Relational Algebra

Chapter 4, Part A

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Relational Query Languages

- * Query languages: Allow manipulation and retrieval of data from a database.
- * Relational model supports simple, powerful QLs:
 - Strong formal foundation based on logic.
 - Allows for much optimization.
- Query Languages != programming languages!
 - QLs not expected to be "Turing complete".
 - QLs not intended to be used for complex calculations.
 - QLs support easy, efficient access to large data sets.

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Formal Relational Query Languages

- Two mathematical Query Languages form the basis for "real" languages (e.g. SQL), and for implementation:
 - *Relational Algebra*: More operational, very useful for representing execution plans.
 - *Relational Calculus*: Lets users describe what they want, rather than how to compute it. (Nonoperational, <u>declarative</u>.)

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Preliminaries

- * A query is applied to *relation instances*, and the result of a query is also a relation instance.
 - *Schemas* of input relations for a query are fixed (but query will run regardless of instance!)
 - The schema for the *result* of a given query is also fixed! Determined by definition of query language constructs.
- * Positional vs. named-field notation:
 - Positional notation easier for formal definitions, named-field notation more readable.
 - Both used in SQL

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Example Schema

Sailors(sid: integer, sname: string, rating: integer, age:real)

Boats(bid: integer, bname: string, color: string) Reserves(sid: integer, bid: integer, day: date).

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Example Instances

R1

sid	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

- "Sailors" and "Reserves" relations for our examples.
- ❖ We'll use positional or named field notation, assume that names of fields in query results are `inherited' from names of fields in query input relations.

S1

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

2	sid	sname	rating	age
	28	yuppy	9	35.0
	31	lubber	8	55.5
	44	guppy	5	35.0
	58	rusty	10	35.0

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Relational Algebra

- * Basic operations:
 - Selection (σ) Selects a subset of rows from relation.
 - <u>Projection</u> (π) Deletes unwanted columns from relation.
 - <u>Cross-product</u> (X) Allows us to combine two relations.
 - <u>Set-difference</u> (—) Tuples in reln. 1, but not in reln. 2.
 - *Union* (U) Tuples in reln. 1 and in reln. 2.
- * Additional operations:
 - Intersection, <u>join</u>, division, renaming: Not essential, but (very!) useful.
- Since each operation returns a relation, operations can be *composed*! (Algebra is "closed".)

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Projection

- Deletes attributes that are not in projection list.
- * Schema of result contains exactly the fields in the projection list, with the same names that they had in the (only) input relation.
- Projection operator has to eliminate duplicates! (Why??)
 - Note: real systems typically don't do duplicate elimination unless the user explicitly asks for it. (Why not?)

sname	rating
yuppy	9
lubber	8
guppy	5
rusty	10

$$\pi_{sname,rating}(S2)$$

age
35.0
55.5

$$\pi_{age}(S2)$$

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Selection

- Selects rows that satisfy selection condition.
- No duplicates in result! (Why?)
- * Schema of result identical to schema of (only) input relation.
- * Result relation can be the *input* for another relational algebra operation! (Operator composition.)

sid	sname	rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

 $\sigma_{rating>8}(S2)$

sname	rating
yuppy	9
rusty	10

 $\pi_{sname,rating}(\sigma_{rating>8}(S2))$

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Union, Intersection, Set-Difference

- * All of these operations take two input relations, which must be union-compatible:
 - Same number of fields.
 - `Corresponding' fields have the same type.
- ❖ What is the *schema* of result?

sid	sname	rating	age
22	dustin	7	45.0

S1-S2

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

 $S1 \cup S2$

sid	sname	rating	age
31	lubber	8	55.5
58	rusty	10	35.0

 $S1 \cap S2$

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Cross-Product

- * Each row of S2 is paired with each row of R1.
- * Result schema has one field per field of S2 and R1, with field names `inherited' if possible.
 - Conflict: Both S2 and R1 have a field called sid.

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

• Renaming operator: $\rho(C(1 \rightarrow sid1, 5 \rightarrow sid2), S1 \times R1)$

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Joins

* Condition Join:
$$R \bowtie_{C} S = \sigma_{C}(R \times S)$$

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0			11/12/96
31	lubber	8	55.5	58	103	11/12/96

$$S1 \bowtie_{S1.sid < R1.sid} R1$$

- * *Result schema* same as that of cross-product.
- ❖ Fewer tuples than cross-product, might be able to compute more efficiently
- * Sometimes called a *theta-join*.

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Joins

* <u>Equi-Join</u>: A special case of condition join where the condition *c* contains only *equalities*.

	• •				
sid	sname	rating	age	bid	day
22	dustin	7	45.0	101	10/10/96
58	rusty	10	35.0	103	11/12/96

$$S1 \bowtie_{sid} R1$$

- * Result schema similar to cross-product, but only one copy of fields for which equality is specified.
- * Natural Join: Equijoin on all common fields.

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Find names of sailors who've reserved boat #103

- ❖ Solution 1: $\pi_{sname}((\sigma_{bid=103} \text{Reserves}) \bowtie Sailors)$
- * Solution 2: ρ (Temp1, $\sigma_{bid=103}$ Reserves) ρ (Temp2, Temp1 \bowtie Sailors) π_{sname} (Temp2)
- * Solution 3: $\pi_{sname}(\sigma_{bid=103}(\text{Reserves} \bowtie Sailors))$

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Find names of sailors who've reserved a red boat

❖ Information about boat color only available in Boats; so need an extra join:

$$\pi_{sname}((\sigma_{color='red}, Boats) \bowtie Reserves \bowtie Sailors)$$

* A more efficient solution:

$$\pi_{sname}(\pi_{sid}((\pi_{bid}\sigma_{color='red'}Boats)\bowtie Res)\bowtie Sailors)$$

A query optimizer can find this, given the first solution!

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Find sailors who've reserved a red or a green boat

 Can identify all red or green boats, then find sailors who've reserved one of these boats:

$$\rho \; (\textit{Tempboats}, (\sigma_{\textit{color} = '\textit{red'}} \lor \textit{color} = '\textit{green'} \; \textit{Boats}))$$

$$\pi_{sname}$$
(Temphoats \bowtie Reserves \bowtie Sailors)

- ❖ Can also define Tempboats using union! (How?)
- * What happens if \vee is replaced by \wedge in this query?

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Find sailors who've reserved a red and a green boat

Previous approach won't work! Must identify sailors who've reserved red boats, sailors who've reserved green boats, then find the intersection (note that *sid* is a key for Sailors):

$$\rho \; (\textit{Tempred}, \, \pi_{\textit{sid}}((\sigma_{\textit{color} = '\textit{red'}} \textit{Boats}) \bowtie \mathsf{Reserves}))$$

$$\rho \; (\textit{Tempgreen}, \, \pi_{\textit{sid}}((\sigma_{\textit{color} = '\textit{green'}} \, \textit{Boats}) \bowtie \mathsf{Reserves}))$$

$$\pi_{\mathit{sname}}((\mathit{Tempred} \cap \mathit{Tempgreen}) \bowtie \mathit{Sailors})$$

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Summary

- The relational model has rigorously defined query languages that are simple and powerful.
- * Relational algebra is more operational; useful as internal representation for query evaluation plans.
- Several ways of expressing a given query; a query optimizer should choose the most efficient version.

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