

# lab2

November 6, 2019

1 №2 “ . ”

Python c Jupyter Notebook - lab2.py.  
jupyter notebook - lab2.ipynb

ex2data1.txt , (

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ex2data2.txt , ( )

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20x20 . ( ).

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9 ( 1 9), 10 ( 0).

## 1.1

1.1.1 ex2data1.txt .

```
[1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

```
[57]: data_row1 = np.genfromtxt('ex2data1.txt', delimiter=',')
data1 = pd.DataFrame(data_row1, columns=list(['grade1', 'grade2', 'isAdmitted']))
data1.describe()
```

```
[57]:
```

	grade1	grade2	isAdmitted
count	100.000000	100.000000	100.000000
mean	65.644274	66.221998	0.600000
std	19.458222	18.582783	0.492366
min	30.058822	30.603263	0.000000
25%	50.919511	48.179205	0.000000
50%	67.032988	67.682381	1.000000
75%	80.212529	79.360605	1.000000
max	99.827858	98.869436	1.000000

### 1.1.2

```
[29]: plt.figure()
ax = data1.loc[data1.isAdmitted == 1].plot(x='grade1', y='grade2', style=['+'],
      ↪label='admitted')
data1.loc[data1.isAdmitted == 0].plot(x='grade1', y='grade2', style=['o'],
      ↪label='not admitted', ax=ax)
ax.set_ylabel('Exam 2 score')
ax.set_xlabel('Exam 1 score')
plt.show()
```

<Figure size 432x288 with 0 Axes>

```
[14]: plot_data = data1.loc[data1.isPassed == 1]['grade1'].append(data1.loc[data1.
      ↪isPassed == 1]['grade2'])
plot_data.describe()
```

```
[14]: count    120.000000
mean       74.337662
std        15.411800
min        40.457551
25%        64.142572
50%        75.369994
```

```

75%      87.183031
max      99.827858
dtype: float64

```

### 1.1.3 $J()$

```

[52]: def sigmoid(X):
      return 1/(1+np.exp(-X))

```

```

[59]: def costFunction(theta, X, y):
      m = y.size
      h = sigmoid(X @ theta)
      J = (-1 / m) * ((y.T @ np.log(h)) + ((1-y).T @ np.log(1-h)))
      error = h - y
      grad = (1 / m) * (X.T @ error)
      return J, grad

```

```

[60]: m, n = data1.shape
      X = data1[['grade1', 'grade2']]
      X.insert(0, 'theta_0', 1)
      X = X.to_numpy()
      y = data1['isAdmitted']
      initial_theta = np.zeros(n)
      cost, grad = costFunction(initial_theta, X, y)
      print(f'Cost at initial theta (zeros): {cost}')
      print(f'Gradient at initial theta (zeros): {grad} \n')

```

```

Cost at initial theta (zeros): 0.6931471805599452
Gradient at initial theta (zeros): [ -0.1      -12.00921659 -11.26284221]

```

### 1.1.4 $\frac{1}{m} \sum_{i=1}^m \left( \frac{1}{2} \left( \frac{\partial}{\partial \theta_0} \right)^2 + \left( \frac{\partial}{\partial \theta_1} \right)^2 \right)$

```

[146]: import scipy.optimize as opt

      def costOptimize(theta, X, y):
          cost, _ = costFunction(theta, X, y)
          return cost

      def gradientOptimize(theta, X, y):
          _, grad = costFunction(theta, X, y)
          return grad

      def optimize(func, gradient, X, y, method):
          n = y.shape[1]

```

```

initial_theta = np.zeros(n)
result = opt.minimize(fun = func, x0 = initial_theta, args = (X, y), method_
↪= method, jac = gradient)
theta = result.x
cost = func(theta, X, y)
print(f'Cost at theta found : {cost}')
print(f'theta: {theta}')
return result

```

### Optimization using gradient information in a truncated Newton algorithm

```
[78]: optimize(costOptimize, gradientOptimize, X, y, 'TNC')
```

```

Cost at theta found : 0.2034977015894746
theta: [-25.16131861  0.20623159  0.20147149]

```

```

[78]:      fun: 0.2034977015894746
      jac: array([8.98032450e-09, 8.46951977e-08, 4.76544166e-07])
      message: 'Local minimum reached (|pg| ~= 0)'
      nfev: 36
      nit: 17
      status: 0
      success: True
      x: array([-25.16131861,  0.20623159,  0.20147149])

```

### Unconstrained minimization of a function using the Newton-CG method

```
[84]: result = optimize(costOptimize, gradientOptimize, X, y, 'Newton-CG')
result
```

```

Cost at theta found : 0.20349771001679343
theta: [-25.15380655  0.20617146  0.20141074]

```

```

[84]:      fun: 0.20349771001679343
      jac: array([1.40815808e-05, 7.48488706e-04, 7.23594998e-04])
      message: 'Optimization terminated successfully.'
      nfev: 64
      nhev: 0
      nit: 26
      njev: 217
      status: 0
      success: True
      x: array([-25.15380655,  0.20617146,  0.20141074])

```

### 1.1.5

```
[95]: def predict(theta, X):  
        predict = sigmoid(np.dot(X, theta))  
        return predict > 0.5  
  
theta = result.x  
prob = sigmoid(np.array([1, 45, 85]) @ theta)  
print(f'For a student with scores 45 and 85, we predict an admission_  
      ↪probability of {prob}')
```

For a student with scores 45 and 85, we predict an admission probability of 0.7762286402437759

```
[98]: p = predict(np.array(theta), X)  
print('Train Accuracy: %f' % ((y[p == y].size / float(y.size)) * 100.0))
```

Train Accuracy: 89.000000

### 1.1.6

2.

```
[99]: plt.figure()  
ax = data1.loc[data1.isAdmitted == 1].plot(x='grade1', y='grade2', style=['+'],  
      ↪label='admitted')  
data1.loc[data1.isAdmitted == 0].plot(x='grade1', y='grade2', style=['o'],  
      ↪label='not admitted', ax=ax)  
ax.set_ylabel('Exam 2 score')  
ax.set_xlabel('Exam 1 score')  
slope = -(theta[1] / theta[2])  
intercept = -(theta[0] / theta[2])  
x_vals = np.array(ax.get_xlim())  
y_vals = intercept + (slope * x_vals)  
plt.plot(x_vals, y_vals, c="k");  
plt.show()
```

<Figure size 432x288 with 0 Axes>

### 1.1.7 ex2data2.txt .

```
[188]: data_row2 = np.genfromtxt('ex2data2.txt', delimiter=',')
data2 = pd.DataFrame(data_row2, columns=list(['test1', 'test2', 'accepted']))
data2.describe()
```

```
[188]:
```

	test1	test2	accepted
count	118.000000	118.000000	118.000000
mean	0.054779	0.183102	0.491525
std	0.496654	0.519743	0.502060
min	-0.830070	-0.769740	0.000000
25%	-0.372120	-0.254385	0.000000
50%	-0.006336	0.213455	0.000000
75%	0.478970	0.646563	1.000000
max	1.070900	1.108900	1.000000

### 1.1.8 , , .

```
[189]: plt.figure()
ax = data2.loc[data2.accepted == 1].plot(x='test1', y='test2', style=['+'],
    ↳label='accepted')
data2.loc[data2.accepted == 0].plot(x='test1', y='test2', style=['o'],
    ↳label='rejected', ax=ax)
```

```
ax.set_ylabel('Test 2')
ax.set_xlabel('Test 1')
plt.show()
```

<Figure size 432x288 with 0 Axes>

1.1.9  $x_1$  ( )  $x_2$  ( ),  
6, ... 1,  $x_1$ ,  $x_2$ ,  $x_1^2$ ,  $x_1x_2$ ,  $x_2^2$ , ...,  $x_1x_2^5$ ,  $x_2^6$  ( 28 ).

```
[108]: def map_feature(x1, x2):
        """
        Maps the two input features to quadratic features.
        Returns a new feature array with more features, comprising of
        X1, X2, X1 ** 2, X2 ** 2, X1*X2, X1*X2 ** 2, etc...
        Inputs X1, X2 must be the same size
        """
        x1.shape = (x1.size, 1)
        x2.shape = (x2.size, 1)
        degree = 6
        out = np.ones(shape=(x1[:, 0].size, 1))

        m, n = out.shape

        for i in range(1, degree + 1):
```

```

        for j in range(i + 1):
            r = (x1 ** (i - j)) * (x2 ** j)
            out = np.append(out, r, axis=1)

    return out

mapped = map_feature(data2['test1'].to_numpy(), data2['test2'].to_numpy())

```

[108]: (118, 28)

### 1.1.10 L2-

```

[224]: def cost_function_reg(theta, X, y, l):
    '''Compute the cost and partial derivatives as grads'''

    h = sigmoid(X.dot(theta))

    thetaR = theta[1:, 0]

    J = (-1.0 / m) * ((y.T @ np.log(h)) + ((1 - y.T) @ np.log(1.0 - h))) + (1 /
    ↪(2.0 * m)) * (thetaR.T @ thetaR)

    y.shape = h.shape
    delta = h - y
    sumdelta = delta.T @ X[:, 1]
    grad1 = (1.0 / m) * sumdelta

    XR = X[:, 1:X.shape[1]]
    sumdelta = delta.T @ XR

    grad = (1.0 / m) * (sumdelta + l * thetaR)

    out = np.zeros(shape=(grad.shape[0], grad.shape[1] + 1))

    out[:, 0] = grad1
    out[:, 1:] = grad

    return J.flatten(), out.T.flatten()

def gradient_descent(X, y, theta, l, alpha, num_iters):
    m = y.shape[0] # Size of training set
    j_history = []
    for i in range(0, num_iters):
        cost, grad = cost_function_reg(theta, X, y, l)
        grad.shape = theta.shape
        theta -= alpha * grad

```



```

        j_history.append(cost)

    return theta, j_history

m, n = data2.shape
y = data2['accepted'].to_numpy()
y.shape = (m, 1)
initial_theta = np.zeros(shape=(mapped.shape[1], 1))
#Set regularization parameter lambda to 1
l = 1
gd_theta, costs = gradient_descent(mapped, y, initial_theta, l, 0.2, 400)

```

### 1.1.11

```

[184]: def cost_decorator(theta, X, y):
        theta.shape = (mapped.shape[1], 1)
        cost, _ = cost_function_reg(theta, X, y, l)
        theta.shape = (mapped.shape[1],)
        return cost

    def gradient_decorator(theta, X, y):
        theta.shape = (mapped.shape[1], 1)
        _, grad = cost_function_reg(theta, X, y, l)
        theta.shape = (mapped.shape[1],)
        return grad

    initial_theta = np.zeros((mapped.shape[1],))
    result = opt.minimize(fun=cost_decorator, x0=initial_theta, args=(mapped, y),
        ↪method='BFGS', jac=gradient_decorator)
    bfgs_theta = result.x

```

### 1.1.12

```

[185]: p = predict(np.array(gd_theta), mapped)
    print('Train Accuracy with gradient descent: %f' % ((y[p == y].size / float(y.
        ↪size)) * 100.0))
    p = predict(np.array(bfgs_theta), mapped)
    p.shape = y.shape
    print('Train Accuracy using the BFGS algorithm: %f' % ((y[p == y].size /
        ↪float(y.size)) * 100.0))

```

Train Accuracy with gradient descent: 80.508475  
 Train Accuracy using the BFGS algorithm: 83.898305

```
[195]: u = np.linspace(-1, 1.5, 50)
v = np.linspace(-1, 1.5, 50)
z = np.zeros(shape=(len(u), len(v)))
for i in range(len(u)):
    for j in range(len(v)):
        z[i, j] = (map_feature(np.array(u[i]), np.array(v[j]))).dot(np.
        ↪array(bfgs_theta))

z = z.T
plt.figure()
ax = data2.loc[data2.accepted == 1].plot(x='test1', y='test2', style=['+'],
    ↪label='accepted')
data2.loc[data2.accepted == 0].plot(x='test1', y='test2', style=['o'],
    ↪label='rejected', ax=ax)
ax.contour(u, v, z)
ax.set_ylabel('Test 2')
ax.set_xlabel('Test 1')
plt.show()
```

<Figure size 432x288 with 0 Axes>

```
[217]: def train_with_plot(l):

    def plot(theta):
        u = np.linspace(-1, 1.5, 50)
        v = np.linspace(-1, 1.5, 50)
        z = np.zeros(shape=(len(u), len(v)))
        for i in range(len(u)):
            for j in range(len(v)):
                z[i, j] = (map_feature(np.array(u[i]), np.array(v[j])).dot(np.
→array(theta)))

        z = z.T
        plt.figure()
        ax = data2.loc[data2.accepted == 1].plot(x='test1', y='test2',
→style=['+'], label='accepted')
        data2.loc[data2.accepted == 0].plot(x='test1', y='test2', style=['o'],
→label='rejected', ax=ax)
        ax.contour(u, v, z)
        ax.set_ylabel('Test 2')
        ax.set_xlabel('Test 1')
        plt.title(f'lambda = {l}')
        plt.show()

    initial_theta = np.zeros(shape=(mapped.shape[1], 1))
    theta, _ = gradient_descent(mapped, y, initial_theta, 1, 0.2, 1000)
    data2 = pd.DataFrame(data_row2, columns=list(['test1', 'test2',
→'accepted']))

    plot(theta)

train_with_plot(0)
```

<Figure size 432x288 with 0 Axes>

```
[200]: train_with_plot(100)
```

```
<Figure size 432x288 with 0 Axes>
```

1.1.15                    ex2data3.mat                    .

```
[225]: import scipy.io

data3 = scipy.io.loadmat('ex2data3.mat')
x = np.array(data3['X'])
y = np.squeeze(data3['y'])
np.place(y, y == 10, 0)
n = x.shape[1]
m = x.shape[0]
labels_count = 10
```

1.1.16                    .                    .

```
[221]: import matplotlib.image as mpimg

subplots = 64
draw_seed = np.random.randint(low=0, high=x.shape[0], size=subplots)
draw_rows = x[draw_seed]
fig, ax = plt.subplots(8, 8, figsize=(8, 8))
for i, axi in enumerate(ax.flat):
    data = np.reshape(draw_rows[i], (20, 20))
    axi.imshow(data, cmap='binary')
```

```
axi.set(xticks=[], yticks=[])
plt.show()
```

1.1.17 ).

1.1.18 L2- .

1.1.19 “ ”.

```
[230]: X = np.ones(shape=(x.shape[0], x.shape[1] + 1))
X[:, 1:] = x
classifiers = np.zeros(shape=(labels_count, n + 1))
```

```

for i in range(0, labels_count):
    label = (y == i).astype(int)
    initial_theta = np.zeros(shape=(X.shape[1], 1))
    theta, costs = gradient_descent(X, label, initial_theta, 0.4, 2.8, 10000)
    classifiers[i, :] = np.squeeze(theta)

```

### 1.1.20

```

[227]: def predict_class(input, classifiers):
        class_probs = sigmoid(input @ classifiers.transpose())
        if len(class_probs.shape) == 1:
            class_probs.shape = (1, class_probs.shape[0])
        predictions = class_probs.argmax(axis=1)
        return predictions

```

### 1.1.21

95%.

```

[229]: predictions = predict_class(X, classifiers)
        print(f'Training accuracy: {str(100 * np.mean(predictions == y))}')

```

Training accuracy: 94.74000000000001

## 1.2

, L2-  
“  
”.

```

[231]: import os
        print(os.environ['PATH'])

```

/opt/miniconda3/bin:/opt/miniconda3/condabin:/Users/stunba/bin:/usr/local/bin:/usr/local/bin:/usr/bin:/bin:/usr/sbin:/sbin:/Users/stunba/anaconda/bin

[ ]: