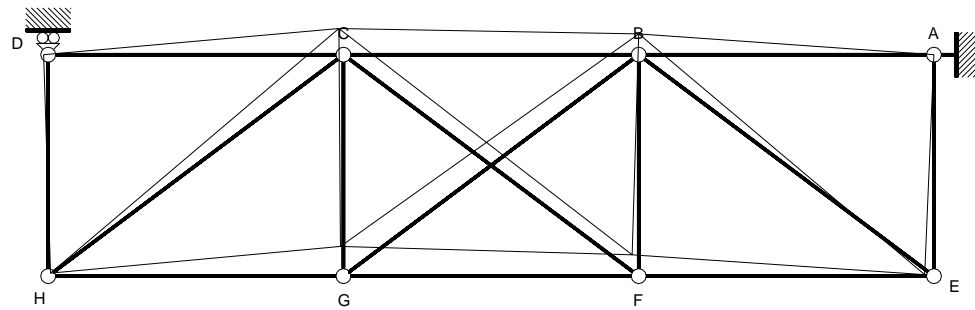
### Matrice di equilibrio

$$\begin{bmatrix} \Phi_{AE} & \Phi_{EF} & \Phi_{FG} & \Phi_{FB} & \Phi_{GH} & \Phi_{GC} & \Phi_{GD} \end{bmatrix} \begin{bmatrix} V_{DB} & H_{BA} & H_{DC} & H_{BE} & H_{CF} & H_{GB} & H_{HC} \end{bmatrix} = \begin{bmatrix} X_B & F_B \end{bmatrix}$$

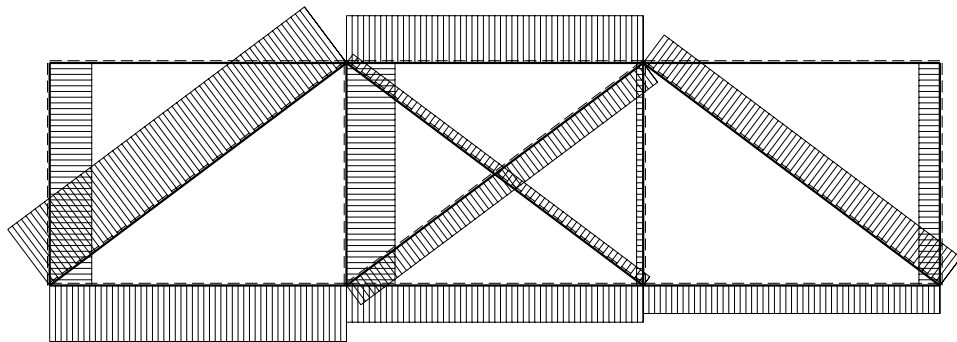
### Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \\ 0 & -2/3 \\ 0 & 0 \\ -1 & -4/9 \\ 0 & -4/9 \\ 0 & 0 \\ -1 & -8/9 \\ 0 & -8/9 \end{bmatrix}$$





1 — 50 Fb/EA



← ⊕ → 1 — 1.2 F

## REAZIONI

$$H_A = 0 \quad V_A = -1/3F \quad V_D = -2/3F$$

$$N_{AB} = 0 \quad N_{BC} = 3/4F \quad N_{CD} = 0 \quad N_{EB} = 5/9F \quad N_{FC} = 25/144F$$

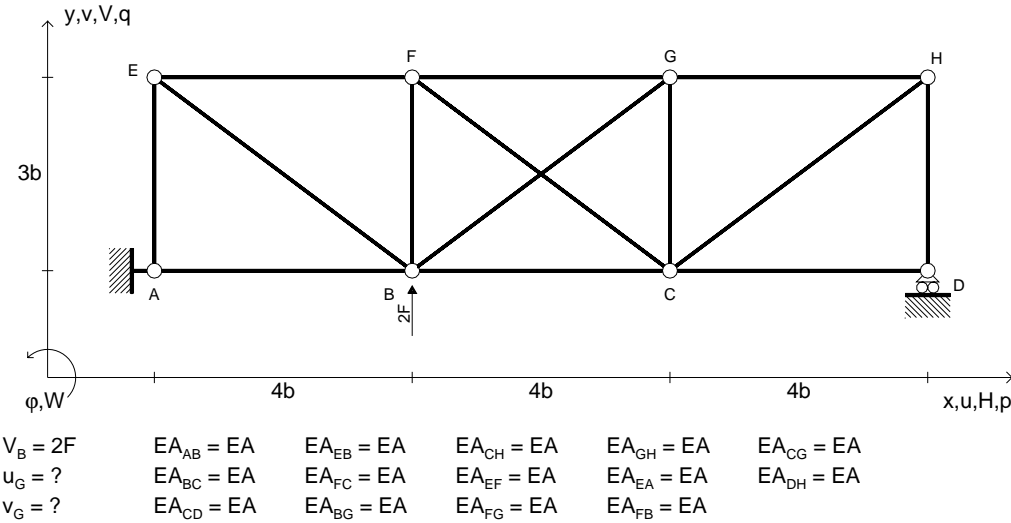
$$N_{BG} = -55/144F \quad N_{CH} = 10/9F \quad N_{EF} = -4/9F \quad N_{FG} = -7/12F \quad N_{GH} = -8/9F$$

$$N_{EA} = -1/3F \quad N_{FB} = -5/48F \quad N_{CG} = -37/48F \quad N_{DH} = -2/3F$$

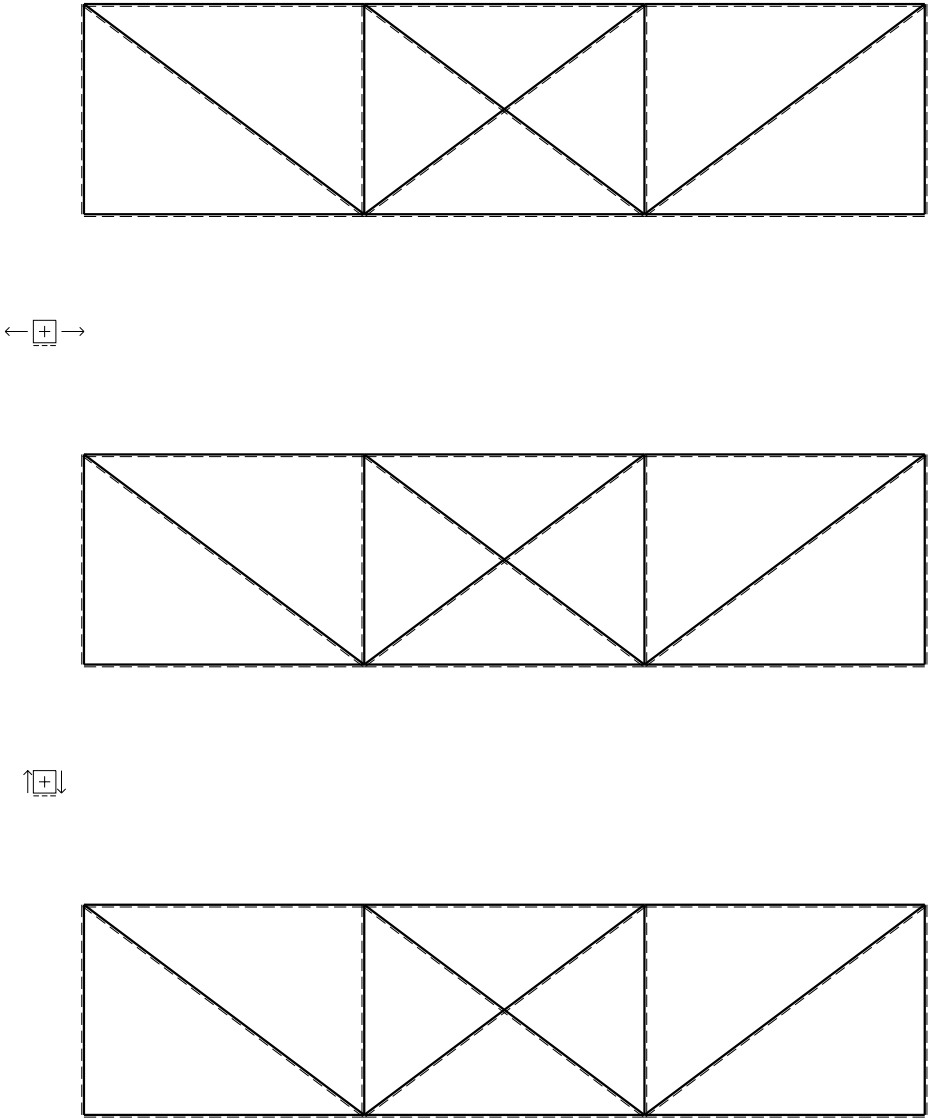
## SPOSTAMENTI ASSOLUTI

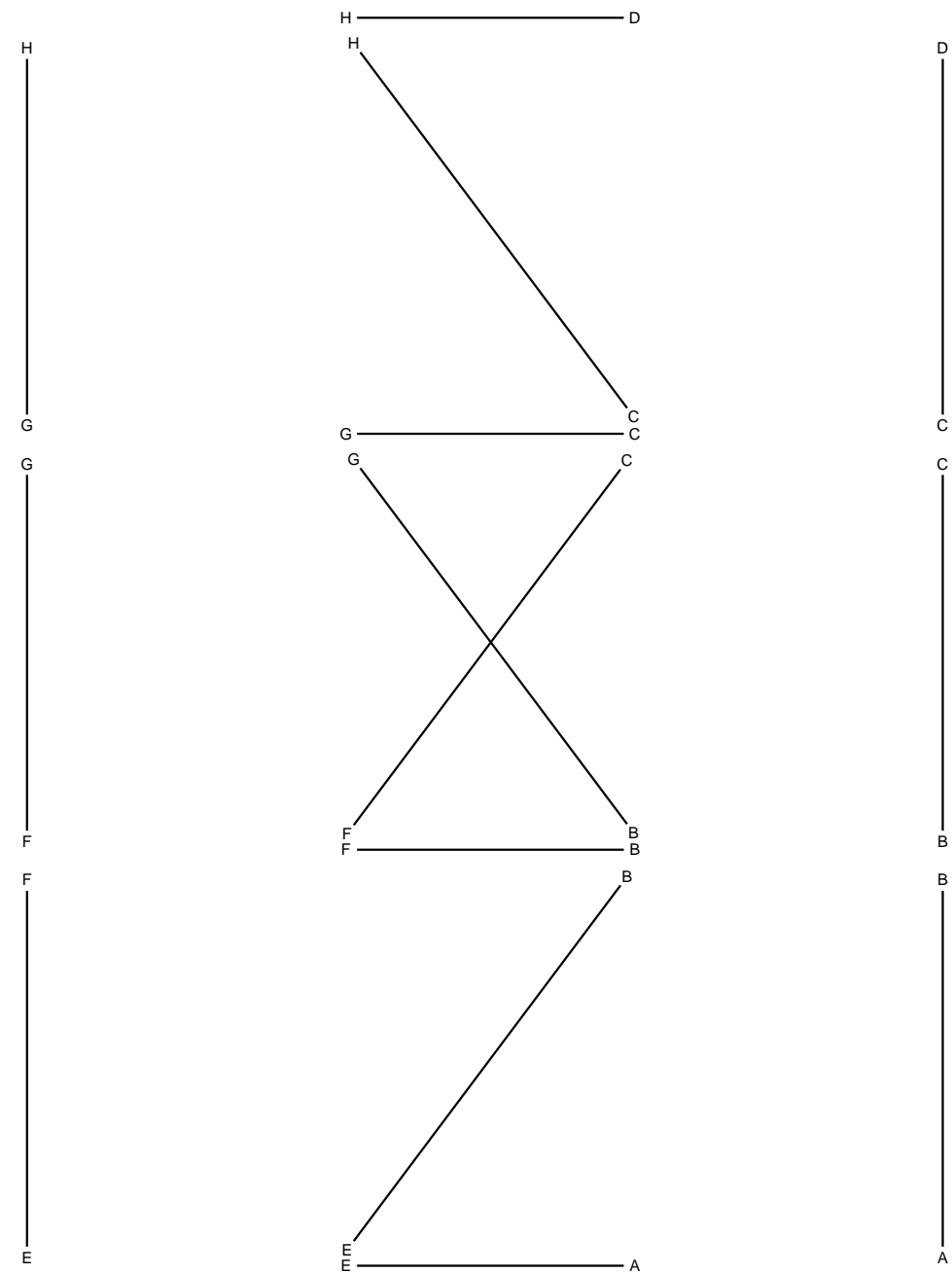
$$u_B = 0$$

$$v_B = 2233/162(Fb/EA)$$



Svolgere l'analisi cinematica.  
Riportare la soluzione su questo foglio.  
Carichi e deformazioni date hanno verso efficace in disegno.  
Calcolare reazioni vincolari della struttura e delle aste.  
Tracciare i diagrammi delle azioni interne nelle aste.  
 $A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.  
Calcolare lo spostamento orizzont. del nodo G  
Calcolare lo spostamento verticale del nodo G  
@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{EB} =$        $N_{FC} =$        $N_{BG} =$

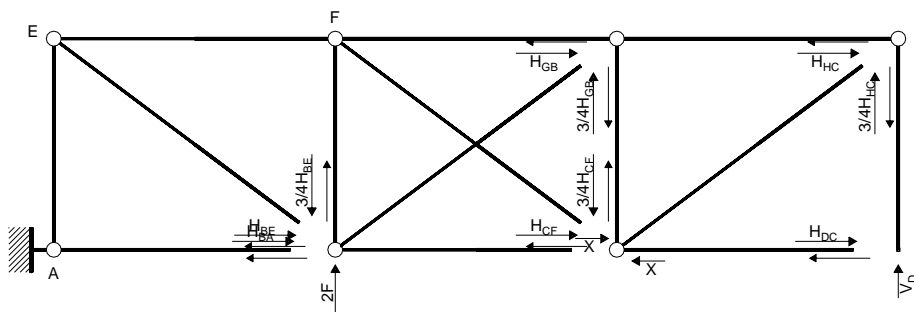
$N_{CH} =$        $N_{EF} =$        $N_{FG} =$        $N_{GH} =$        $N_{EA} =$        $N_{FB} =$

$N_{CG} =$        $N_{DH} =$

SPOSTAMENTI ASSOLUTI

$u_G =$

$v_G =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b = -8Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b - 3H_{BA} b = -8Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$8V_D b - 3H_{GB} b = 3Xb$$

Rotazione intorno a F: aste FB BC BG

$$-3H_{BA} b - 3H_{BE} b + 3H_{GB} b = -3Xb$$

Rotazione intorno a G: aste GH HD

$$4V_D b - 3H_{DC} b - 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$3H_{DC} b - 3H_{CF} b + 3H_{HC} b = 3Xb$$

Rotazione intorno a H: aste HD

$$-3H_{DC} b = 0$$

## Matrice di equilibrio

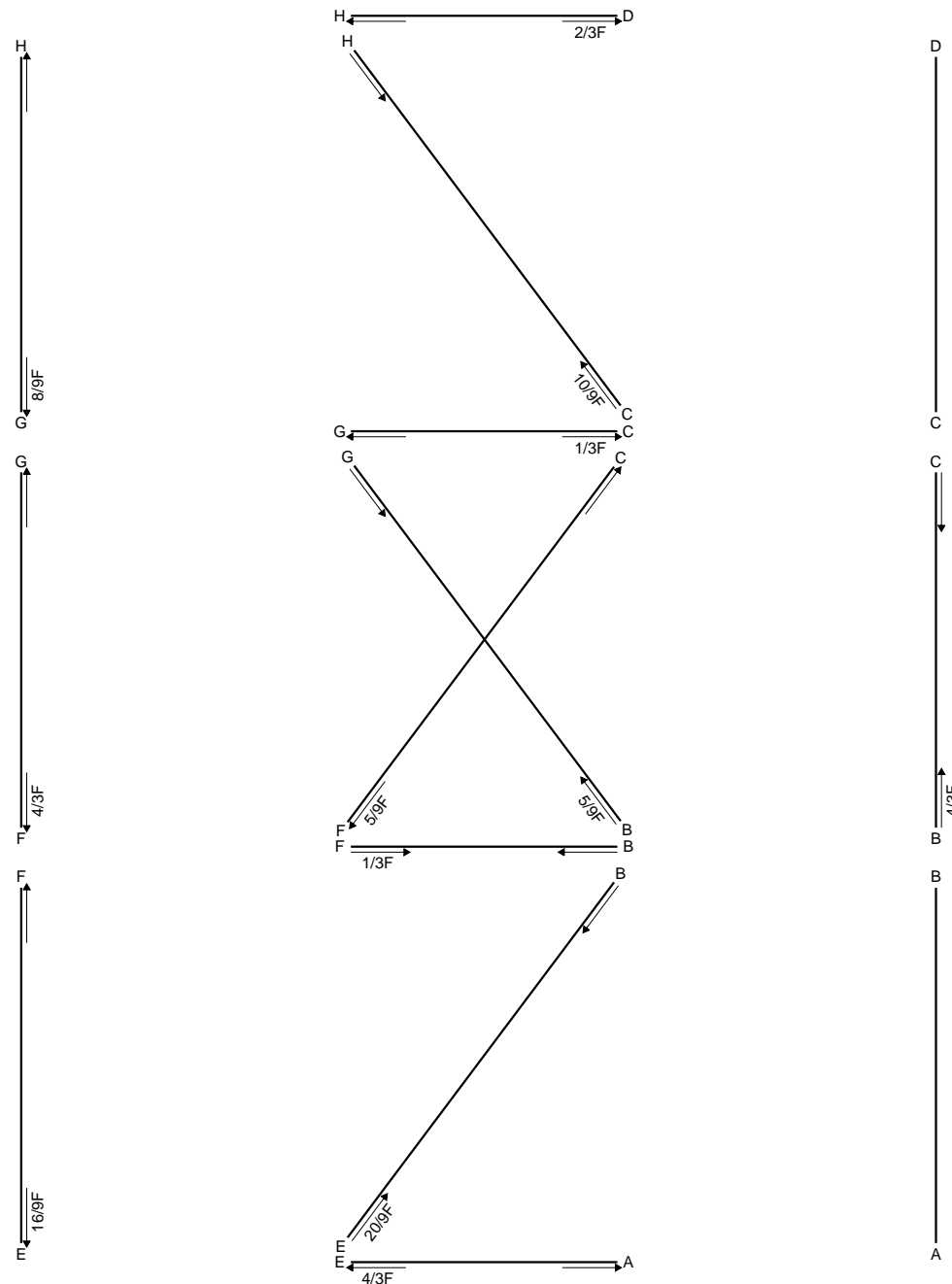
$$\begin{bmatrix} \phi_{AE} \\ \phi_{EF} \\ \phi_{FG} \\ \phi_{FB} \\ \phi_{GH} \\ \phi_{GC} \\ \phi_{HD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{DC} b & H_{BE} b & H_{CF} b & H_{GB} b & H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

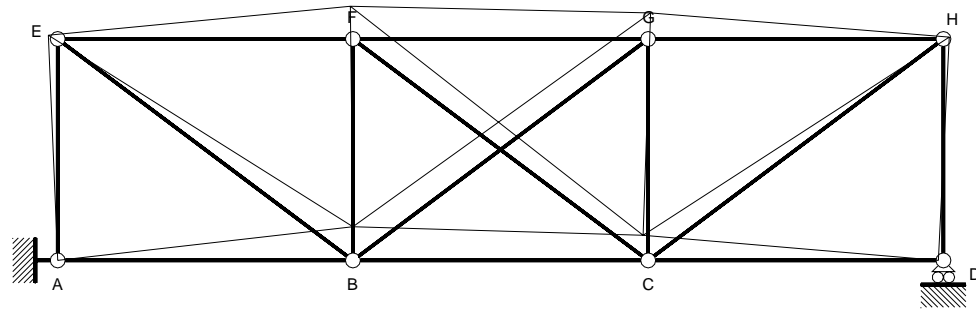
$$\begin{bmatrix} 12 & 0 & 0 & 0 & 0 & 0 & 0 \\ 12 & -3 & 0 & 0 & 0 & 0 & 0 \\ 8 & 0 & 0 & 0 & 0 & -3 & 0 \\ 0 & -3 & 0 & -3 & 0 & 3 & 0 \\ 4 & 0 & -3 & 0 & 0 & 0 & -3 \\ 0 & 0 & 3 & 0 & -3 & 0 & 3 \\ 0 & 0 & -3 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & -8 \\ 0 & -8 \\ 3 & 0 \\ -3 & 0 \\ 0 & 0 \\ 3 & 0 \\ 0 & 0 \end{bmatrix}$$

## Soluzione del sistema

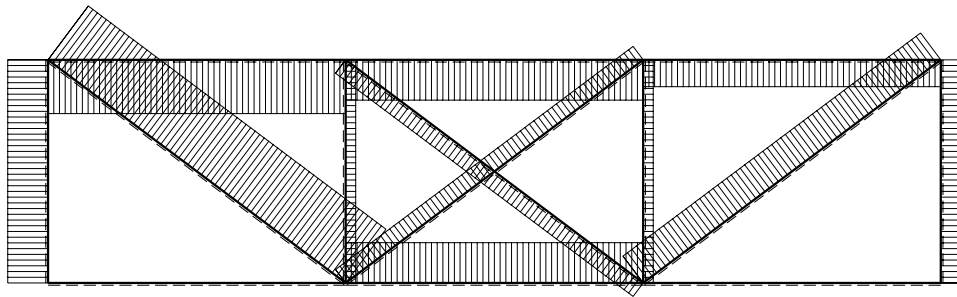
$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 0 & -2/3 \\ 0 & 0 \\ -1 & -16/9 \\ 0 & -16/9 \\ 0 & 0 \\ -1 & -8/9 \\ 0 & -8/9 \end{bmatrix}$$





80 Fb/EA



← ⊕ → 2.5 F

## REAZIONI

$$H_A = 0 \quad V_A = -4/3F \quad V_D = -2/3F$$

$$N_{AB} = 0 \quad N_{BC} = -4/3F \quad N_{CD} = 0 \quad N_{EB} = -20/9F \quad N_{FC} = 5/9F \quad N_{BG} = -5/9F$$

$$N_{CH} = -10/9F \quad N_{EF} = 16/9F \quad N_{FG} = 4/3F \quad N_{GH} = 8/9F \quad N_{EA} = 4/3F \quad N_{FB} = -1/3F$$

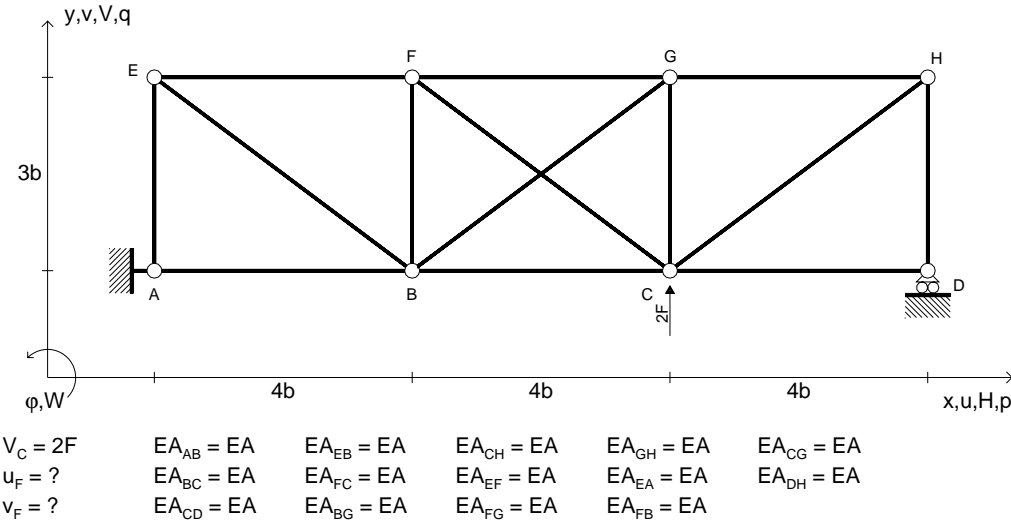
$$N_{CG} = 1/3F \quad N_{DH} = 2/3F$$

## SPOSTAMENTI ASSOLUTI

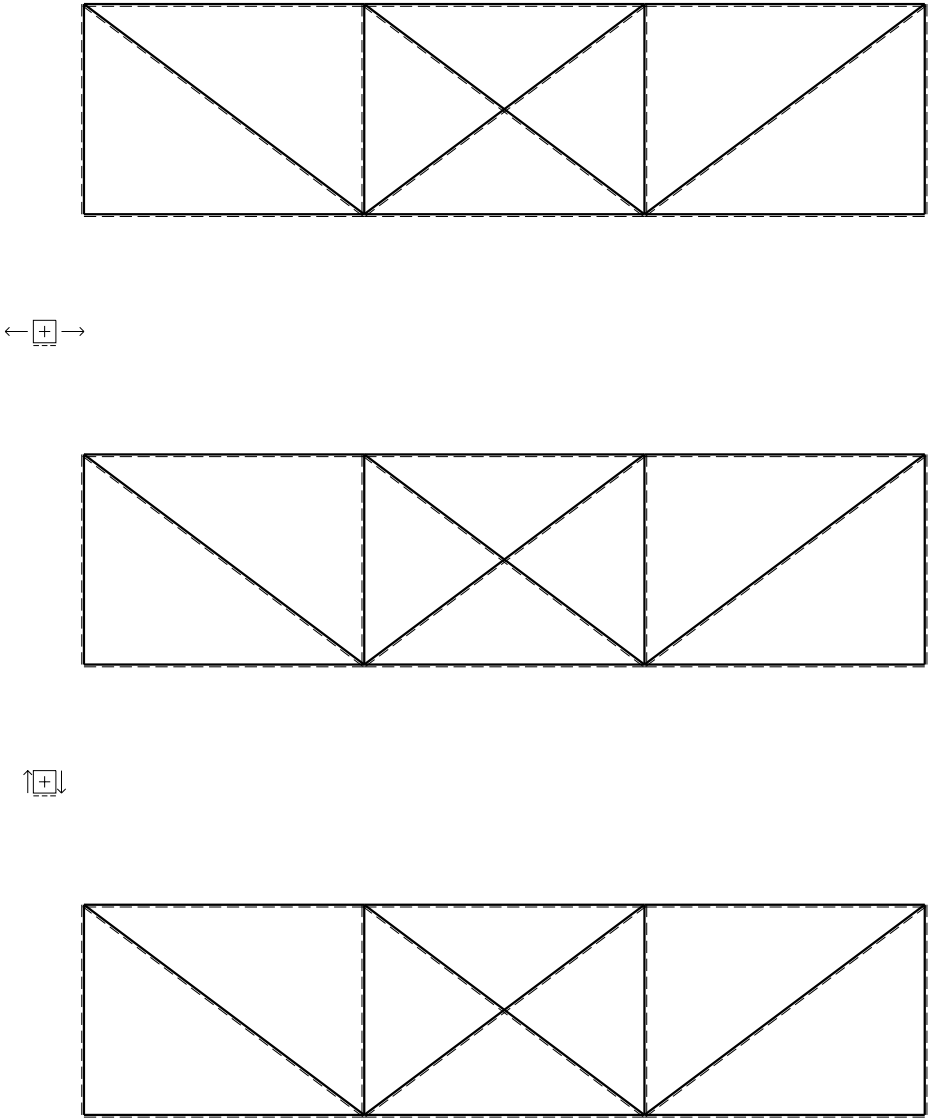
$$u_G = 70/27(Fb/EA)$$

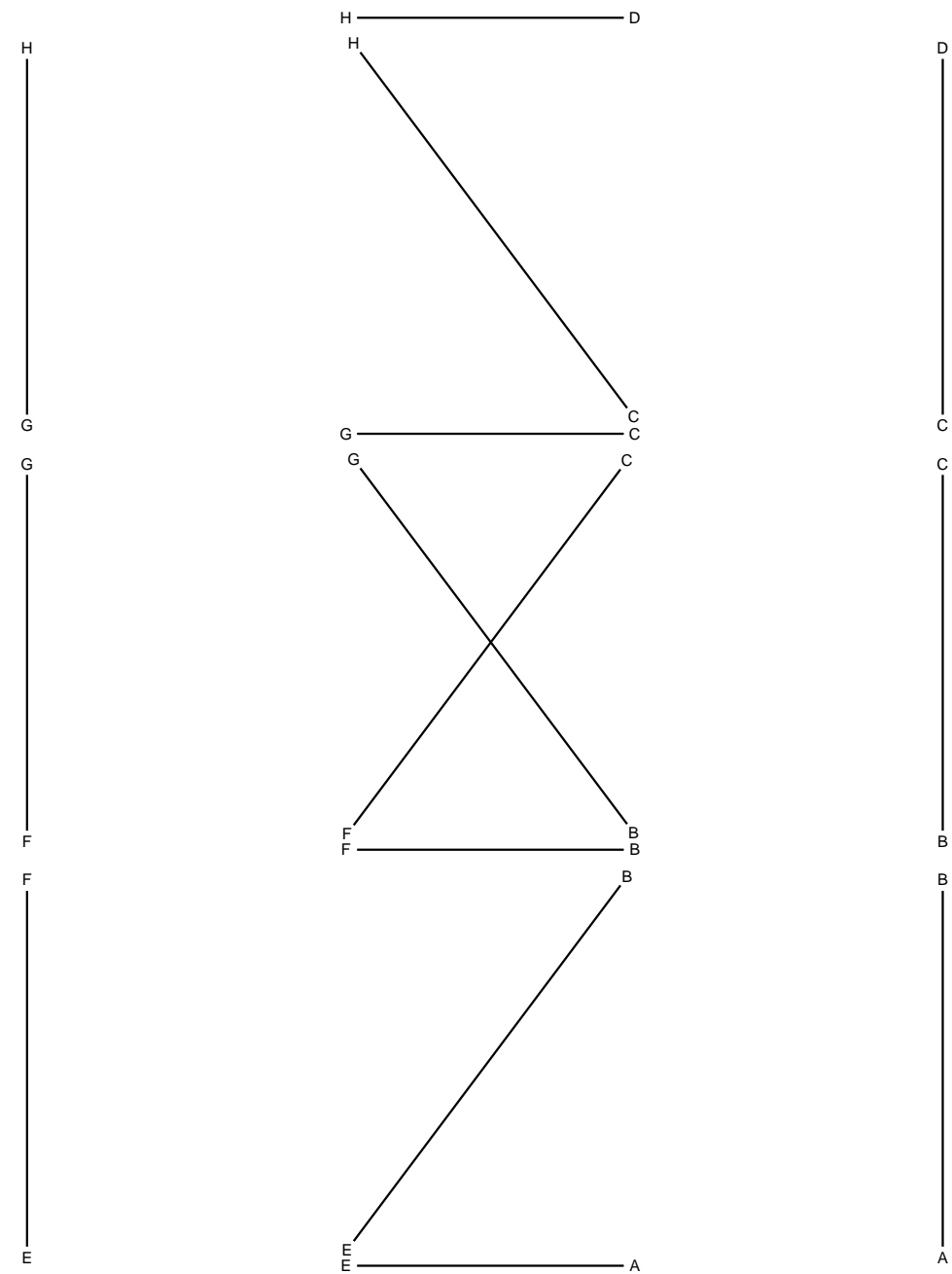
$$v_G = 2233/81(Fb/EA)$$





Svolgere l'analisi cinematica.  
Riportare la soluzione su questo foglio.  
Carichi e deformazioni date hanno verso efficace in disegno.  
Calcolare reazioni vincolari della struttura e delle aste.  
Tracciare i diagrammi delle azioni interne nelle aste.  
 $A_{YZ} - x_{YZ} - \theta_{YZ}$  riferimento locale asta YZ con origine in Y.  
Calcolare lo spostamento orizzont. del nodo F  
Calcolare lo spostamento verticale del nodo F  
@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$        $V_A =$        $V_D =$

$N_{AB} =$        $N_{BC} =$        $N_{CD} =$        $N_{EB} =$        $N_{FC} =$        $N_{BG} =$

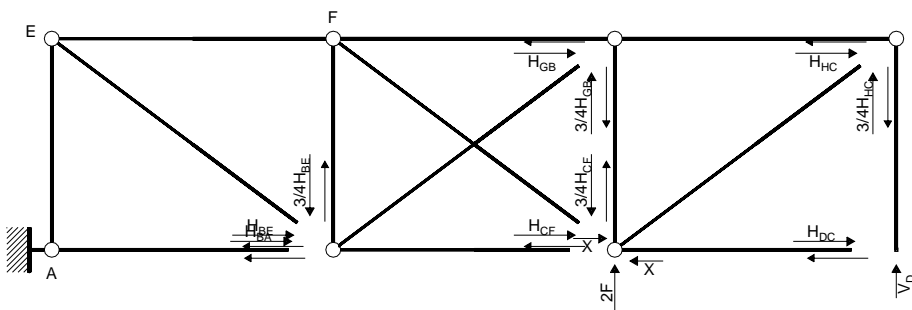
$N_{CH} =$        $N_{EF} =$        $N_{FG} =$        $N_{GH} =$        $N_{EA} =$        $N_{FB} =$

$N_{CG} =$        $N_{DH} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$12V_{Db} = -16Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b - 3H_{BA} b = -16Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$8V_D b - 3H_{GB} b = 3Xb - 8Fb$$

Rotazione intorno a F: aste FB BC BG

$$-3H_{BA}b - 3H_{BF}b + 3H_{GB}b = -3Xb$$

Rotazione intorno a G: aste GH HD

$$4V_{D,b} - 3H_{DG,b} - 3H_{HG,b} = 0$$

Rotazione intorno a G: aste GC CD CH

$$3H_{DC}b - 3H_{CF}b + 3H_{HC}b = 3Xb$$

Rotazione intorno a H: aste HD

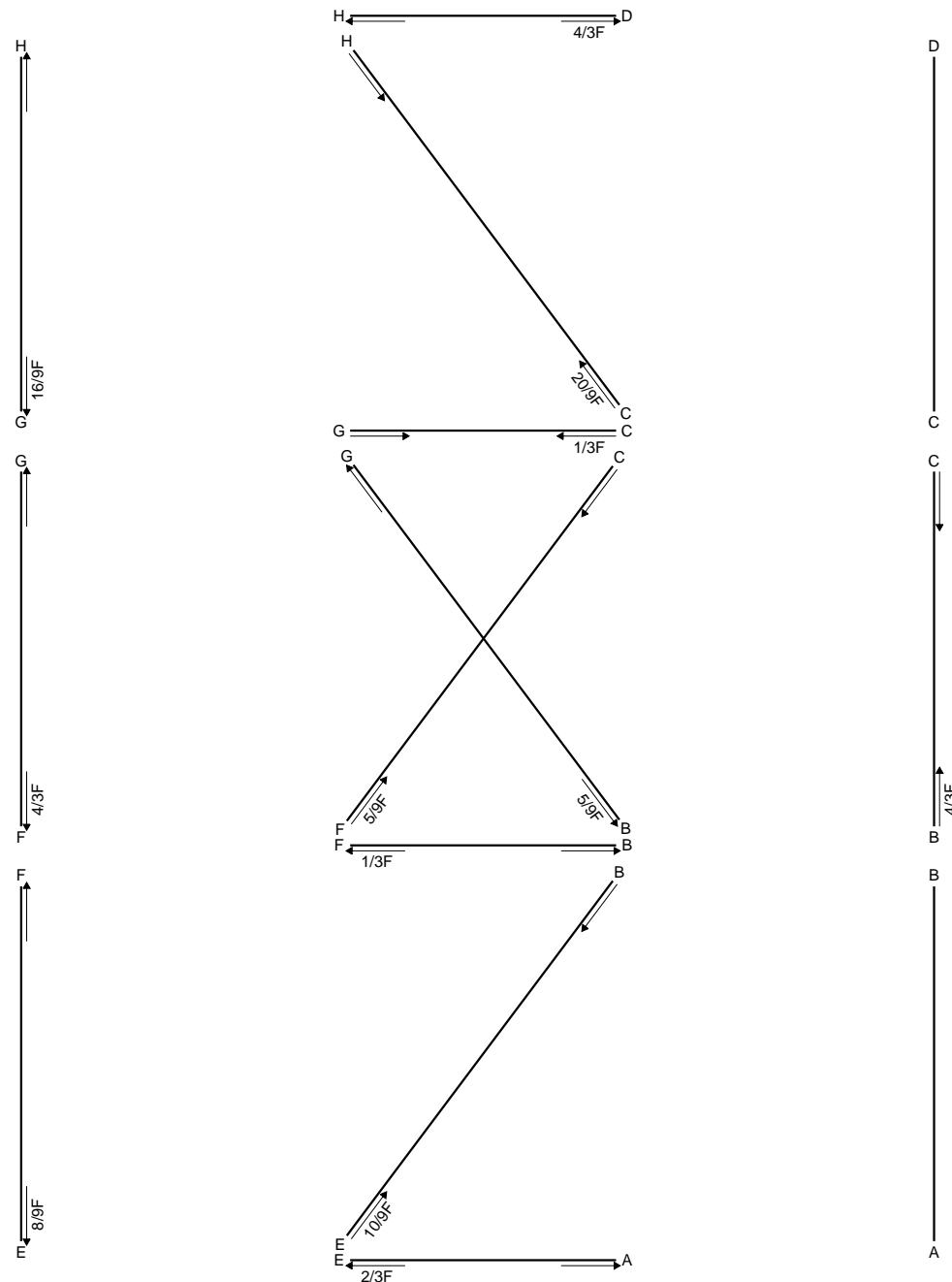
$$-3H_{DC}b = 0$$

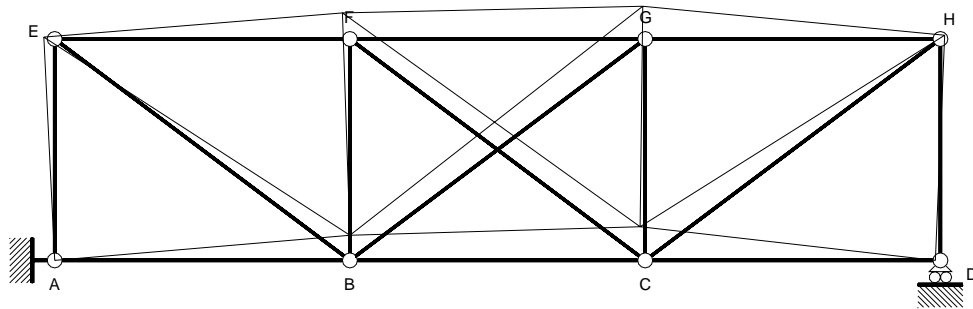
### Matrice di equilibrio

$$\begin{bmatrix} \Phi_{AE} \\ \Phi_{EF} \\ \Phi_{FG} \\ \Phi_{FB} \\ \Phi_{GH} \\ \Phi_{GC} \\ \Phi_{GD} \end{bmatrix} \begin{bmatrix} V_D & H_{BA} & H_{DC} & H_{BE} & H_{CF} & H_{GB} & H_{HC} \\ b & b & b & b & b & b & b \end{bmatrix} = \begin{bmatrix} X_B & F_B \\ F_D & F_D \end{bmatrix}$$

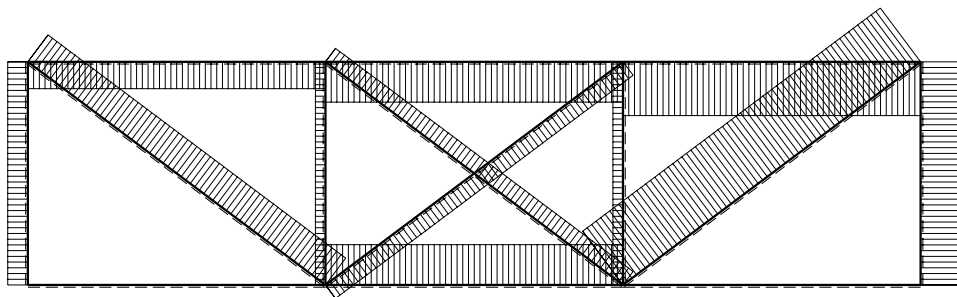
### Soluzione del sistema

$$\begin{bmatrix} V_{\text{p}}b \\ H_{\text{BA}}b \\ H_{\text{GB}}b \\ H_{\text{BE}}b \\ H_{\text{DC}}b \\ H_{\text{CF}}b \\ H_{\text{HC}}b \end{bmatrix} = \begin{bmatrix} \text{Xb} & \text{Fb} \\ 0 & -4/3 \\ 0 & 0 \\ -1 & -8/9 \\ 0 & -8/9 \\ 0 & 0 \\ -1 & -16/9 \\ 0 & -16/9 \end{bmatrix}$$





80 Fb/EA



2.5 F

## REAZIONI

$$H_A = 0 \quad V_A = -2/3F \quad V_D = -4/3F$$

$$N_{AB} = 0 \quad N_{BC} = -4/3F \quad N_{CD} = 0 \quad N_{EB} = -10/9F \quad N_{FC} = -5/9F \quad N_{BG} = 5/9F$$

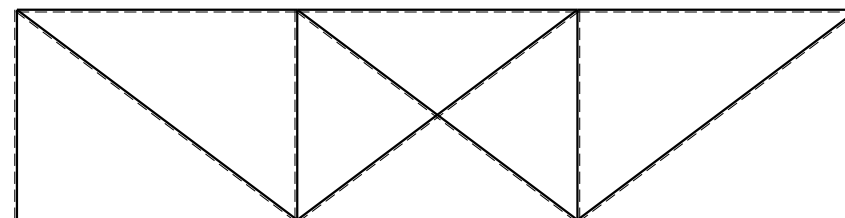
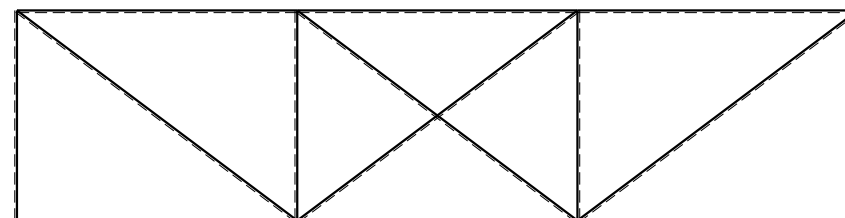
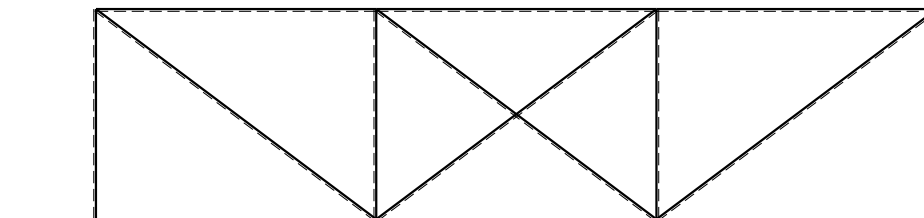
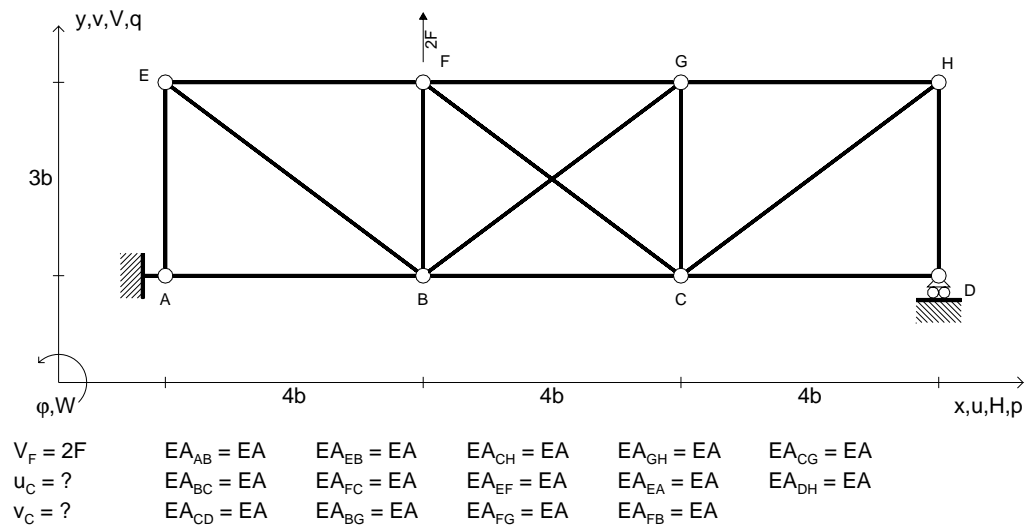
$$N_{CH} = -20/9F \quad N_{EF} = 8/9F \quad N_{FG} = 4/3F \quad N_{GH} = 16/9F \quad N_{EA} = 2/3F \quad N_{FB} = 1/3F$$

$$N_{CG} = -1/3F \quad N_{DH} = 4/3F$$

## SPOSTAMENTI ASSOLUTI

$$u_F = -214/27(Fb/EA)$$

$$v_F = 2233/81(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ}$  -  $x_{YZ}$  -  $\theta_{YZ}$  riferimento locale asta YZ con origine in Y.

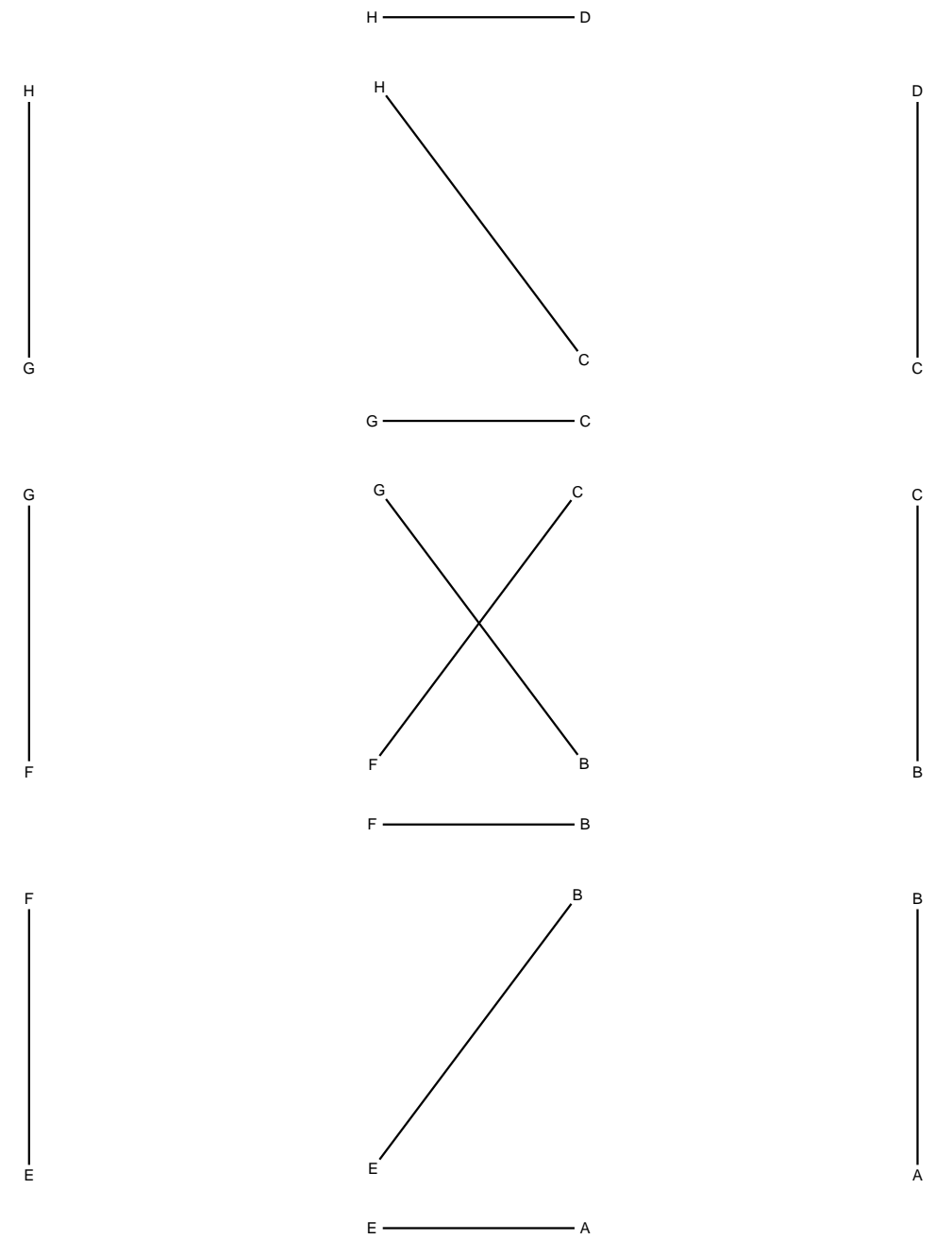
Calcolare lo spostamento orizzont. del nodo C

Calcolare lo spostamento verticale del nodo C

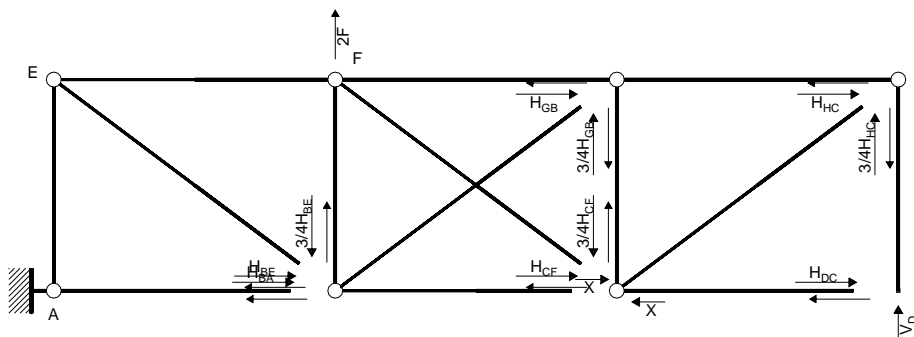
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REAZIONI					
$H_A =$	$V_A =$	$V_D =$			
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EB} =$	$N_{FC} =$	$N_{BG} =$
$N_{CH} =$	$N_{EF} =$	$N_{FG} =$	$N_{GH} =$	$N_{EA} =$	$N_{FB} =$
$N_{CG} =$	$N_{DH} =$				
SPOSTAMENTI ASSOLUTI					
$u_C =$					
$v_C =$					



## EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EB EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b = -8Fb$$

Rotazione intorno a E: aste EF FC FG FB BC BG GH GC CD CH HD

$$12V_D b - 3H_{BA} b = -8Fb$$

Rotazione intorno a F: aste FG GH GC CD CH HD

$$8V_D b - 3H_{GB} b = 3Xb$$

Rotazione intorno a G: aste FB BC BG

$$-3H_{BA} b - 3H_{BE} b + 3H_{GB} b = -3Xb$$

Rotazione intorno a H: aste GH HD

$$4V_D b - 3H_{DC} b - 3H_{HC} b = 0$$

Rotazione intorno a G: aste GC CD CH

$$3H_{DC} b - 3H_{CF} b + 3H_{HC} b = 3Xb$$

Rotazione intorno a H: aste HD

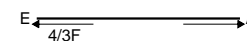
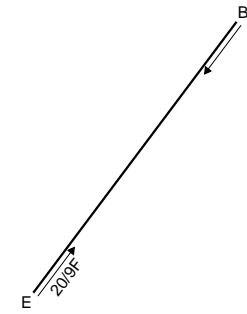
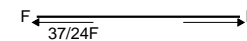
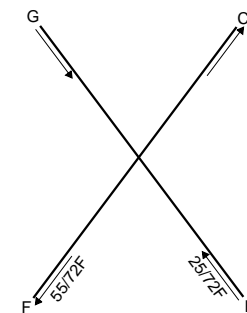
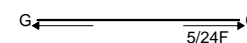
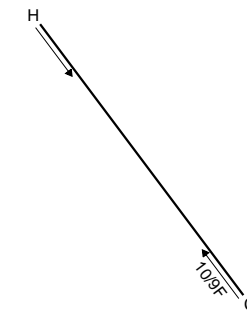
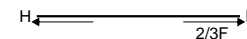
$$-3H_{DC} b = 0$$

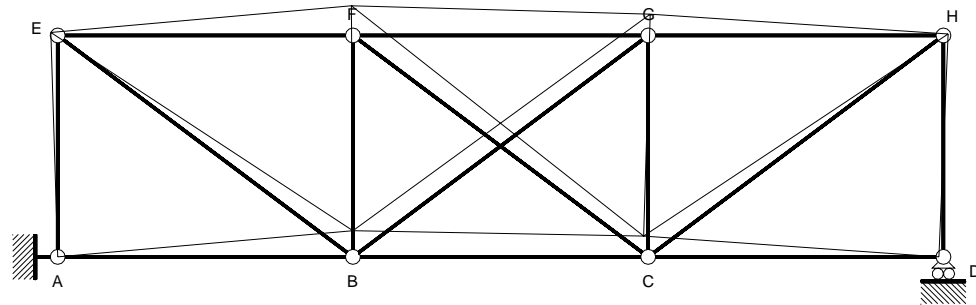
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EF} \\ \phi_{FG} \\ \phi_{FB} \\ \phi_{GH} \\ \phi_{GC} \\ \phi_{HD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{DC} b & H_{BE} b & H_{CF} b & H_{GB} b & H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

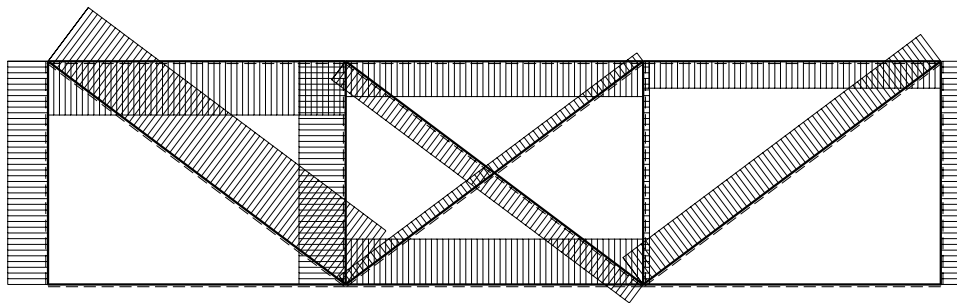
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{GB} b \\ H_{BE} b \\ H_{DC} b \\ H_{CF} b \\ H_{HC} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$





100 Fb/EA



← ⊕ → 2.5 F

## REAZIONI

$$H_A = 0 \quad V_A = -4/3F \quad V_D = -2/3F$$

$$N_{AB} = 0 \quad N_{BC} = -3/2F \quad N_{CD} = 0 \quad N_{EB} = -20/9F \quad N_{FC} = 55/72F \quad N_{BG} = -25/72F$$

$$N_{CH} = -10/9F \quad N_{EF} = 16/9F \quad N_{FG} = 7/6F \quad N_{GH} = 8/9F \quad N_{EA} = 4/3F \quad N_{FB} = 37/24F$$

$$N_{CG} = 5/24F \quad N_{DH} = 2/3F$$

## SPOSTAMENTI ASSOLUTI

$$u_C = -6(Fb/EA)$$

$$v_C = 2233/81(Fb/EA)$$