

Practice Exercises for Parameter Optimization

Sean Matthew Nolan

February 23, 2021

1 Inequality Problem

Problem

$$\min_{\mathbf{u}} J = x^2 - u^2 \quad (1.1)$$

Subject to:

$$g = x^2 + u^2 - 4 \leq 0 \quad (1.2)$$

2 Maximum Steady Rate of Climb for Aircraft[1]

Problem

This problem aims to find the maximum steady rate of climb of an aircraft.

The rate of climb is $v \sin \gamma$, so the cost function is

$$\min J = -v \sin \gamma \quad (2.1)$$

For a steady climb, acceleration, thus force, in both directions must be zero:

$$\mathbf{f}(v, \gamma, \alpha) = \begin{bmatrix} T(v) \cos(\alpha + \epsilon) - D(v, \alpha) - mg \sin \gamma \\ T(v) \sin(\alpha + \epsilon) + L(v, \alpha) - mg \cos \gamma \end{bmatrix} = 0 \quad (2.2)$$

Where:

v = velocity

γ = flight path angle

α = angle of attack

m = mass

g = gravity

ϵ = angle between thrust axis and zero-lift axis

$T(\alpha)$ = thrust

$L(v, \alpha)$ = lift

$D(v, \alpha)$ = drag

References

- [1] A. E. Bryson and Y.-C. Ho, *Applied optimal control: optimization, estimation, and control*. Washington : New York: Hemisphere Pub. Corp. ; distributed by Halsted Press, rev. printing ed., 1975.