

Homework 1

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Problem 1

- (a) Using $Q = 1$, $R = 4 \times 10^7 \text{m}$, $B = 10$ Tesla, we find

$$\begin{aligned} E &= Q \left(\frac{R}{\text{meter}} \right) \left(\frac{B}{\text{Tesla}} \right) 0.3 \text{ GeV} \\ &= (4 \times 10^7)(10)(0.3) \text{ GeV} \\ &= 1.2 \times 10^7 \text{ GeV} \end{aligned}$$

- (b) Power loss due to synchrotron radiation is given by

$$P = \frac{0.3\gamma^4}{R/\text{meter}} \text{ eV/s.}$$

The time to complete one loop is given by $2\pi R$. Then,

$$\begin{aligned} E &= \frac{0.3\gamma^4}{R/\text{meter}} 2\pi R \text{ eV} = 0.6\pi \left(\frac{E}{m_e} \right)^4 \text{ eV} \\ \implies E &\approx 77 \text{ MeV} \end{aligned}$$

- (c) We have that

$$N_{\text{turns}} = \frac{\gamma\tau c}{2\pi R} = \frac{\tau c E}{2\pi R m_\mu}.$$

With $E = 10 \text{TeV}$, and plugging in the mass and lifetime of the muon, this gives

$$N_{\text{turns}} \approx 2300$$

- (d) The event rate is given by

$$\frac{dN}{dt} = \sigma \mathcal{L}.$$

Given a cross section of $\sigma = 100 \text{ nb}$ and an instantaneous luminosity of $10 \text{nb}^{-1} \text{s}^{-1}$ (from google), this gives a total event rate of

$$\frac{dN}{dt} = 1000 \text{ Hz,}$$

which seems rather low... If you can only record events at 100 Hz, then your trigger needs a suppression factor of 10.

- (e) Using the power formula stated in part (b), with $E = 200$ GeV and $2\pi R = 2.7 \times 10^4$ m, we find that the power per particle is

$$P = 4.1 \times 10^{-2} \text{ W}.$$

With 10^{12} particles in the ring, that's a total power of

$$P_{\text{total}} = 4.1 \times 10^{10} \text{ W} = 41 \text{ gigawatts}$$

Problem 2

- (a)
- (b) The Feynman diagram for the process is shown in Figure 1.

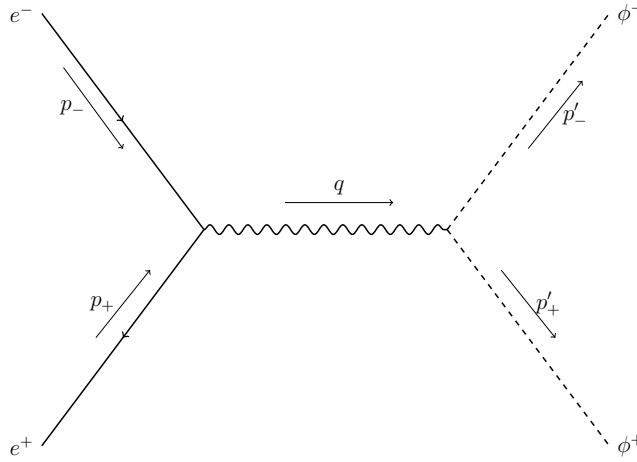


Figure 1: The Feynman diagram for $e^+e^- \rightarrow \phi^+\phi^-$