

# Schema Refinement and Normal Forms

Chapter 19

**Instructor: Vladimir Zadorozhny**

[vladimir@sis.pitt.edu](mailto:vladimir@sis.pitt.edu)

Information Science Program

School of Information Sciences,

University of Pittsburgh

## The Evils of Redundancy

- ❖ *Redundancy* is at the root of several problems associated with relational schemas:
  - *redundant storage, insert/delete/update anomalies*
- ❖ Integrity constraints, in particular *functional dependencies*, can be used to identify schemas with such problems and to suggest refinements.
- ❖ Main refinement technique: *decomposition* (replacing ABCD with, say, AB and BCD, or ACD and ABD).
- ❖ Decomposition should be used judiciously:
  - Is there reason to decompose a relation?
  - What problems (if any) does the decomposition cause?

## Example

- ❖ Consider the relation schema:  
*Lending-schema* = (*branch-name*, *branch-city*, *assets*,  
*customer-name*, *loan-number*, *amount*)

<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>	<i>customer-name</i>	<i>loan-number</i>	<i>amount</i>
Downtown	Brooklyn	9000000	Jones	L-17	1000
Redwood	Palo Alto	2100000	Smith	L-23	2000
Perryridge	Horseneck	1700000	Hayes	L-15	1500
Downtown	Brooklyn	9000000	Jackson	L-14	1500

- ❖ Redundancy:
  - Data for *branch-name*, *branch-city*, *assets* are repeated for each loan that a branch makes
  - Wastes space
  - Complicates updating, introducing possibility of inconsistency of *assets* value
- ❖ Null values
  - Cannot store information about a branch if no loans exist
  - Can use null values, but they are difficult to handle.

## Decomposition of a Relation Scheme

- ❖ Suppose that relation R contains attributes *A1* ... *An*. A *decomposition* of R consists of replacing R by two or more relations such that:
  - Each new relation scheme contains a subset of the attributes of R (and no attributes that do not appear in R), and
  - Every attribute of R appears as an attribute of one of the new relations.
- ❖ Intuitively, decomposing R means we will store instances of the relation schemes produced by the decomposition, instead of instances of R.
- ❖ E.g., Can decompose SNLRWH into SNLRH and RW.

## Lossless Join Decompositions

- ❖ Decomposition of R into X and Y is *lossless-join* w.r.t. a set of FDs F if, for every instance  $r$  that satisfies F:
  - $\pi_X(r) \bowtie \pi_Y(r) = r$
- ❖ It is always true that  $r \subseteq \pi_X(r) \bowtie \pi_Y(r)$ 
  - In general, the other direction does not hold! If it does, the decomposition is lossless-join.
- ❖ Definition extended to decomposition into 3 or more relations in a straightforward way.
- ❖ *It is essential that all decompositions used to deal with redundancy be lossless!*

## Functional Dependencies (FDs)

- ❖ A functional dependency  $X \rightarrow Y$  holds over relation R if, for every allowable instance  $r$  of R:
  - $t1 \in r, t2 \in r, \pi_X(t1) = \pi_X(t2)$  implies  $\pi_Y(t1) = \pi_Y(t2)$
  - i.e., given two tuples in  $r$ , if the X values agree, then the Y values must also agree. (X and Y are *sets* of attributes.)
- ❖ An FD is a statement about *all* allowable relations.
  - Must be identified based on semantics of application.
  - Given some allowable instance  $r1$  of R, we can check if it violates some FD  $f$ , but we cannot tell if  $f$  holds over R!
- ❖ K is a candidate key for R means that  $K \rightarrow R$ 
  - However,  $K \rightarrow R$  does not require K to be *minimal*!

## Example

- ❖ Consider relation Hourly\_Emps:
  - Hourly\_Emps (ssn, name, lot, rating, hrly\_wages, hrs\_worked)
- ❖ **Notation:** We will denote this relation schema by listing the attributes: **SNLRWH**
  - This is really the **set** of attributes {S,N,L,R,W,H}.
  - Sometimes, we will refer to all attributes of a relation by using the relation name. (e.g., Hourly\_Emps for SNLRWH)
- ❖ Some FDs on Hourly\_Emps:
  - **ssn is the key:**  $S \rightarrow \text{SNLRWH}$
  - **rating determines hrly\_wages:**  $R \rightarrow W$

## Example (Contd.)

- ❖ Problems due to  $R \rightarrow W$ :
  - **Update anomaly:** Can we change W in just the 1st tuple of SNLRWH?
  - **Insertion anomaly:** What if we want to insert an employee and don't know the hourly wage for his rating?
  - **Deletion anomaly:** If we delete all employees with rating 5, we lose the information about the wage for rating 5!

S	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
131-24-3650	Smethurst	35	5	7	30
434-26-3751	Guldu	35	5	7	32
612-67-4134	Madayan	35	8	10	40

S	N	L	R	H
123-22-3666	Attishoo	48	8	40
231-31-5368	Smiley	22	8	30
131-24-3650	Smethurst	35	5	30
434-26-3751	Guldu	35	5	32
612-67-4134	Madayan	35	8	40

Hourly\_Emps2

R	W
8	10
5	7

Wages

## Reasoning About FDs

- ❖ Given some FDs, we can usually infer additional FDs:
  - $ssn \rightarrow did, did \rightarrow lot$  implies  $ssn \rightarrow lot$
- ❖ An FD  $f$  is *implied by* a set of FDs  $F$  if  $f$  holds whenever all FDs in  $F$  hold.
  - $F^+ = \text{closure of } F$  is the set of all FDs that are implied by  $F$ .
- ❖ Armstrong's Axioms ( $X, Y, Z$  are sets of attributes):
  - Reflexivity: If  $Y \subseteq X$ , then  $X \rightarrow Y$
  - Augmentation: If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any  $Z$
  - Transitivity: If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$
- ❖ These are *sound* and *complete* inference rules for FDs!

## Reasoning About FDs (Contd.)

- ❖ Couple of additional rules (that follow from AA):
  - *Union*: If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$
  - *Decomposition*: If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$
- ❖ Example: **Contracts**(*cid,sid,jid,did,pid,qty,value*), and:
  - $C$  is the key:  $C \rightarrow CSJDPQV$
  - Project purchases each part using single contract:  $JP \rightarrow C$
  - Dept purchases at most one part from a supplier:  $SD \rightarrow P$
- ❖  $JP \rightarrow C, C \rightarrow CSJDPQV$  imply  $JP \rightarrow CSJDPQV$
- ❖  $SD \rightarrow P$  implies  $SDJ \rightarrow JP$
- ❖  $SDJ \rightarrow JP, JP \rightarrow CSJDPQV$  imply  $SDJ \rightarrow CSJDPQV$

## Reasoning About FDs (Contd.)

- ❖ Computing the closure of a set of FDs can be expensive. (Size of closure is exponential in # attrs!)
- ❖ Typically, we just want to check if a given FD  $X \rightarrow Y$  is in the closure of a set of FDs  $F$ . An efficient check:
  - Compute *attribute closure* of  $X$  (denoted  $X^+$ ) wrt  $F$ :
    - ◆ Set of all attributes  $A$  such that  $X \rightarrow A$  is in  $F^+$
    - ◆ There is a linear time algorithm to compute this.
  - Check if  $Y$  is in  $X^+$
- ❖ Does  $F = \{A \rightarrow B, B \rightarrow C, CD \rightarrow E\}$  imply  $A \rightarrow E$ ?
  - i.e, is  $A \rightarrow E$  in the closure  $F^+$ ? Equivalently, is  $E$  in  $A^+$ ?

## More on Lossless Join

- ❖ The decomposition of  $R$  into  $X$  and  $Y$  is *lossless-join wrt  $F$*  if and only if the closure of  $F$  contains:
  - $X \cap Y \rightarrow X$ , or
  - $X \cap Y \rightarrow Y$
- ❖ In particular, the decomposition of  $R$  into  $UV$  and  $R - V$  is lossless-join if  $U \rightarrow V$  holds over  $R$ .

A	B	C
1	2	3
4	5	6
7	2	8



A	B
1	2
4	5
7	2

B	C
2	3
5	6
2	8



A	B	C
1	2	3
4	5	6
7	2	8
1	2	8
7	2	3

## Normalization Using Functional Dependencies

- ❖ When we decompose a relation schema  $R$  with a set of functional dependencies  $F$  into  $R_1, R_2, \dots, R_n$  we want
  - **Lossless-join decomposition:** Otherwise decomposition would result in information loss.
  - **No redundancy:** The relations  $R_i$  preferably should be in either Boyce-Codd Normal Form or Third Normal Form.
  - **Dependency preservation:** We will talk about it a little later.

## Normal Forms

- ❖ Returning to the issue of schema refinement, the first question to ask is whether any refinement is needed!
- ❖ If a relation is in a certain *normal form* (BCNF, 3NF etc.), it is known that certain kinds of problems are avoided/minimized. This can be used to help us decide whether decomposing the relation will help.
- ❖ Role of FDs in detecting redundancy:
  - Consider a relation  $R$  with 3 attributes,  $ABC$ .
    - ♦ **No FDs hold:** There is no redundancy here.
    - ♦ **Given  $A \rightarrow B$ :** Several tuples could have the same  $A$  value, and if so, they'll all have the same  $B$  value!

## Boyce-Codd Normal Form (BCNF)

- ❖ Reln R with FDs  $F$  is in **BCNF** if, for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  (called a *trivial* FD), or
  - $X$  contains a key for R.
- ❖ In other words, R is in BCNF if the only non-trivial FDs that hold over R are key constraints.
  - No redundancy in R that can be detected using FDs alone.
  - If we are shown two tuples that agree upon the X value, we cannot infer the A value in one tuple from the A value in the other.
  - If example relation is in BCNF, the 2 tuples must be identical (since X is a key).

X	Y	A
x	y1	a
x	y2	?

## Decomposition into BCNF

- ❖ Consider relation R with FDs  $F$ . If  $X \rightarrow Y$  violates BCNF, decompose R into  $R - Y$  and  $XY$ .
  - **Repeated application** of this idea will give us a collection of relations that are in BCNF; **lossless join decomposition**, and guaranteed to terminate.
  - e.g., CSJDPQV, key C,  $JP \rightarrow C$ ,  $SD \rightarrow P$ ,  $J \rightarrow S$
  - To deal with  $SD \rightarrow P$ , decompose into SDP, CSJDQV.
  - To deal with  $J \rightarrow S$ , decompose CSJDQV into JS and CJDQV
- ❖ In general, several dependencies may cause violation of BCNF. The order in which we ``deal with'' them could lead to very different sets of relations!



## Example of BCNF Decomposition

$R = (\text{branch-name}, \text{branch-city}, \text{assets}, \text{customer-name}, \text{loan-number}, \text{amount})$

$F = \{\text{branch-name} \rightarrow \text{assets branch-city}$   
 $\text{loan-number} \rightarrow \text{amount branch-name}\}$

Key =  $\{\text{loan-number}, \text{customer-name}\}$

### Decomposition

- $R_1 = (\text{branch-name}, \text{branch-city}, \text{assets})$
- $R_2 = (\text{branch-name}, \text{customer-name}, \text{loan-number}, \text{amount})$
- $R_3 = (\text{branch-name}, \text{loan-number}, \text{amount})$
- $R_4 = (\text{customer-name}, \text{loan-number})$

### Final decomposition

$R_1, R_3, R_4$

## Dependency Preserving Decomposition

- ❖ Consider CSJDPQV, C is key,  $JP \rightarrow C$  and  $SD \rightarrow P$ .
  - BCNF decomposition: CSJDQV and SDP
  - Problem: Checking  $JP \rightarrow C$  requires a join!
- ❖ **Dependency preserving decomposition:**
  - If R is decomposed into X, Y and Z, and we enforce the FDs that hold on X, on Y and on Z, then all FDs that were given to hold on R must also hold.
  - I.e., we should be able to check all functional dependencies on individual tables without doing joins

## BCNF and Dependency Preservation

- ❖ In general, there may not be a dependency preserving decomposition into BCNF.
  - e.g., CSZ,  $CS \rightarrow Z$ ,  $Z \rightarrow C$
  - Can't decompose while preserving 1st FD; not in BCNF.
- ❖ Similarly, decomposition of CSJDPQV into SDP, JS and CJDQV is not dependency preserving (w.r.t. the FDs  $JP \rightarrow C$ ,  $SD \rightarrow P$  and  $J \rightarrow S$ ).
  - However, it is a lossless join decomposition.
  - In this case, adding JPC to the collection of relations gives us a dependency preserving decomposition.
    - ♦ JPC tuples stored only for checking FD! (*Redundancy!*)

## Third Normal Form (3NF)

- ❖ Reln R with FDs F is in 3NF if, for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  (called a *trivial* FD), or
  - X contains a key for R, or
  - A is part of some key for R.
- ❖ *Minimality* of a key is crucial in third condition above!
- ❖ If R is in BCNF, obviously in 3NF.
- ❖ If R is in 3NF, some redundancy is possible. It is a compromise, used when BCNF not achievable (e.g., no ``good'' decomp, or performance considerations).
  - *Lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations always possible.*

## *Summary of Schema Refinement*

- ❖ If a relation is in BCNF, it is free of redundancies that can be detected using FDs. Thus, trying to ensure that all relations are in BCNF is a good heuristic.
- ❖ If a relation is not in BCNF, we can try to decompose it into a collection of BCNF relations.
  - Must consider whether all FDs are preserved. If a lossless-join, dependency preserving decomposition into BCNF is not possible (or unsuitable, given typical queries), should consider decomposition into 3NF.
  - Decompositions should be carried out and/or re-examined while keeping *performance requirements* in mind.