

$$\begin{array}{lllll}
 V_A = -16F & EA_{CB} = 4EA & EA_{DA} = 3EA & EA_{EC} = 2EA & EA_{DE} = EA \\
 EA_{AB} = 5EA & EA_{AC} = 4EA & EA_{DC} = 3EA & EA_{FE} = 2EA & EA_{FD} = EA
 \end{array}$$

Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

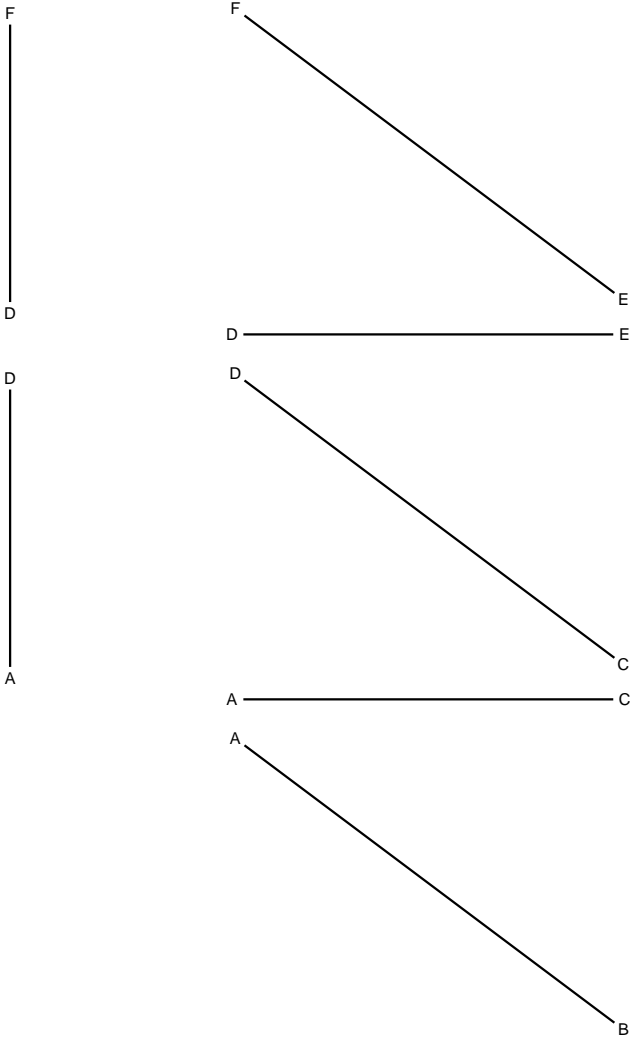
Calcolare spostamento e rotazione di tutti i nodi.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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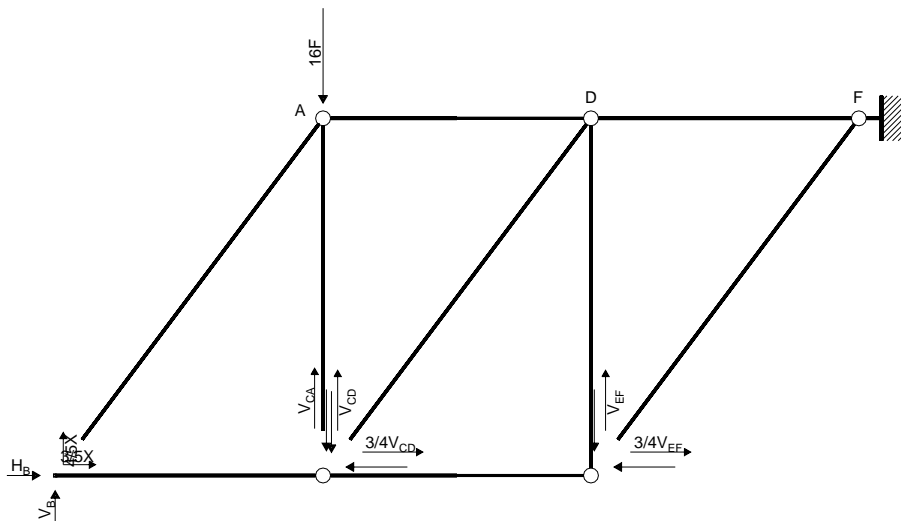


REAZIONI

$H_B =$	$V_B =$	$H_F =$	$V_F =$		
$N_{AB} =$	$N_{CB} =$	$N_{AC} =$	$N_{DA} =$	$N_{DC} =$	
$N_{EC} =$	$N_{FE} =$	$N_{DE} =$	$N_{FD} =$		

SPOSTAMENTI NODALI

$u_A =$	$u_B =$	$u_C =$	$u_D =$
$v_A =$	$v_B =$	$v_C =$	$v_D =$
$u_E =$	$u_F =$		
$v_E =$	$v_F =$		



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DA DC DE AB AC EC CB

$$4H_B b - 9V_B b = 24/5 Xb - 96Fb$$

Rotazione intorno a D: aste DA AB AC

$$-3V_{CA} b = 12/5 Xb - 48Fb$$

Rotazione intorno a D: aste DE EC CB

$$4H_B b - 6V_B b + 3V_{CA} b - 3V_{EF} b = 0$$

Rotazione intorno a E: aste EC CB

$$-6V_B b + 3V_{CA} b + 3V_{CD} b = 0$$

Rotazione intorno a C: aste CB

$$-3V_B b = 0$$

Matrice di equilibrio

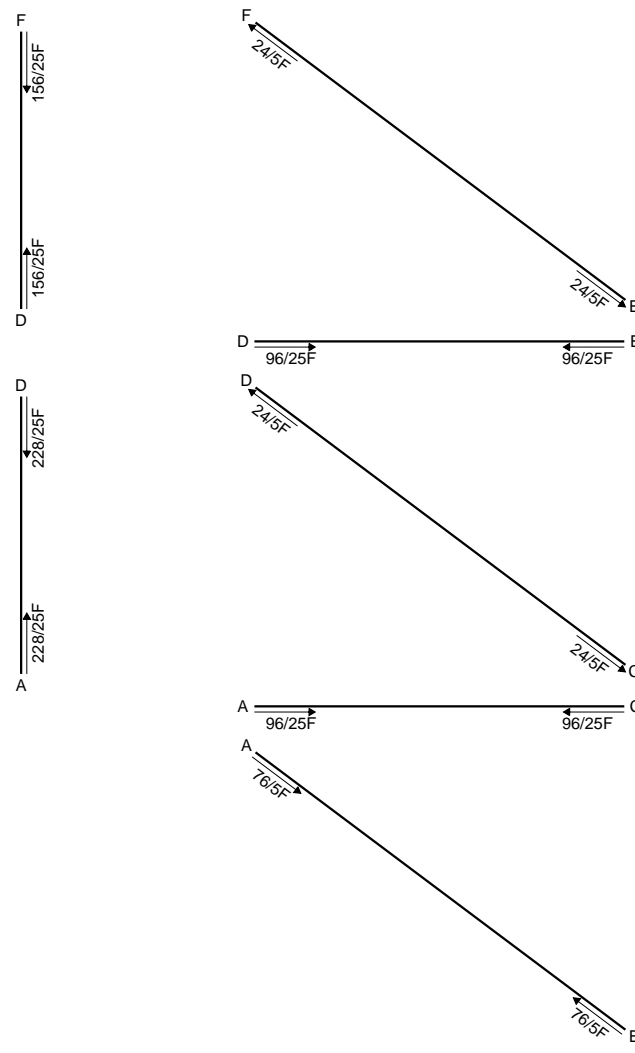
$$\begin{bmatrix} \phi_{FD} \\ \phi_{DA} \\ \phi_{DE} \\ \phi_{EC} \\ \phi_{CB} \end{bmatrix} \begin{bmatrix} H_B b & V_B b & V_{CA} b & V_{CD} b & V_{EF} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

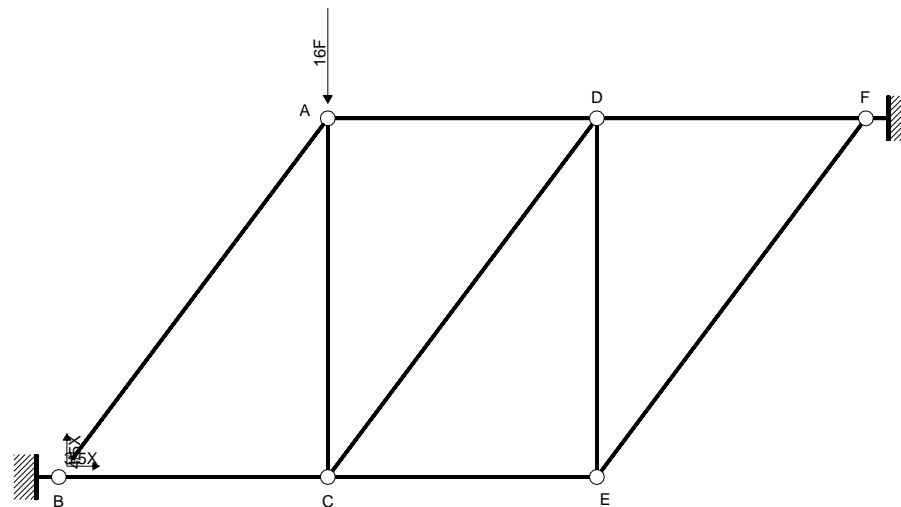
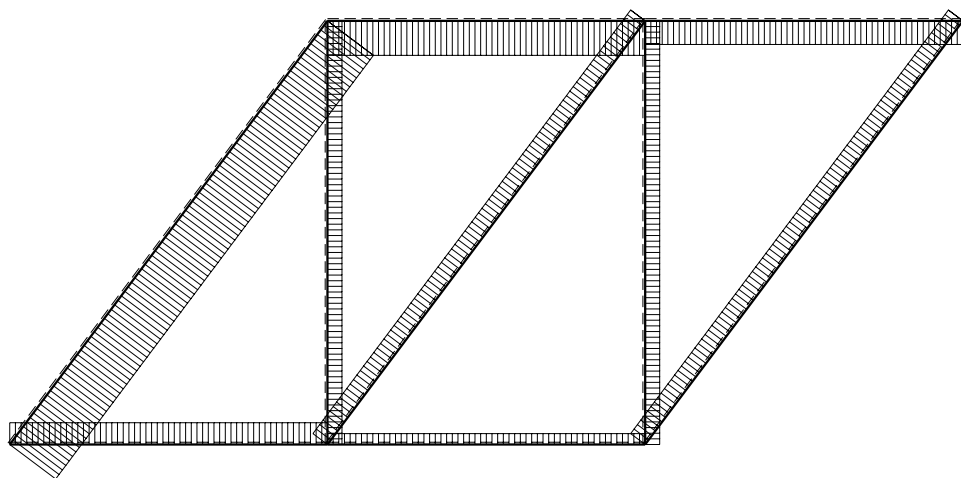
$$\begin{bmatrix} 4 & -9 & 0 & 0 & 0 \\ 0 & 0 & -3 & 0 & 0 \\ 4 & -6 & 3 & 0 & -3 \\ 0 & -6 & 3 & 3 & 0 \\ 0 & -3 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 24/5 & -96 \\ 12/5 & -48 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_B b \\ V_{CA} b \\ V_B b \\ V_{CD} b \\ V_{EF} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 6/5 & -24 \\ -4/5 & 16 \\ 0 & 0 \\ 4/5 & -16 \\ 4/5 & -16 \end{bmatrix}$$





REAZIONI IPERSTATICHE

$$X = V_{BA}$$

CALCOLO DELLE REAZIONI IPERSTATICHE

$$L_{AB}^{XX} = N_{AB}^X N_{AB}^X I_{AB}/EA_{AB} = -1 \cdot (-1) \cdot 5 \cdot 1/5 \cdot Fb/EA = Fb/EA$$

$$L_{CB}^{XX} = N_{CB}^X N_{CB}^X I_{CB}/EA_{CB} = -6/5 \cdot (-6/5) \cdot 3 \cdot 1/4 \cdot Fb/EA = 27/25 \cdot Fb/EA$$

$$L_{AC}^{XX} = N_{AC}^X N_{AC}^X I_{AC}/EA_{AC} = 4/5 \cdot 4/5 \cdot 4 \cdot 1/4 \cdot Fb/EA = 16/25 \cdot Fb/EA$$

$$L_{DA}^{XX} = N_{DA}^X N_{DA}^X I_{DA}/EA_{DA} = -3/5 \cdot (-3/5) \cdot 3 \cdot 1/3 \cdot Fb/EA = 9/25 \cdot Fb/EA$$

$$L_{DC}^{XX} = N_{DC}^X N_{DC}^X I_{DC}/EA_{DC} = -1 \cdot (-1) \cdot 5 \cdot 1/3 \cdot Fb/EA = 5/3 \cdot Fb/EA$$

$$L_{EC}^{XX} = N_{EC}^X N_{EC}^X I_{EC}/EA_{EC} = -3/5 \cdot (-3/5) \cdot 3 \cdot 1/2 \cdot Fb/EA = 27/50 \cdot Fb/EA$$

$$L_{FE}^{XX} = N_{FE}^X N_{FE}^X I_{FE}/EA_{FE} = -1 \cdot (-1) \cdot 5 \cdot 1/2 \cdot Fb/EA = 5/2 \cdot Fb/EA$$

$$L_{DE}^{XX} = N_{DE}^X N_{DE}^X I_{DE}/EA_{DE} = 4/5 \cdot 4/5 \cdot 4 \cdot 1 \cdot Fb/EA = 64/25 \cdot Fb/EA$$

$$L_{FD}^{XX} = N_{FD}^X N_{FD}^X I_{FD}/EA_{FD} = -6/5 \cdot (-6/5) \cdot 3 \cdot 1 \cdot Fb/EA = 108/25 \cdot Fb/EA$$

$$L_{CB}^{Xo} = N_{CB}^X N_{CB}^o I_{CB}/EA_{CB} = -6/5 \cdot 24 \cdot 3 \cdot 1/4 \cdot Fb/EA = -108/5 \cdot Fb/EA$$

$$L_{AC}^{x_0} = N_{AC}^x N_{AC}^0 I_{AC}/EA_{AC} = 4/5 \quad (-16) \quad 4 \quad 1/4 \quad Fb/EA = -64/5 \quad Fb/EA$$

$$L_{DC}^{x_0} = N_{DC}^x N_{DC}^0 I_{DC}/EA_{DC} = -1 \quad 20 \quad 5 \quad 1/3 \quad Fb/EA = -100/3 \quad Fb/EA$$

$$L_{EC}^{x_0} = N_{EC}^x N_{EC}^0 I_{EC}/EA_{EC} = -3/5 \quad 12 \quad 3 \quad 1/2 \quad Fb/EA = -54/5 \quad Fb/EA$$

$$L_{FE}^{x_0} = N_{FE}^x N_{FE}^0 I_{FE}/EA_{FE} = -1 \quad 20 \quad 5 \quad 1/2 \quad Fb/EA = -50 \quad Fb/EA$$

$$L_{DE}^{x_0} = N_{DE}^x N_{DE}^0 I_{DE}/EA_{DE} = 4/5 \quad (-16) \quad 4 \quad 1 \quad Fb/EA = -256/5 \quad Fb/EA$$

$$L_{FD}^{x_0} = N_{FD}^x N_{FD}^0 I_{FD}/EA_{FD} = -6/5 \quad 12 \quad 3 \quad 1 \quad Fb/EA = -216/5 \quad Fb/EA$$

Contributi nulli elementi

$$L_{AB}^{x_0} \quad L_{DA}^{x_0}$$

Contributi nulli nodi vincolati

$$L_B^{xx} \quad L_F^{xx} \quad L_B^{x_0} \quad L_F^{x_0}$$

Espressione risolvete

$$\left(L_{AB}^{xx} + L_{CB}^{xx} + L_{AC}^{xx} + L_{DA}^{xx} + L_{DC}^{xx} + L_{EC}^{xx} + L_{FE}^{xx} + L_{DE}^{xx} + L_{FD}^{xx} \right) X = - \left(L_{CB}^{x_0} + L_{AC}^{x_0} + L_{DC}^{x_0} + L_{EC}^{x_0} + L_{FE}^{x_0} + L_{DE}^{x_0} + L_{FD}^{x_0} \right)$$

$$\left(1 + 27/25 + 16/25 + 9/25 + 5/3 + 27/50 + 5/2 + 64/25 + 108/25 \right) X = \left(108/5 + 64/5 + 100/3 + 54/5 + 50 + 256/5 + 216/5 \right) F$$

$$44/3 X = 3344/15 F$$

Soluzione

$$X = 304/25 F$$

REAZIONI

$$H_B = 84/25F \quad V_B = 304/25F \quad H_F = -84/25F \quad V_F = 96/25F$$

$$N_{AB} = -76/5F \quad N_{CB} = 144/25F \quad N_{AC} = -96/25F \quad N_{DA} = -228/25F \quad N_{DC} = 24/5F$$

$$N_{EC} = 72/25F \quad N_{FE} = 24/5F \quad N_{DE} = -96/25F \quad N_{FD} = -156/25F$$

SPOSTAMENTI NODALI

$$u_A = 696/25(Fb/EA) \quad u_B = 0$$

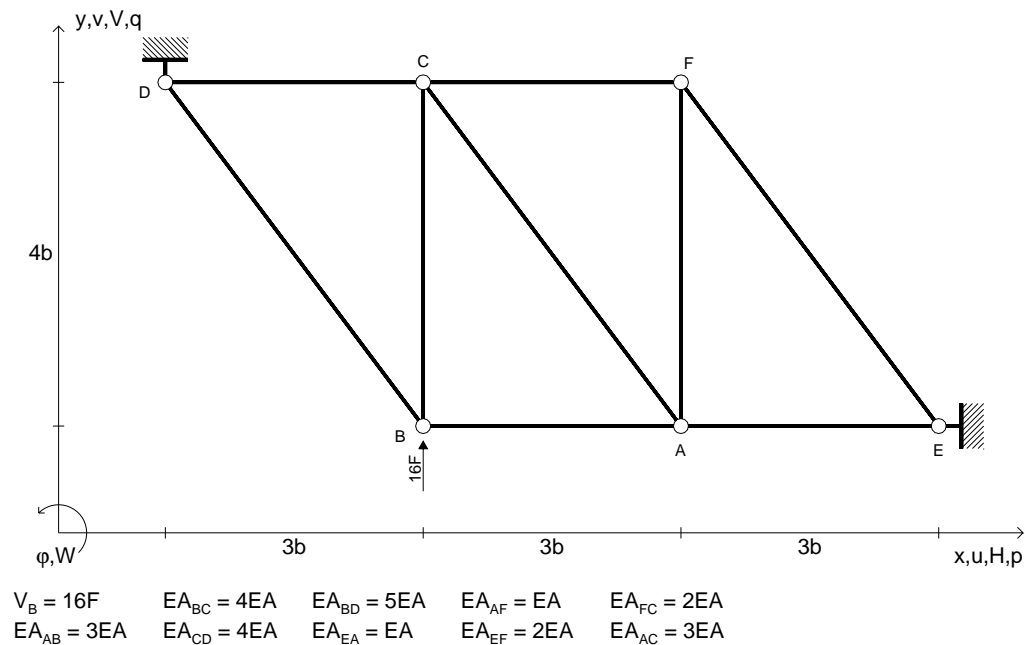
$$v_A = -997/25(Fb/EA) \quad v_B = 0$$

$$u_C = 108/25(Fb/EA) \quad u_D = 468/25(Fb/EA)$$

$$v_C = -901/25(Fb/EA) \quad v_D = -921/25(Fb/EA)$$

$$u_E = 216/25(Fb/EA) \quad u_F = 0$$

$$v_E = -537/25(Fb/EA) \quad v_F = 0$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

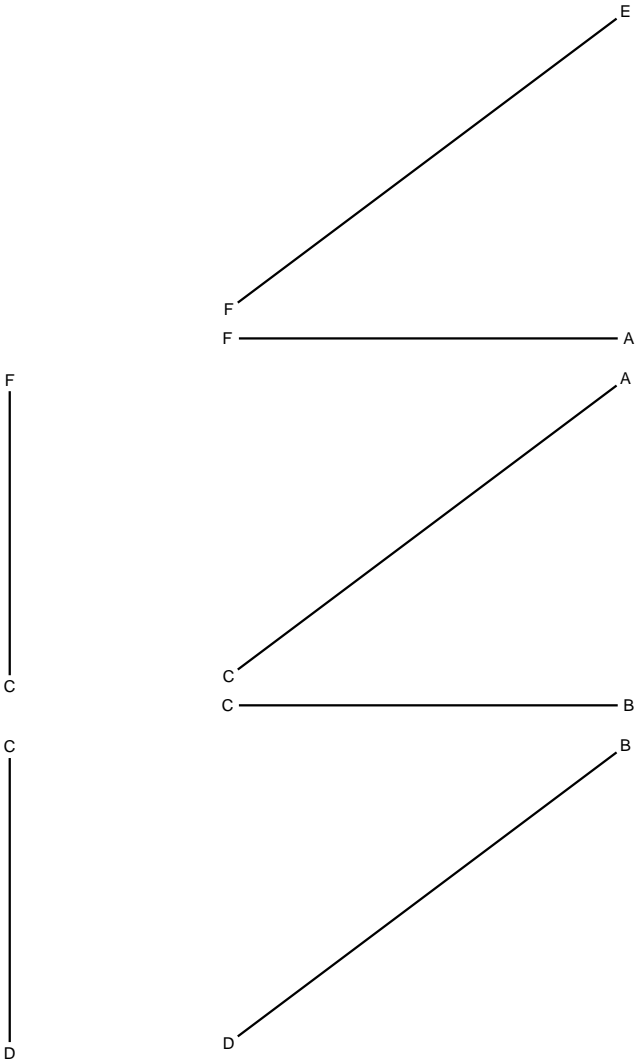
Tracciare i diagrammi delle azioni interne nelle aste.

Calcolare spostamento e rotazione di tutti i nodi.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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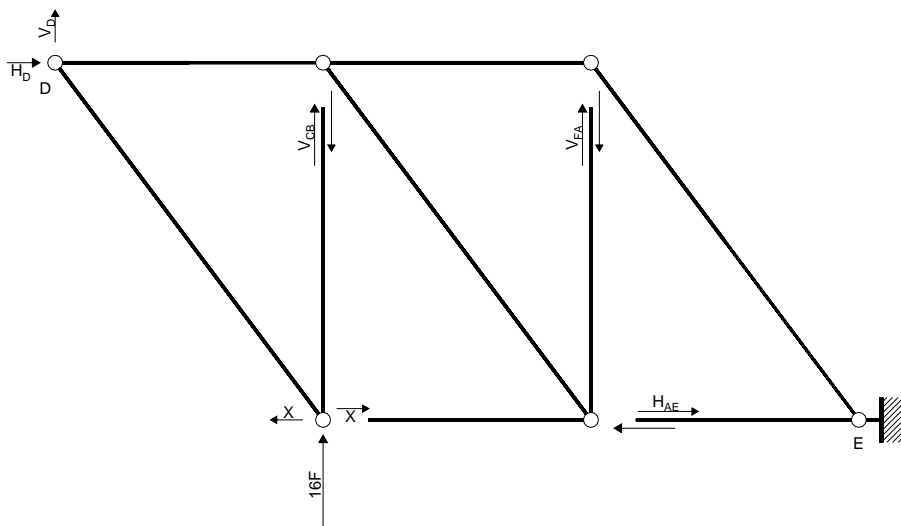


REAZIONI

$H_D =$	$V_D =$	$H_E =$	$V_E =$	
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{BD} =$	$N_{EA} =$
$N_{AF} =$	$N_{EF} =$	$N_{FC} =$	$N_{AC} =$	

SPOSTAMENTI NODALI

$u_A =$	$u_B =$	$u_C =$	$u_D =$
$v_A =$	$v_B =$	$v_C =$	$v_D =$
$u_E =$	$u_F =$		
$v_E =$	$v_F =$		



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a E: aste EF FC CD CA AB DB AF BC

$$-4H_D b - 9V_D b = 96Fb$$

Rotazione intorno a F: aste FC CD CA AB DB AF BC

$$-6V_D b - 4H_{AE} b = 48Fb$$

Rotazione intorno a C: aste CD DB BC

$$-3V_D b = 4Xb$$

Rotazione intorno a C: aste CA AB AF

$$-4H_{AE}b + 3V_{FA}b = -4Xb$$

Rotazione intorno a D: aste DB BC

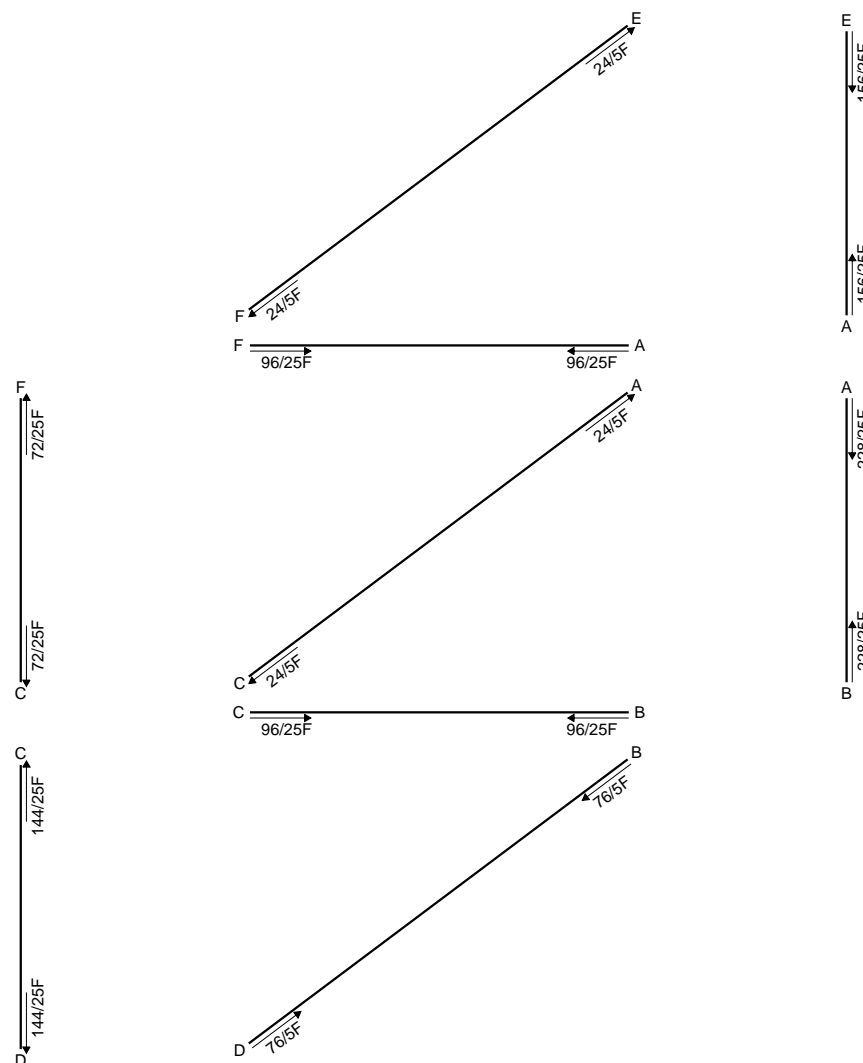
$$3V_{CB}b = 4Xb - 48Fb$$

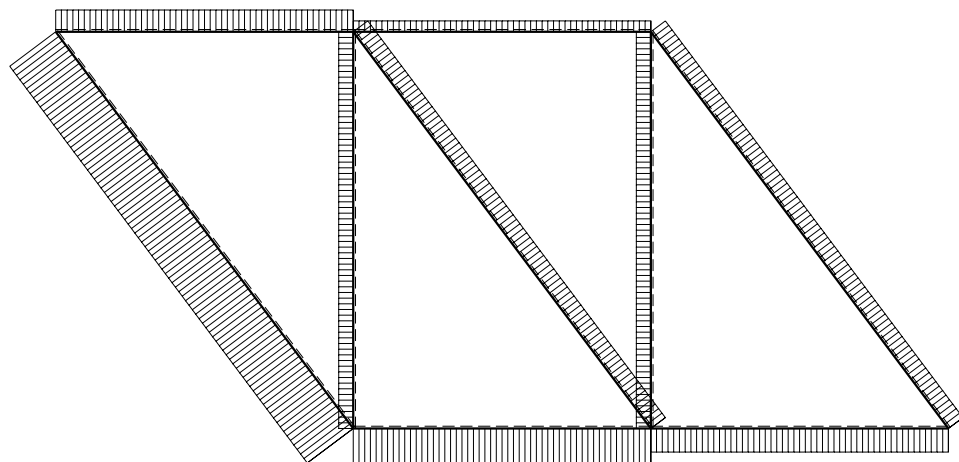
Matrice di equilibrio

$$\begin{bmatrix} \Phi_{EF} & \Phi_{FC} & \Phi_{CD} & \Phi_{CA} & \Phi_{DB} \end{bmatrix} \begin{bmatrix} H_D^b & V_D^b & V_{CB}^b & H_{AE}^b & V_{FA}^b \end{bmatrix} = \begin{bmatrix} X_b & F_b \end{bmatrix} \begin{bmatrix} 0 & 96 \\ 0 & 48 \\ 4 & 0 \\ -4 & 0 \\ 4 & -48 \end{bmatrix}$$

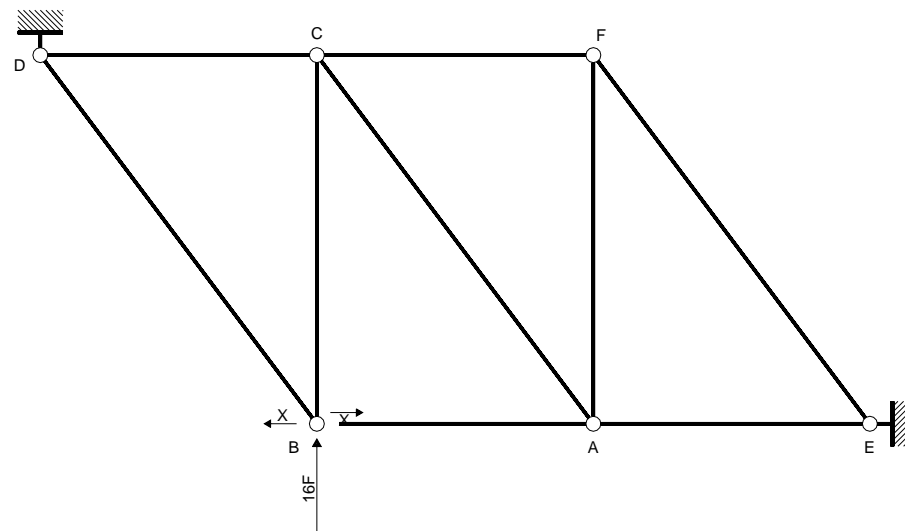
Soluzione del sistema

$$\begin{bmatrix} H_D b \\ V_D b \\ H_{AE} b \\ V_{FA} b \\ V_{CB} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \\ 3 & -24 \\ -4/3 & 0 \\ 2 & -12 \\ 4/3 & -16 \end{bmatrix}$$





← ⊕ → | 20 F



REAZIONI IPERSTATICHE

$$X = H_{BA}$$

CALCOLO DELLE REAZIONI IPERSTATICHE

$$L_{AB}^{XX} = N_{AB}^X N_{AB}^X I_{AB}/EA_{AB} = -1 \cdot (-1) \cdot 3 \cdot 1/3 \cdot Fb/EA = Fb/EA$$

$$L_{BC}^{XX} = N_{BC}^X N_{BC}^X I_{BC}/EA_{BC} = 4/3 \cdot 4/3 \cdot 4 \cdot 1/4 \cdot Fb/EA = 16/9 \cdot Fb/EA$$

$$L_{CD}^{XX} = N_{CD}^X N_{CD}^X I_{CD}/EA_{CD} = -2 \cdot (-2) \cdot 3 \cdot 1/4 \cdot Fb/EA = 3 \cdot Fb/EA$$

$$L_{BD}^{XX} = N_{BD}^X N_{BD}^X I_{BD}/EA_{BD} = -5/3 \cdot (-5/3) \cdot 5 \cdot 1/5 \cdot Fb/EA = 25/9 \cdot Fb/EA$$

$$L_{EA}^{XX} = N_{EA}^X N_{EA}^X I_{EA}/EA_{EA} = -2 \cdot (-2) \cdot 3 \cdot 1 \cdot Fb/EA = 12 \cdot Fb/EA$$

$$L_{AF}^{XX} = N_{AF}^X N_{AF}^X I_{AF}/EA_{AF} = 4/3 \cdot 4/3 \cdot 4 \cdot 1 \cdot Fb/EA = 64/9 \cdot Fb/EA$$

$$L_{EF}^{XX} = N_{EF}^X N_{EF}^X I_{EF}/EA_{EF} = -5/3 \cdot (-5/3) \cdot 5 \cdot 1/2 \cdot Fb/EA = 125/18 \cdot Fb/EA$$

$$L_{FC}^{XX} = N_{FC}^X N_{FC}^X I_{FC}/EA_{FC} = -1 \cdot (-1) \cdot 3 \cdot 1/2 \cdot Fb/EA = 3/2 \cdot Fb/EA$$

$$L_{AC}^{XX} = N_{AC}^X N_{AC}^X I_{AC}/EA_{AC} = -5/3 \cdot (-5/3) \cdot 5 \cdot 1/3 \cdot Fb/EA = 125/27 \cdot Fb/EA$$

$$L_{BC}^{Xo} = N_{BC}^X N_{BC}^o I_{BC}/EA_{BC} = 4/3 \cdot (-16) \cdot 4 \cdot 1/4 \cdot Fb/EA = -64/3 \cdot Fb/EA$$

$$L_{CD}^{x_0} = N_{CD}^x N_{CD}^0 \quad I_{CD}/EA_{CD} = -2 \quad 24 \quad 3 \quad 1/4 \quad Fb/EA = -36 \quad Fb/EA$$

$$L_{EA}^{x_0} = N_{EA}^x N_{EA}^0 \quad I_{EA}/EA_{EA} = -2 \quad 12 \quad 3 \quad 1 \quad Fb/EA = -72 \quad Fb/EA$$

$$L_{AF}^{x_0} = N_{AF}^x N_{AF}^0 \quad I_{AF}/EA_{AF} = 4/3 \quad (-16) \quad 4 \quad 1 \quad Fb/EA = -256/3 \quad Fb/EA$$

$$L_{EF}^{x_0} = N_{EF}^x N_{EF}^0 \quad I_{EF}/EA_{EF} = -5/3 \quad 20 \quad 5 \quad 1/2 \quad Fb/EA = -250/3 \quad Fb/EA$$

$$L_{FC}^{x_0} = N_{FC}^x N_{FC}^0 \quad I_{FC}/EA_{FC} = -1 \quad 12 \quad 3 \quad 1/2 \quad Fb/EA = -18 \quad Fb/EA$$

$$L_{AC}^{x_0} = N_{AC}^x N_{AC}^0 \quad I_{AC}/EA_{AC} = -5/3 \quad 20 \quad 5 \quad 1/3 \quad Fb/EA = -500/9 \quad Fb/EA$$

Contributi nulli elementi

$$L_{AB}^{x_0} \quad L_{BD}^{x_0}$$

Contributi nulli nodi vincolati

$$L_D^{xx} \quad L_E^{xx} \quad L_D^{x_0} \quad L_E^{x_0}$$

Espressione risolvante

$$\left(L_{AB}^{xx} + L_{BC}^{xx} + L_{CD}^{xx} + L_{BD}^{xx} + L_{EA}^{xx} + L_{AF}^{xx} + L_{EF}^{xx} + L_{FC}^{xx} + L_{AC}^{xx} \right) X = - \left(L_{BC}^{x_0} + L_{CD}^{x_0} + L_{EA}^{x_0} + L_{AF}^{x_0} + L_{EF}^{x_0} + L_{FC}^{x_0} + L_{AC}^{x_0} \right)$$

$$\left(1 + 16/9 + 3 + 25/9 + 12 + 64/9 + 125/18 + 3/2 + 125/27 \right) X = \left(64/3 + 36 + 72 + 256/3 + 250/3 + 18 + 500/9 \right) F$$

$$1100/27 X = 3344/9 F$$

Soluzione

$$X = 228/25 F$$

REAZIONI

$$H_D = 84/25F \quad V_D = -304/25F \quad H_E = -84/25F \quad V_E = -96/25F$$

$$N_{AB} = -228/25F \quad N_{BC} = -96/25F \quad N_{CD} = 144/25F \quad N_{BD} = -76/5F \quad N_{EA} = -156/25F$$

$$N_{AF} = -96/25F \quad N_{EF} = 24/5F \quad N_{FC} = 72/25F \quad N_{AC} = 24/5F$$

SPOSTAMENTI NODALI

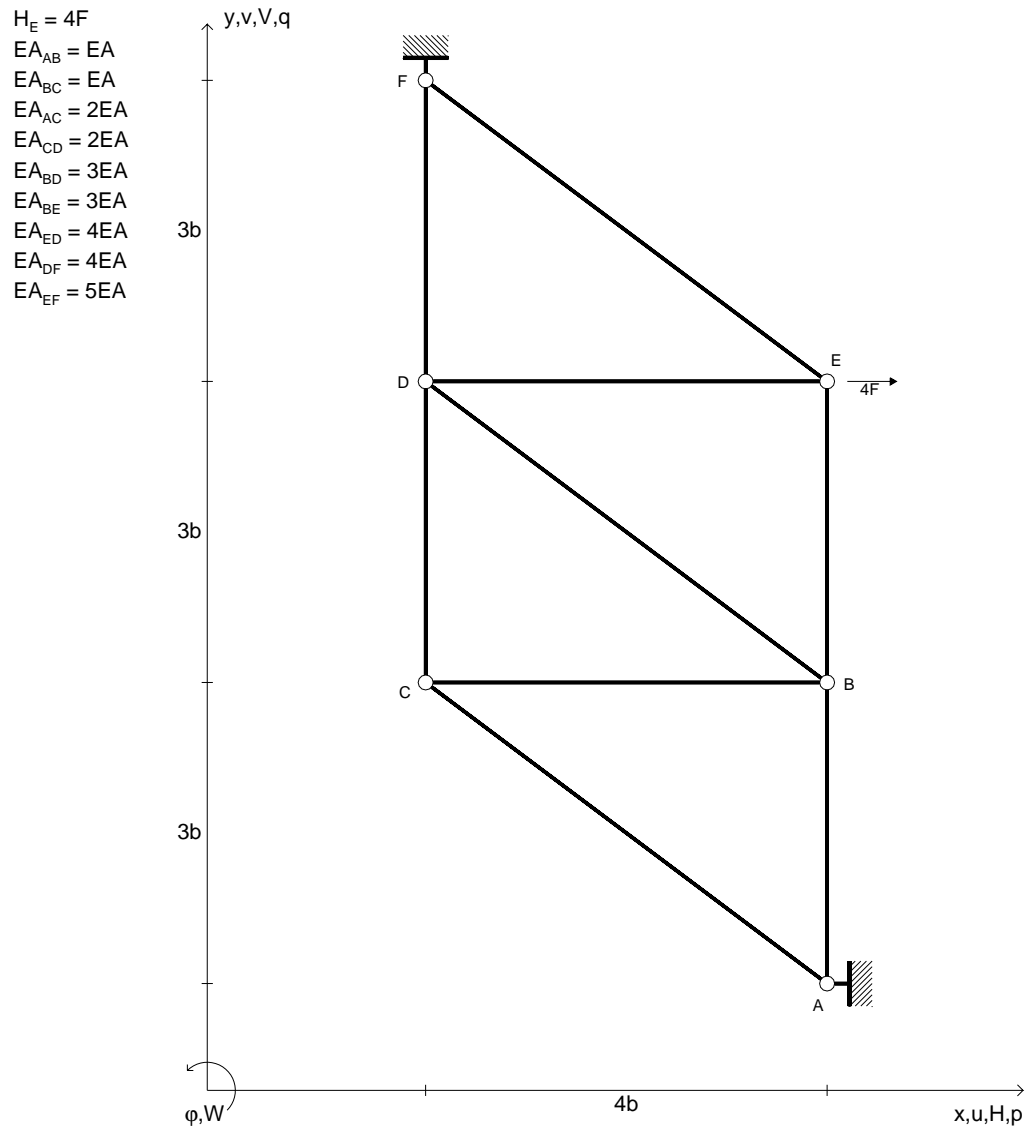
$$\begin{aligned} u_A &= 468/25(Fb/EA) & u_B &= 696/25(Fb/EA) & u_C &= 108/25(Fb/EA) & u_D &= 0 \\ v_A &= 921/25(Fb/EA) & v_B &= 997/25(Fb/EA) & v_C &= 901/25(Fb/EA) & v_D &= 0 \end{aligned}$$

$$u_E = 0$$

$$u_F = 216/25(Fb/EA)$$

$$v_E = 0$$

$$v_F = 537/25(Fb/EA)$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

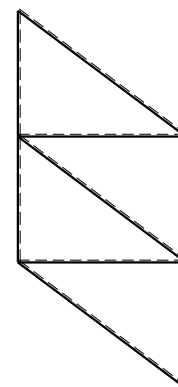
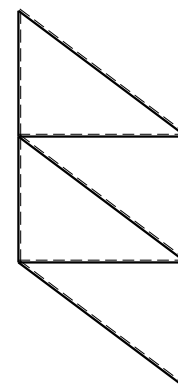
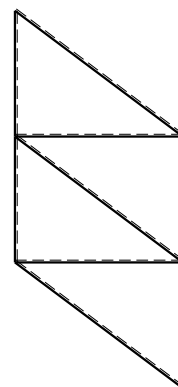
Calcolare reazioni vincolari della struttura e delle aste.

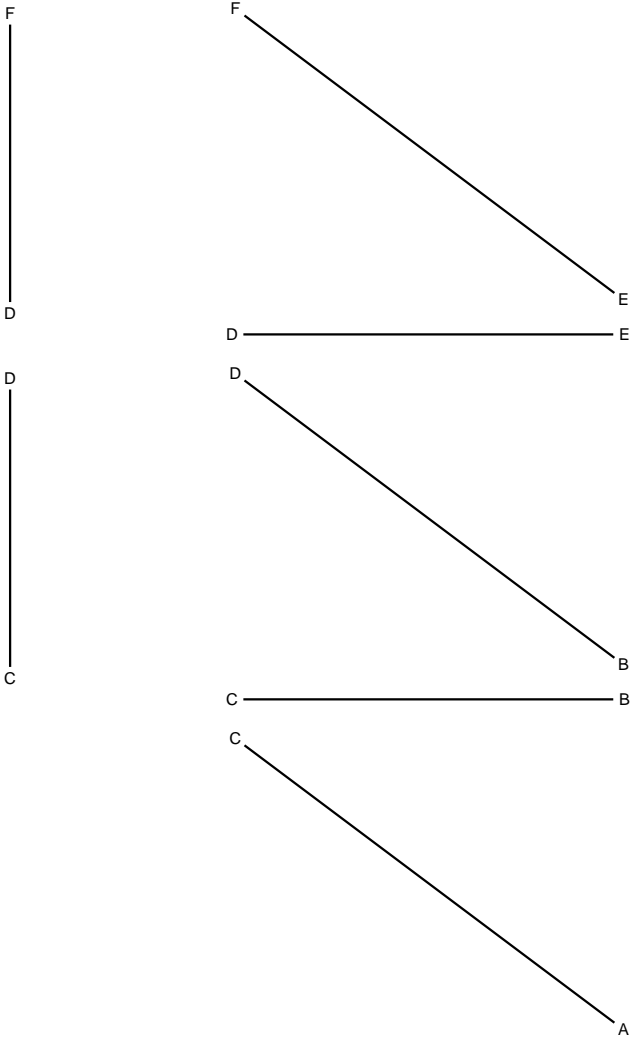
Tracciare i diagrammi delle azioni interne nelle aste.

Calcolare spostamento e rotazione di tutti i nodi.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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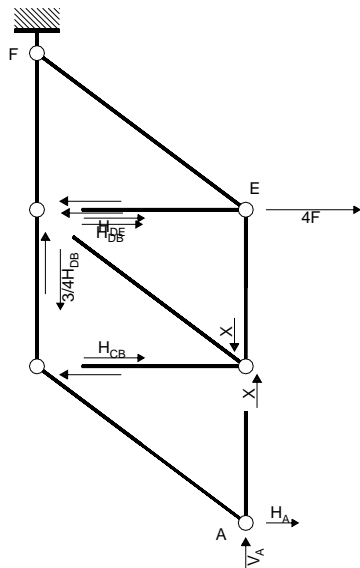
REAZIONI

$H_A =$	$V_A =$	$H_F =$	$V_F =$		
$N_{AB} =$	$N_{BC} =$	$N_{AC} =$	$N_{CD} =$	$N_{BD} =$	$N_{BE} =$
$N_{ED} =$	$N_{DF} =$	$N_{EF} =$			

SPOSTAMENTI NODALI

$u_A =$	$u_B =$	$u_C =$	$u_D =$
$v_A =$	$v_B =$	$v_C =$	$v_D =$
$u_E =$	$u_F =$		
$v_E =$	$v_F =$		





EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DC CA AB

$$9H_A b + 4V_A b - 6H_{CB} b - 3H_{DB} b - 3H_{DE} b = -4Xb$$

Rotazione intorno a F: aste FE EB ED BC BD

$$6H_{CB} b + 3H_{DB} b + 3H_{DE} b = 4Xb - 12Fb$$

Rotazione intorno a D: aste DC CA AB

$$6H_A b + 4V_A b - 3H_{CB} b = -4Xb$$

Rotazione intorno a E: aste EB BC BD

$$3H_{CB} b + 3H_{DB} b = 0$$

Rotazione intorno a C: aste CA AB

$$3H_A b + 4V_A b = -4Xb$$

Matrice di equilibrio

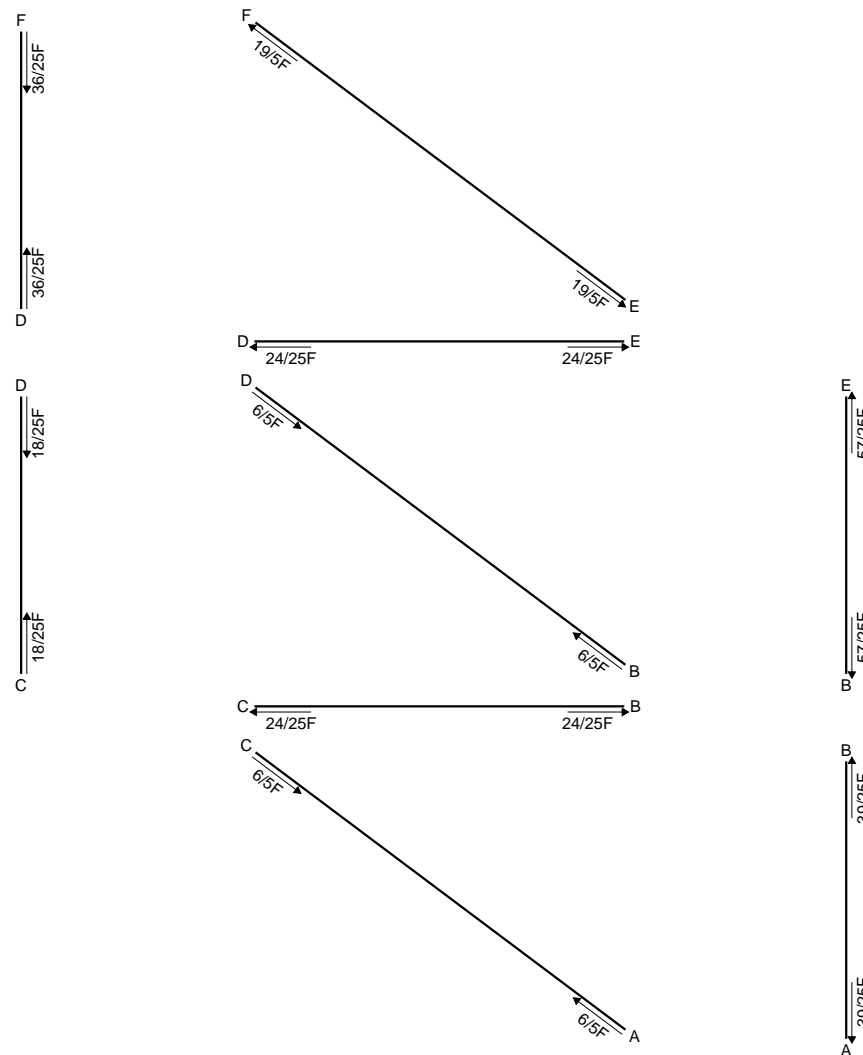
$$\begin{bmatrix} \varphi_{FD} \\ \varphi_{FE} \\ \varphi_{DC} \\ \varphi_{EB} \\ \varphi_{CA} \end{bmatrix} \begin{bmatrix} H_A b & V_A b & H_{CB} b & H_{DB} b & H_{DE} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

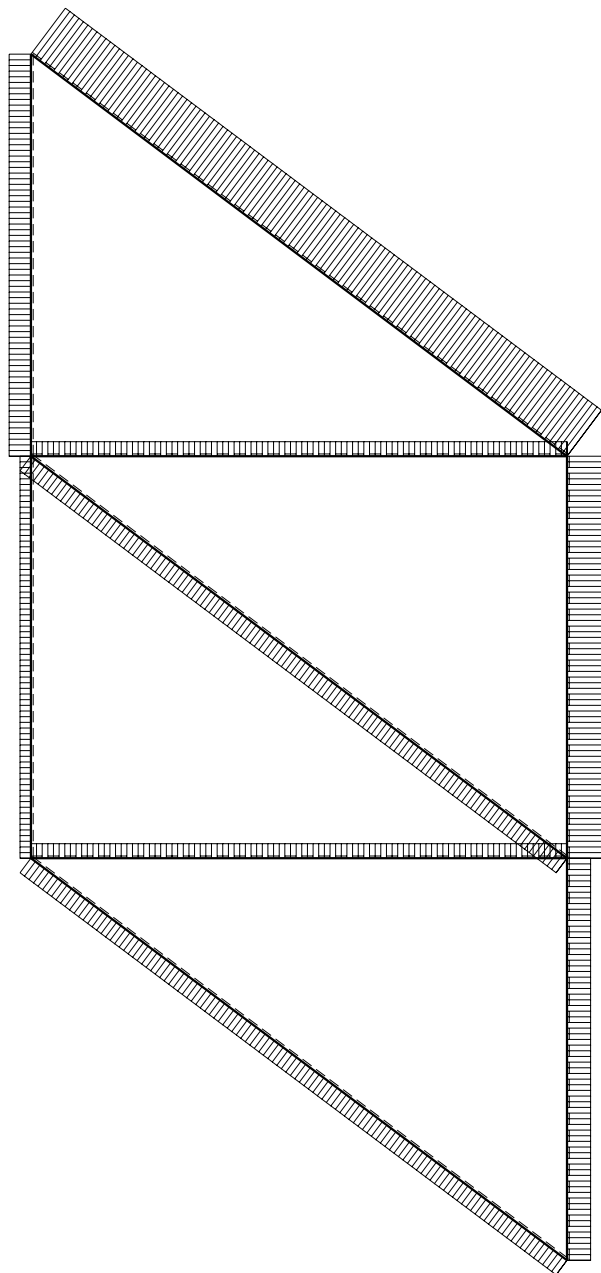
$$\begin{bmatrix} 9 & 4 & -6 & -3 & -3 \\ 0 & 0 & 6 & 3 & 3 \\ 6 & 4 & -3 & 0 & 0 \\ 0 & 0 & 3 & 3 & 0 \\ 3 & 4 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} -4 & 0 \\ 4 & -12 \\ -4 & 0 \\ 0 & 0 \\ -4 & 0 \end{bmatrix}$$

Soluzione del sistema

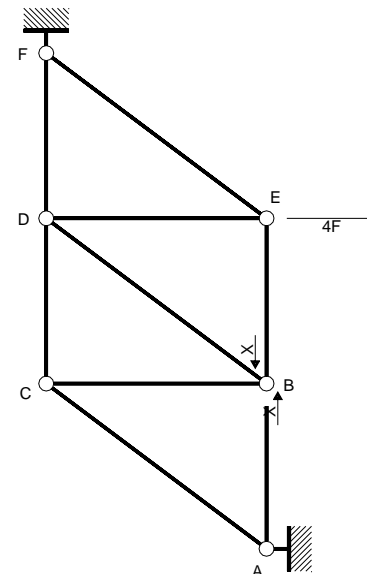
$$\begin{bmatrix} H_A b \\ H_{CB} b \\ V_A b \\ H_{DB} b \\ H_{DE} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

$$\begin{bmatrix} 2/3 & -2 \\ 2/3 & -2 \\ -3/2 & 3/2 \\ -2/3 & 2 \\ 2/3 & -2 \end{bmatrix}$$





← ⊕ → | 5 F



REAZIONI IPERSTATICHE

$$X = V_{BA}$$

CALCOLO DELLE REAZIONI IPERSTATICHE

$$L_{AB}^{xx} = N_{AB}^x N_{AB}^x I_{AB}/EA_{AB} = 1 \ 1 \ 3 \ 1 \ Fb/EA = 3 \ Fb/EA$$

$$L_{BC}^{xx} = N_{BC}^x N_{BC}^x I_{BC}/EA_{BC} = -2/3 \ (-2/3) \ 4 \ 1 \ Fb/EA = 16/9 \ Fb/EA$$

$$L_{AC}^{xx} = N_{AC}^x N_{AC}^x I_{AC}/EA_{AC} = 5/6 \ 5/6 \ 5 \ 1/2 \ Fb/EA = 125/72 \ Fb/EA$$

$$L_{CD}^{xx} = N_{CD}^x N_{CD}^x I_{CD}/EA_{CD} = 1/2 \ 1/2 \ 3 \ 1/2 \ Fb/EA = 3/8 \ Fb/EA$$

$$L_{BD}^{xx} = N_{BD}^x N_{BD}^x I_{BD}/EA_{BD} = 5/6 \ 5/6 \ 5 \ 1/3 \ Fb/EA = 125/108 \ Fb/EA$$

$$L_{BE}^{xx} = N_{BE}^x N_{BE}^x I_{BE}/EA_{BE} = 1/2 \ 1/2 \ 3 \ 1/3 \ Fb/EA = 1/4 \ Fb/EA$$

$$L_{ED}^{xx} = N_{ED}^x N_{ED}^x I_{ED}/EA_{ED} = -2/3 \ (-2/3) \ 4 \ 1/4 \ Fb/EA = 4/9 \ Fb/EA$$

$$L_{DF}^{xx} = N_{DF}^x N_{DF}^x I_{DF}/EA_{DF} = 1 \ 1 \ 3 \ 1/4 \ Fb/EA = 3/4 \ Fb/EA$$

$$L_{EF}^{xx} = N_{EF}^x N_{EF}^x I_{EF}/EA_{EF} = 5/6 \ 5/6 \ 5 \ 1/5 \ Fb/EA = 25/36 \ Fb/EA$$

$$L_{BC}^{x_0} = N_{BC}^x N_{BC}^0 I_{BC}/EA_{BC} = -2/3 \quad 2 \quad 4 \quad 1 \quad Fb/EA = -16/3 \quad Fb/EA$$

$$L_{AC}^{x_0} = N_{AC}^x N_{AC}^0 I_{AC}/EA_{AC} = 5/6 \quad (-5/2) \quad 5 \quad 1/2 \quad Fb/EA = -125/24 \quad Fb/EA$$

$$L_{CD}^{x_0} = N_{CD}^x N_{CD}^0 I_{CD}/EA_{CD} = 1/2 \quad (-3/2) \quad 3 \quad 1/2 \quad Fb/EA = -9/8 \quad Fb/EA$$

$$L_{BD}^{x_0} = N_{BD}^x N_{BD}^0 I_{BD}/EA_{BD} = 5/6 \quad (-5/2) \quad 5 \quad 1/3 \quad Fb/EA = -125/36 \quad Fb/EA$$

$$L_{BE}^{x_0} = N_{BE}^x N_{BE}^0 I_{BE}/EA_{BE} = 1/2 \quad 3/2 \quad 3 \quad 1/3 \quad Fb/EA = 3/4 \quad Fb/EA$$

$$L_{ED}^{x_0} = N_{ED}^x N_{ED}^0 I_{ED}/EA_{ED} = -2/3 \quad 2 \quad 4 \quad 1/4 \quad Fb/EA = -4/3 \quad Fb/EA$$

$$L_{DF}^{x_0} = N_{DF}^x N_{DF}^0 I_{DF}/EA_{DF} = 1 \quad (-3) \quad 3 \quad 1/4 \quad Fb/EA = -9/4 \quad Fb/EA$$

$$L_{EF}^{x_0} = N_{EF}^x N_{EF}^0 I_{EF}/EA_{EF} = 5/6 \quad 5/2 \quad 5 \quad 1/5 \quad Fb/EA = 25/12 \quad Fb/EA$$

Contributi nulli elementi

$$L_{AB}^{x_0}$$

Contributi nulli nodi vincolati

$$L_A^{xx} \quad L_F^{xx} \quad L_A^{x_0} \quad L_F^{x_0}$$

Espressione risolvante

$$\left(L_{AB}^{xx} + L_{BC}^{xx} + L_{AC}^{xx} + L_{CD}^{xx} + L_{BD}^{xx} + L_{BE}^{xx} + L_{ED}^{xx} + L_{DF}^{xx} + L_{EF}^{xx} \right) X = - \left(L_{BC}^{x_0} + L_{AC}^{x_0} + L_{CD}^{x_0} + L_{BD}^{x_0} + L_{BE}^{x_0} + L_{ED}^{x_0} + L_{DF}^{x_0} + L_{EF}^{x_0} \right)$$

$$\left(3 + 16/9 + 125/72 + 3/8 + 125/108 + 1/4 + 4/9 + 3/4 + 25/36 \right) X = \left(16/3 + 125/24 + 9/8 + 125/36 - 3/4 + 4/3 + 9/4 - 25/12 \right) F$$

$$275/27 X = 143/9 F$$

Soluzione

$$X = 39/25 F$$

REAZIONI

$$H_A = -24/25F \quad V_A = -21/25F \quad H_F = -76/25F \quad V_F = 21/25F$$

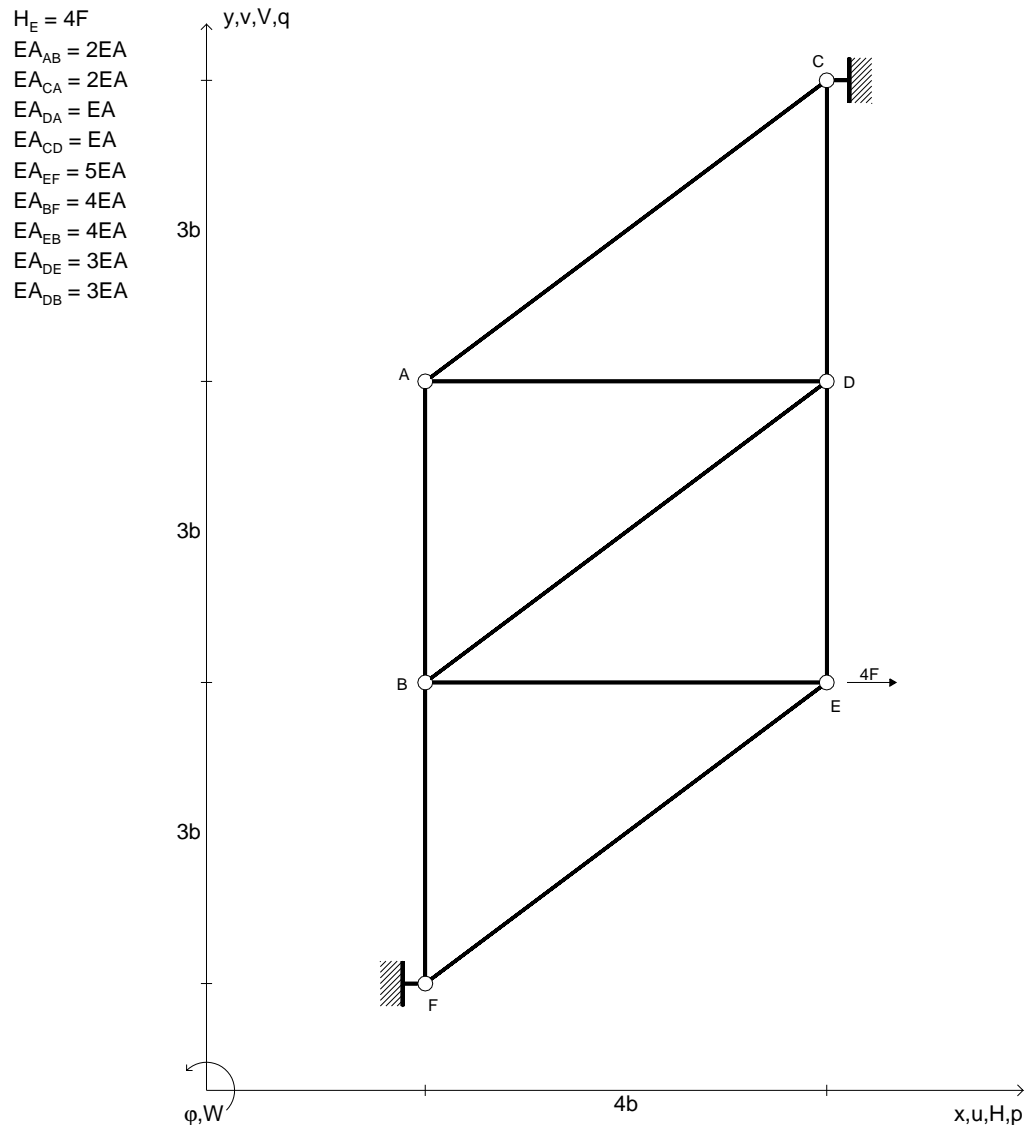
$$N_{AB} = 39/25F \quad N_{BC} = 24/25F \quad N_{AC} = -6/5F \quad N_{CD} = -18/25F \quad N_{BD} = -6/5F \quad N_{BE} = 57/25F$$

$$N_{ED} = 24/25F \quad N_{DF} = -36/25F \quad N_{EF} = 19/5F$$

SPOSTAMENTI NODALI

$$\begin{array}{llll} u_A = 0 & u_B = 921/100(Fb/EA) & u_C = 537/100(Fb/EA) & u_D = 901/100(Fb/EA) \\ v_A = 0 & v_B = 117/25(Fb/EA) & v_C = 54/25(Fb/EA) & v_D = 27/25(Fb/EA) \end{array}$$

$$\begin{array}{ll} u_E = 997/100(Fb/EA) & u_F = 0 \\ v_E = 174/25(Fb/EA) & v_F = 0 \end{array}$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

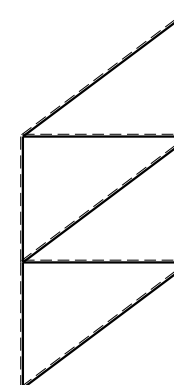
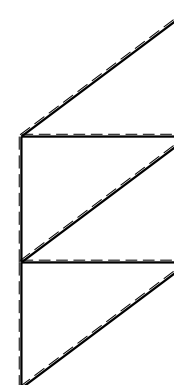
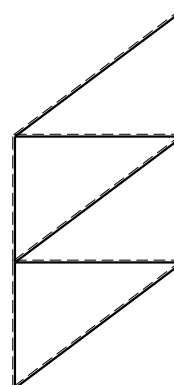
Calcolare reazioni vincolari della struttura e delle aste.

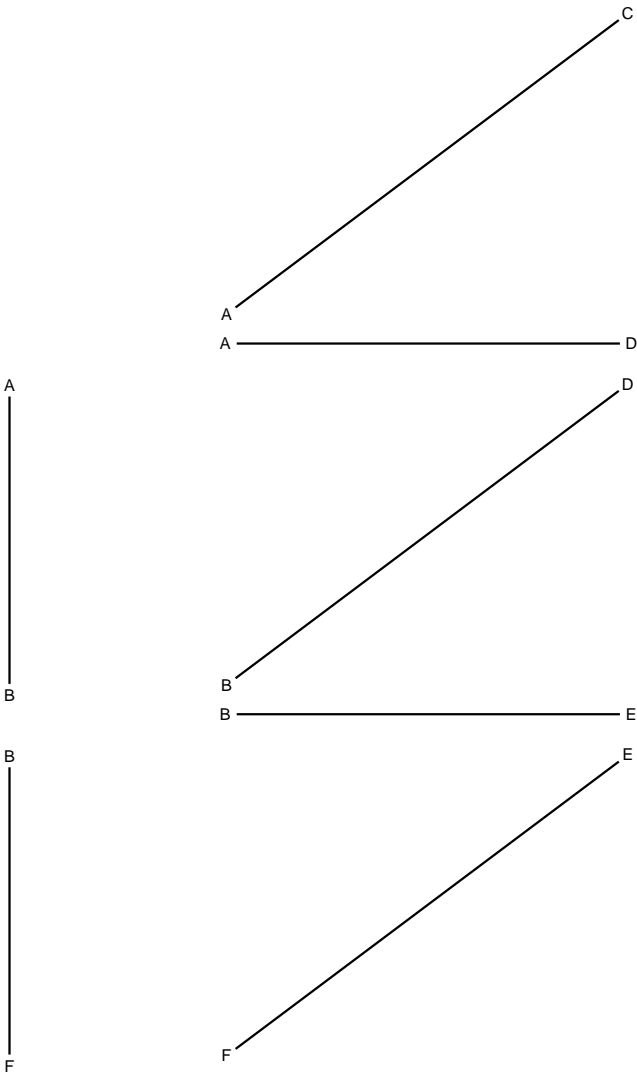
Tracciare i diagrammi delle azioni interne nelle aste.

Calcolare spostamento e rotazione di tutti i nodi.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

@ Adolfo Zavelani Rossi, Politecnico di Milano



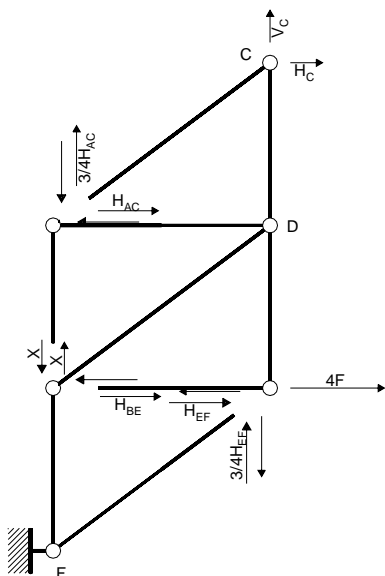


REAZIONI

$H_C =$	$V_C =$	$H_F =$	$V_F =$		
$N_{AB} =$	$N_{CA} =$	$N_{DA} =$	$N_{CD} =$	$N_{EF} =$	$N_{BF} =$
$N_{EB} =$	$N_{DE} =$	$N_{DB} =$			

SPOSTAMENTI NODALI

$u_A =$	$u_B =$	$u_C =$	$u_D =$
$v_A =$	$v_B =$	$v_C =$	$v_D =$
$u_E =$	$u_F =$		
$v_E =$	$v_F =$		



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FB BD DA DC DE AB CA EB

$$-9H_Cb + 4V_Cb = 12Fb$$

Rotazione intorno a B: aste BD DA DC DE AB CA EB

$$-6H_Cb + 4V_Cb - 3H_{EF}b = 0$$

Rotazione intorno a D: aste DA AB

$$3H_{AC}b = 4Xb$$

Rotazione intorno a D: aste DC CA

$$-3H_Cb - 3H_{AC}b = 0$$

Rotazione intorno a D: aste DE EB

$$-3H_{EF}b + 3H_{BE}b = -12Fb$$

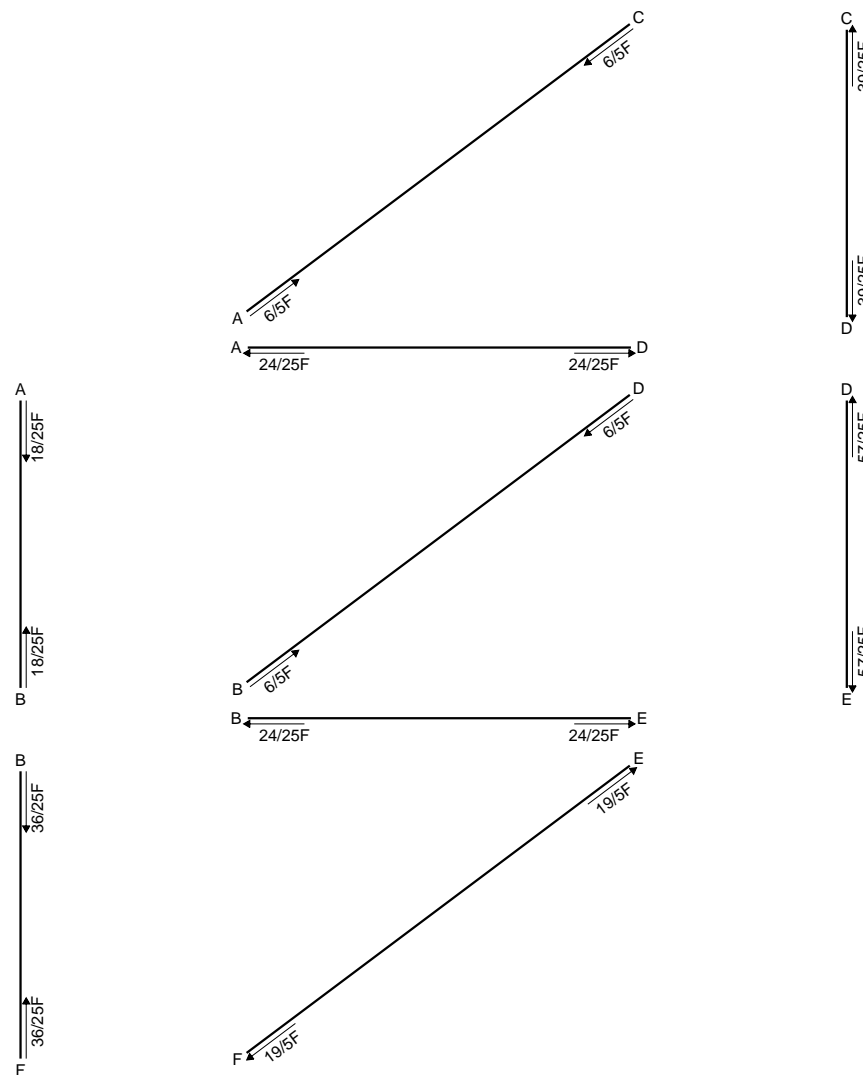
Matrice di equilibrio

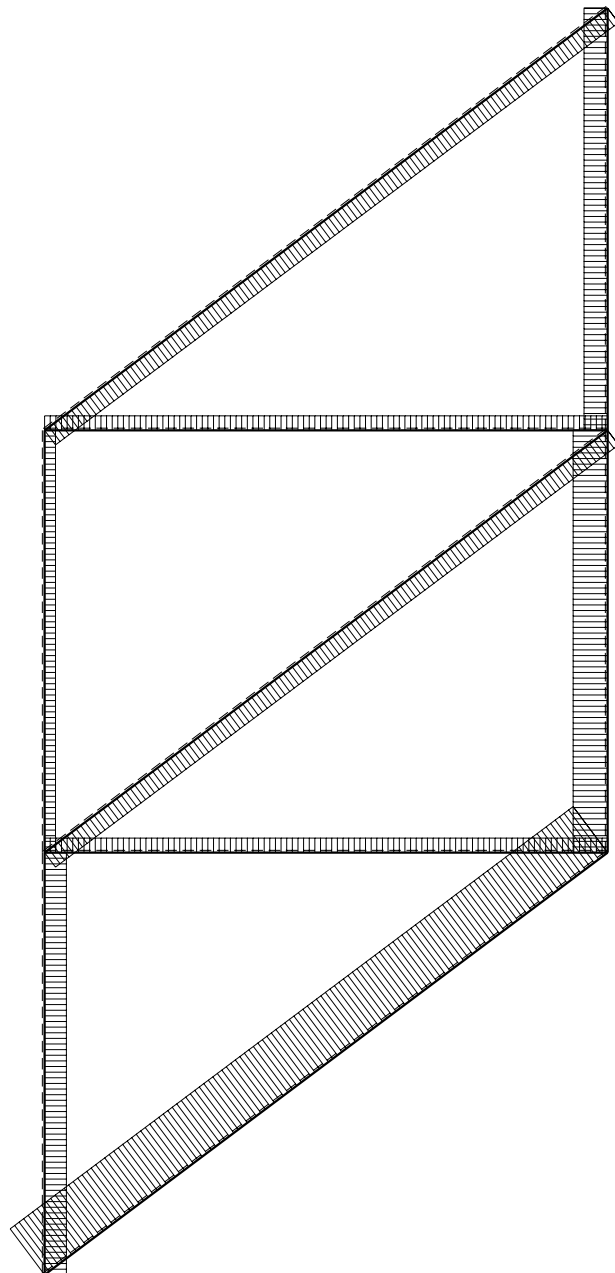
$$\begin{bmatrix} \phi_{FB} \\ \phi_{BD} \\ \phi_{DA} \\ \phi_{DC} \\ \phi_{DE} \end{bmatrix} \begin{bmatrix} H_Cb & V_Cb & H_{AC}b & H_{EF}b & H_{BE}b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix}$$

$$\begin{bmatrix} -9 & 4 & 0 & 0 & 0 \\ -6 & 4 & 0 & -3 & 0 \\ 0 & 0 & 3 & 0 & 0 \\ -3 & 0 & -3 & 0 & 0 \\ 0 & 0 & 0 & -3 & 3 \end{bmatrix} = \begin{bmatrix} 0 & 12 \\ 0 & 0 \\ 4 & 0 \\ 0 & 0 \\ 0 & -12 \end{bmatrix}$$

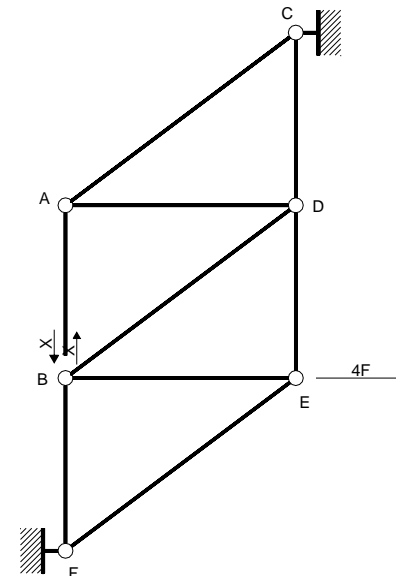
Soluzione del sistema

$$\begin{bmatrix} H_Cb \\ V_Cb \\ H_{AC}b \\ H_{EF}b \\ H_{BE}b \end{bmatrix} = \begin{bmatrix} -4/3 & 0 \\ -3 & 3 \\ 4/3 & 0 \\ -4/3 & 4 \\ -4/3 & 0 \end{bmatrix}$$





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REAZIONI IPERSTATICHE

$$X = V_{BA}$$

CALCOLO DELLE REAZIONI IPERSTATICHE

$$L_{AB}^{xx} = N_{AB}^x N_{AB}^x I_{AB}/EA_{AB} = -1 \quad (-1) \quad 3 \quad 1/2 \quad Fb/EA = 3/2 \quad Fb/EA$$

$$L_{CA}^{xx} = N_{CA}^x N_{CA}^x I_{CA}/EA_{CA} = -5/3 \quad (-5/3) \quad 5 \quad 1/2 \quad Fb/EA = 125/18 \quad Fb/EA$$

$$L_{DA}^{xx} = N_{DA}^x N_{DA}^x I_{DA}/EA_{DA} = 4/3 \quad 4/3 \quad 4 \quad 1 \quad Fb/EA = 64/9 \quad Fb/EA$$

$$L_{CD}^{xx} = N_{CD}^x N_{CD}^x I_{CD}/EA_{CD} = -2 \quad (-2) \quad 3 \quad 1 \quad Fb/EA = 12 \quad Fb/EA$$

$$L_{EF}^{xx} = N_{EF}^x N_{EF}^x I_{EF}/EA_{EF} = -5/3 \quad (-5/3) \quad 5 \quad 1/5 \quad Fb/EA = 25/9 \quad Fb/EA$$

$$L_{BF}^{xx} = N_{BF}^x N_{BF}^x I_{BF}/EA_{BF} = -2 \quad (-2) \quad 3 \quad 1/4 \quad Fb/EA = 3 \quad Fb/EA$$

$$L_{EB}^{xx} = N_{EB}^x N_{EB}^x I_{EB}/EA_{EB} = 4/3 \quad 4/3 \quad 4 \quad 1/4 \quad Fb/EA = 16/9 \quad Fb/EA$$

$$L_{DE}^{xx} = N_{DE}^x N_{DE}^x I_{DE}/EA_{DE} = -1 \quad (-1) \quad 3 \quad 1/3 \quad Fb/EA = Fb/EA$$

$$L_{DB}^{xx} = N_{DB}^x N_{DB}^x I_{DB}/EA_{DB} = -5/3 \quad (-5/3) \quad 5 \quad 1/3 \quad Fb/EA = 125/27 \quad Fb/EA$$

$$L_{CD}^{x_0} = N_{CD}^x N_{CD}^0 \quad I_{CD}/EA_{CD} = -2 \quad 3 \quad 3 \quad 1 \quad Fb/EA = -18 \quad Fb/EA$$

$$L_{EF}^{x_0} = N_{EF}^x N_{EF}^0 \quad I_{EF}/EA_{EF} = -5/3 \quad 5 \quad 5 \quad 1/5 \quad Fb/EA = -25/3 \quad Fb/EA$$

$$L_{DE}^{x_0} = N_{DE}^x N_{DE}^0 \quad I_{DE}/EA_{DE} = -1 \quad 3 \quad 3 \quad 1/3 \quad Fb/EA = -3 \quad Fb/EA$$

Contributi nulli elementi

$$L_{AB}^{x_0} \quad L_{CA}^{x_0} \quad L_{DA}^{x_0} \quad L_{BF}^{x_0} \quad L_{EB}^{x_0} \quad L_{DB}^{x_0}$$

Contributi nulli nodi vincolati

$$L_C^{xx} \quad L_F^{xx} \quad L_C^{x_0} \quad L_F^{x_0}$$

Espressione risolvente

$$\left(L_{AB}^{xx} + L_{CA}^{xx} + L_{DA}^{xx} + L_{CD}^{xx} + L_{EF}^{xx} + L_{BF}^{xx} + L_{EB}^{xx} + L_{DE}^{xx} + L_{DB}^{xx} \right) X = - \left(L_{CD}^{x_0} + L_{EF}^{x_0} + L_{DE}^{x_0} \right)$$

$$\left(3/2 + 125/18 + 64/9 + 12 + 25/9 + 3 + 16/9 + 1 + 125/27 \right) X = \left(18 + 25/3 + 3 \right) F$$

$$1100/27 X = 88/3 F$$

Soluzione

$$X = 18/25 F$$

REAZIONI

$$H_C = -24/25F \quad V_C = 21/25F \quad H_F = -76/25F \quad V_F = -21/25F$$

$$N_{AB} = -18/25F \quad N_{CA} = -6/5F \quad N_{DA} = 24/25F \quad N_{CD} = 39/25F \quad N_{EF} = 19/5F \quad N_{BF} = -36/25F$$

$$N_{EB} = 24/25F \quad N_{DE} = 57/25F \quad N_{DB} = -6/5F$$

SPOSTAMENTI NODALI

$$\begin{aligned} u_A &= 537/100(Fb/EA) & u_B &= 901/100(Fb/EA) & u_C &= 0 & u_D &= 921/100(Fb/EA) \\ v_A &= -54/25(Fb/EA) & v_B &= -27/25(Fb/EA) & v_C &= 0 & v_D &= -117/25(Fb/EA) \end{aligned}$$

$$\begin{aligned} u_E &= 997/100(Fb/EA) & u_F &= 0 \\ v_E &= -174/25(Fb/EA) & v_F &= 0 \end{aligned}$$

$$H_A = -8F$$

$$EA_{AB} = 5EA$$

$$EA_{CB} = 4EA$$

$$EA_{AC} = 4EA$$

$$EA_{DA} = 3EA$$

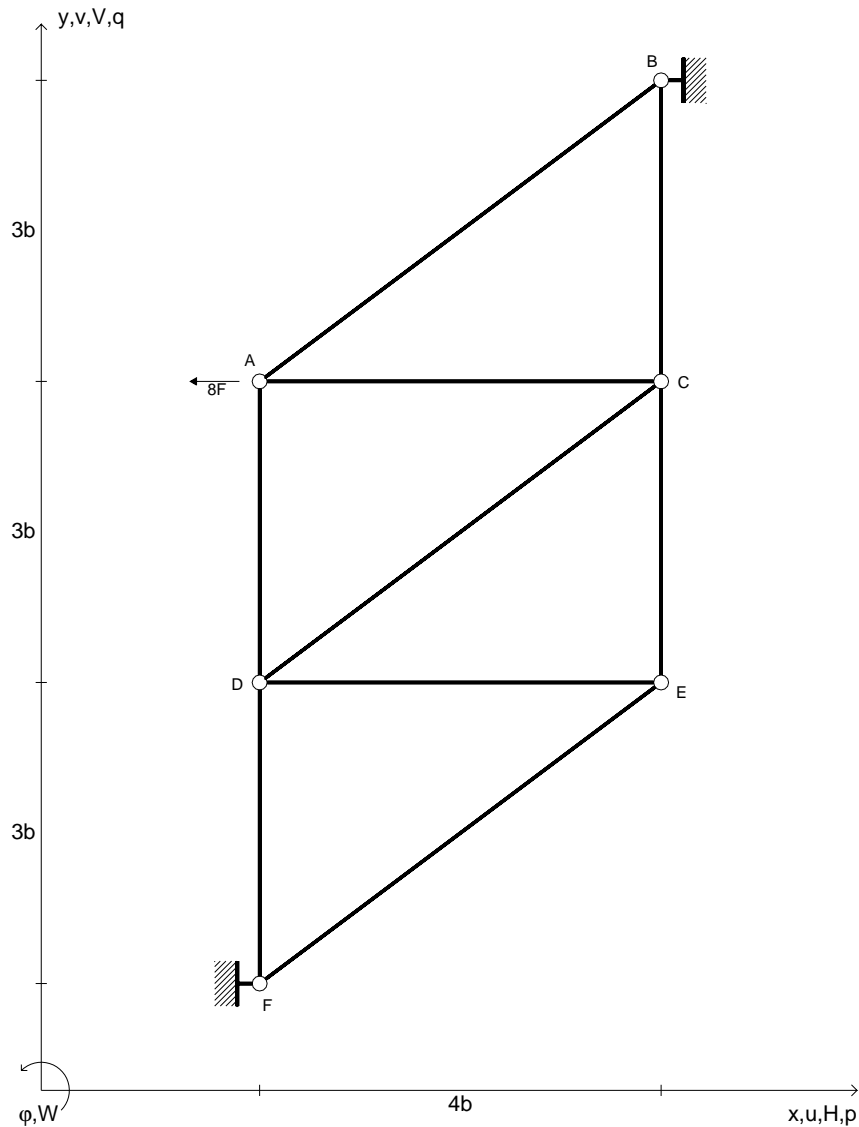
$$EA_{DC} = 3EA$$

$$EA_{EC} = 2EA$$

$$EA_{FE} = 2EA$$

$$EA_{DE} = EA$$

$$EA_{FD} = EA$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

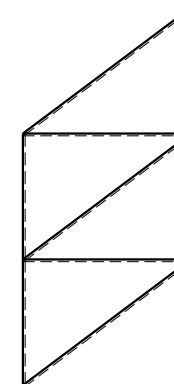
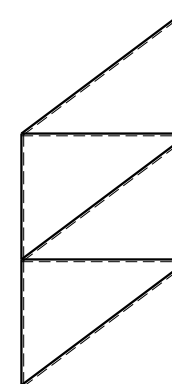
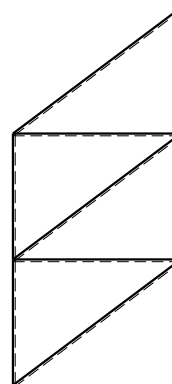
Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi delle azioni interne nelle aste.

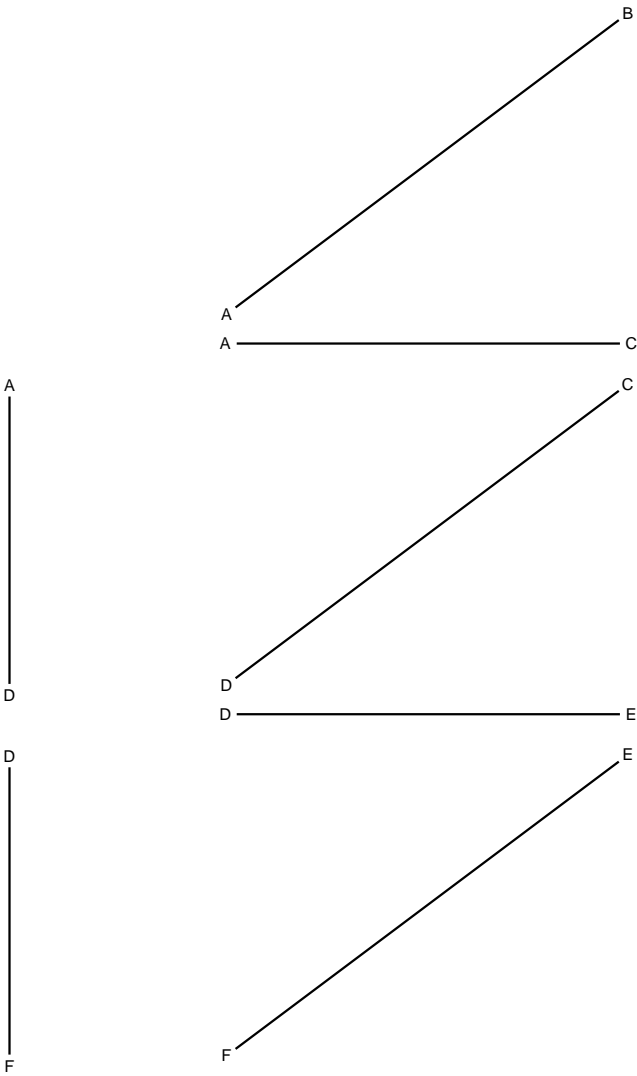
Calcolare spostamento e rotazione di tutti i nodi.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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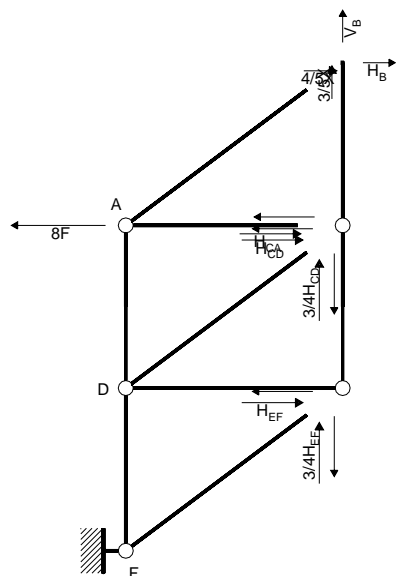


REAZIONI

$H_B =$	$V_B =$	$H_F =$	$V_F =$		
$N_{AB} =$	$N_{CB} =$	$N_{AC} =$	$N_{DA} =$	$N_{DC} =$	$N_{EC} =$
$N_{FE} =$	$N_{DE} =$	$N_{FD} =$			

SPOSTAMENTI NODALI

$u_A =$	$u_B =$	$u_C =$	$u_D =$
$v_A =$	$v_B =$	$v_C =$	$v_D =$
$u_E =$	$u_F =$		
$v_E =$	$v_F =$		



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a F: aste FD DA DC DE AB AC EC CB

$$-9H_B b + 4V_B b = 24/5 Xb - 48Fb$$

Rotazione intorno a D: aste DA AB AC

$$-3H_{CA} b = 12/5 Xb - 24Fb$$

Rotazione intorno a D: aste DE EC CB

$$-6H_B b + 4V_B b + 3H_{CA} b - 3H_{EF} b = 0$$

Rotazione intorno a E: aste EC CB

$$-6H_B b + 3H_{CA} b + 3H_{CD} b = 0$$

Rotazione intorno a C: aste CB

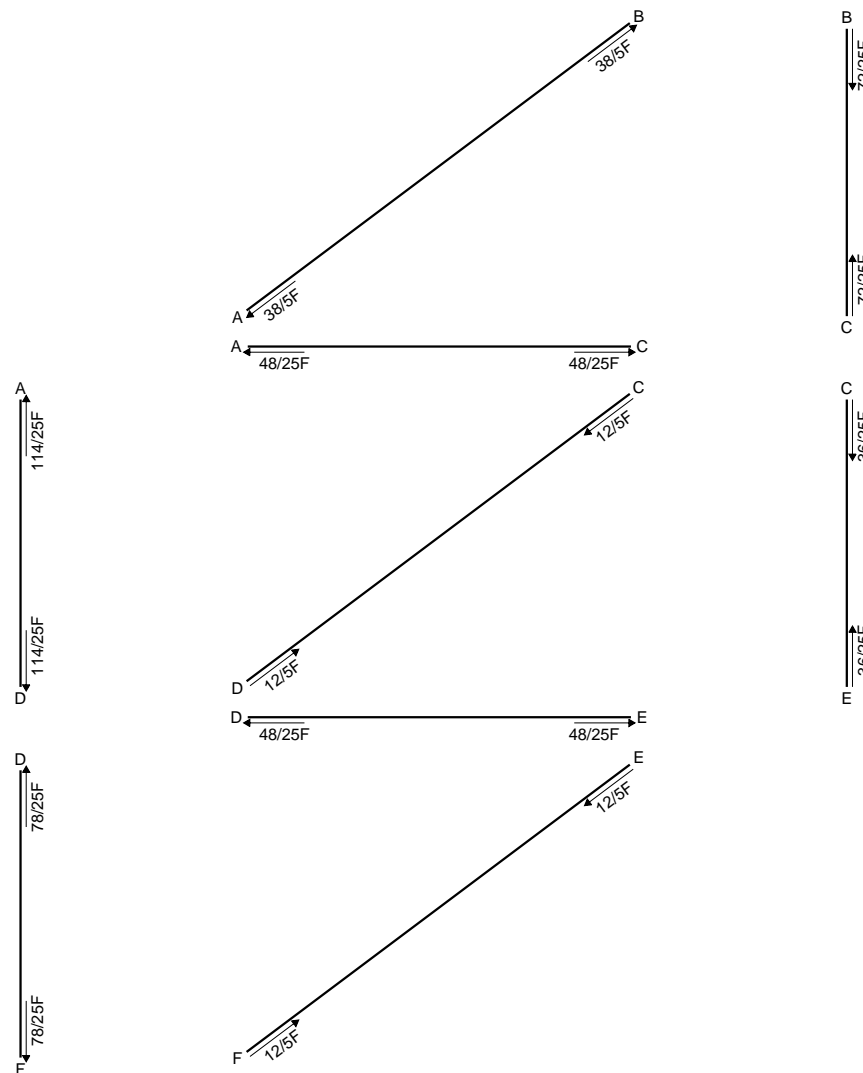
$$-3H_B b = 0$$

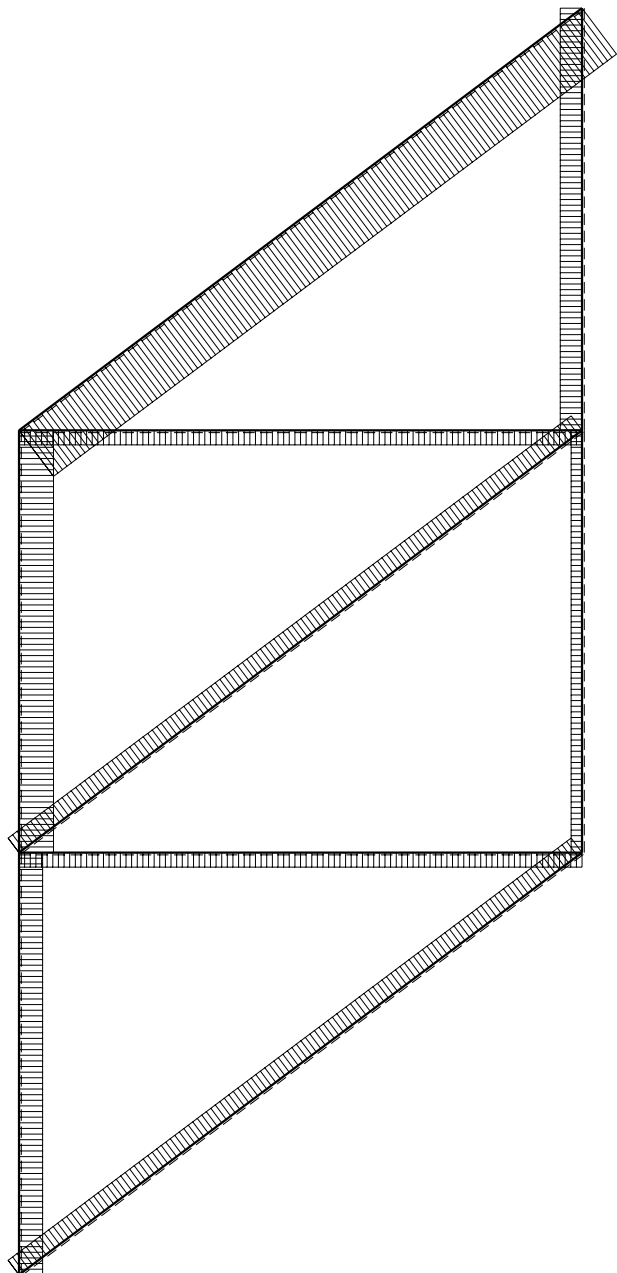
Matrice di equilibrio

$$\begin{bmatrix} \varphi_{FD} \\ \varphi_{DA} \\ \varphi_{DE} \\ \varphi_{EC} \\ \varphi_{CB} \end{bmatrix} \begin{bmatrix} H_B b & V_B b & H_{CA} b & H_{CD} b & H_{EF} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix} \begin{bmatrix} 24/5 & -48 \\ 12/5 & -24 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

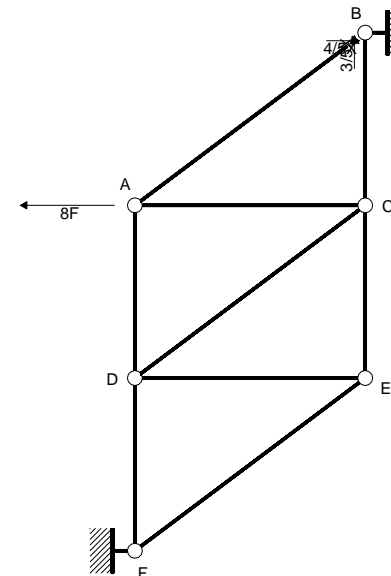
Soluzione del sistema

$$\begin{bmatrix} H_B b \\ H_{CA} b \\ V_B b \\ H_{CD} b \\ H_{EF} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \end{bmatrix} \begin{bmatrix} 0 & 0 \\ -4/5 & 8 \\ 6/5 & -12 \\ 4/5 & -8 \\ 4/5 & -8 \end{bmatrix}$$





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REAZIONI IPERSTATICHE

$$X = H_{BA}$$

CALCOLO DELLE REAZIONI IPERSTATICHE

$$L_{AB}^{xx} = N_{AB}^x N_{AB}^x I_{AB}/EA_{AB} = 1 \cdot 1 \cdot 5 \cdot 1/5 Fb/EA = Fb/EA$$

$$L_{CB}^{xx} = N_{CB}^x N_{CB}^x I_{CB}/EA_{CB} = 6/5 \cdot 6/5 \cdot 3 \cdot 1/4 Fb/EA = 27/25 Fb/EA$$

$$L_{AC}^{xx} = N_{AC}^x N_{AC}^x I_{AC}/EA_{AC} = -4/5 \cdot (-4/5) \cdot 4 \cdot 1/4 Fb/EA = 16/25 Fb/EA$$

$$L_{DA}^{xx} = N_{DA}^x N_{DA}^x I_{DA}/EA_{DA} = 3/5 \cdot 3/5 \cdot 3 \cdot 1/3 Fb/EA = 9/25 Fb/EA$$

$$L_{DC}^{xx} = N_{DC}^x N_{DC}^x I_{DC}/EA_{DC} = 1 \cdot 1 \cdot 5 \cdot 1/3 Fb/EA = 5/3 Fb/EA$$

$$L_{EC}^{xx} = N_{EC}^x N_{EC}^x I_{EC}/EA_{EC} = 3/5 \cdot 3/5 \cdot 3 \cdot 1/2 Fb/EA = 27/50 Fb/EA$$

$$L_{FE}^{xx} = N_{FE}^x N_{FE}^x I_{FE}/EA_{FE} = 1 \cdot 1 \cdot 5 \cdot 1/2 Fb/EA = 5/2 Fb/EA$$

$$L_{DE}^{xx} = N_{DE}^x N_{DE}^x I_{DE}/EA_{DE} = -4/5 \cdot (-4/5) \cdot 4 \cdot 1 Fb/EA = 64/25 Fb/EA$$

$$L_{FD}^{xx} = N_{FD}^x N_{FD}^x I_{FD}/EA_{FD} = 6/5 \cdot 6/5 \cdot 3 \cdot 1 Fb/EA = 108/25 Fb/EA$$

$$L_{CB}^{x_0} = N_{CB}^x N_{CB}^0 I_{CB}/EA_{CB} = 6/5 \quad (-12) \quad 3 \quad 1/4 \quad Fb/EA = -54/5 \quad Fb/EA$$

$$L_{AC}^{x_0} = N_{AC}^x N_{AC}^0 I_{AC}/EA_{AC} = -4/5 \quad 8 \quad 4 \quad 1/4 \quad Fb/EA = -32/5 \quad Fb/EA$$

$$L_{DC}^{x_0} = N_{DC}^x N_{DC}^0 I_{DC}/EA_{DC} = 1 \quad (-10) \quad 5 \quad 1/3 \quad Fb/EA = -50/3 \quad Fb/EA$$

$$L_{EC}^{x_0} = N_{EC}^x N_{EC}^0 I_{EC}/EA_{EC} = 3/5 \quad (-6) \quad 3 \quad 1/2 \quad Fb/EA = -27/5 \quad Fb/EA$$

$$L_{FE}^{x_0} = N_{FE}^x N_{FE}^0 I_{FE}/EA_{FE} = 1 \quad (-10) \quad 5 \quad 1/2 \quad Fb/EA = -25 \quad Fb/EA$$

$$L_{DE}^{x_0} = N_{DE}^x N_{DE}^0 I_{DE}/EA_{DE} = -4/5 \quad 8 \quad 4 \quad 1 \quad Fb/EA = -128/5 \quad Fb/EA$$

$$L_{FD}^{x_0} = N_{FD}^x N_{FD}^0 I_{FD}/EA_{FD} = 6/5 \quad (-6) \quad 3 \quad 1 \quad Fb/EA = -108/5 \quad Fb/EA$$

Contributi nulli elementi

$$L_{AB}^{x_0} \quad L_{DA}^{x_0}$$

Contributi nulli nodi vincolati

$$L_B^{xx} \quad L_F^{xx} \quad L_B^{x_0} \quad L_F^{x_0}$$

Espressione risolvante

$$\left(L_{AB}^{xx} + L_{CB}^{xx} + L_{AC}^{xx} + L_{DA}^{xx} + L_{DC}^{xx} + L_{EC}^{xx} + L_{FE}^{xx} + L_{DE}^{xx} + L_{FD}^{xx} \right) X = - \left(L_{CB}^{x_0} + L_{AC}^{x_0} + L_{DC}^{x_0} + L_{EC}^{x_0} + L_{FE}^{x_0} + L_{DE}^{x_0} + L_{FD}^{x_0} \right)$$

$$\left(1 + 27/25 + 16/25 + 9/25 + 5/3 + 27/50 + 5/2 + 64/25 + 108/25 \right) X = \left(54/5 + 32/5 + 50/3 + 27/5 + 25 + 128/5 + 108/5 \right) F$$

$$44/3 X = 1672/15 F$$

Soluzione

$$X = 152/25 F$$

REAZIONI

$$H_B = 152/25F \quad V_B = 42/25F \quad H_F = 48/25F \quad V_F = -42/25F$$

$$N_{AB} = 38/5F \quad N_{CB} = -72/25F \quad N_{AC} = 48/25F \quad N_{DA} = 114/25F \quad N_{DC} = -12/5F \quad N_{EC} = -36/25F$$

$$N_{FE} = -12/5F \quad N_{DE} = 48/25F \quad N_{FD} = 78/25F$$

SPOSTAMENTI NODALI

$$u_A = -997/50(Fb/EA)$$

$$u_B = 0$$

$$u_C = -901/50(Fb/EA)$$

$$u_D = -921/50(Fb/EA)$$

$$v_A = 348/25(Fb/EA)$$

$$v_B = 0$$

$$v_C = 54/25(Fb/EA)$$

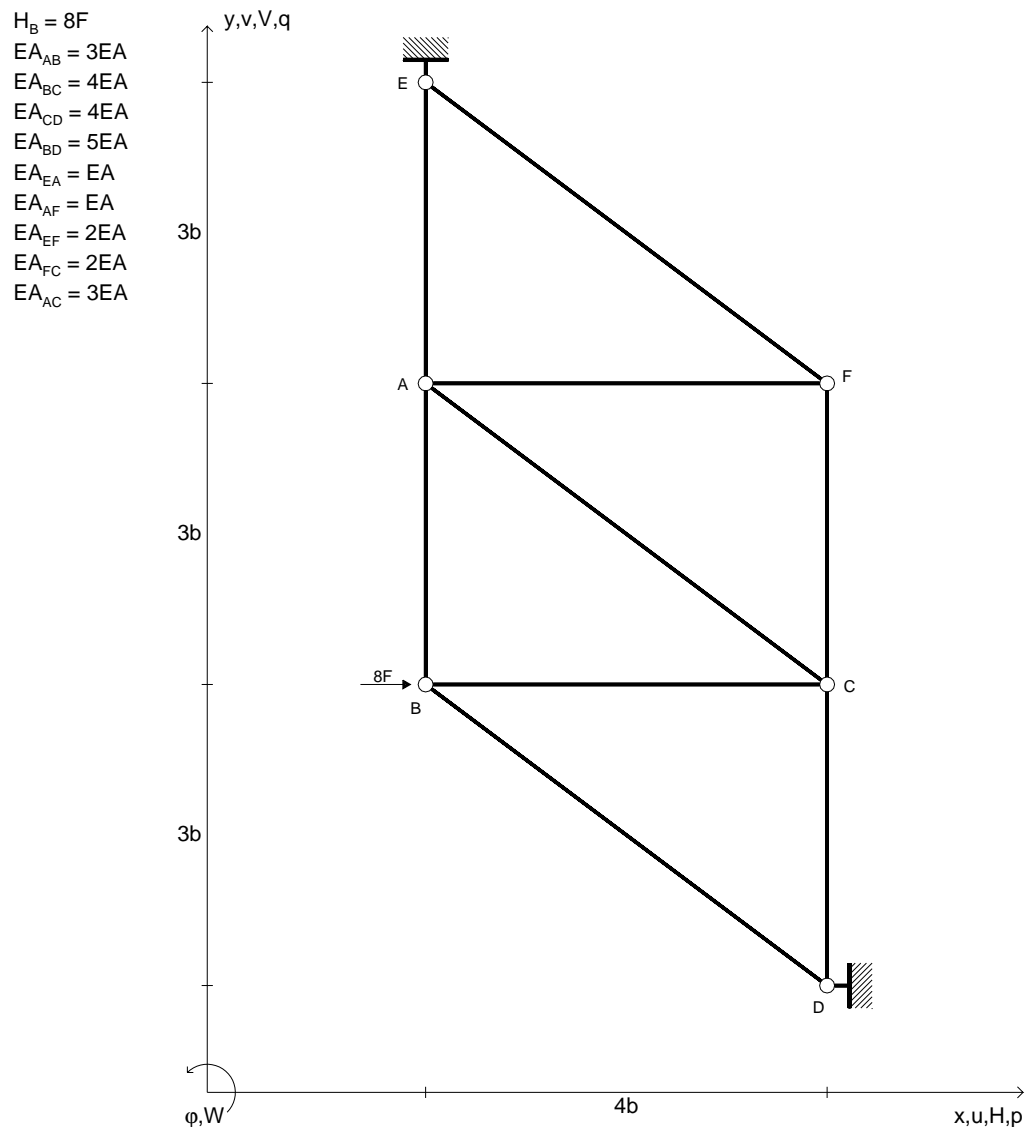
$$v_D = 234/25(Fb/EA)$$

$$u_E = -537/50(Fb/EA)$$

$$u_F = 0$$

$$v_E = 108/25(Fb/EA)$$

$$v_F = 0$$



Svolgere l'analisi cinematica.

Riportare la soluzione su questo foglio.

Carichi e deformazioni date hanno verso efficace in disegno.

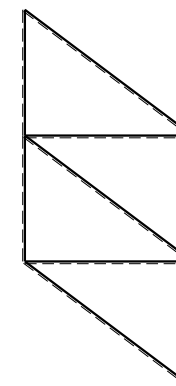
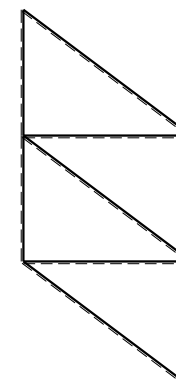
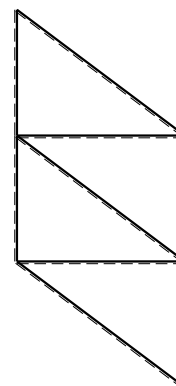
Calcolare reazioni vincolari della struttura e delle aste.

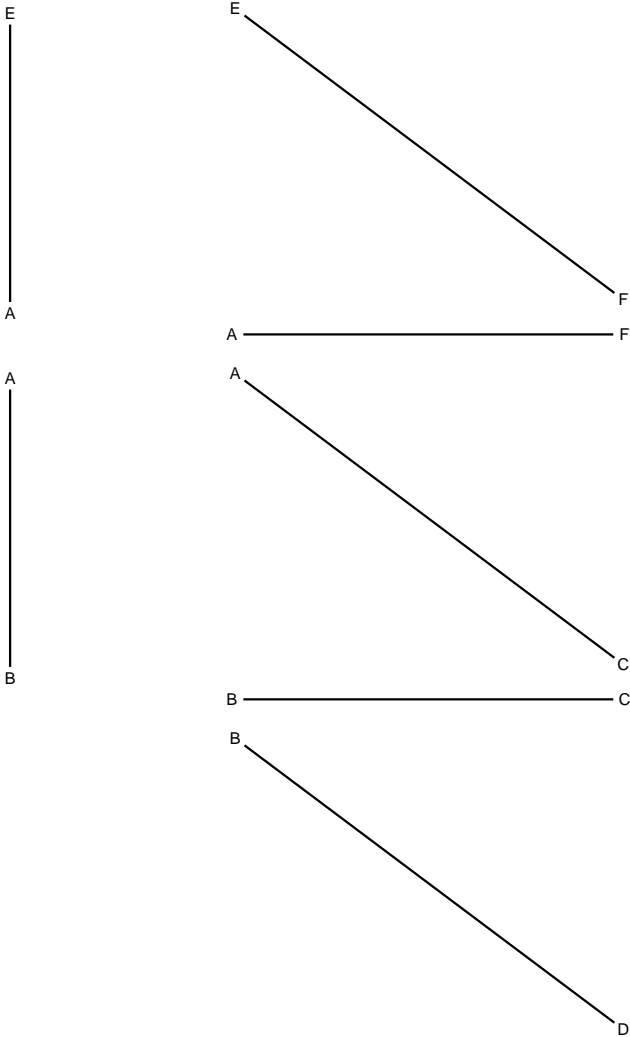
Tracciare i diagrammi delle azioni interne nelle aste.

Calcolare spostamento e rotazione di tutti i nodi.

$A_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

@ Adolfo Zavelani Rossi, Politecnico di Milano



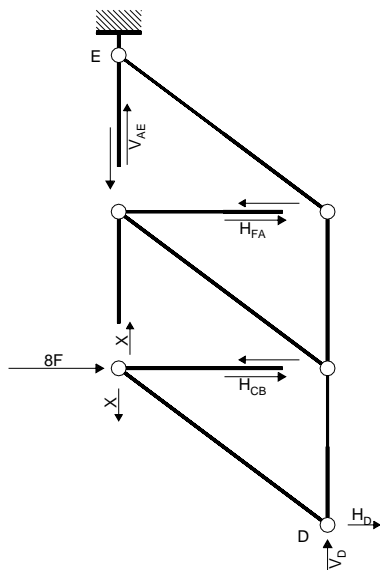


REAZIONI

$H_D =$	$V_D =$	$H_E =$	$V_E =$	
$N_{AB} =$	$N_{BC} =$	$N_{CD} =$	$N_{BD} =$	$N_{EA} =$
$N_{AF} =$	$N_{EF} =$	$N_{FC} =$	$N_{AC} =$	

SPOSTAMENTI NODALI

$u_A =$	$u_B =$	$u_C =$	$u_D =$
$v_A =$	$v_B =$	$v_C =$	$v_D =$
$u_E =$	$u_F =$		
$v_E =$	$v_F =$		



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a E: aste EF FC CD CA AB DB AF BC

$$9H_D b + 4V_D b = -48Fb$$

Rotazione intorno a F: aste FC CD CA AB DB AF BC

$$6H_D b + 4V_{AE} b = -24Fb$$

Rotazione intorno a C: aste CD DB BC

$$3H_D b = -4Xb$$

Rotazione intorno a C: aste CA AB AF

$$4V_{AE} b - 3H_{FA} b = 4Xb$$

Rotazione intorno a D: aste DB BC

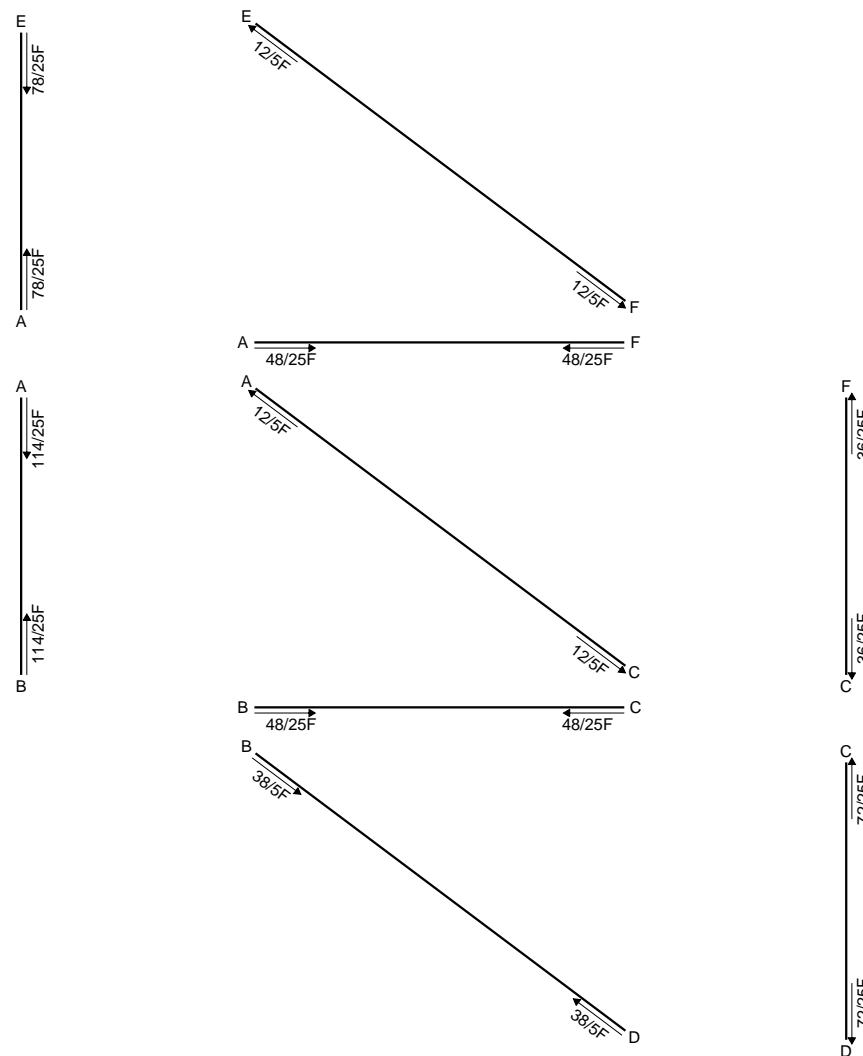
$$-3H_{CB} b = -4Xb + 24Fb$$

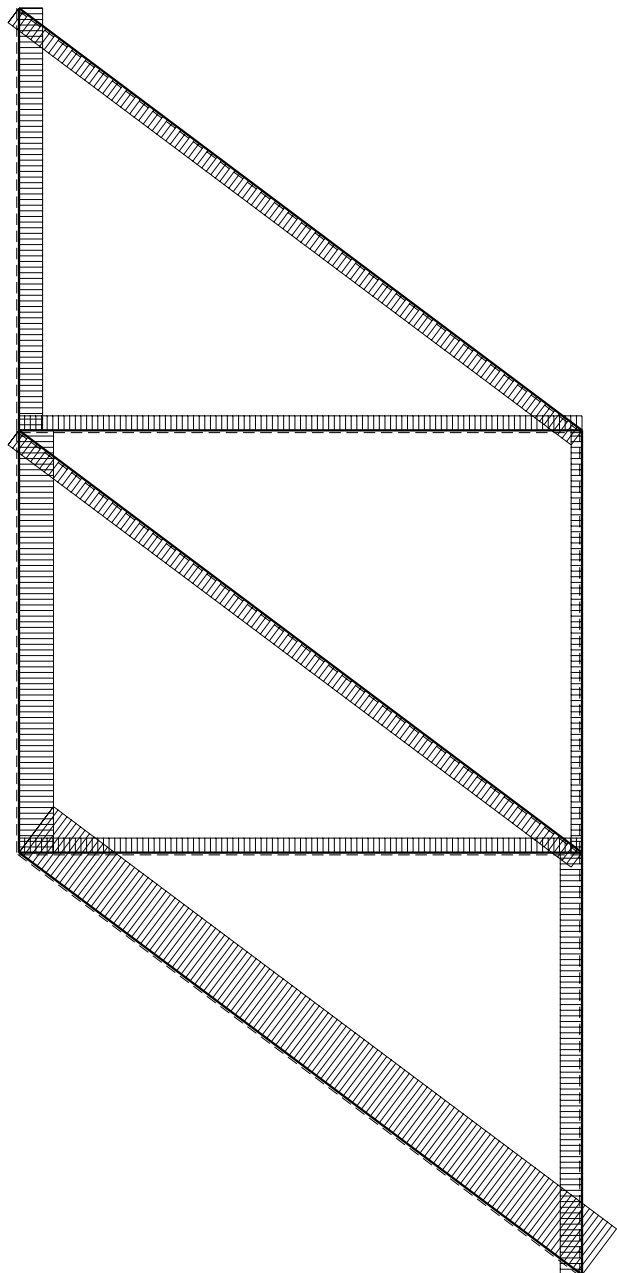
Matrice di equilibrio

$$\begin{bmatrix} \varphi_{EF} \\ \varphi_{FC} \\ \varphi_{CD} \\ \varphi_{CA} \\ \varphi_{DB} \end{bmatrix} \begin{bmatrix} H_D b & V_D b & H_{CB} b & V_{AE} b & H_{FA} b \\ 9 & 4 & 0 & 0 & 0 \\ 6 & 0 & 0 & 4 & 0 \\ 3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 4 & -3 \\ 0 & 0 & -3 & 0 & 0 \end{bmatrix} = \begin{bmatrix} Xb & Fb \\ 0 & -48 \\ 0 & -24 \\ -4 & 0 \\ 4 & 0 \\ -4 & 24 \end{bmatrix}$$

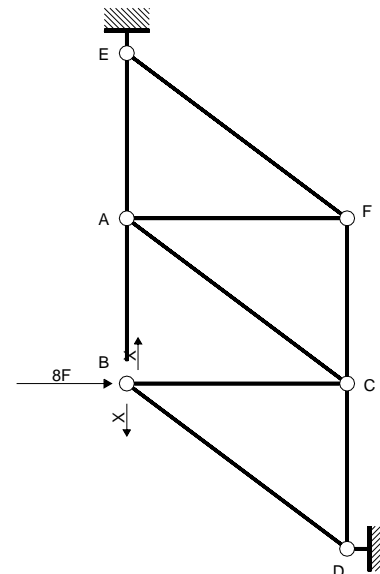
Soluzione del sistema

$$\begin{bmatrix} H_D b \\ V_D b \\ V_{AE} b \\ H_{FA} b \\ H_{CB} b \end{bmatrix} = \begin{bmatrix} Xb & Fb \\ -4/3 & 0 \\ 3 & -12 \\ 2 & -6 \\ 4/3 & -8 \end{bmatrix}$$





← ⊕ → | 10 F



REAZIONI IPERSTATICHE

$$X = V_{BA}$$

CALCOLO DELLE REAZIONI IPERSTATICHE

$$L_{AB}^{xx} = N_{AB}^x N_{AB}^x I_{AB}/EA_{AB} = -1 \cdot (-1) \cdot 3 \cdot 1/3 Fb/EA = Fb/EA$$

$$L_{BC}^{xx} = N_{BC}^x N_{BC}^x I_{BC}/EA_{BC} = 4/3 \cdot 4/3 \cdot 4 \cdot 1/4 Fb/EA = 16/9 Fb/EA$$

$$L_{CD}^{xx} = N_{CD}^x N_{CD}^x I_{CD}/EA_{CD} = -2 \cdot (-2) \cdot 3 \cdot 1/4 Fb/EA = 3 Fb/EA$$

$$L_{BD}^{xx} = N_{BD}^x N_{BD}^x I_{BD}/EA_{BD} = -5/3 \cdot (-5/3) \cdot 5 \cdot 1/5 Fb/EA = 25/9 Fb/EA$$

$$L_{EA}^{xx} = N_{EA}^x N_{EA}^x I_{EA}/EA_{EA} = -2 \cdot (-2) \cdot 3 \cdot 1 Fb/EA = 12 Fb/EA$$

$$L_{AF}^{xx} = N_{AF}^x N_{AF}^x I_{AF}/EA_{AF} = 4/3 \cdot 4/3 \cdot 4 \cdot 1 Fb/EA = 64/9 Fb/EA$$

$$L_{EF}^{xx} = N_{EF}^x N_{EF}^x I_{EF}/EA_{EF} = -5/3 \cdot (-5/3) \cdot 5 \cdot 1/2 Fb/EA = 125/18 Fb/EA$$

$$L_{FC}^{xx} = N_{FC}^x N_{FC}^x I_{FC}/EA_{FC} = -1 \cdot (-1) \cdot 3 \cdot 1/2 Fb/EA = 3/2 Fb/EA$$

$$L_{AC}^{xx} = N_{AC}^x N_{AC}^x I_{AC}/EA_{AC} = -5/3 \cdot (-5/3) \cdot 5 \cdot 1/3 Fb/EA = 125/27 Fb/EA$$

$$L_{BC}^{x_0} = N_{BC}^x N_{BC}^0 I_{BC}/EA_{BC} = 4/3 \quad (-8) \quad 4 \quad 1/4 \quad Fb/EA = -32/3 \quad Fb/EA$$

$$L_{CD}^{x_0} = N_{CD}^x N_{CD}^0 I_{CD}/EA_{CD} = -2 \quad 12 \quad 3 \quad 1/4 \quad Fb/EA = -18 \quad Fb/EA$$

$$L_{EA}^{x_0} = N_{EA}^x N_{EA}^0 I_{EA}/EA_{EA} = -2 \quad 6 \quad 3 \quad 1 \quad Fb/EA = -36 \quad Fb/EA$$

$$L_{AF}^{x_0} = N_{AF}^x N_{AF}^0 I_{AF}/EA_{AF} = 4/3 \quad (-8) \quad 4 \quad 1 \quad Fb/EA = -128/3 \quad Fb/EA$$

$$L_{EF}^{x_0} = N_{EF}^x N_{EF}^0 I_{EF}/EA_{EF} = -5/3 \quad 10 \quad 5 \quad 1/2 \quad Fb/EA = -125/3 \quad Fb/EA$$

$$L_{FC}^{x_0} = N_{FC}^x N_{FC}^0 I_{FC}/EA_{FC} = -1 \quad 6 \quad 3 \quad 1/2 \quad Fb/EA = -9 \quad Fb/EA$$

$$L_{AC}^{x_0} = N_{AC}^x N_{AC}^0 I_{AC}/EA_{AC} = -5/3 \quad 10 \quad 5 \quad 1/3 \quad Fb/EA = -250/9 \quad Fb/EA$$

Contributi nulli elementi

$$L_{AB}^{x_0} \quad L_{BD}^{x_0}$$

Contributi nulli nodi vincolati

$$L_D^{xx} \quad L_E^{xx} \quad L_D^{x_0} \quad L_E^{x_0}$$

Espressione risolvante

$$\left(L_{AB}^{xx} + L_{BC}^{xx} + L_{CD}^{xx} + L_{BD}^{xx} + L_{EA}^{xx} + L_{AF}^{xx} + L_{EF}^{xx} + L_{FC}^{xx} + L_{AC}^{xx} \right) X = - \left(L_{BC}^{x_0} + L_{CD}^{x_0} + L_{EA}^{x_0} + L_{AF}^{x_0} + L_{EF}^{x_0} + L_{FC}^{x_0} + L_{AC}^{x_0} \right)$$

$$\left(1 + 16/9 + 3 + 25/9 + 12 + 64/9 + 125/18 + 3/2 + 125/27 \right) X = \left(32/3 + 18 + 36 + 128/3 + 125/3 + 9 + 250/9 \right) F$$

$$1100/27 X = 1672/9 F$$

Soluzione

$$X = 114/25 F$$

REAZIONI

$$H_D = -152/25F \quad V_D = 42/25F \quad H_E = -48/25F \quad V_E = -42/25F$$

$$N_{AB} = -114/25F \quad N_{BC} = -48/25F \quad N_{CD} = 72/25F \quad N_{BD} = -38/5F \quad N_{EA} = -78/25F$$

$$N_{AF} = -48/25F \quad N_{EF} = 12/5F \quad N_{FC} = 36/25F \quad N_{AC} = 12/5F$$

SPOSTAMENTI NODALI

$$u_A = 921/50(Fb/EA) \quad u_B = 997/50(Fb/EA) \quad u_C = 901/50(Fb/EA) \quad u_D = 0$$

$$v_A = 234/25(Fb/EA) \quad v_B = 348/25(Fb/EA) \quad v_C = 54/25(Fb/EA) \quad v_D = 0$$

$$u_E = 0 \quad u_F = 537/50(Fb/EA)$$

$$v_E = 0 \quad v_F = 108/25(Fb/EA)$$

