

Universidad ICESI

Sean Quintero - Bryan Guapacha

Paola Osorio - John Kennedy

Análisis de complejidad temporal de algoritmos de ordenamiento.

Insertion sort:

```
public static void insertionSortImperative(int[] input) {  
    for (int i = 1; i < input.length; i++) {  
        int key = input[i];  
        int j = i - 1;  
        while (j >= 0 && input[j] > key) {  
            input[j + 1] = input[j];  
            j = j - 1;  
        }  
        input[j + 1] = key;  
    }  
}
```

Instrucción	Veces que se repite (Big O)
1. for (int i = 1; i < input.length; i++) {	n
2. int key = input[i];	n-1
3. int j = i - 1;	n-1
4. while (j >= 0 && input[j] > key) {	$(n*(n-1))/2$
5. input[j + 1] = input[j];	$((n*(n-1))/2)-1$
6. j = j - 1;	$((n*(n-1))/2)-1$
7. input[j + 1] = key;	n-1
Total:	n^2

Radix sort:

```
private static int findMaximumNumberIn(int[] arr) {  
    return Arrays.stream(arr).max().getAsInt();  
}
```

Instrucción	Veces que se repite (Big O)
1.return Arrays.stream(arr).max().getAsInt();	1
Total:	O(1)

```
private static int calculateNumberOfDigitsIn(int number) {
```

```
return (int) Math.log10(number) + 1; // valid only if number > 0
```

Instrucción	Veces que se repite (Big O)
1. return (int) Math.log10(number) + 1; // valid only if number > 0	1
Total:	O(1)

```
private static void applyCountingSortOn(int[] numbers, int placeValue) {
```

```
    int range = 10; // radix or the base
```

```
    int length = numbers.length;
```

```
    int[] frequency = new int[range];
```

```
    int[] sortedValues = new int[length];
```

```
    for (int i = 0; i < length; i++) {
```

```
        int digit = (numbers[i] / placeValue) % range;
```

```
        frequency[digit]++;
```

```
    }
```

```
    for (int i = 1; i < range; i++) {
```

```
        frequency[i] += frequency[i - 1];
```

```
    }
```

```
    for (int i = length - 1; i >= 0; i--) {
```

```
        int digit = (numbers[i] / placeValue) % range;
```

```
        sortedValues[frequency[digit] - 1] = numbers[i];
```

```
        frequency[digit]--;
```

```
    }
```

```

    System.arraycopy(sortedValues, 0, numbers, 0, length);
}

```

Instrucción	Veces que se repite (Big O)
1. int range = 10; // radix or the base	1
2. int length = numbers.length;	1
3. int[] frequency = new int[range];	1
4. int[] sortedValues = new int[length];	1
5. for (int i = 0; i < length; i++) {	m+1
6. int digit = (numbers[i] / placeValue) % range;	m
7. frequency[digit]++;	m
8. for (int i = 1; i < range; i++) {	m+1
9. frequency[i] += frequency[i - 1];	m
10. for (int i = length - 1; i >= 0; i--) {	m+ 1
11. int digit = (numbers[i] / placeValue) % range;	m

12. sortedValues[frequency[digit] - 1] = numbers[i];	m
13. frequency[digit]--;	m
14. System.arraycopy(sortedValues, 0, numbers, 0, length);	1
Total:	O(m)

```

public static void radixSort(int numbers[]) {
    int maximumNumber = findMaximumNumberIn(numbers);

    int numberOfDigits = calculateNumberOfDigitsIn(maximumNumber);

    int placeValue = 1;

    while (numberOfDigits-- > 0) {
        applyCountingSortOn(numbers, placeValue);
        placeValue *= 10;
    }
}

```

Instrucción	Veces que se repite (Big O)
1. <code>int maximumNumber = findMaximumNumberIn(numbers);</code>	1
2. <code>Int numberOfDigits = calculateNumberOfDigitsIn(maximumNumber);</code>	1
3. <code>int placeValue = 1;</code>	1
4. <code>while (numberOfDigits-- > 0) {</code>	$n + 1$
5. <code>applyCountingSortOn(numbers, placeValue);</code>	$n * O(m)$
6. <code>placeValue *= 10;</code>	n
Total:	$O(mn)$