Problem 1

$$\begin{split} & \text{In} \text{[12]:= } \mathbf{H}_{\text{FI}} [\texttt{t}_{_}] \; = \; \frac{\hbar}{2} \; \left(- \, \delta \, [\texttt{t}] \; \sigma_{\text{z}} \; + \; \text{Re} \left[\Omega_{\theta} \, [\texttt{t}] \right] \; \sigma_{\text{x}} \; + \; \text{Im} \left[\Omega_{\theta} \, [\texttt{t}] \right] \; \sigma_{\text{y}} \right) ; \\ & \text{rho} \; = \; \left\{ \left\{ \rho_{11} , \; \rho_{12} \right\} , \; \left\{ \rho_{21} , \; \rho_{22} \right\} \right\} ; \\ & \dot{\rho} \; = \; \frac{1}{\dot{\mathbf{n}}} \; \text{Comm} \left[\mathbf{H}_{\text{FI}} \left[\texttt{t} \right] , \; \text{rho} \right] ; \\ & \dot{\rho} \; \; / \; / \; \text{CleanUp} \\ & \text{Out} \text{[15]} / \text{TraditionalForm=} \\ & \left(\; - \frac{1}{2} \, i \, (\rho_{21} \, \Omega_{0}(t)^{*} - \rho_{12} \, \Omega_{0}(t)) \; \quad \frac{1}{2} \, i \, ((\rho_{11} - \rho_{22}) \, \Omega_{0}(t)^{*} + 2 \, \rho_{12} \, \delta(t)) \\ & \left(- \frac{1}{2} \, i \, (2 \, \rho_{21} \, \delta(t) + (\rho_{11} - \rho_{22}) \, \Omega_{0}(t)) \; \quad \frac{1}{2} \, i \, (\rho_{21} \, \Omega_{0}(t)^{*} - \rho_{12} \, \Omega_{0}(t)) \; \right) \end{split}$$

Problem 2

```
\begin{split} & \text{In[16]:= } \{ \{ \mathbf{Tr}[\dot{\rho}.\sigma_{\mathbf{x}}] \text{, } \mathbf{Tr}[\dot{\rho}.\sigma_{\mathbf{y}}] \text{, } \mathbf{Tr}[\dot{\rho}.\sigma_{\mathbf{z}}] \} \}^{\mathsf{T}} \text{ // CleanUp} \\ & \text{Out[16]//TraditionalForm=} \\ & \begin{pmatrix} (\rho_{11} - \rho_{22}) \operatorname{Im}(\Omega_{0}(t)) + i \left(\rho_{12} - \rho_{21}\right) \delta(t) \\ (\rho_{22} - \rho_{11}) \operatorname{Re}(\Omega_{0}(t)) - \left(\rho_{12} + \rho_{21}\right) \delta(t) \\ -i \left(\rho_{21} \ \Omega_{0}(t)^{*} - \rho_{12} \ \Omega_{0}(t)\right) \end{pmatrix} \end{split}
```

Problem 3

```
In[17]:= rho[t_{-}] = \{\{a[t], b[t]\}, \{c[t], d[t]\}\};
H[t_{-}] = \frac{\hbar}{2} \left(-\omega_{\theta} \, \sigma_{z} + \Omega_{\theta} \, e^{i\,\omega\,t} \, \sigma_{+} + \left(\Omega_{\theta} \, e^{i\,\omega\,t} \, \sigma_{+}\right)^{\dagger}\right);
rhoDot[t_{-}] = \frac{1}{i\,\hbar} \left(Comm[H[t], rho[t]] - i\,\hbar\,\gamma \left(\sigma_{\theta}.rho[t] + rho[t].\sigma_{\theta}\right) + 2\,i\,\hbar\,\gamma\,\sigma_{-}.rho[t].\sigma_{+}\right);
rhoDot[t] \ // \ CleanUp
```

```
ln[21]:= DSolve[{a'[t] == (rhoDot[t][1, 1]] /. {d[t] \rightarrow 1 - a[t], c[t] \rightarrow b[t]*}),
            b'[t] = (rhoDot[t][1, 2] /. \{d[t] \rightarrow 1 - a[t], c[t] \rightarrow b[t]^*\}),
            a[0] = 1, c[0] = 0} // FullSimplify, {a, b}, t] // CleanUp
```

Problem 4

```
In[23]:= \psi = \{\{\cos[\theta/2]\}, \{e^{i\phi}\sin[\theta/2]\}\};
            ((\psi^{\dagger}.#.\psi) [1]) & /@ {\sigma_x, \sigma_y, \sigma_z} // CleanUp
Out[24]//TraditionalForm=
             \sin(\theta)\cos(\phi)
              \sin(\theta)\sin(\phi)
\cos(\theta)
```

Problem 5

In[25]:=