hw1 F24 Solution SYW

September 26, 2024

24Fall Advanced Control for Robotics

Homework 1

Name: Siyuan Wang SID: 12443028

Problem 1 - Python Basics

• a.

```
[1]: from datetime import datetime
now = datetime.now()
print("current date and time: ", now)
```

current date and time: 2024-09-26 01:45:28.155770

• b.

```
[2]: simple_list = ['aa', 'bb', 'cc', 'dd', 'ee', 'ff', 'gg']
  remove_index = [0, 4, 5]

for i in reversed(remove_index):
     simple_list.pop(i)

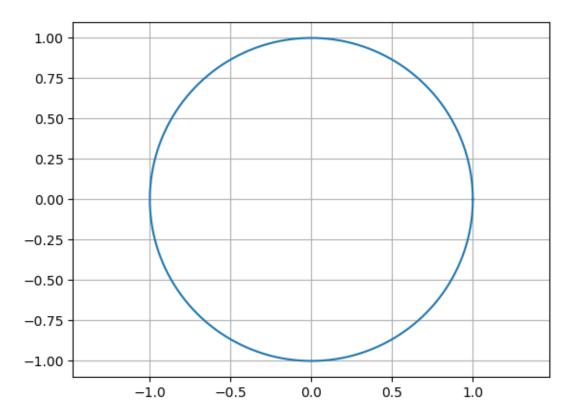
simple_list
```

- [2]: ['bb', 'cc', 'dd', 'gg']
 - c.

```
[3]: class Student():
    def __init__(self, name, age):
        self.name = name
        self.age = age
    def print_info(self):
        print("Student Name: {}".format(self.name))
        print("Student Age: {}".format(self.age))
weizhang = Student(name='weizhang', age=18)
```

```
weizhang.print_info()
    Student Name: weizhang
    Student Age: 18
    Problem 2 - Linear Algebra
          a.
[4]: import numpy as np
     A = np.array([
         [1, -2, 4],
         [1, -1, 1],
         [1, 0, 0],
         [1, 1, 1]
     ])
     B = np.array([
         [1, 2, 3],
         [1, 2, 3],
         [1, 2, 3],
         [1, 2, 3],
    ])
     A, B
[4]: (array([[ 1, -2, 4],
             [1, -1, 1],
             [1, 0, 0],
             [1, 1, 1]]),
      array([[1, 2, 3],
             [1, 2, 3],
             [1, 2, 3],
             [1, 2, 3]]))
          b.
[5]: print("The second row of A:", A[1, :])
     print("The second row of B:", B[:, 2])
    The second row of A: [1 -1 1]
    The second row of B: [3 3 3 3]
           c.
[6]: print("A + B = \n", A+B)
     print("A - B = \n", A-B)
    A + B =
     [[2 0 7]
```

```
[2 1 4]
     [2 2 3]
     [2 3 4]]
    A - B =
    [[0-41]
     [ 0 -3 -2]
     [0 -2 -3]
     [ 0 -1 -2]]
      • d.
[7]: res = np.concatenate((A, B), axis=1)
    res
[7]: array([[ 1, -2, 4, 1, 2, 3],
           [ 1, -1, 1, 1, 2,
                                3],
           [1, 0, 0, 1, 2, 3],
           [1, 1, 1, 1, 2, 3]])
      • e.
[8]: A.transpose() @ B
[8]: array([[ 4, 8, 12],
           [-2, -4, -6],
           [ 6, 12, 18]])
    Problem 3 - Matplotlib
      • a.
[9]: import matplotlib.pyplot as plt
    def plot_unit_circle():
        p = np.linspace(0, 2*np.pi, 1000)
        x = np.cos(p)
        y = np.sin(p)
        plt.plot(x, y)
        plt.axis('equal')
        plt.grid()
    plot_unit_circle()
```



• b.

```
plot_unit_circle()

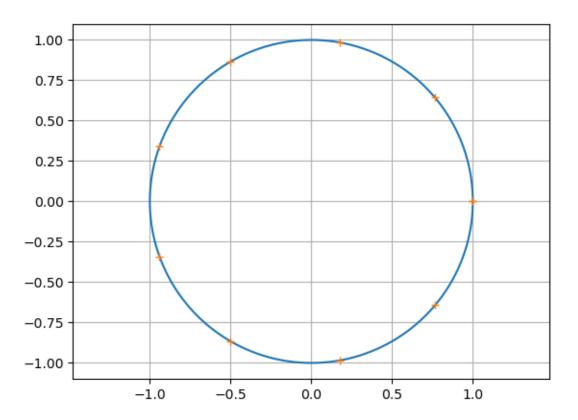
plus_signs = np.linspace(0, 2*np.pi, 10)

x_plus_signs = np.cos(plus_signs)

y_plus_signs = np.sin(plus_signs)

plt.plot(x_plus_signs, y_plus_signs, '+')
```

[10]: [<matplotlib.lines.Line2D at 0x7faa2f6677c0>]



Problem 7 - Ellipsoids

• 3.

```
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.patches import Ellipse

def draw_ellipse(center, major_axis, minor_axis, a, b, fig_padding=1):
    #
    center_x, center_y = center

#
    major_axis_dx, major_axis_dy = major_axis
    minor_axis_dx, minor_axis_dy = minor_axis

#
    angle = np.degrees(np.arctan2(major_axis_dy, major_axis_dx))

#
    ellipse = Ellipse(xy=(center_x, center_y), width=2*a, height=2*b, uplangle=angle, edgecolor='r', fc='None', lw=2)
```

```
#
fig, ax = plt.subplots()
ax.add_patch(ellipse)

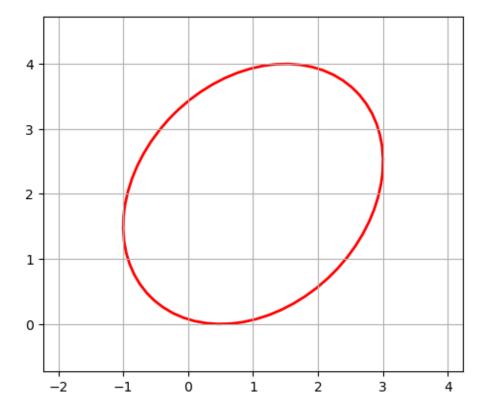
#
ax.set_xlim(center_x - a - fig_padding, center_x + a + fig_padding)
ax.set_ylim(center_y - b - fig_padding, center_y + b + fig_padding)

plt.grid()

#
plt.gca().set_aspect('equal', adjustable='box')
plt.show()
```

```
[12]: # Plotting Ellipsoid
    center = (1, 2)  #
    major_axis = (1, 1)  #
    minor_axis = (1, -1)  #
    a = np.sqrt(5)  #
    b = np.sqrt(3)  #

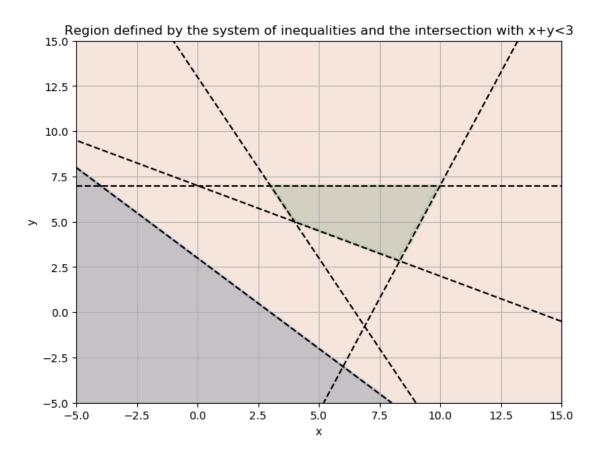
    draw_ellipse(center, major_axis, minor_axis, a, b)
```



Problem 8 - Polyhedron

• 2.

```
[13]: import numpy as np
      import matplotlib.pyplot as plt
               \boldsymbol{A}
      A = np.array([
                      2x - 3y < 5
          [0, 1], #
          [5, -2], #
                       x + y < 4
          [-1, -2], #
                         -x + 2y < 3
          [-4, -2] # 3x - y < 7
      ])
      b = np.array([7, 36, -14, -26])
      A_new = np.array([[1, 1]]) # x + y < 3
      b_new = np.array([3])
      x_min, x_max = -5, 15
      y_min, y_max = -5, 15
      xx, yy = np.meshgrid(np.linspace(x_min, x_max, 100), np.linspace(y_min, y_max,_
      →100))
      Z = np.ones_like(xx, dtype=bool)
      for i in range(A.shape[0]):
          Z \&= (A[i, 0] * xx + A[i, 1] * yy < b[i])
      Z_{new} = (A_{new}[0, 0] * xx + A_{new}[0, 1] * yy < b_{new}[0])
      Z_intersection = Z & Z_new
      plt.figure(figsize=(8, 6))
      plt.contourf(xx, yy, Z, alpha=0.3, cmap='Greens')
      plt.contourf(xx, yy, Z_new, alpha=0.3, cmap='Blues')
```



```
[14]: import numpy as np
      import matplotlib.pyplot as plt
      A = np.array([
          [0,1],
          [5,-2],
          [-1, -2],
          [-4, -2]
      ])
      b = np.array([7, 36, -14, -26])
      x_min, x_max = -5, 15
      y_{min}, y_{max} = -5, 15
      xx, yy = np.meshgrid(np.linspace(x_min, x_max, 100), np.linspace(y_min, y_max,_

→100))

      Z = np.ones_like(xx, dtype=bool)
      for i in range(A.shape[0]):
          Z \&= (A[i, 0] * xx + A[i, 1] * yy < b[i])
```

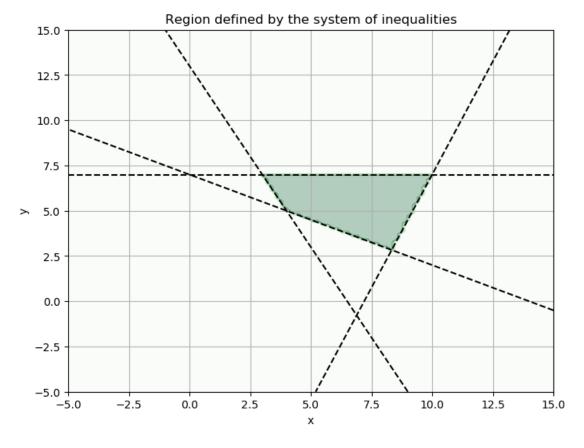
```
plt.figure(figsize=(8, 6))
plt.contourf(xx, yy, Z, alpha=0.3, cmap='Greens') #
for i in range(A.shape[0]):
    plt.contour(xx, yy, A[i, 0] * xx + A[i, 1] * yy, [b[i]], colors='k',
    clinestyles='dashed') #
plt.xlim(x_min, x_max)
plt.ylim(y_min, y_max)

plt.ylim(y_min, y_max)

plt.xlabel('x')
plt.ylabel('y')

plt.title('Region defined by the system of inequalities')
plt.grid(True)

plt.show()
```



```
[15]: import numpy as np import matplotlib.pyplot as plt
```

```
a = np.array([1, 1])
b = 5

x = np.linspace(-10, 10, 400)

y = (b - a[0] * x) / a[1]

fig, ax = plt.subplots()

ax.plot(x, y, label=r'$x + y \leq 5$')

ax.fill_between(x, y, -10, where=y >= -10, alpha=0.3)

ax.legend()
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.grid()
ax.set_title('Feasible region for the given inequalities')
```

[15]: Text(0.5, 1.0, 'Feasible region for the given inequalities')

