Project 1 – Distances in ABG

Sean G Meyer

Reachability Rules

I created my program so that every reachability rule is input as a simple function, with parameters of x-distance and y-distance between the first and second positions, along with the actual x/y values for 1st and 2nd position (only used if necessary, in this case only for the pawn). Below are the reachability rules I created for each piece (different ones can easily be input manually when running program).

```
(defn king
  [x-dist y-dist & xy]
  (and
    (<= x-dist 1)
    (<= y-dist 1)))</pre>
(defn knight
  [x-dist y-dist & xy]
  (or
    (and
      (= x-dist 2)
      (= y-dist 1))
      (= x-dist 1)
      (= y-dist 2))))
(defn queen
  [x-dist y-dist & xy]
  (or
    (= x-dist ∅)
    (= y-dist ∅)
    (= x-dist y-dist)))
(defn rook
  [x-dist y-dist & xy]
  (or
    (= x-dist ∅)
    (= y-dist 0)))
(defn bishop
  [x-dist y-dist & xy]
  (= x-dist y-dist))
```

```
(defn pawn
  [x-dist y-dist x1 y1 x2 y2]
  (and
    (= x-dist 0)
    (= (- y1 y2) 1)))
```

Sample Tables

Below are tables, one per chess piece, with sample locations computed. Each chess piece was placed on a different board of varying size with varying obstacles.

Pawn on an 8x8 board with no obstacles, starting at position c2

	\mathbf{a}	\mathbf{b}	\mathbf{c}	\mathbf{d}	\mathbf{e}	f	\mathbf{g}	\mathbf{h}
8	X	x x x x x x x x	6	x	X	X	x	X
7	X	\mathbf{x}	5	\mathbf{x}	\mathbf{x}	X	\mathbf{x}	X
6	x	\mathbf{x}	4	X	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}
5	X	\mathbf{x}	3	\mathbf{x}	\mathbf{x}	X	\mathbf{x}	X
4	x	\mathbf{x}	2	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}
3	X	\mathbf{x}	1	\mathbf{x}	\mathbf{x}	X	\mathbf{x}	X
2	X	\mathbf{x}	0	\mathbf{x}	\mathbf{x}	X	\mathbf{x}	X
1	x	\mathbf{x}	X	\mathbf{x}	X	\mathbf{x}	\mathbf{x}	\mathbf{x}

King on an 8x8 board with obstacles at positions marked []

	\mathbf{a}	b	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}
8	1	1 0	1	2	3	4	5	6
7	1	0	1	2	3	4	5	6
6	1	1 2 3 4 5	1	2			5	6
5	2	2	2	2			6	6
4	3	3	3	3			6	7
3	4	4	4	4	4	5	6	7
2	5	5	5	5	5	5	6	7
1	6	6	6	6	6	6	6	7

Knight on a 10x10 board with obstacles

	a	b	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j
15	4	3	4	3	4	3	4	3	4	3
14	3	4	3	4	3	2	3	2	3	4
13	4	3	2	3			2	3	2	3
12	3	2	3	4			1	4	3	2
11	4	3	2	1			4	1	2	3
10	3	2	3	2	3	0	3	\mathbf{x}	3	2
9	4	3	2	1	2	3	2	\mathbf{x}	2	3
8	3	2	X	4	1	2	1	4	3	4
7	4	3	X	3	2	3	2	3	2	3
6	3	4	3	2	3	2	3	2	3	4

Queen on a 10x10 board with no obstacles

	\mathbf{a}	\mathbf{b}	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j
10	1	2	2	2	2	1	2	2	2	2
9	2	1	2	2	2	1	2	2	2	1
8	2	2	1	2	2	1	2	2	1	2
7	2	2	2	1	2	1	2	1	2	2
6	2	2	2	2	1	1	1	2	2	2
5	1	1	1	1	1	0	1	1	1	1
4	2	2	2	2	1	1	1	2	2	2
3	2	2	2	1	2	1	2	1	2	2
2	2	2	1	2	2	1	2	2	1	2
1	2	1	2	2	2	1	2	2	2	1

Bishop on a 10x10 board with obstacles

	a	b	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	h	i	j
10	X	2	X	2	X	2	X	2	X	1
9	3	X	2	\mathbf{x}	2	X	2	x	1	x
8	x	3	X	2	X	2	\mathbf{x}	1	X	2
7	2	X	3	\mathbf{x}	2	X	1	x	2	x
6	x	3	X		X	1	\mathbf{x}	2	X	2
5	3	X	4		0		~	x	2	x
4	x	3	X		X	1		~	X	2
3	3		_	\mathbf{x}	2		1	x	2	x
2	x	3	X	2		~	\mathbf{x}	1	X	2
1	4	x	2		2	x	2	x	1	x

Rook on a 10x10 board with obstacles

	a	b	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	h	i	j
10	2	2	2	2	1	2	2	2	2	2
9	2	2	2	2	1	2	2	2	2	2
8	2	2	2	2	1	2	2	2	2	2
7	2	2	2	2	1	2	2	2	2	2
6	3	3	3	П	1	2	2	2	2	2
5	3	3	3		0	1	1	1	1	1
4	3	3	3		1	2	2	2	2	2
3	2	2	2	$\overline{2}$	1	2	2	2	2	2
2	2	2	2	2	1	2	2	2	2	2
1	2	2	2	2	1	2	2	2	2	2

15x15 Tables

Below are the 15x15 tables my program generated for each piece. These are generated when the input ABG is 8x8 with no obstacles.

 $\rm King~15x15$

	\mathbf{a}	b	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j	\mathbf{k}	1	\mathbf{m}	\mathbf{n}	o
15	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7
14	7	6	6	6	6	6	6	6	6	6	6	6	6	6	7
13	7	6	5	5	5	5	5	5	5	5	5	5	5	6	7
12	7	6	5	4	4	4	4	4	4	4	4	4	5	6	7
11	7	6	5	4	3	3	3	3	3	3	3	4	5	6	7
10	7	6	5	4	3	2	2	2	2	2	3	4	5	6	7
9	7	6	5	4	3	2	1	1	1	2	3	4	5	6	7
8	7	6	5	4	3	2	1	0	1	2	3	4	5	6	7
7	7	6	5	4	3	2	1	1	1	2	3	4	5	6	7
6	7	6	5	4	3	2	2	2	2	2	3	4	5	6	7
5	7	6	5	4	3	3	3	3	3	3	3	4	5	6	7
4	7	6	5	4	4	4	4	4	4	4	4	4	5	6	7
3	7	6	5	5	5	5	5	5	5	5	5	5	5	6	7
2	7	6	6	6	6	6	6	6	6	6	6	6	6	6	7
1	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7

Knight 15x15

	a	\mathbf{b}	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j	\mathbf{k}	1	\mathbf{m}	\mathbf{n}	o
15	6	5	6	5	4	5	4	5	4	5	4	5	4	5	6
14	5	6	5	4	5	4	5	4	5	4	5	4	5	4	5
13	6	5	4	5	4	3	4	3	4	3	4	3	4	5	4
12	5	4	5	4	3	4	3	4	3	4	3	4	3	4	5
11	4	5	4	3	4	3	2	3	2	3	2	3	4	3	4
10	5	4	3	4	3	2	3	2	3	2	3	2	3	4	3
9	4	5	4	3	2	3	4	1	2	1	4	3	2	3	4
8	5	4	3	4	3	2	1	2	3	2	1	2	3	4	3
7	4	5	4	3	2	3	2	3	0	3	2	3	2	3	4
6	5	4	3	4	3	2	1	2	3	2	1	2	3	4	3
5	4	5	4	3	2	3	4	1	2	1	4	3	2	3	4
4	5	4	3	4	3	2	3	2	3	2	3	2	3	4	3
3	4	5	4	3	4	3	2	3	2	3	2	3	4	3	4
2	5	4	5	4	3	4	3	4	3	4	3	4	3	4	5
1	6	5	4	5	4	3	4	3	4	3	4	3	4	5	4

Queen 15x15

	a	\mathbf{b}	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j	\mathbf{k}	1	\mathbf{m}	\mathbf{n}	o
15	1	2	2	2	2	2	2	1	2	2	2	2	2	2	1
14	2	1	2	2	2	2	2	1	2	2	2	2	2	1	2
13	2	2	1	2	2	2	2	1	2	2	2	2	1	2	2
12	2	2	2	1	2	2	2	1	2	2	2	1	2	2	2
11	2	2	2	2	1	2	2	1	2	2	1	2	2	2	2
10	2	2	2	2	2	1	2	1	2	1	2	2	2	2	2
9	2	2	2	2	2	2	1	1	1	2	2	2	2	2	2
8	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
7	2	2	2	2	2	2	1	1	1	2	2	2	2	2	2
6	2	2	2	2	2	1	2	1	2	1	2	2	2	2	2
5	2	2	2	2	1	2	2	1	2	2	1	2	2	2	2
4	2	2	2	1	2	2	2	1	2	2	2	1	2	2	2
3	2	2	1	2	2	2	2	1	2	2	2	2	1	2	2
2	2	1	2	2	2	2	2	1	2	2	2	2	2	1	2
1	1	2	2	2	2	2	2	1	2	2	2	2	2	2	1

${\rm Rook}~15{\rm x}15$

	a	\mathbf{b}	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j	\mathbf{k}	l	\mathbf{m}	\mathbf{n}	o
15	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
14	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
13	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
12	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
11	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
10	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
9	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
8	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
7	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2
1	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2

Bishop 15x15

	\mathbf{a}	\mathbf{b}	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	\mathbf{h}	i	j	\mathbf{k}	1	\mathbf{m}	\mathbf{n}	o
15	1	X	2	X	2	X	2	X	2	X	2	X	2	X	1
14	x	1	\mathbf{x}	2	\mathbf{x}	2	\mathbf{x}	2	X	2	\mathbf{x}	2	X	1	X
13	2	X	1	x	2	X	2	X	2	X	2	\mathbf{x}	1	x	2
12	x	2	\mathbf{x}	1	X	2	\mathbf{x}	2	X	2	\mathbf{x}	1	X	2	X
11	2	X	2	x	1	\mathbf{x}	2	\mathbf{x}	2	\mathbf{x}	1	\mathbf{x}	2	X	2
10	x	2	\mathbf{x}	2	X	1	\mathbf{x}	2	X	1	\mathbf{x}	2	X	2	X
9	2	X	2	x	2	X	1	X	1	X	2	\mathbf{x}	2	x	2
8	x	2	X	2	\mathbf{x}	2	\mathbf{x}	0	\mathbf{x}	2	x	2	X	2	X
7	2	X	2	\mathbf{x}	2	X	1	X	1	X	2	\mathbf{x}	2	x	2
6	x	2	\mathbf{x}	2	X	1	\mathbf{x}	2	X	1	\mathbf{x}	2	X	2	X
5	2	X	2	\mathbf{x}	1	X	2	X	2	X	1	\mathbf{x}	2	x	2
4	x	2	X	1	\mathbf{x}	2	\mathbf{x}	2	\mathbf{x}	2	x	1	X	2	X
3	2	X	1	\mathbf{x}	2	X	2	X	2	X	2	\mathbf{x}	1	x	2
2	x	1	x	2	X	2	\mathbf{x}	2	X	2	\mathbf{x}	2	X	1	X
1	1	\mathbf{x}	2	\mathbf{x}	2	\mathbf{x}	2	\mathbf{x}	2	X	2	\mathbf{x}	2	\mathbf{x}	1

Pawn 15x15

	a	b	\mathbf{c}	\mathbf{d}	\mathbf{e}	\mathbf{f}	\mathbf{g}	h	i	j	\mathbf{k}	l	\mathbf{m}	n	o
15	X	X	X	X	X	X	X	7	X	X	X	X	X	X	X
14	x	X	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{X}	6	X	X	\mathbf{x}	X	X	\mathbf{x}	X
13	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	5	X	X	\mathbf{x}	X	X	X	X
12	\mathbf{x}	X	X	x	\mathbf{x}	\mathbf{x}	X	4	X	X	x	X	X	\mathbf{x}	X
11	X	\mathbf{x}	x	\mathbf{x}	X	X	\mathbf{x}	3	X	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	X
10	X	\mathbf{x}	x	\mathbf{x}	X	X	\mathbf{x}	2	X	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	X
9	X	\mathbf{x}	x	\mathbf{x}	X	X	\mathbf{x}	1	X	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	X
8	X	\mathbf{x}	x	\mathbf{x}	X	X	\mathbf{x}	0	X	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}	X
7	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	X	\mathbf{x}	X	X	X	X
6	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	X	\mathbf{x}	X	X	X	X
5	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	X	\mathbf{x}	X	X	X	X
4	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	X	\mathbf{x}	X	X	X	X
3	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	X	\mathbf{x}	X	X	X	X
2	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	X	\mathbf{x}	X	X	X	X
1	\mathbf{x}	\mathbf{x}	X	\mathbf{x}	X	X	\mathbf{x}	\mathbf{x}	X	X	\mathbf{x}	X	X	\mathbf{x}	X

${\bf Implementation}$

The code was implemented in the programming language Clojure. Source code is included in a file alongside this report. There is no runnable executable at this time, but one can be created on request if needed.