

Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Allungamento termico assegnato ε su asta BC.

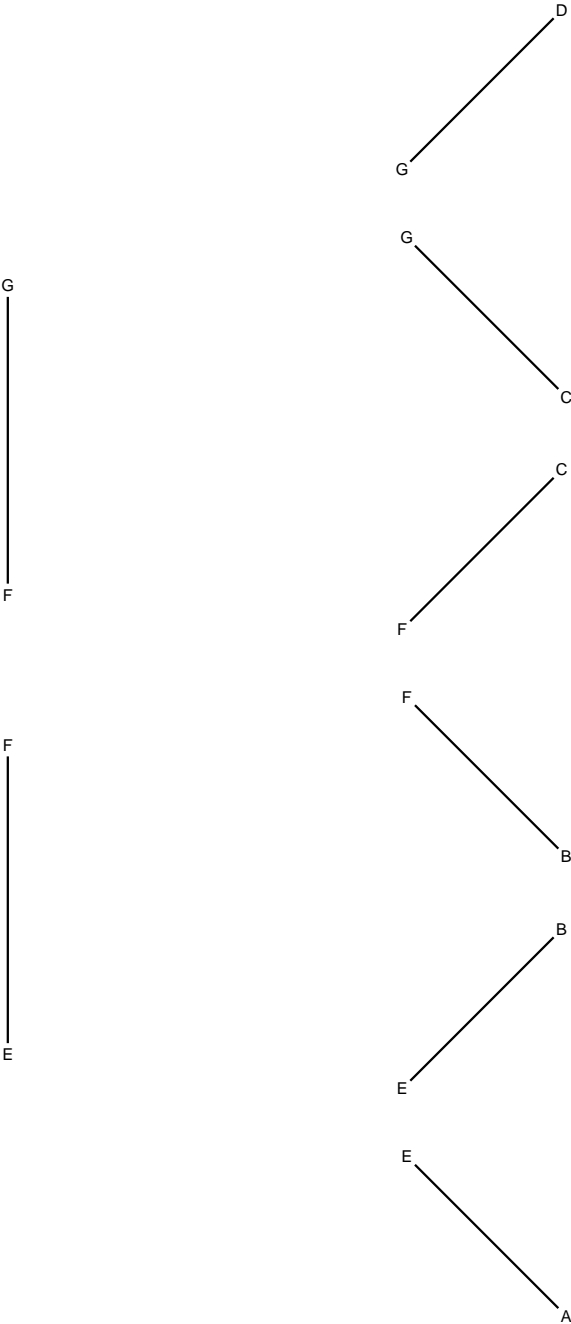
Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

@ Adolfo Zavelani Rossi, Politecnico di Milano



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REAZIONI

$H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

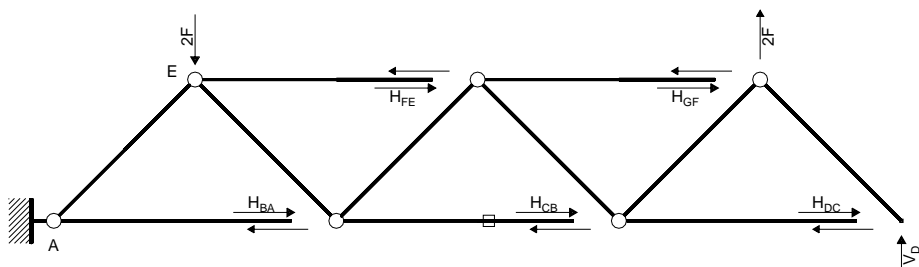
$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -8Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -8Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -6Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = -4Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = -2Fb$$

Rotazione intorno a G: aste GD

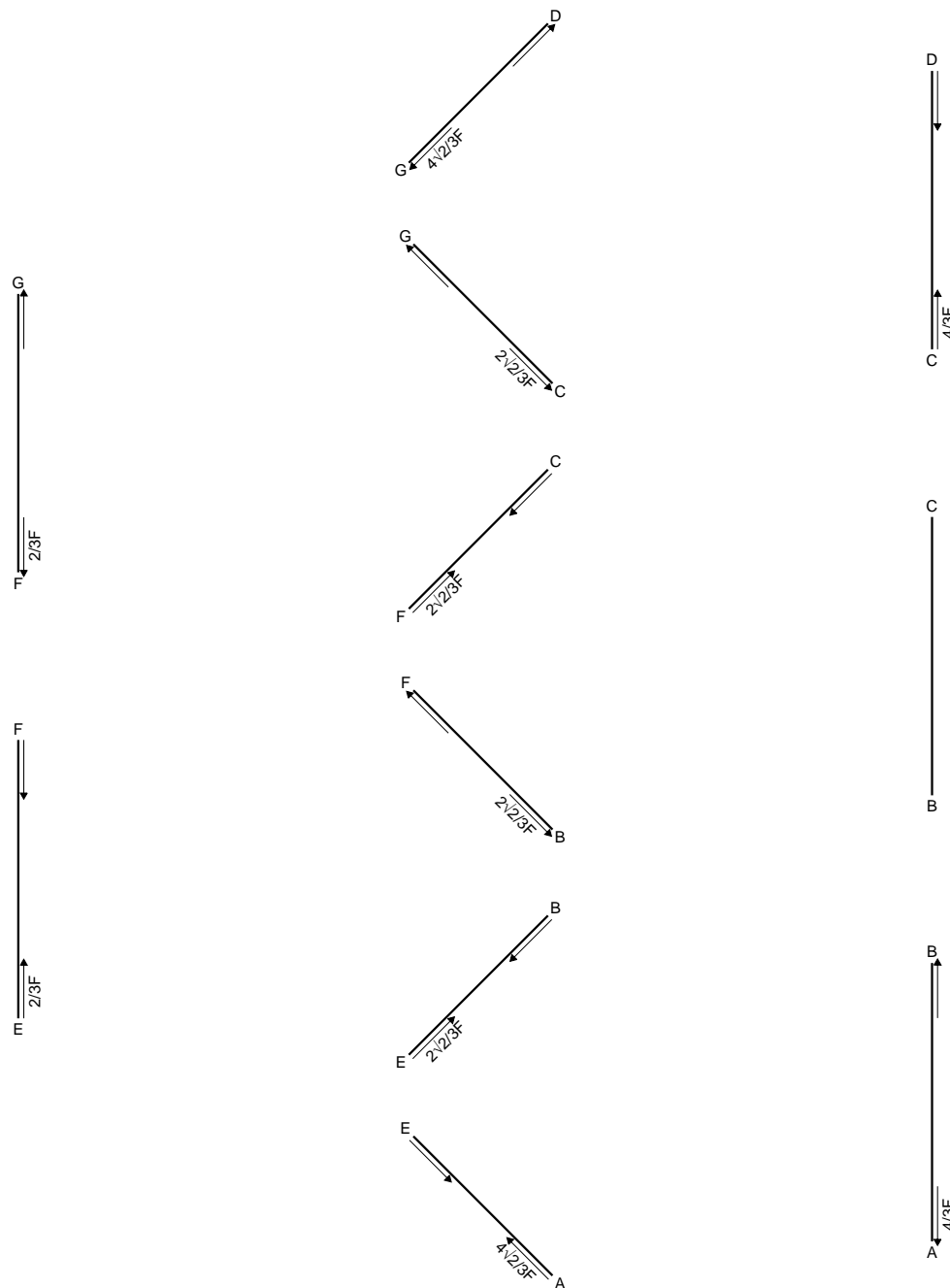
$$V_D b - H_{DC} b = 0$$

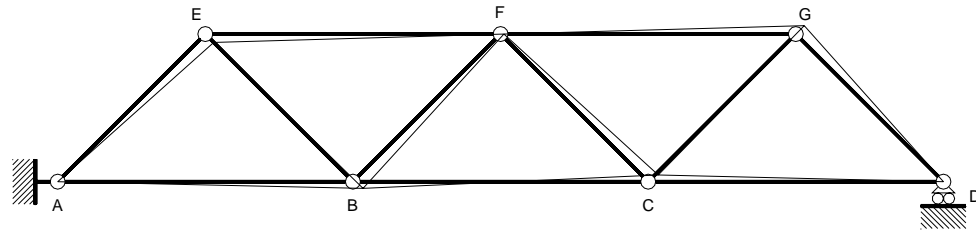
Matrice di equilibrio

$$\begin{bmatrix} \varphi_{AE} \\ \varphi_{EB} \\ \varphi_{BF} \\ \varphi_{FC} \\ \varphi_{CG} \\ \varphi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -8 \\ -8 \\ -6 \\ -4 \\ -2 \\ 0 \end{bmatrix} Fb$$

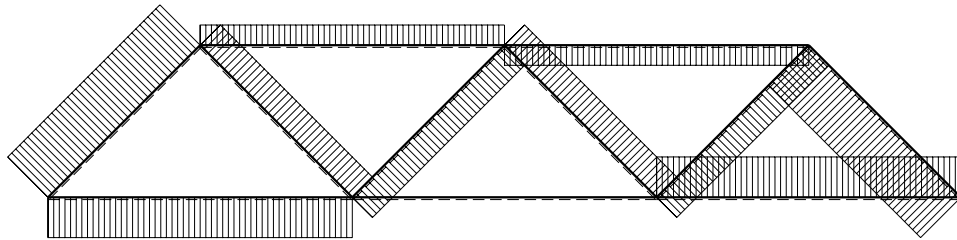
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -4/3 \\ 4/3 \\ -2/3 \\ 0 \\ 2/3 \\ -4/3 \end{bmatrix} Fb$$





1 — 20 Fb/EA



← ⊕ → 1 — 2.5 F

REAZIONI

$$H_A = 0 \quad V_A = 4/3F \quad V_D = -4/3F$$

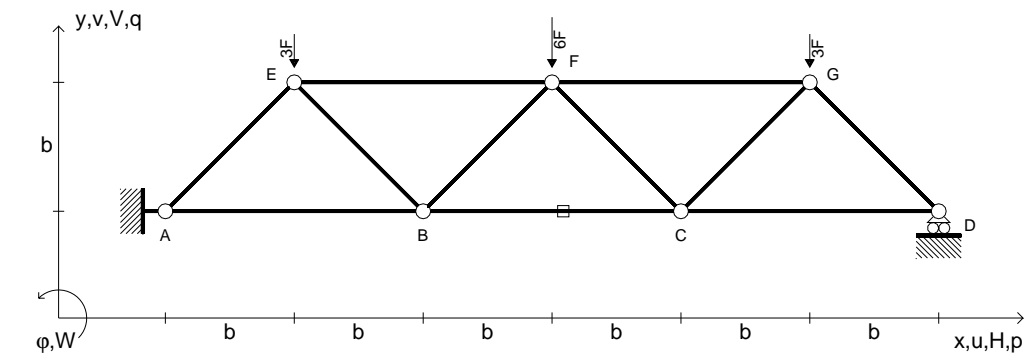
$$N_{AB} = 4/3F \quad N_{BC} = 0 \quad N_{CD} = -4/3F \quad N_{EF} = -2/3F \quad N_{FG} = 2/3F \quad N_{AE} = -4\sqrt{2}/3F$$

$$N_{EB} = -2\sqrt{2}/3F \quad N_{BF} = 2\sqrt{2}/3F \quad N_{FC} = -2\sqrt{2}/3F \quad N_{CG} = 2\sqrt{2}/3F \quad N_{GD} = 4\sqrt{2}/3F$$

SPOSTAMENTI ASSOLUTI

$$u_F = 26/9(Fb/EA)$$

$$v_F = -6(Fb/EA)$$

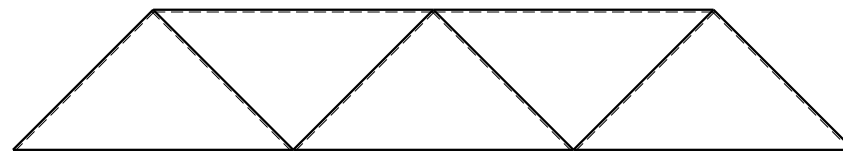
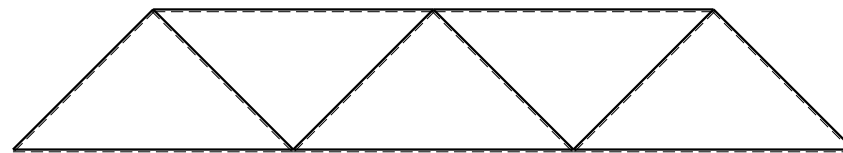
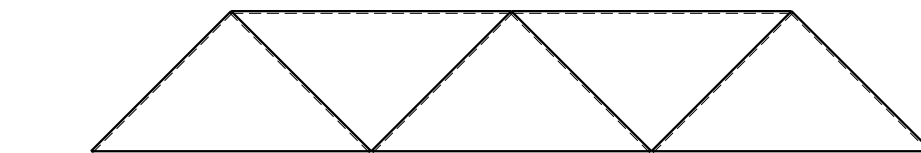


$$\begin{aligned} V_E &= -3F \\ V_F &= -6F \\ V_G &= -3F \\ \varepsilon_{BC} &= 2\alpha T = 2F/EA \\ u_F &= ? \end{aligned}$$

$$\begin{aligned} v_F &= ? \\ EA_{AB} &= EA \\ EA_{BC} &= 3EA \\ EA_{CD} &= EA \\ EA_{EF} &= EA \end{aligned}$$

$$\begin{aligned} EA_{FG} &= EA \\ EA_{AE} &= EA \\ EA_{EB} &= EA \\ EA_{BF} &= EA \\ EA_{FC} &= EA \end{aligned}$$

$$\begin{aligned} EA_{CG} &= EA \\ EA_{GD} &= EA \end{aligned}$$



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Tracciare i diagrammi delle azioni interne nelle aste.

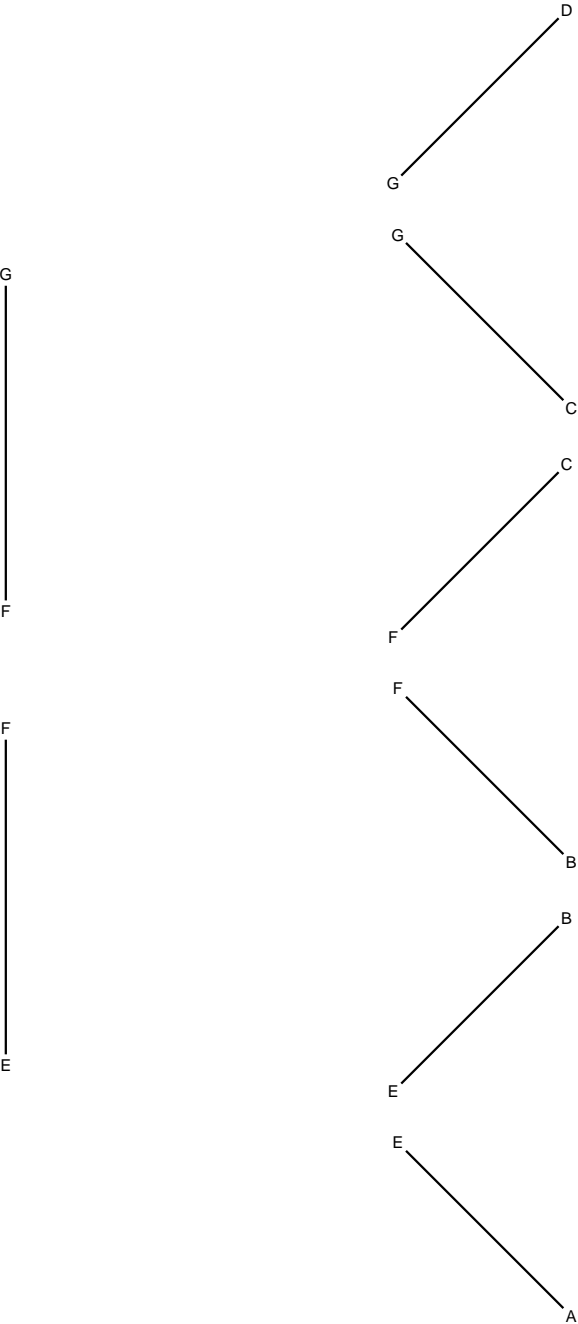
A_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

Allungamento termico assegnato ε su asta BC.

Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

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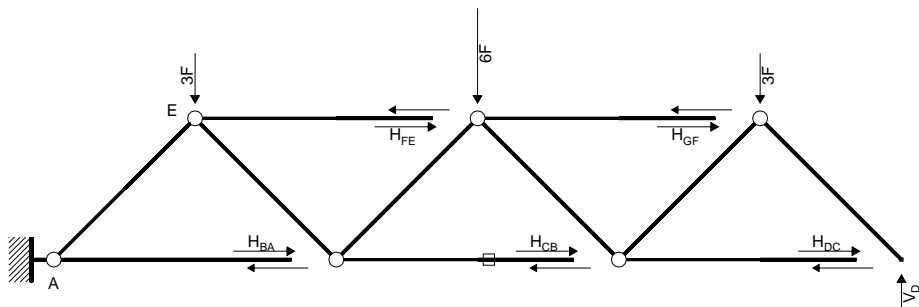
REAZIONI
 $H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

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SPOSTAMENTI ASSOLUTI
 $u_F =$
 $v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 36Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 24Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 15Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 6Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 3Fb$$

Rotazione intorno a G: aste GD

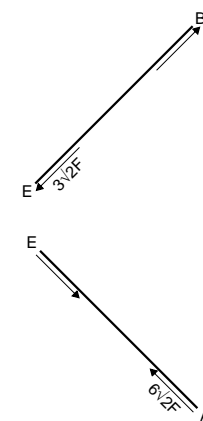
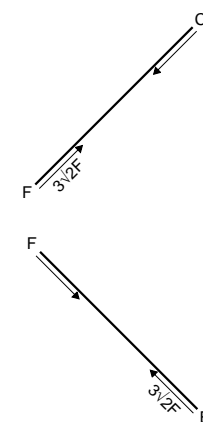
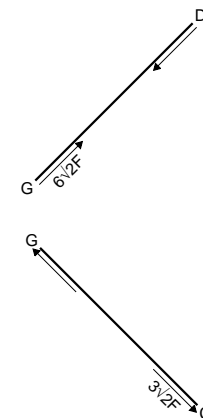
$$V_D b - H_{DC} b = 0$$

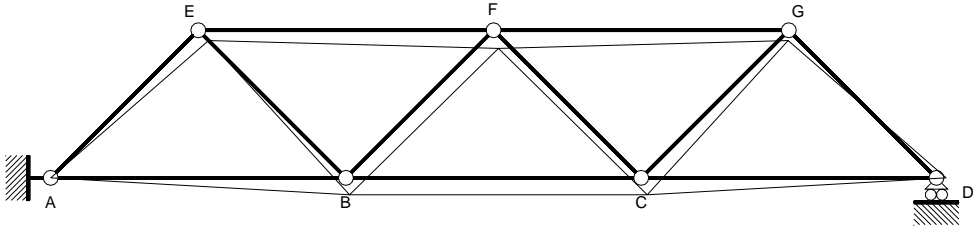
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 36 \\ 24 \\ 15 \\ 6 \\ 3 \\ 0 \end{bmatrix} Fb$$

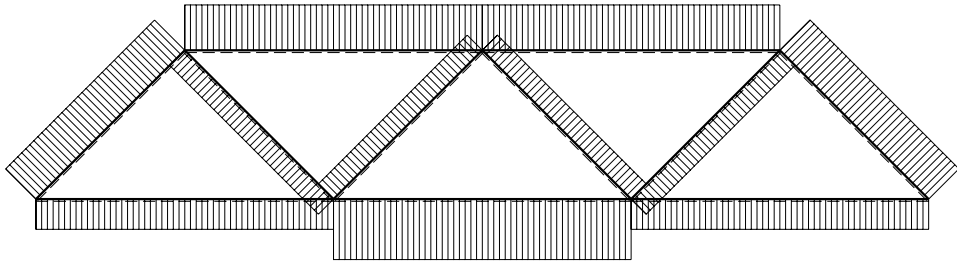
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 6 \\ 6 \\ -9 \\ 12 \\ -9 \\ 6 \end{bmatrix} Fb$$





250 Fb/EA



15 F

REAZIONI

$H_A = 0$ $V_A = 6F$ $V_D = 6F$

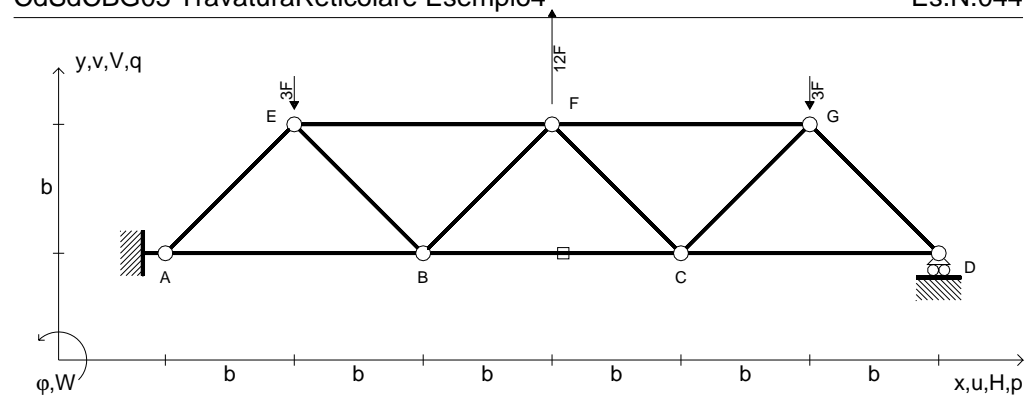
$N_{AB} = 6F$ $N_{BC} = 12F$ $N_{CD} = 6F$ $N_{EF} = -9F$ $N_{FG} = -9F$ $N_{AE} = -6\sqrt{2}F$

$N_{EB} = 3\sqrt{2}F$ $N_{BF} = -3\sqrt{2}F$ $N_{FC} = -3\sqrt{2}F$ $N_{CG} = 3\sqrt{2}F$ $N_{GD} = -6\sqrt{2}F$

SPOSTAMENTI ASSOLUTI

$u_F = 18(Fb/EA)$

$v_F = -(66+24\sqrt{2})(Fb/EA)$



$$\begin{aligned} V_E &= -3F \\ V_F &= 12F \\ V_G &= -3F \\ \varepsilon_{BC} &= 2\alpha T = 2F/EA \\ u_F &= ? \end{aligned}$$

$$\begin{aligned} v_F &= ? \\ EA_{AB} &= EA \\ EA_{BC} &= 4EA \\ EA_{CD} &= EA \\ EA_{EF} &= EA \end{aligned}$$

$$\begin{aligned} EA_{FG} &= EA \\ EA_{AE} &= EA \\ EA_{EB} &= EA \\ EA_{BF} &= EA \\ EA_{FC} &= EA \end{aligned}$$

$$\begin{aligned} EA_{CG} &= EA \\ EA_{GD} &= EA \end{aligned}$$



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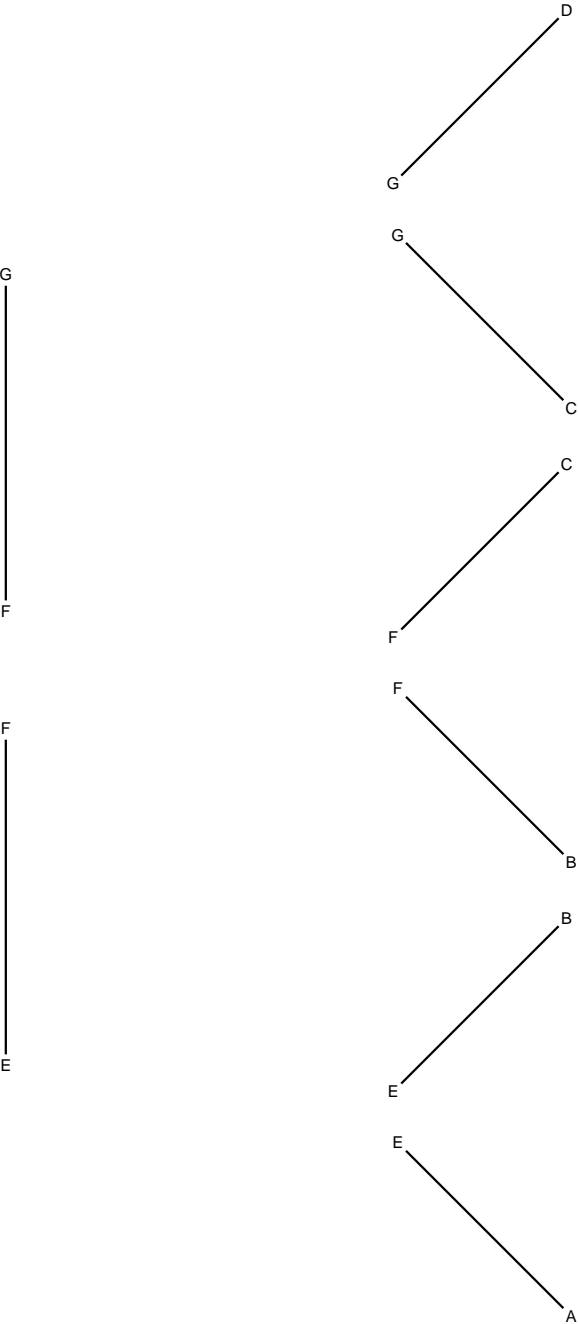
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Allungamento termico assegnato ε su asta BC.

Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

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REAZIONI

$H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

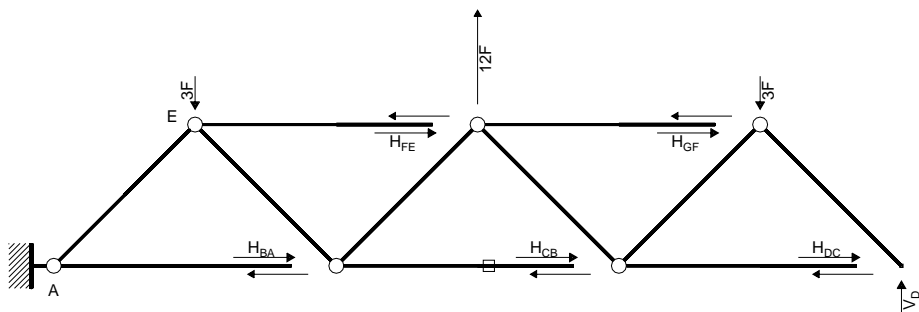
$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -18Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -12Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -3Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 6Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 3Fb$$

Rotazione intorno a G: aste GD

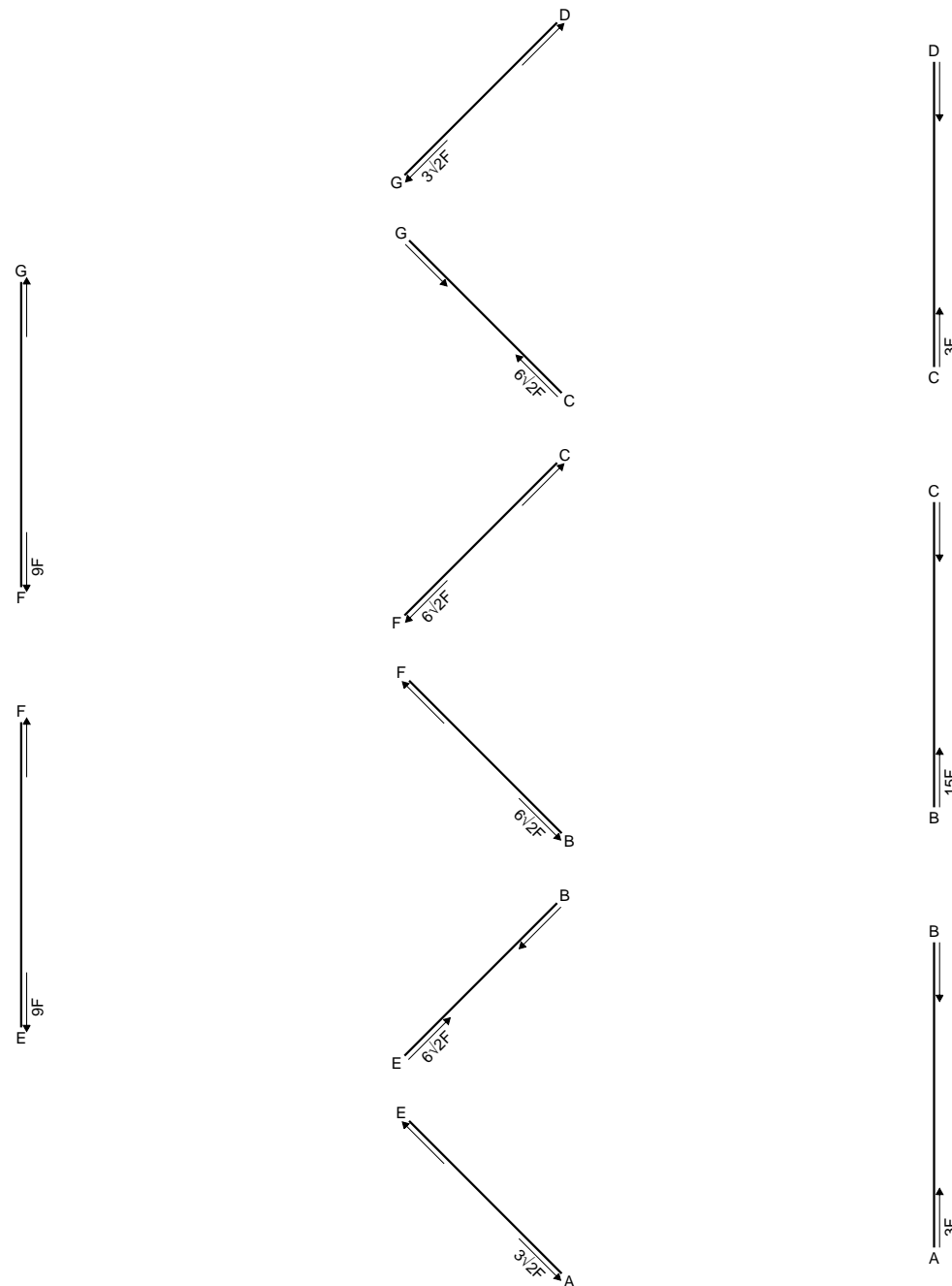
$$V_D b - H_{DC} b = 0$$

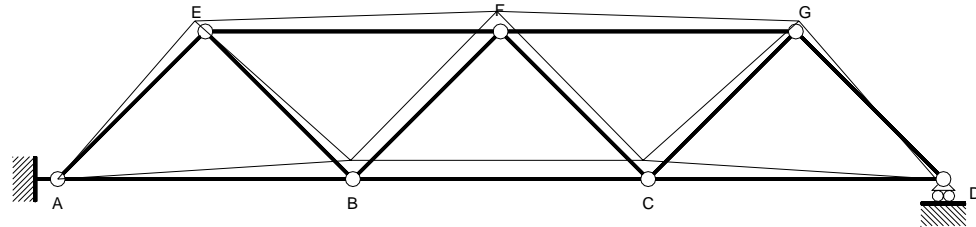
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -18 \\ -12 \\ -3 \\ 6 \\ 3 \\ 0 \end{bmatrix} Fb$$

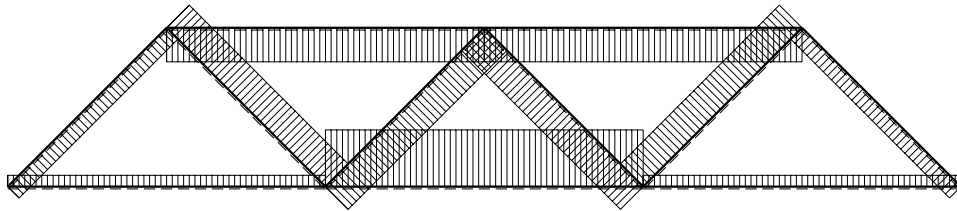
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -3 \\ -3 \\ 9 \\ -15 \\ 9 \\ -3 \end{bmatrix} Fb$$





← 200 Fb/EA



← + → | 20 F

REAZIONI

$$H_A = 0 \quad V_A = -3F \quad V_D = -3F$$

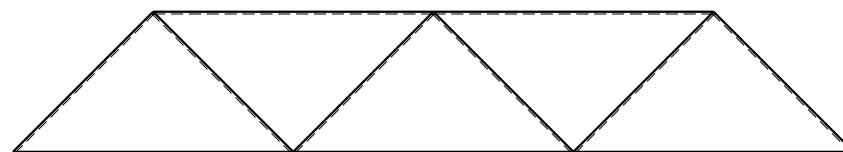
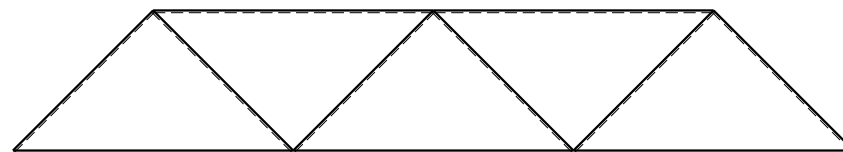
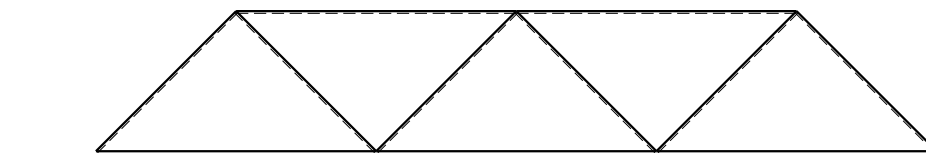
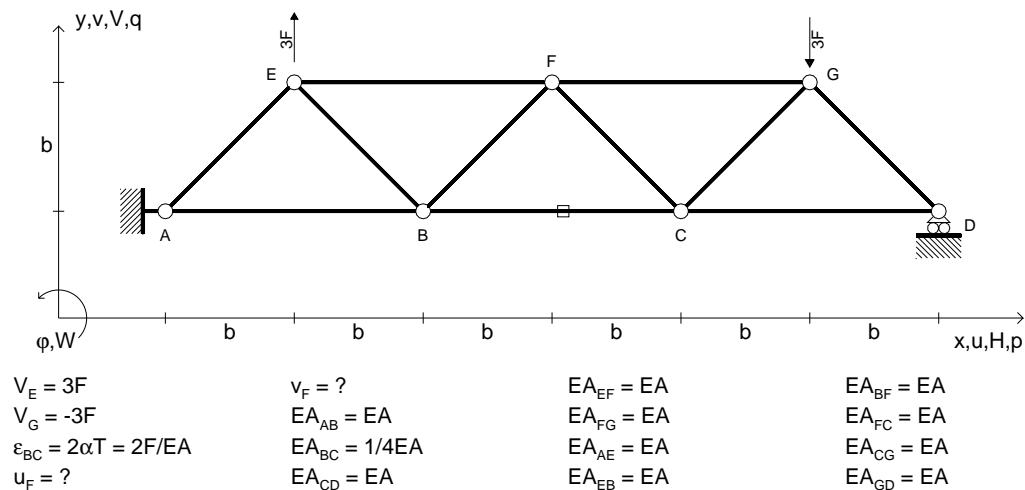
$$N_{AB} = -3F \quad N_{BC} = -15F \quad N_{CD} = -3F \quad N_{EF} = 9F \quad N_{FG} = 9F \quad N_{AE} = 3\sqrt{2}F$$

$$N_{EB} = -6\sqrt{2}F \quad N_{BF} = 6\sqrt{2}F \quad N_{FC} = 6\sqrt{2}F \quad N_{CG} = -6\sqrt{2}F \quad N_{GD} = 3\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

$$u_F = -31/4(Fb/EA)$$

$$v_F = (189+120\sqrt{2})/4(Fb/EA)$$



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Allungamento termico assegnato ε su asta BC.

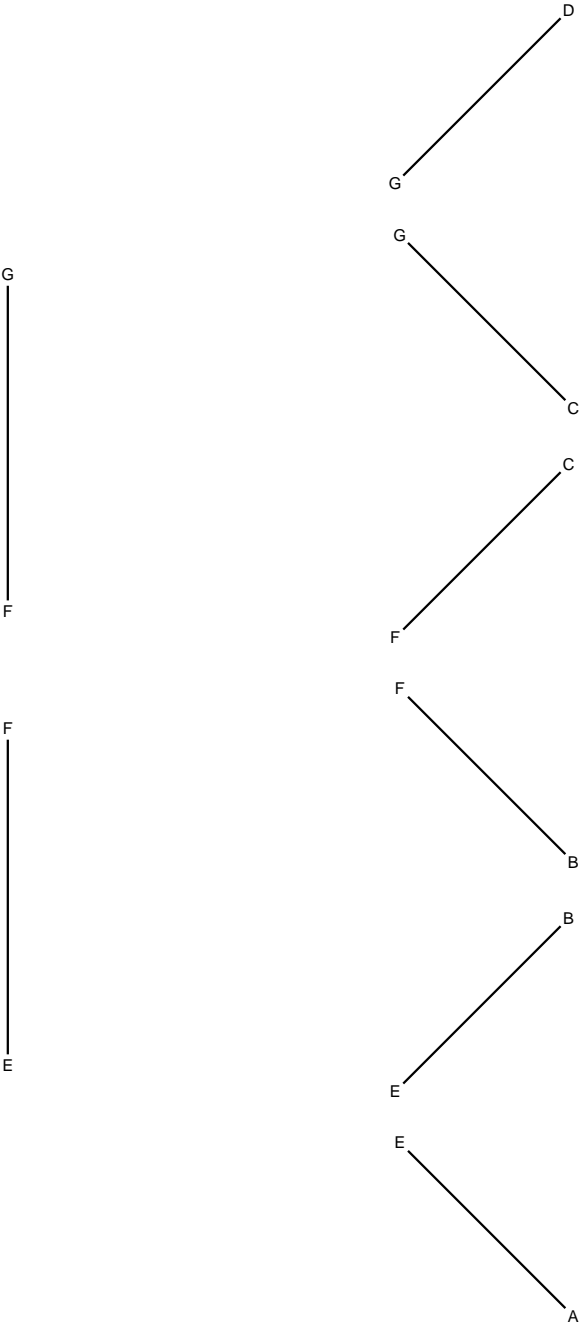
Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

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REAZIONI

$H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

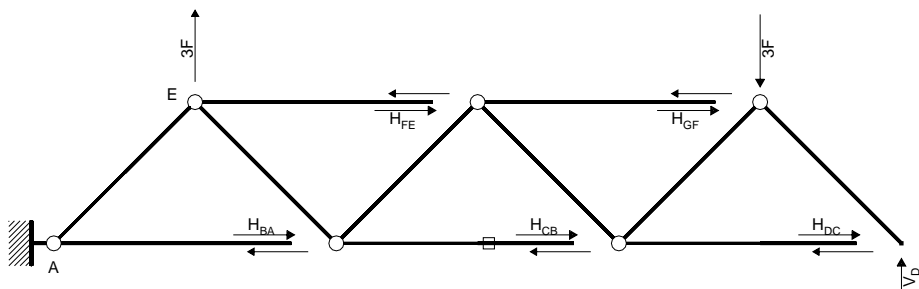
$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 12Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 12Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 9Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 6Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 3Fb$$

Rotazione intorno a G: aste GD

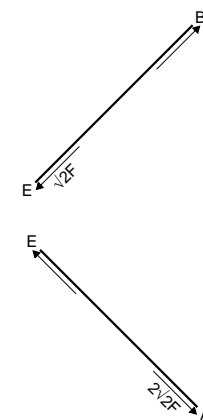
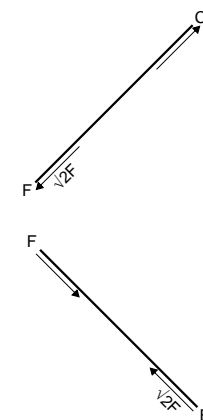
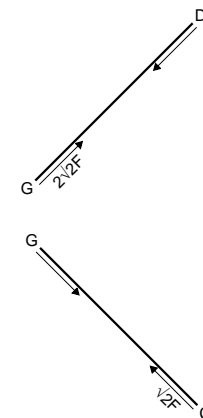
$$V_D b - H_{DC} b = 0$$

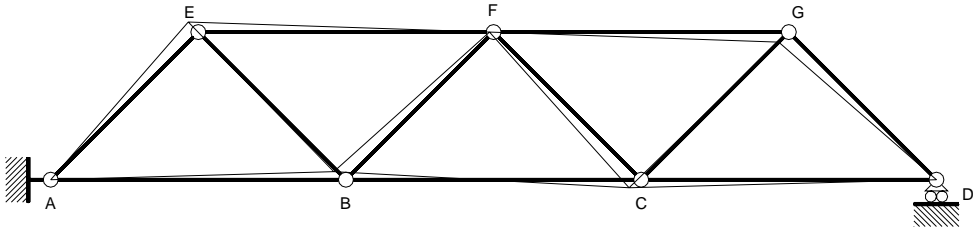
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 12 \\ 12 \\ 9 \\ 6 \\ 3 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

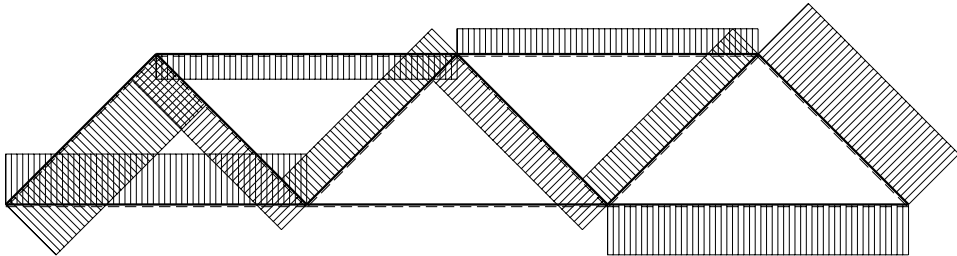
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 2 \\ -2 \\ 1 \\ 0 \\ -1 \\ 2 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





← 25 Fb/EA →



← + → ← 3 F →

REAZIONI

$H_A = 0 \quad V_A = -2F \quad V_D = 2F$

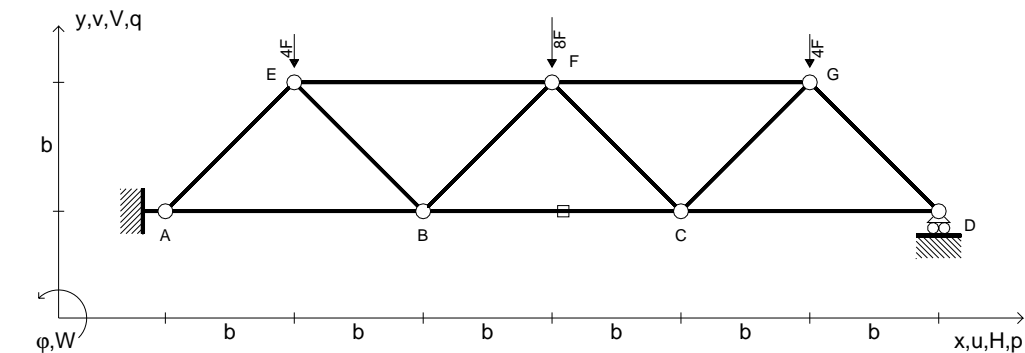
$N_{AB} = -2F \quad N_{BC} = 0 \quad N_{CD} = 2F \quad N_{EF} = F \quad N_{FG} = -F \quad N_{AE} = 2\sqrt{2}F$

$N_{EB} = \sqrt{2}F \quad N_{BF} = -\sqrt{2}F \quad N_{FC} = \sqrt{2}F \quad N_{CG} = -\sqrt{2}F \quad N_{GD} = -2\sqrt{2}F$

SPOSTAMENTI ASSOLUTI

$u_F = 2/3(Fb/EA)$

$v_F = -6(Fb/EA)$

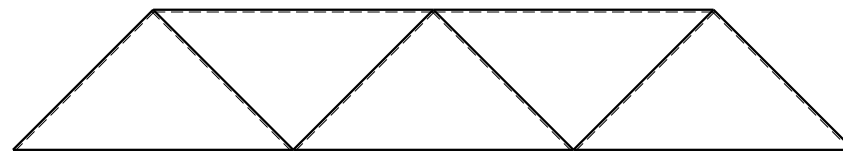
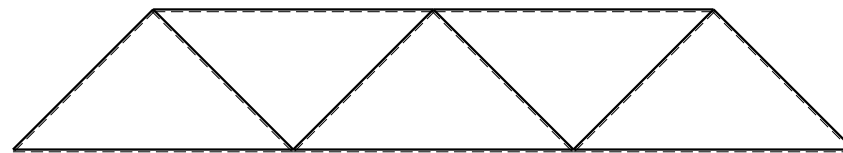
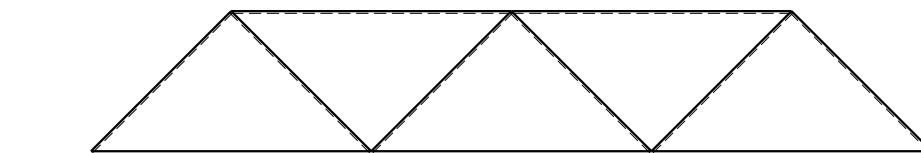


$$\begin{aligned} V_E &= -4F \\ V_F &= -8F \\ V_G &= -4F \\ \varepsilon_{BC} &= 2\alpha T = 2F/EA \\ u_F &= ? \end{aligned}$$

$$\begin{aligned} v_F &= ? \\ EA_{AB} &= EA \\ EA_{BC} &= 1/3EA \\ EA_{CD} &= EA \\ EA_{EF} &= EA \end{aligned}$$

$$\begin{aligned} EA_{FG} &= EA \\ EA_{AE} &= EA \\ EA_{EB} &= EA \\ EA_{BF} &= EA \\ EA_{FC} &= EA \end{aligned}$$

$$\begin{aligned} EA_{CG} &= EA \\ EA_{GD} &= EA \end{aligned}$$



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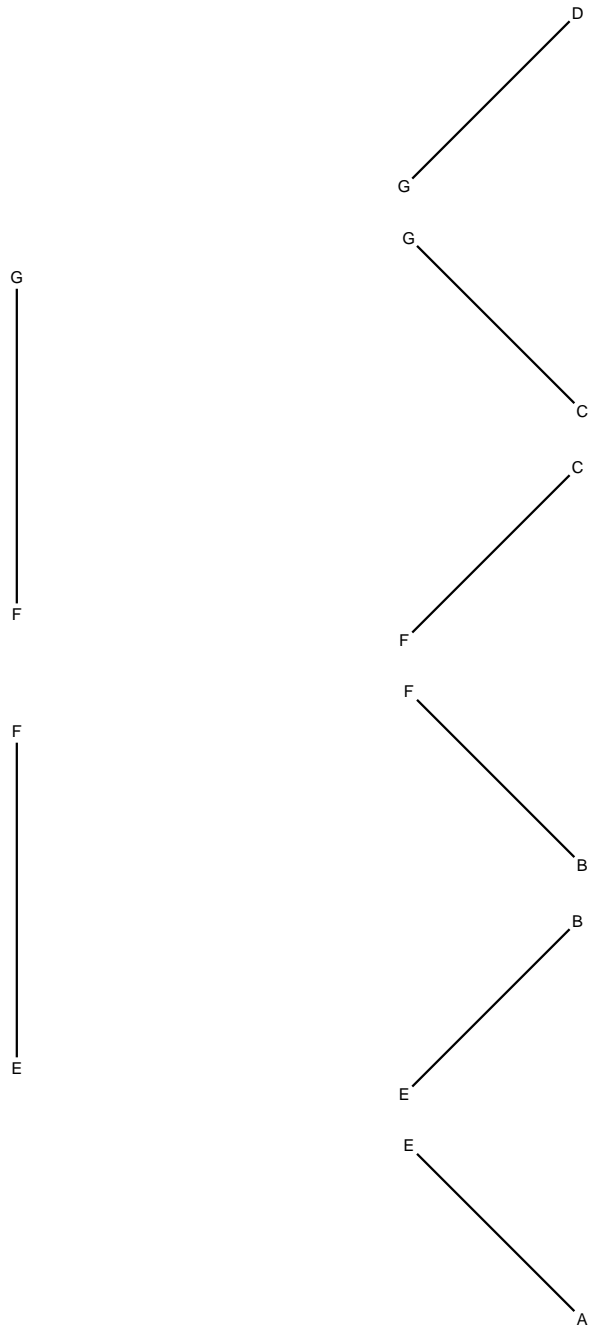
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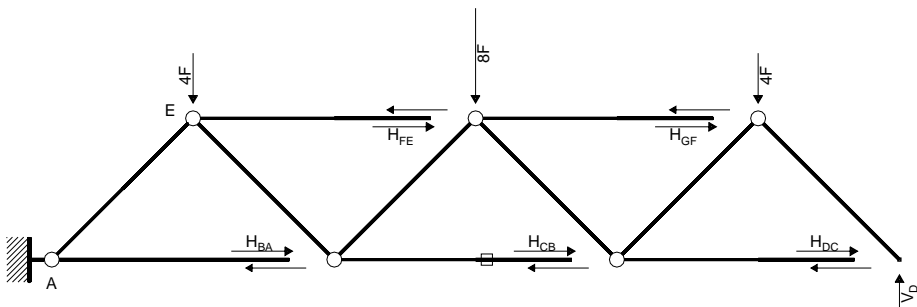


REAZIONI

$$H_A = \quad V_A = \quad V_D =$$
$$N_{AB} = \quad N_{BC} = \quad N_{CD} = \quad N_{EF} = \quad N_{FG} = \quad N_{AE} =$$
$$N_{EB} = \quad N_{BF} = \quad N_{FC} = \quad N_{CG} = \quad N_{GD} =$$

SPOSTAMENTI ASSOLUTI

$$u_F =$$
 $V_F =$ 



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 48Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 32Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 20Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 8Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 4Fb$$

Rotazione intorno a G: aste GD

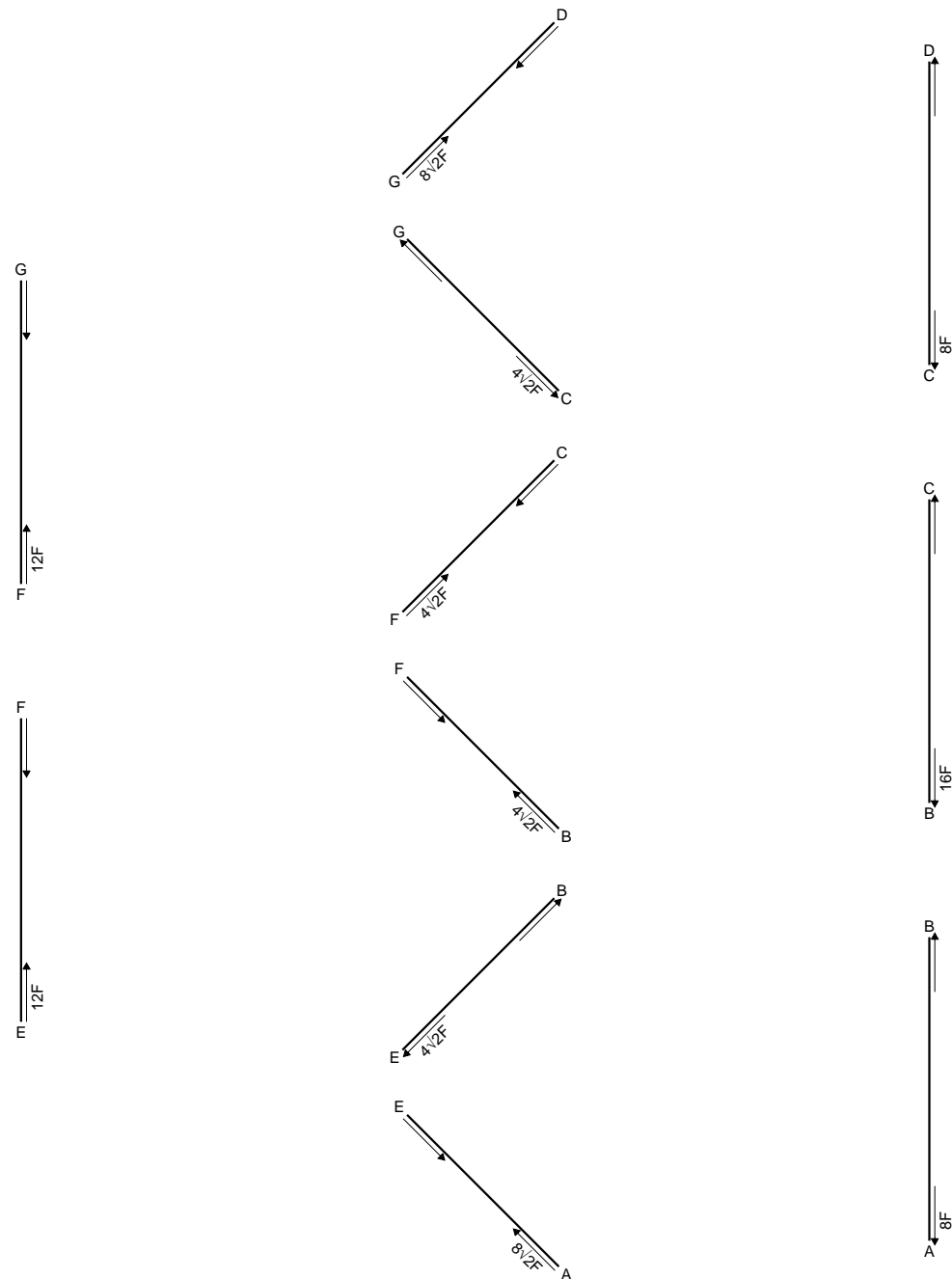
$$V_D b - H_{DC} b = 0$$

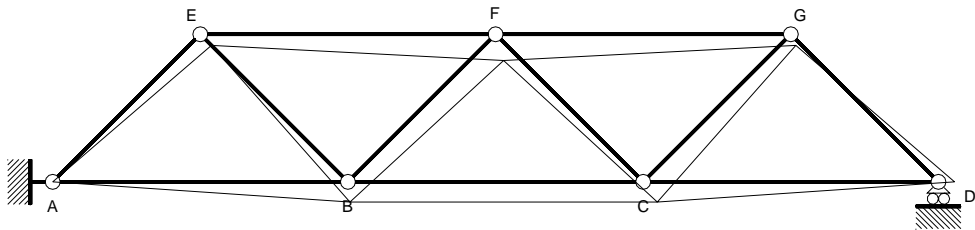
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 48 \\ 32 \\ 20 \\ 8 \\ 4 \\ 0 \end{bmatrix} Fb$$

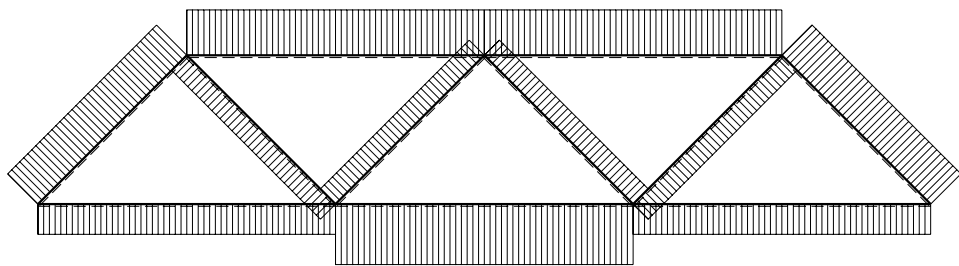
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 8 \\ 8 \\ -12 \\ 16 \\ -12 \\ 8 \end{bmatrix} Fb$$





600 Fb/EA



20 F

REAZIONI

$H_A = 0$ $V_A = 8F$ $V_D = 8F$

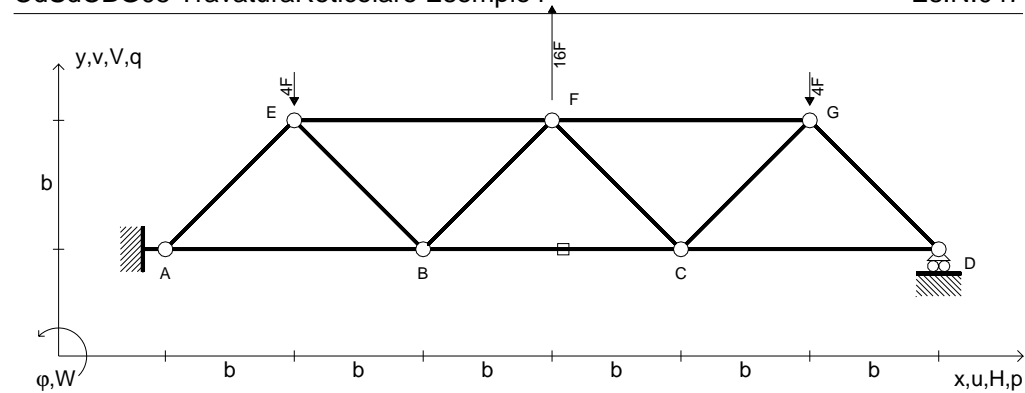
$N_{AB} = 8F$ $N_{BC} = 16F$ $N_{CD} = 8F$ $N_{EF} = -12F$ $N_{FG} = -12F$ $N_{AE} = -8\sqrt{2}F$

$N_{EB} = 4\sqrt{2}F$ $N_{BF} = -4\sqrt{2}F$ $N_{FC} = -4\sqrt{2}F$ $N_{CG} = 4\sqrt{2}F$ $N_{GD} = -8\sqrt{2}F$

SPOSTAMENTI ASSOLUTI

$u_F = 66(Fb/EA)$

$v_F = -(214+32\sqrt{2})(Fb/EA)$



$$\begin{aligned} V_E &= -4F \\ V_F &= 16F \\ V_G &= -4F \\ \varepsilon_{BC} &= 2\alpha T = 2F/EA \\ u_F &= ? \end{aligned}$$

$$\begin{aligned} v_F &= ? \\ EA_{AB} &= EA \\ EA_{BC} &= 1/2EA \\ EA_{CD} &= EA \\ EA_{EF} &= EA \end{aligned}$$

$$\begin{aligned} EA_{FG} &= EA \\ EA_{AE} &= EA \\ EA_{EB} &= EA \\ EA_{BF} &= EA \\ EA_{FC} &= EA \end{aligned}$$

$$\begin{aligned} EA_{CG} &= EA \\ EA_{GD} &= EA \end{aligned}$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

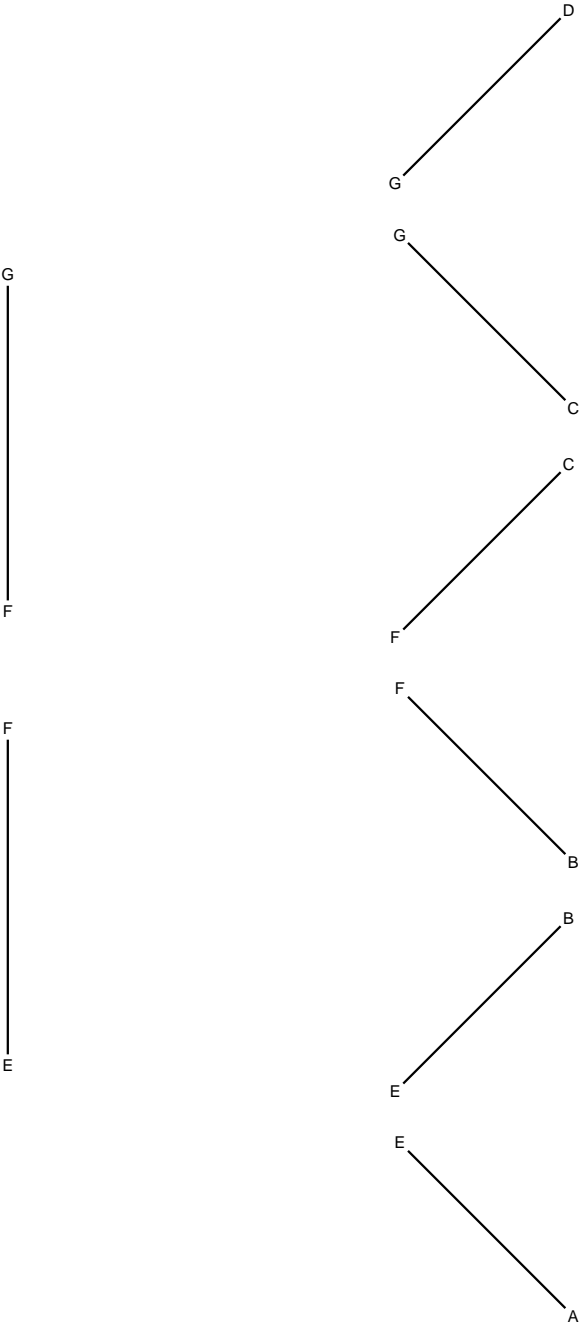
A_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

Allungamento termico assegnato ε su asta BC.

Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

@ Adolfo Zavelani Rossi, Politecnico di Milano



REAZIONI

$H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

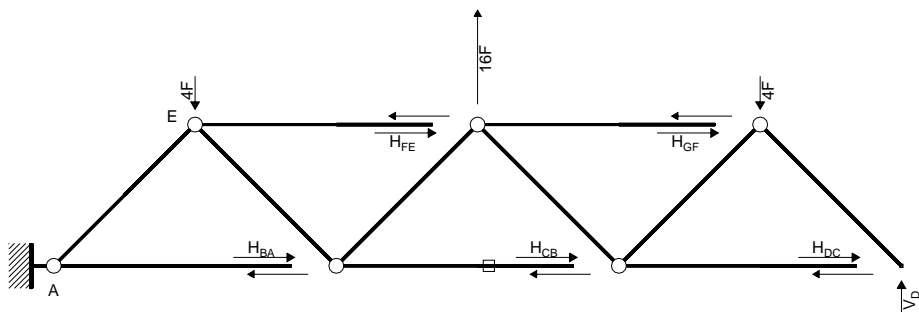
$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -24Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -16Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -4Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 8Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 4Fb$$

Rotazione intorno a G: aste GD

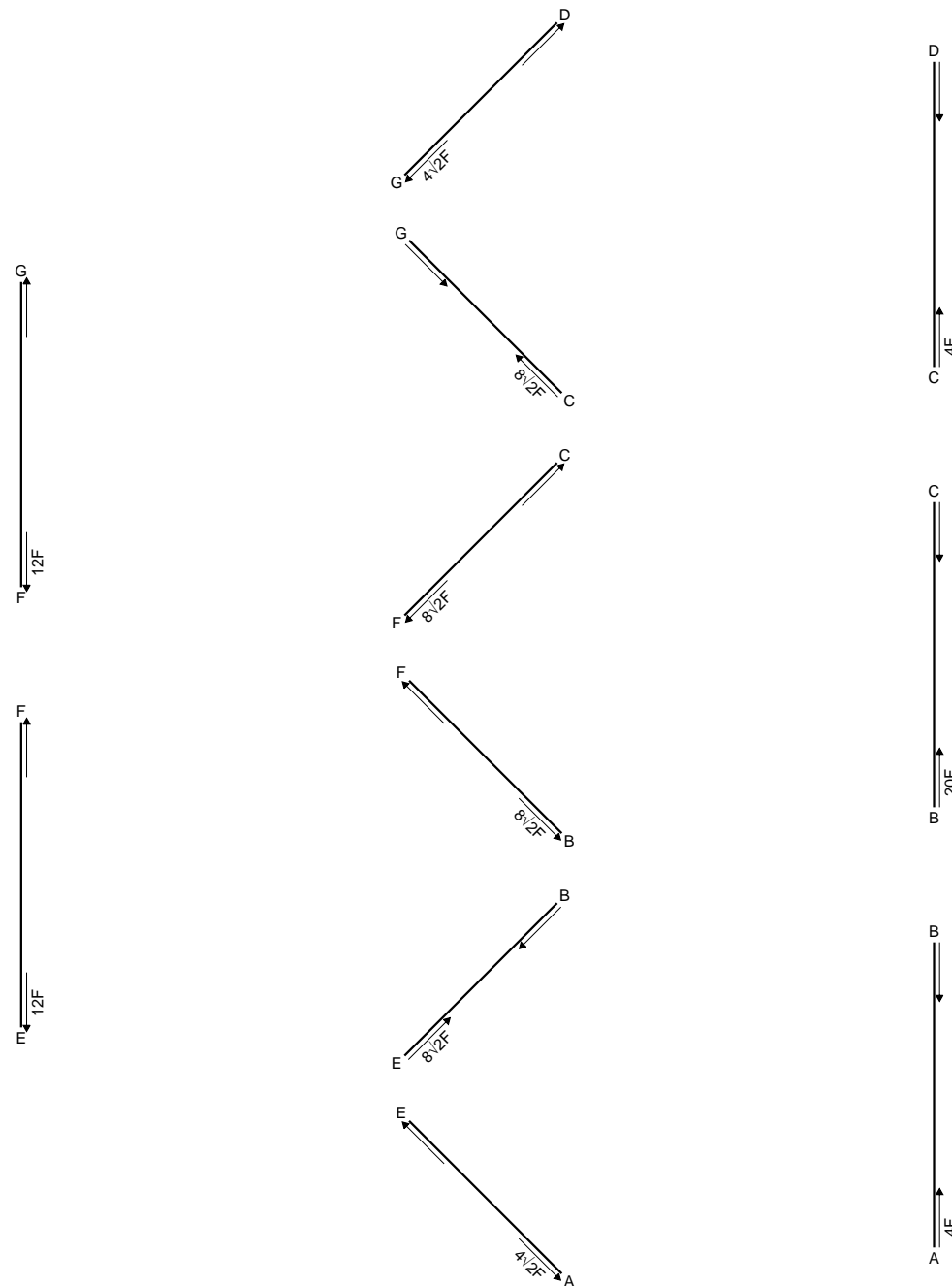
$$V_D b - H_{DC} b = 0$$

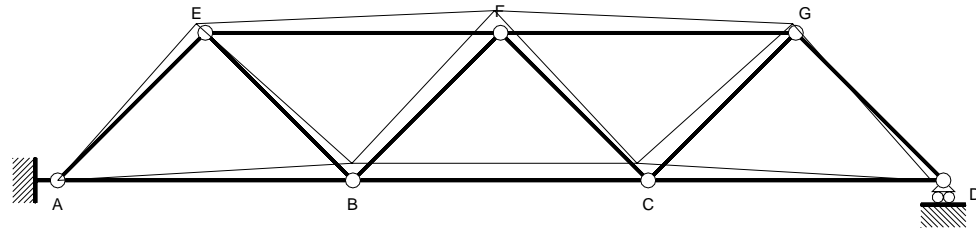
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} Fb \\ -24 \\ -16 \\ -4 \\ 8 \\ 4 \\ 0 \end{bmatrix}$$

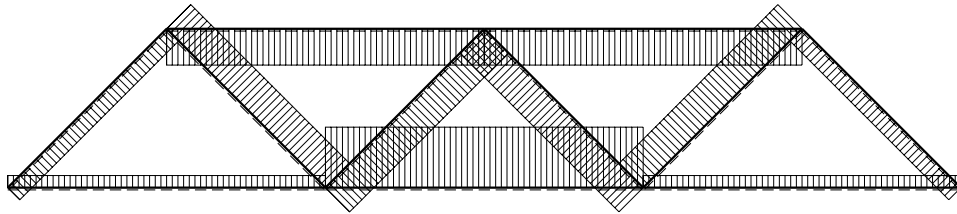
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} Fb \\ -4 \\ -4 \\ 12 \\ -20 \\ 12 \\ -4 \end{bmatrix}$$





1 — 600 Fb/EA



← ⊕ → 1 — 25 F

REAZIONI

$$H_A = 0 \quad V_A = -4F \quad V_D = -4F$$

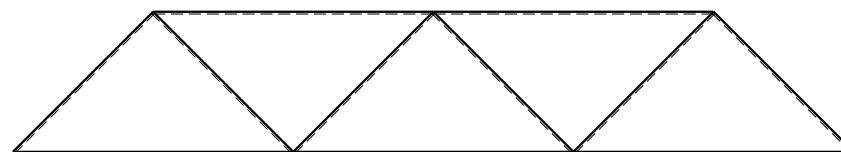
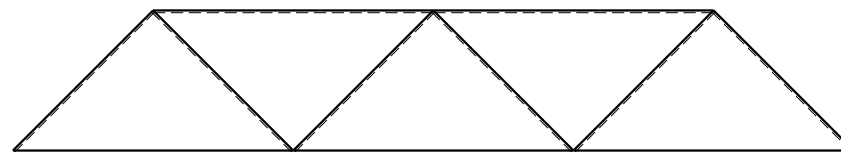
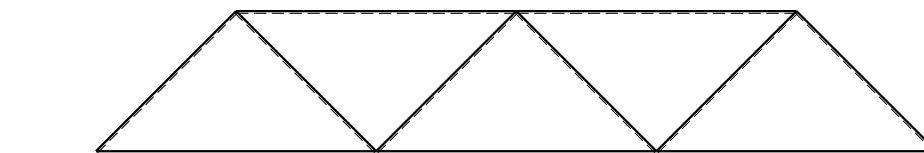
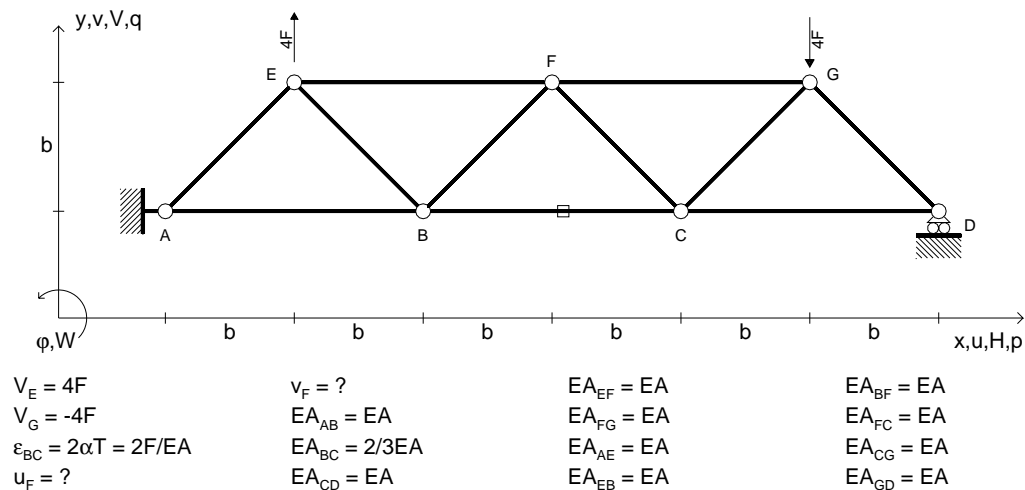
$$N_{AB} = -4F \quad N_{BC} = -20F \quad N_{CD} = -4F \quad N_{EF} = 12F \quad N_{FG} = 12F \quad N_{AE} = 4\sqrt{2}F$$

$$N_{EB} = -8\sqrt{2}F \quad N_{BF} = 8\sqrt{2}F \quad N_{FC} = 8\sqrt{2}F \quad N_{CG} = -8\sqrt{2}F \quad N_{GD} = 4\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

$$u_F = -46(Fb/EA)$$

$$v_F = (170+40\sqrt{2})(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Allungamento termico assegnato ε su asta BC.

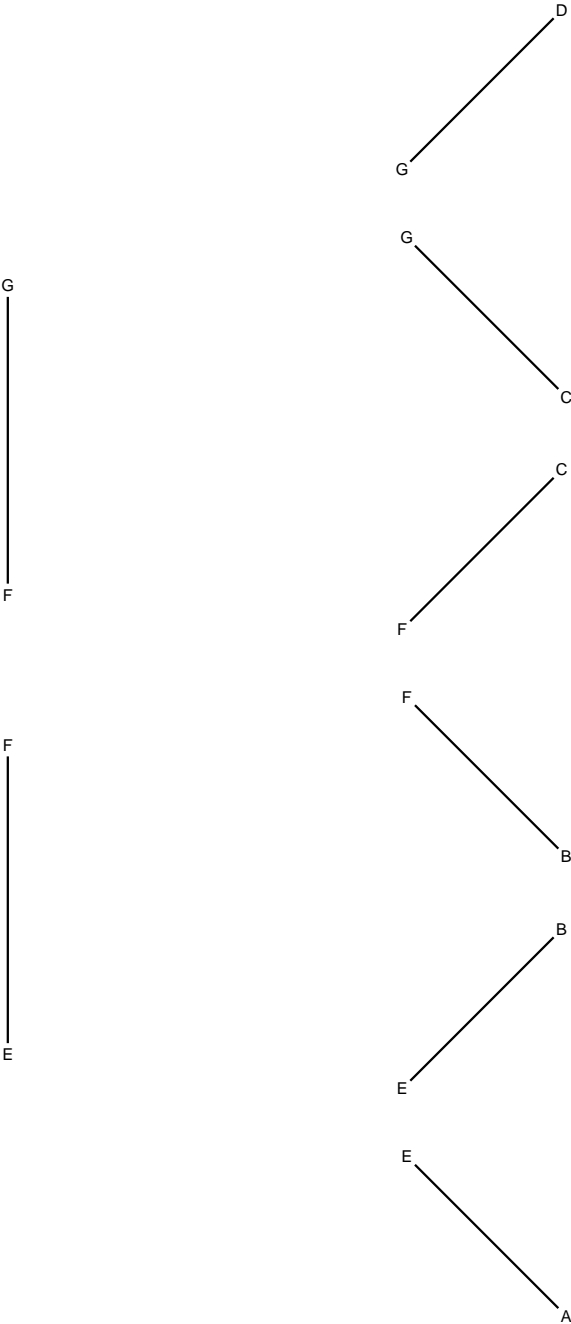
Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

@ Adolfo Zavelani Rossi, Politecnico di Milano



@ Adolfo Zavelani Rossi, Politecnico di Milano



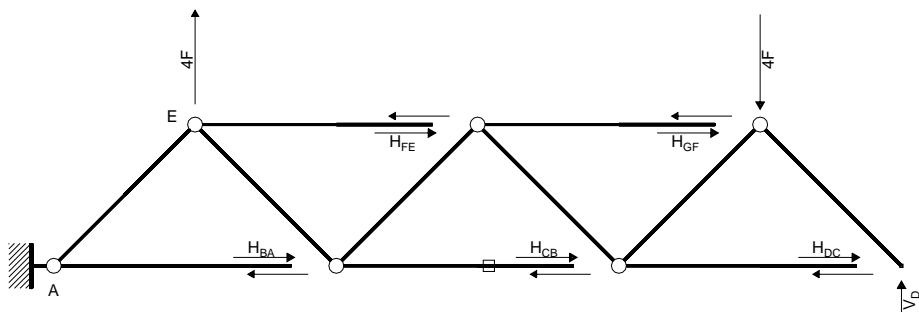
REAZIONI

$H_A =$	$V_A =$	$V_D =$			
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EF} =$	$N_{FG} =$	$N_{AE} =$
$N_{EB} =$	$N_{BF} =$	$N_{FC} =$	$N_{CG} =$	$N_{GD} =$	

SPOSTAMENTI ASSOLUTI

$u_F =$	
$v_F =$	





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 16Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 16Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 12Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 8Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = 4Fb$$

Rotazione intorno a G: aste GD

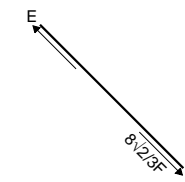
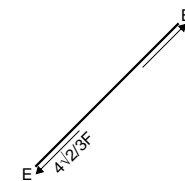
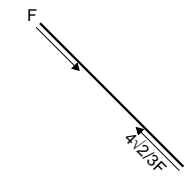
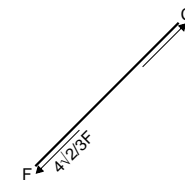
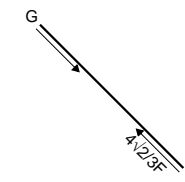
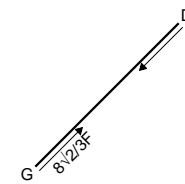
$$V_D b - H_{DC} b = 0$$

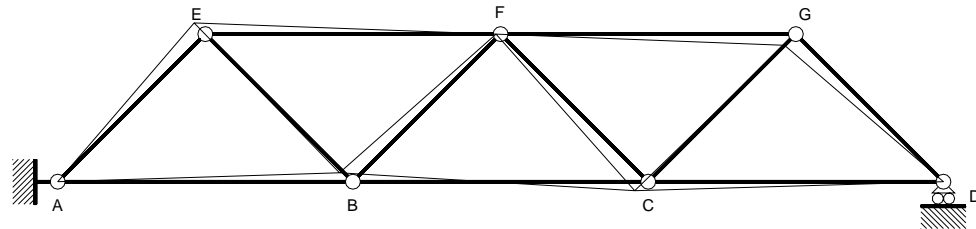
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 16 \\ 16 \\ 12 \\ 8 \\ 4 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

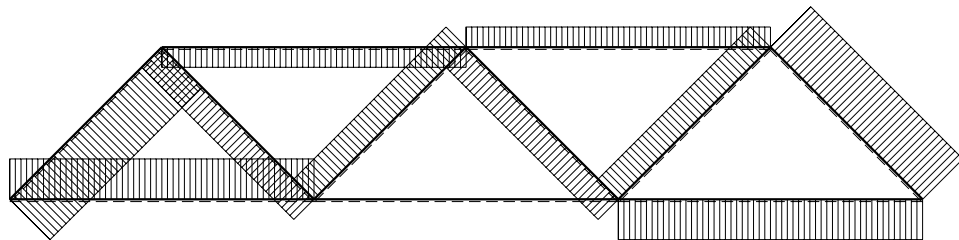
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 8/3 \\ -8/3 \\ 4/3 \\ 0 \\ -4/3 \\ 8/3 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





1 — 30 Fb/EA



← ⊕ → 1 — 5 F

REAZIONI

$$H_A = 0 \quad V_A = -8/3F \quad V_D = 8/3F$$

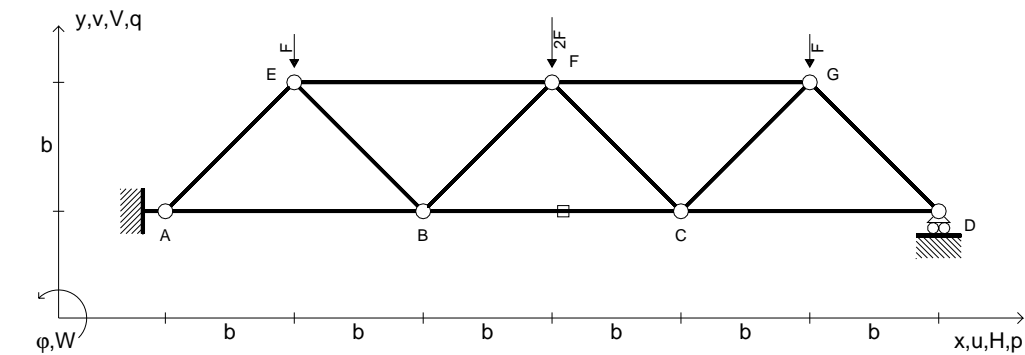
$$N_{AB} = -8/3F \quad N_{BC} = 0 \quad N_{CD} = 8/3F \quad N_{EF} = 4/3F \quad N_{FG} = -4/3F \quad N_{AE} = 8\sqrt{2}/3F$$

$$N_{EB} = 4\sqrt{2}/3F \quad N_{BF} = -4\sqrt{2}/3F \quad N_{FC} = 4\sqrt{2}/3F \quad N_{CG} = -4\sqrt{2}/3F \quad N_{GD} = -8\sqrt{2}/3F$$

SPOSTAMENTI ASSOLUTI

$$u_F = 2/9(Fb/EA)$$

$$v_F = -6(Fb/EA)$$

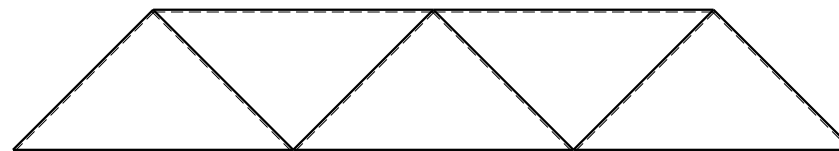
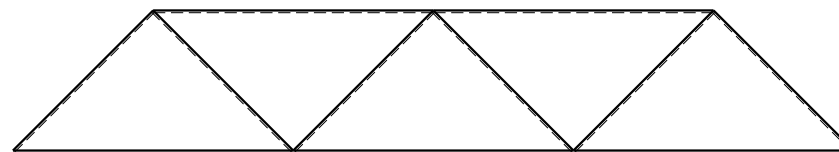
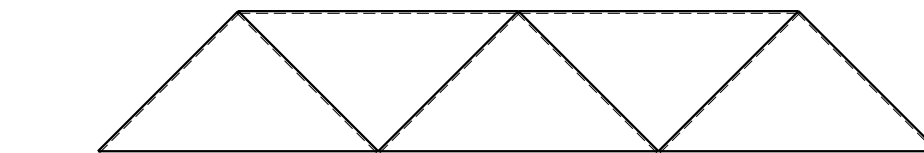


$$\begin{aligned} V_E &= -F \\ V_F &= -2F \\ V_G &= -F \\ \varepsilon_{BC} &= -3\alpha T = -3F/EA \\ u_F &= ? \end{aligned}$$

$$\begin{aligned} V_F &= ? \\ EA_{AB} &= EA \\ EA_{BC} &= 3/4 EA \\ EA_{CD} &= EA \\ EA_{EF} &= EA \end{aligned}$$

$$\begin{aligned} EA_{FG} &= EA \\ EA_{AE} &= EA \\ EA_{EB} &= EA \\ EA_{BF} &= EA \\ EA_{FC} &= EA \end{aligned}$$

$$\begin{aligned} EA_{CG} &= EA \\ EA_{GD} &= EA \end{aligned}$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

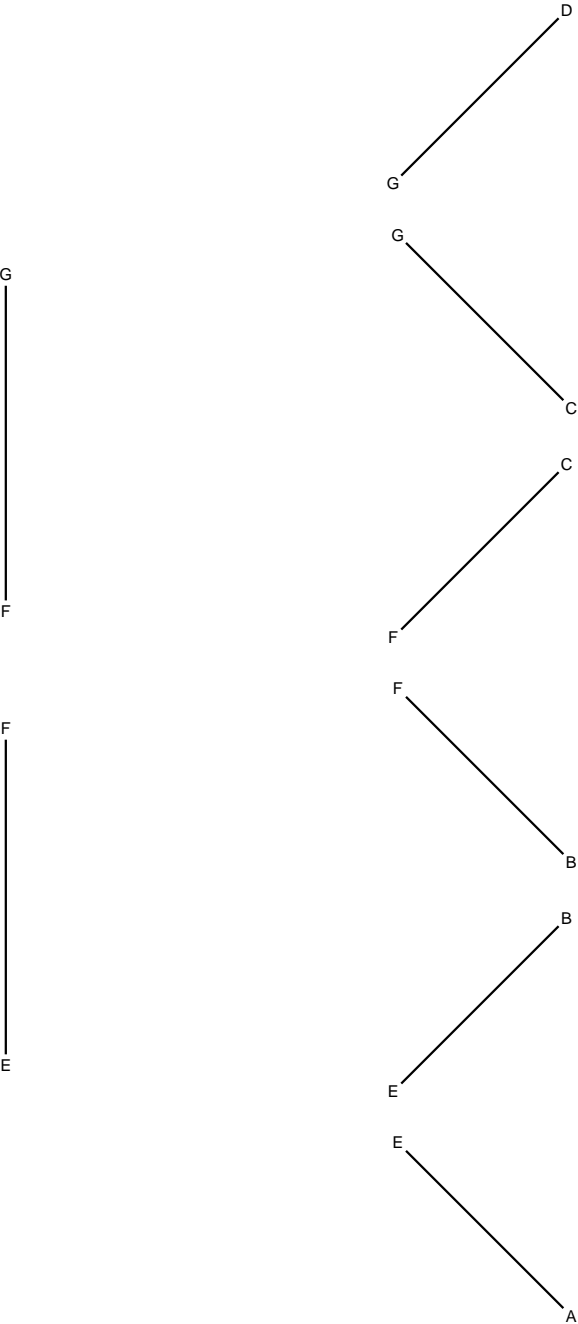
A_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

Allungamento termico assegnato ε su asta BC.

Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

@ Adolfo Zavelani Rossi, Politecnico di Milano



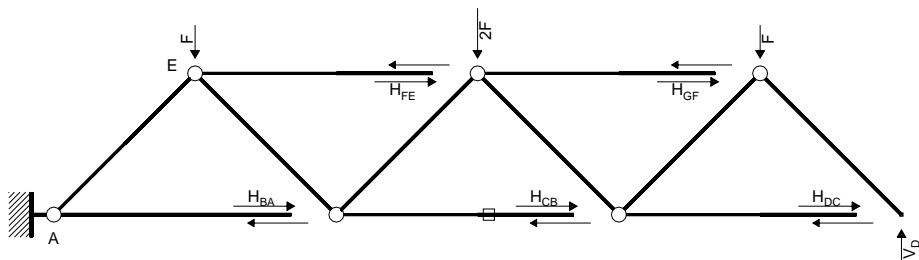
REAZIONI
 $H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI
 $u_F =$
 $v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = 12Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = 8Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = 5Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 2Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = Fb$$

Rotazione intorno a G: aste GD

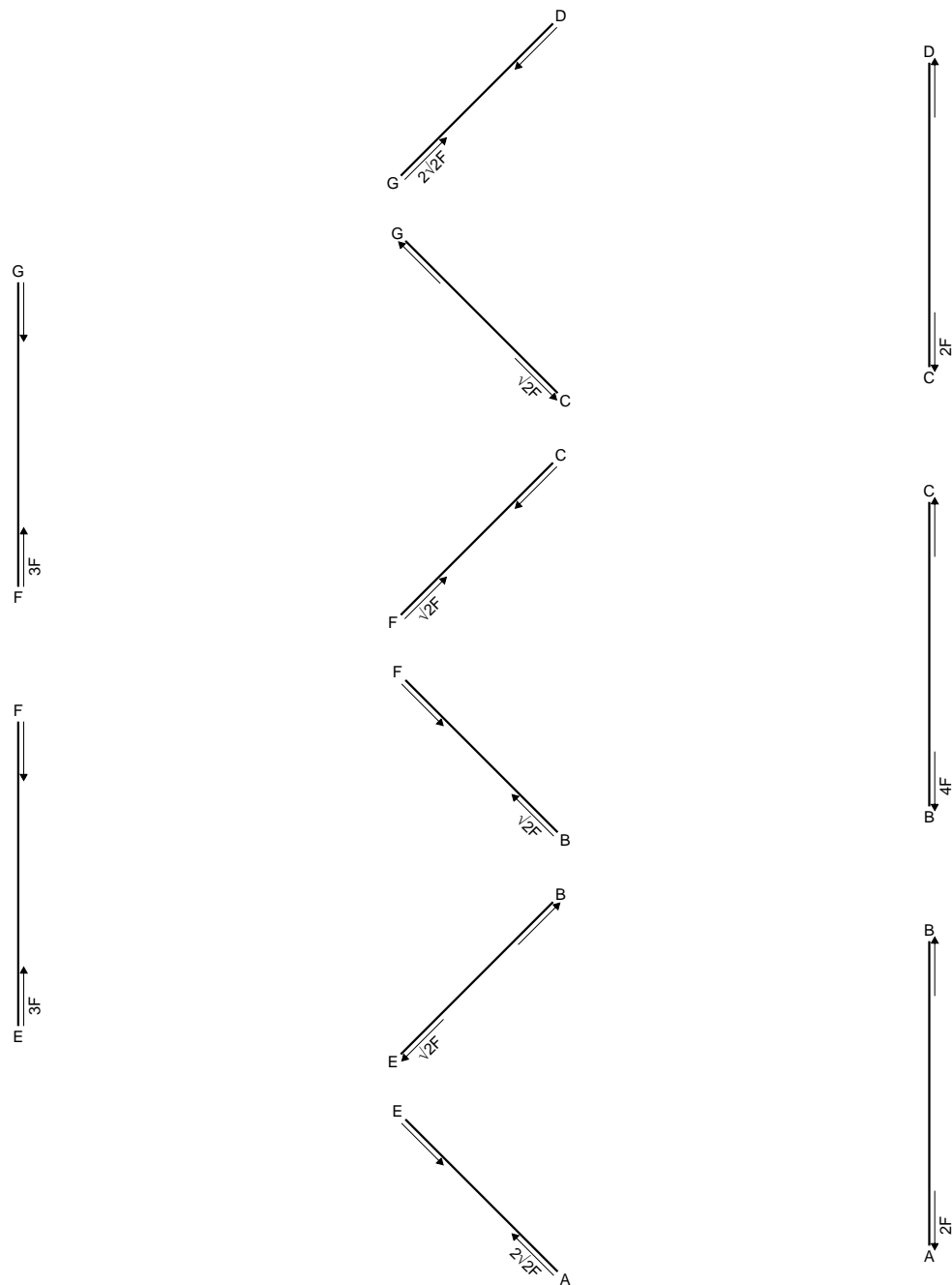
$$V_D b - H_{DC} b = 0$$

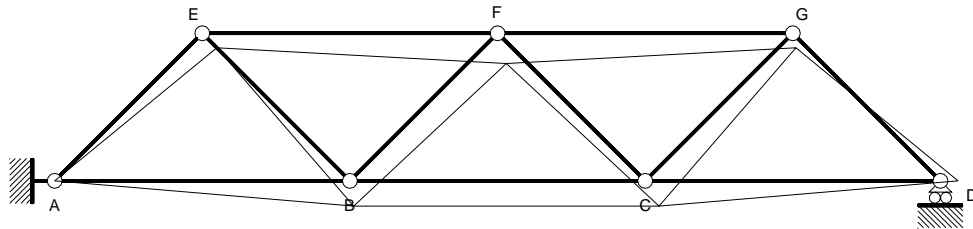
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} 12 \\ 8 \\ 5 \\ 2 \\ 1 \\ 0 \end{bmatrix} Fb$$

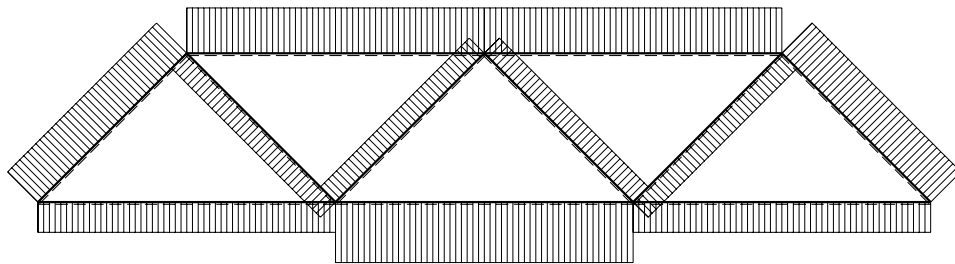
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \\ -3 \\ 4 \\ -3 \\ 2 \end{bmatrix} Fb$$





1 — 80 Fb/EA



← ⊕ → 1 — 5 F

REAZIONI

$$H_A = 0 \quad V_A = 2F \quad V_D = 2F$$

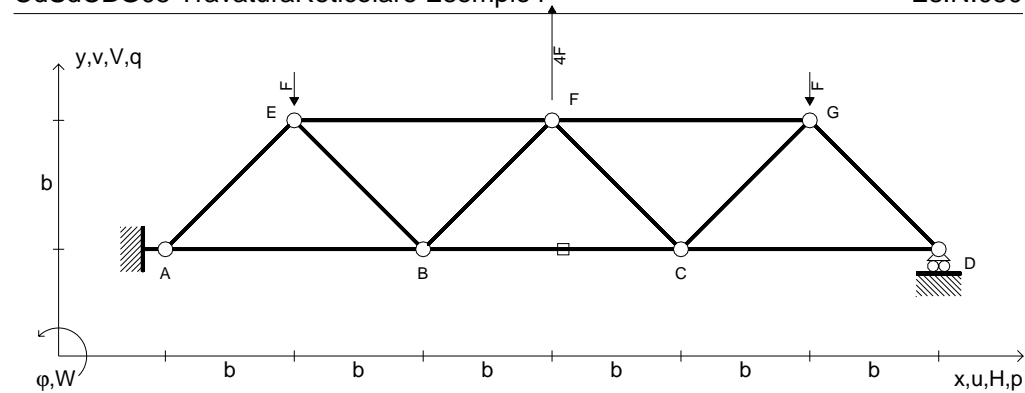
$$N_{AB} = 2F \quad N_{BC} = 4F \quad N_{CD} = 2F \quad N_{EF} = -3F \quad N_{FG} = -3F \quad N_{AE} = -2\sqrt{2}F$$

$$N_{EB} = \sqrt{2}F \quad N_{BF} = -\sqrt{2}F \quad N_{FC} = -\sqrt{2}F \quad N_{CG} = \sqrt{2}F \quad N_{GD} = -2\sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

$$u_F = 19/3(Fb/EA)$$

$$v_F = -(23+8\sqrt{2})(Fb/EA)$$



$$V_E = -F$$

$$V_F = 4F$$

$$V_G = -F$$

$$\varepsilon_{BC} = -3\alpha T = -3F/EA$$

$$u_F = ?$$

$$V_F = ?$$

$$EA_{AB} = EA$$

$$EA_{BC} = EA$$

$$EA_{CD} = EA$$

$$EA_{EF} = EA$$

$$EA_{FG} = EA$$

$$EA_{AE} = EA$$

$$EA_{EB} = EA$$

$$EA_{BF} = EA$$

$$EA_{FC} = EA$$

$$EA_{CG} = EA$$

$$EA_{GD} = EA$$

Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

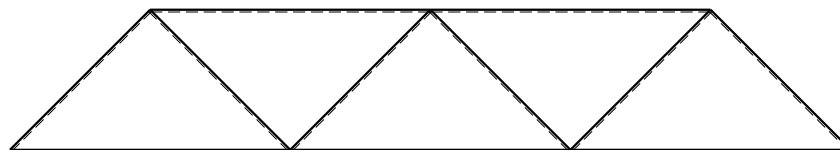
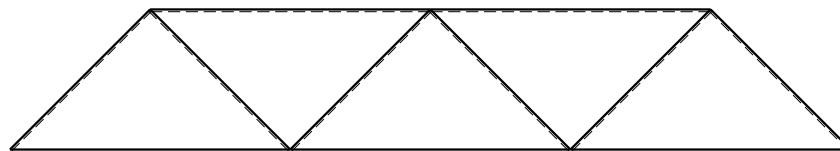
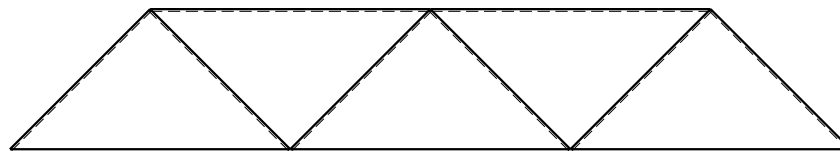
A_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

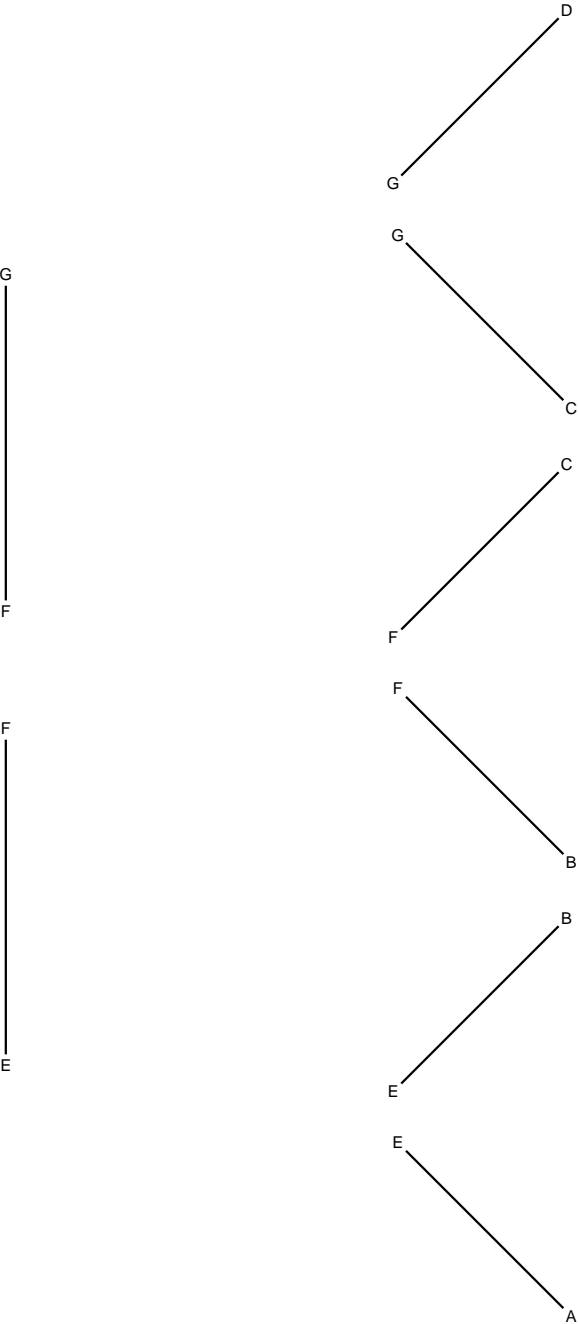
Allungamento termico assegnato ε su asta BC.

Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

@ Adolfo Zavelani Rossi, Politecnico di Milano





REAZIONI

$H_A =$ $V_A =$ $V_D =$

$N_{AB} =$ $N_{BC} =$ $N_{CD} =$ $N_{EF} =$ $N_{FG} =$ $N_{AE} =$

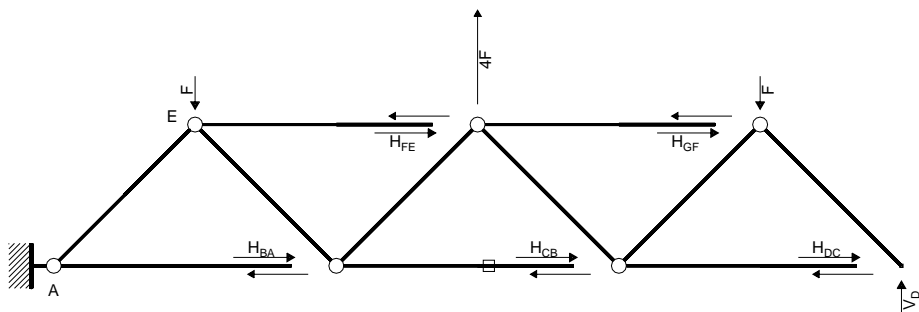
$N_{EB} =$ $N_{BF} =$ $N_{FC} =$ $N_{CG} =$ $N_{GD} =$

SPOSTAMENTI ASSOLUTI

$u_F =$

$v_F =$





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -6Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -4Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = 2Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = Fb$$

Rotazione intorno a G: aste GD

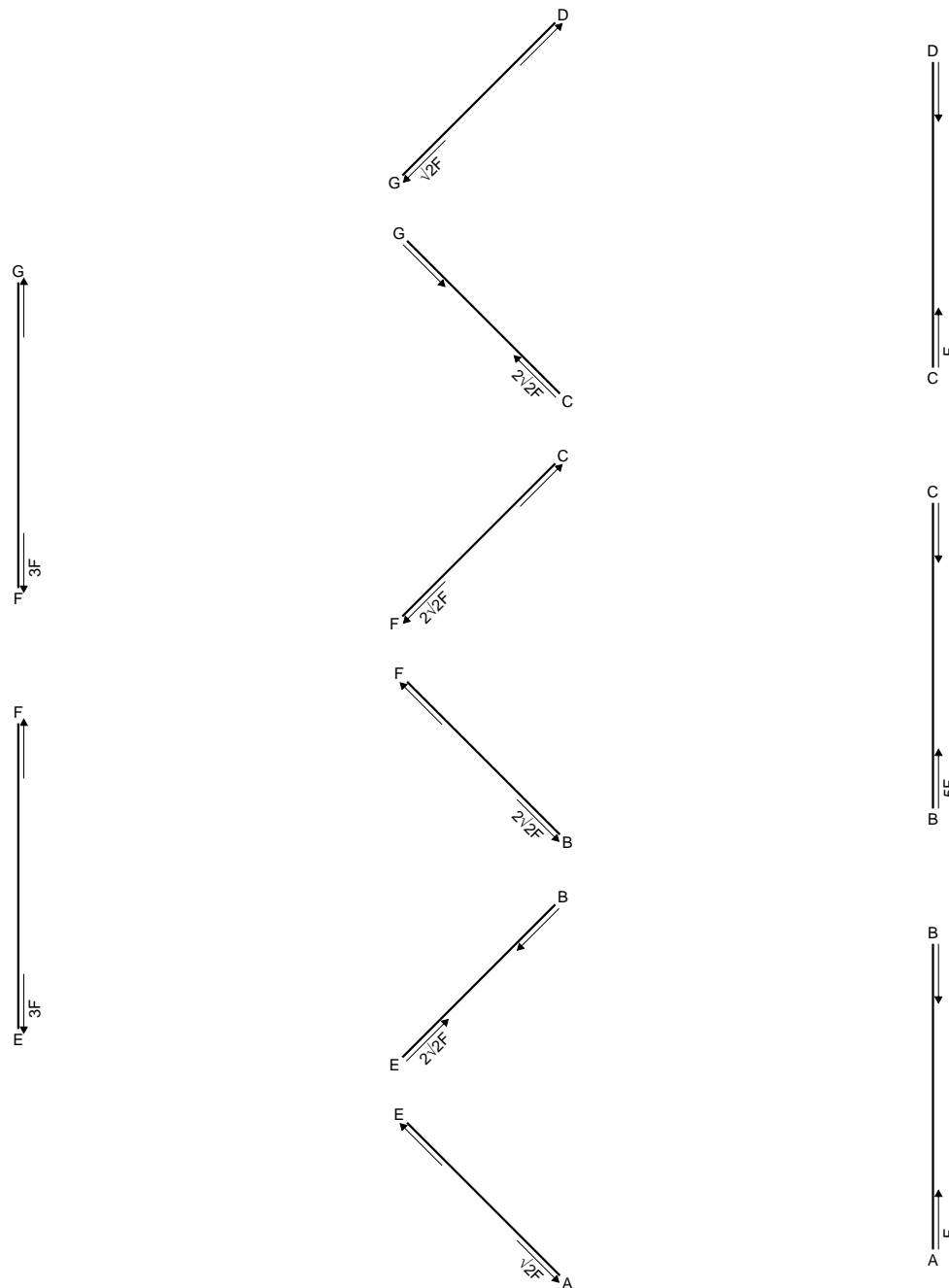
$$V_D b - H_{DC} b = 0$$

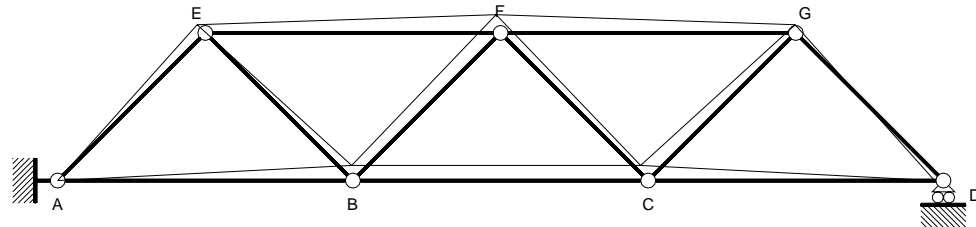
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -6 \\ -4 \\ -1 \\ 2 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$

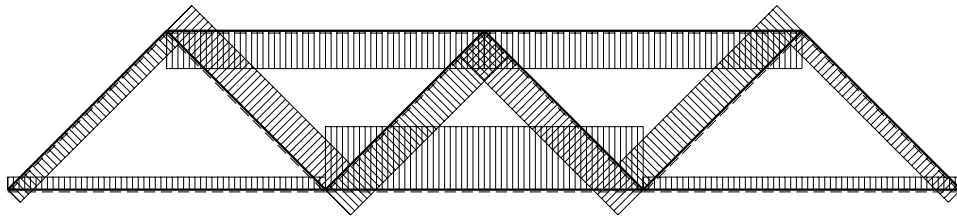
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -1 \\ -1 \\ 3 \\ -5 \\ 3 \\ -1 \end{bmatrix} \begin{bmatrix} Fb \end{bmatrix}$$





120 Fb/EA



6 F

REAZIONI

$$H_A = 0 \quad V_A = -F \quad V_D = -F$$

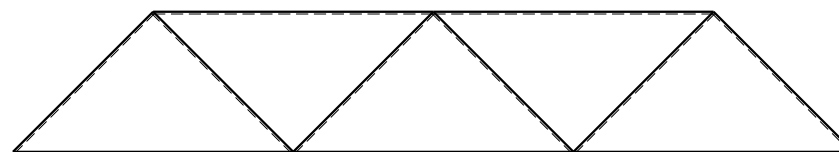
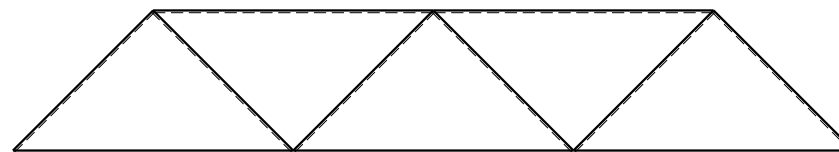
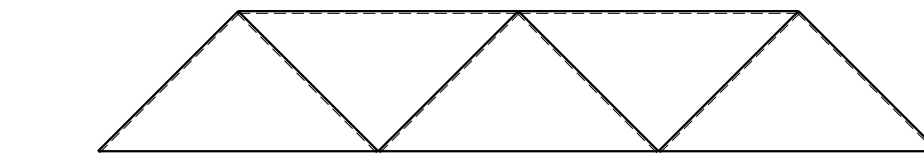
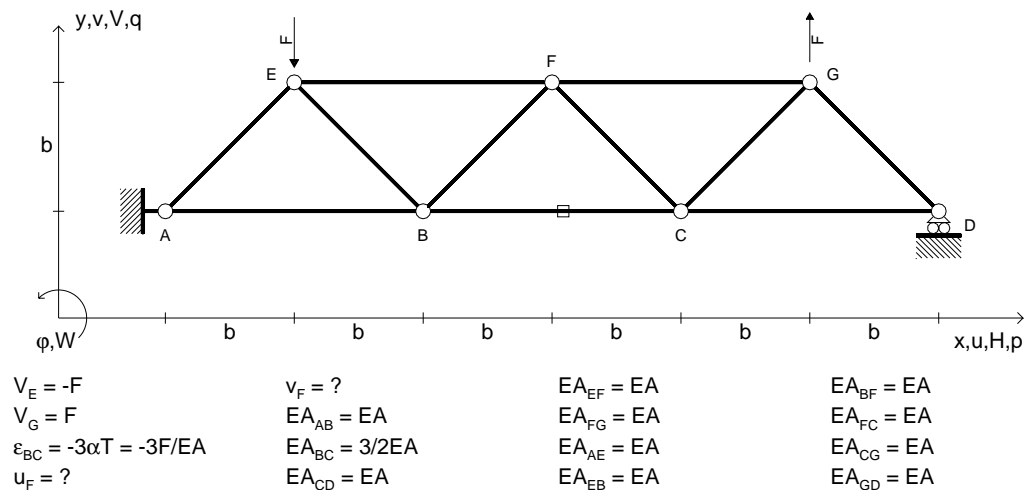
$$N_{AB} = -F \quad N_{BC} = -5F \quad N_{CD} = -F \quad N_{EF} = 3F \quad N_{FG} = 3F \quad N_{AE} = \sqrt{2}F$$

$$N_{EB} = -2\sqrt{2}F \quad N_{BF} = 2\sqrt{2}F \quad N_{FC} = 2\sqrt{2}F \quad N_{CG} = -2\sqrt{2}F \quad N_{GD} = \sqrt{2}F$$

SPOSTAMENTI ASSOLUTI

$$u_F = -10(Fb/EA)$$

$$v_F = (38+10\sqrt{2})(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Allungamento termico assegnato ε su asta BC.

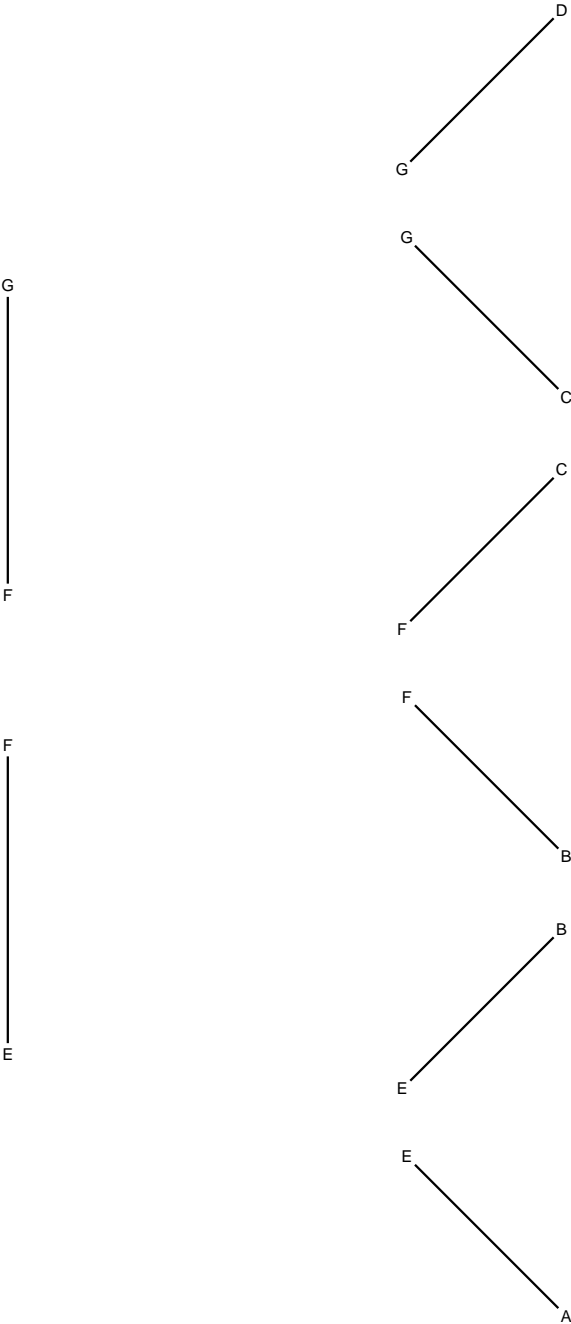
Calcolare lo spostamento orizzont. del nodo F

Calcolare lo spostamento verticale del nodo F

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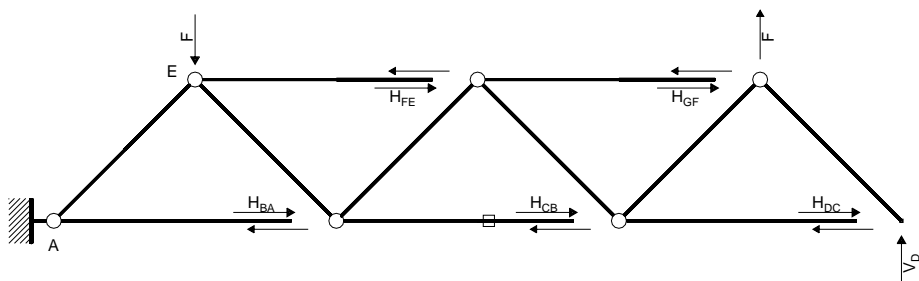
REAZIONI

$H_A =$	$V_A =$	$V_D =$			
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{EF} =$	$N_{FG} =$	$N_{AE} =$
$N_{EB} =$	$N_{BF} =$	$N_{FC} =$	$N_{CG} =$	$N_{GD} =$	

SPOSTAMENTI ASSOLUTI

$u_F =$	
$v_F =$	





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a A: aste AE EF EB BC BF FG FC CD CG GD

$$6V_D b = -4Fb$$

Rotazione intorno a E: aste EB BC BF FG FC CD CG GD

$$5V_D b - H_{BA} b = -4Fb$$

Rotazione intorno a B: aste BF FG FC CD CG GD

$$4V_D b + H_{FE} b = -3Fb$$

Rotazione intorno a F: aste FC CD CG GD

$$3V_D b - H_{CB} b = -2Fb$$

Rotazione intorno a C: aste CG GD

$$2V_D b + H_{GF} b = -Fb$$

Rotazione intorno a G: aste GD

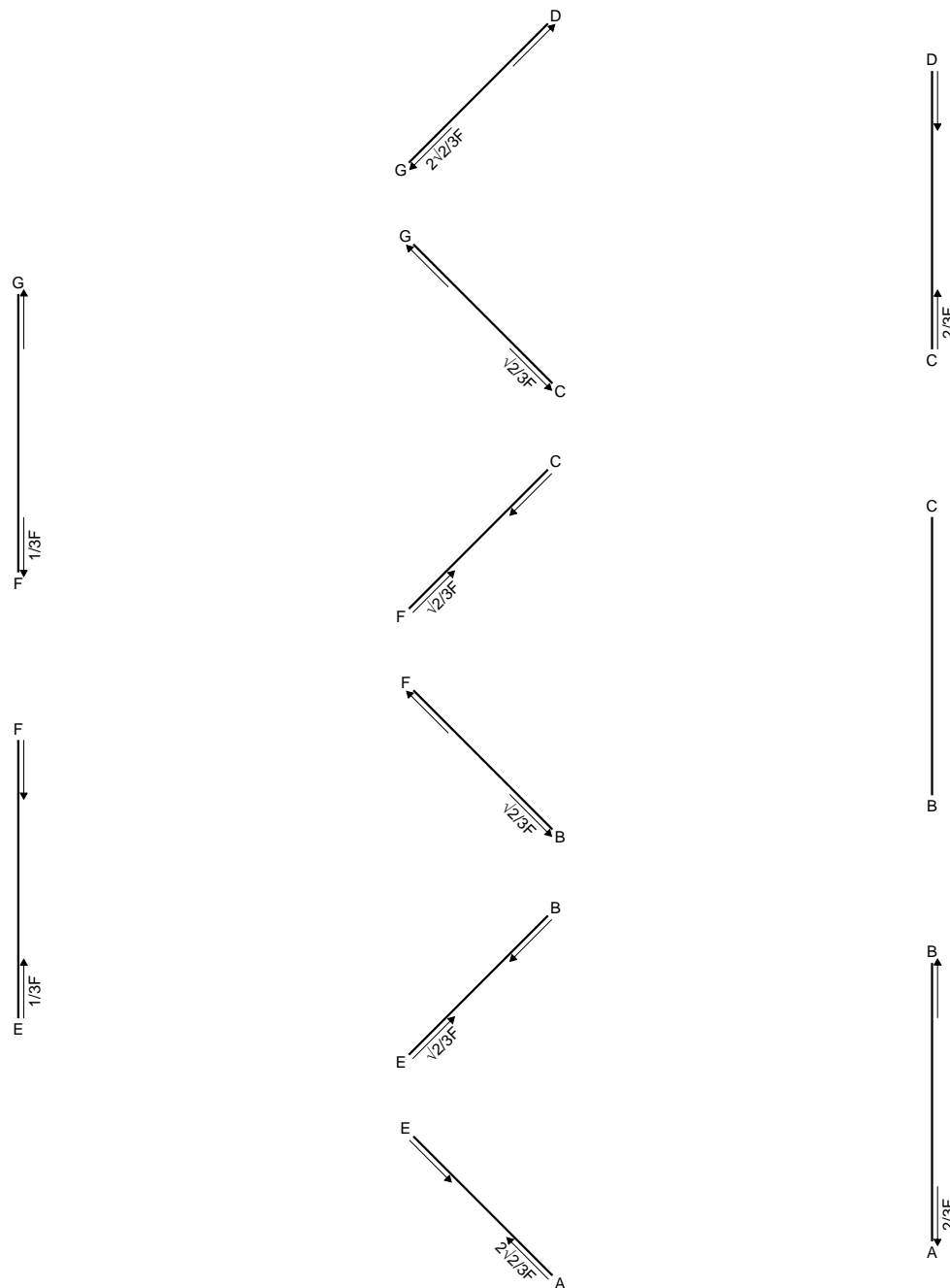
$$V_D b - H_{DC} b = 0$$

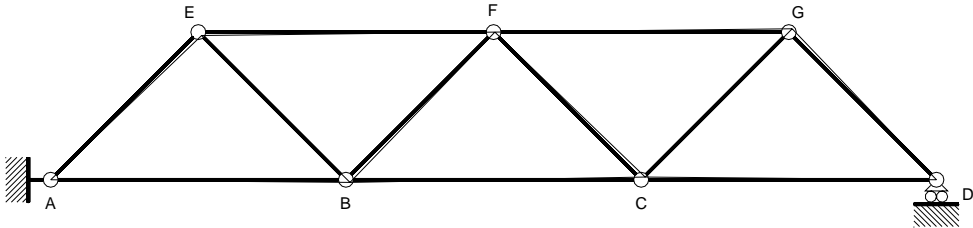
Matrice di equilibrio

$$\begin{bmatrix} \phi_{AE} \\ \phi_{EB} \\ \phi_{BF} \\ \phi_{FC} \\ \phi_{CG} \\ \phi_{GD} \end{bmatrix} \begin{bmatrix} V_D b & H_{BA} b & H_{CB} b & H_{DC} b & H_{FE} b & H_{GF} b \end{bmatrix} = \begin{bmatrix} -4 \\ -4 \\ -3 \\ -2 \\ -1 \\ 0 \end{bmatrix} Fb$$

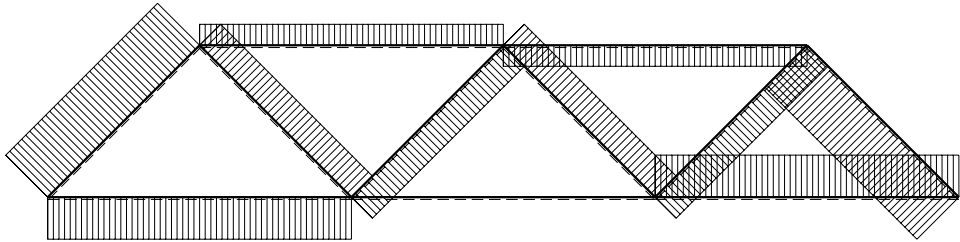
Soluzione del sistema

$$\begin{bmatrix} V_D b \\ H_{BA} b \\ H_{FE} b \\ H_{CB} b \\ H_{GF} b \\ H_{DC} b \end{bmatrix} = \begin{bmatrix} -2/3 \\ 2/3 \\ -1/3 \\ 0 \\ 1/3 \\ -2/3 \end{bmatrix} Fb$$





1 25 Fb/EA



← + → 1 1.2 F

REAZIONI

$H_A = 0$ $V_A = 2/3F$ $V_D = -2/3F$

$N_{AB} = 2/3F$ $N_{BC} = 0$ $N_{CD} = -2/3F$ $N_{EF} = -1/3F$ $N_{FG} = 1/3F$ $N_{AE} = -2\sqrt{2}/3F$

$N_{EB} = -\sqrt{2}/3F$ $N_{BF} = \sqrt{2}/3F$ $N_{FC} = -\sqrt{2}/3F$ $N_{CG} = \sqrt{2}/3F$ $N_{GD} = 2\sqrt{2}/3F$

SPOSTAMENTI ASSOLUTI

$u_F = -23/9(Fb/EA)$

$v_F = 9(Fb/EA)$