

## **Lab 3: A 1GHz Microstrip Solid-State Amplifier**

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## 1. Introduction

The purpose of this lab is to design, build and test an amplifier at 1GHz frequency to achieve optimal gain. The amplifier consists three parts: the BJT transistor amplifier circuit, input and output matching networks. Through conjugate matching, we determined the stub lengths of the matching networks to reduce the reflections from input and output ports, and to maximize the transducer gain. Stability is also examined in designing to prevent oscillation of the network.

The amplifier circuit is designed and tuned for maximum simulated gain with ADS software, and then fabricated and tested using the VNA to measure the actual gain.

## 2. Design Procedures

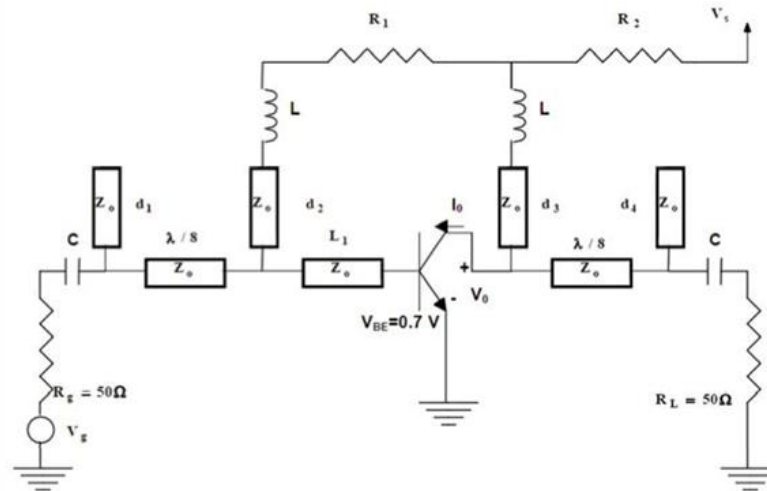


Fig 1: amplifier network schematics

Step 1: Separate the input or output networks, replace them by equivalent lumped element models and simulate the circuit at 1GHz on ADS. Detailed schematics for the input and output equivalent circuit are shown in section 3, Fig 3.3 and 3.6.

Step 2: Start by sweeping the length of the stubs which are closer to the transistor (e.g.  $d_2$  or  $d_3$ ), and disable the other ones further away from the input ( $d_1$ ) or output ( $d_4$ ) to the BJT. Results are shown in Figures in Section 3. Use the stubs closer to the transistor ( $d_2$  and  $d_3$ ) to tune the real part of input and output admittances ( $Y_{in}$  and  $Y_{out}$ ). Find the lengths of  $d_2$  when  $\text{Re}\{Y_{in}\}=1$  and the lengths of  $d_3$  when  $\text{Re}\{Y_{out}\}=1$ .

Step 3: Fix the lengths of  $d_2$  and  $d_3$  with values obtained from Step 2. Now, sweep  $d_1$  and  $d_4$  to have imaginary parts of  $Y_{in}$  and  $Y_{out}$  equals 0. Record the lengths of  $d_1$  when  $\text{Im}\{Y_{in}\}=0$  and the lengths of  $d_4$  when  $\text{Im}\{Y_{out}\}=0$ .

Step 4: Validate the design by assembling together all 4 stubs ( $d_1$  to  $d_4$ ) with designed lengths. Record S parameters and shown in Fig 3.12 in Section 3.3.

### 3. Simulated Plots

#### 3.1 Stub Length Tuning with Ideal Transmission Lines

##### 3.1.1 Input Matching Network

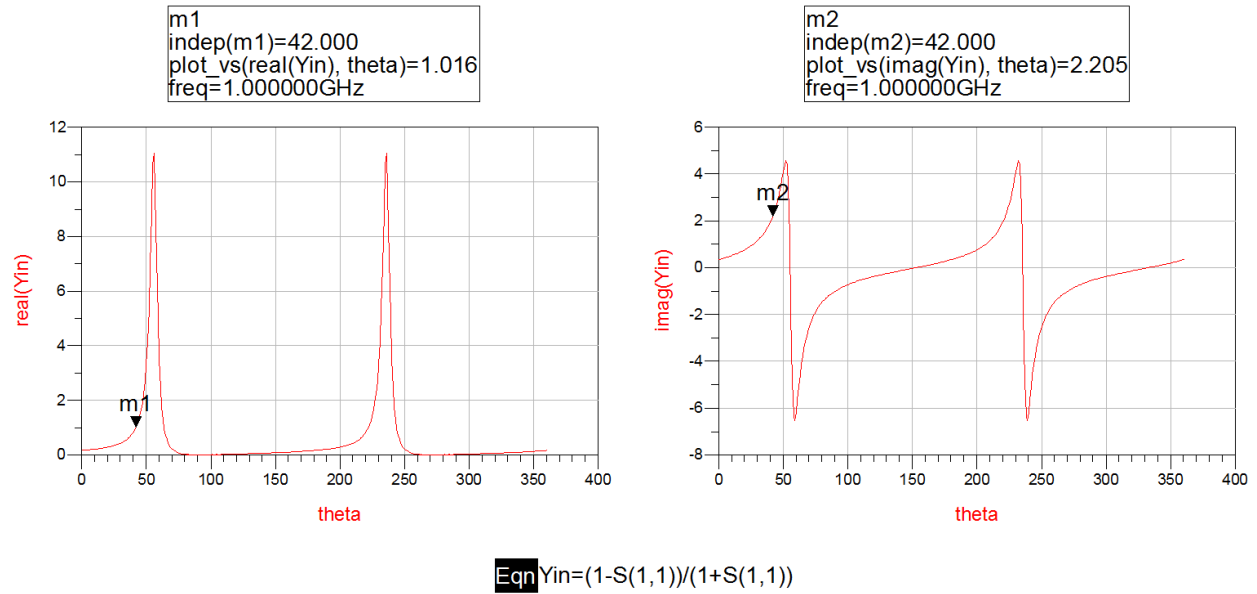


Fig 3.1: Sweeping  $d_2$  while  $d_1$  disabled.  $d_2 = 42^\circ, 64^\circ, 222^\circ$ , and  $244^\circ$  when  $\text{Re}\{Y_{in}\}=1$ .

By keeping  $L_1 = 25\text{mm}$  and the strip line between  $d_1$  and  $d_2$  at  $\lambda/8$ , we disable  $d_1$  and sweep length of  $d_2$  from  $0^\circ$  to  $360^\circ$ . The sweep yielded four possible solutions at  $42^\circ, 64^\circ, 222^\circ$ , and  $244^\circ$  when  $\text{Re}\{Y_{in}\}=1$ . We first chose the shortest length at  $42^\circ$ , but it resulted  $d_1=114^\circ$  in the later simulation, which the stub length is too long and thus not desired. So we chose the second shortest stub length for  $d_2$  at  $64^\circ$  to minimize the total stub length of  $d_1+d_2$  for saving space. When keeping  $d_2$  fixed at  $64^\circ$ , the shortest  $d_1$  is found to be  $76^\circ$  shown as follows:

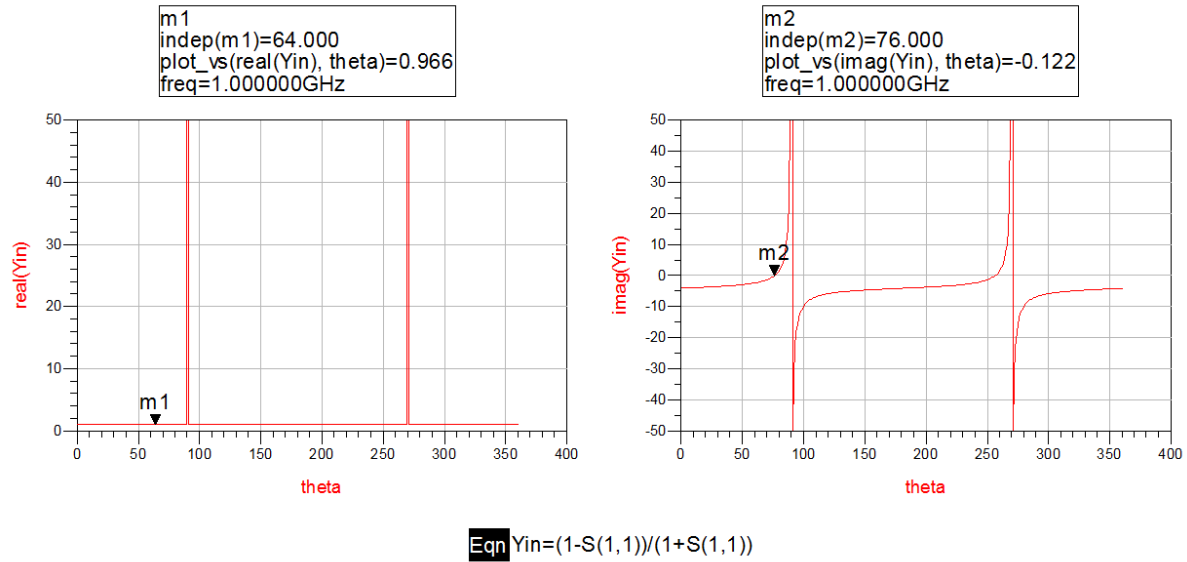


Fig 3.2: Sweeping  $d_1$  while  $d_2 = 64^\circ$ . Imaginary part of  $Y_{in}$  is 0 when  $d_1 = 76^\circ$

The final optimized input matching network is shown below:

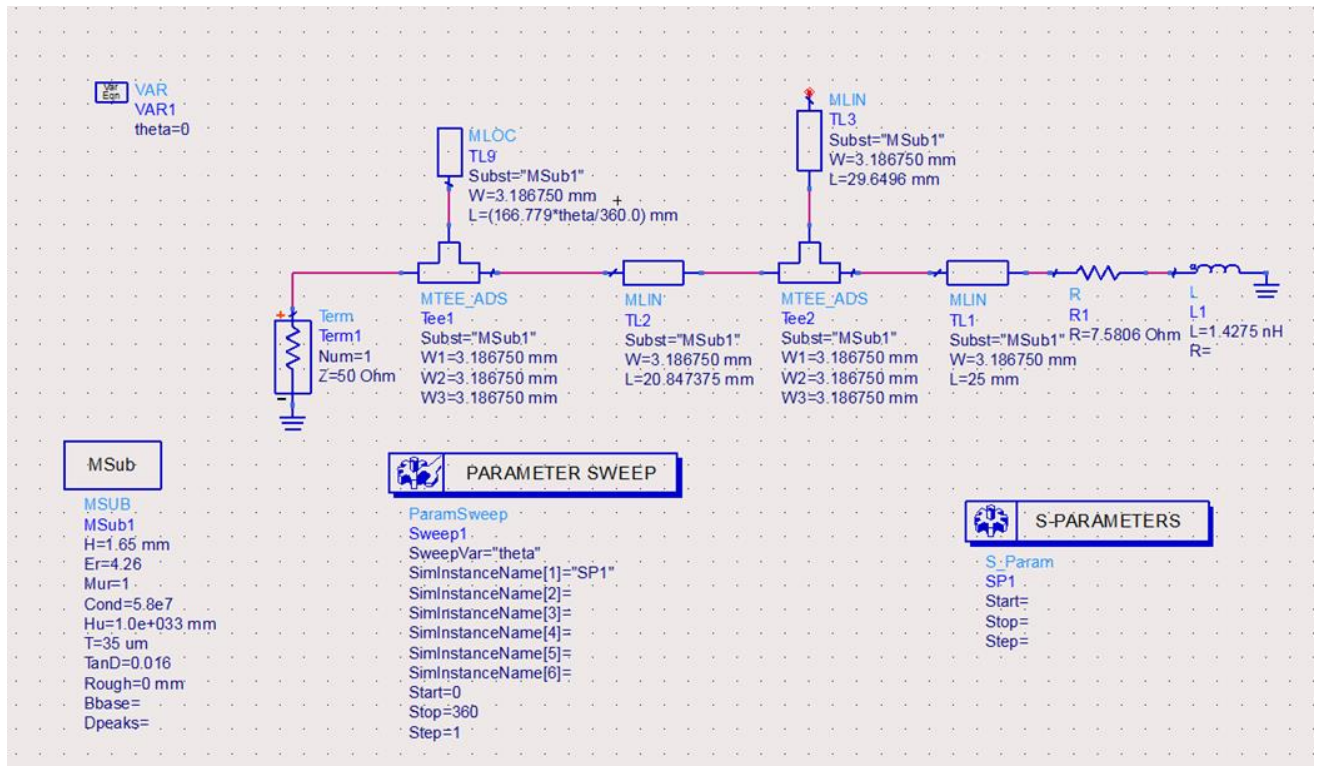


Fig 3.3: We relabelled  $d_1$  as TL9,  $d_2$  as TL3, and the stripline between  $d_1$  and  $d_2$  as TL2.

### 3.1.2 Output Matching Network

We find the optimized stub lengths for  $d_3$  and  $d_4$  following the similar procedures carried out previously in 3.1.1.

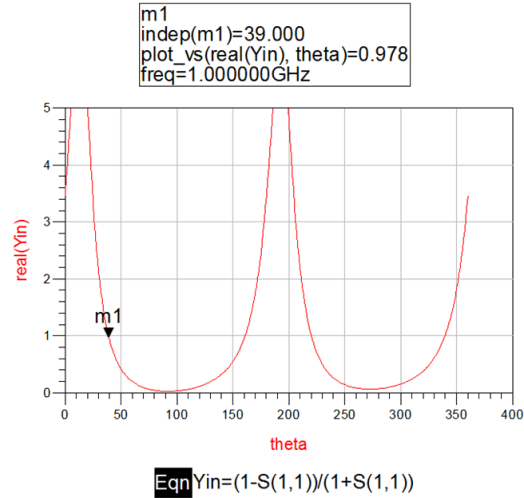


Fig 3.4: Sweeping  $d_3$  while  $d_4$  disabled. The shortest  $d_3 = 39^\circ$  when  $\text{Re}\{Y_{in}\}=1$ .

By keeping the strip line between  $d_3$  and  $d_4$  fixed at  $\lambda/8$ , we sweep length of  $d_3$  from  $0^\circ$  to  $360^\circ$ . Again, the sweep yielded four different solutions when  $\text{Re}\{Y_{out}\}=1$ . We chose the shortest stub length for  $d_3$  at  $39^\circ$  to find the length  $d_4$ . By keeping  $d_3$  fixed at  $39^\circ$ , the shortest  $d_4$  is found to be  $76^\circ$  shown as follows:

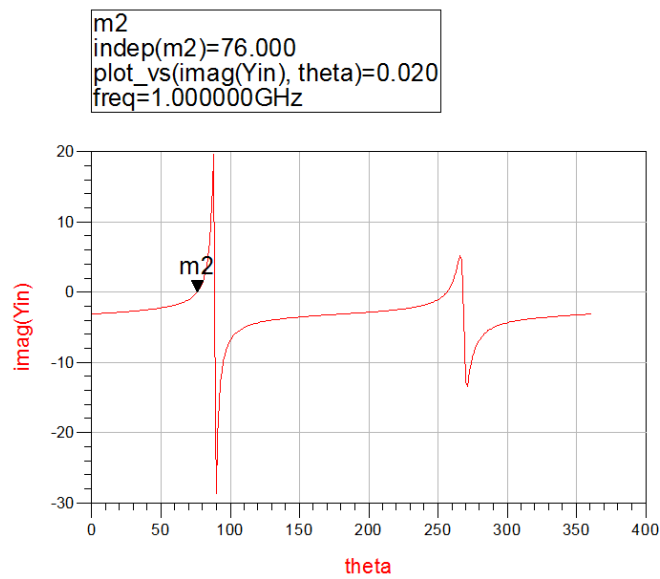


Fig 3.5: Sweeping  $d_4$  while  $d_3 = 39^\circ$ . Imaginary part of  $Y_{out}$  is 0 when  $d_4 = 76^\circ$

The final optimized input matching network is shown below:

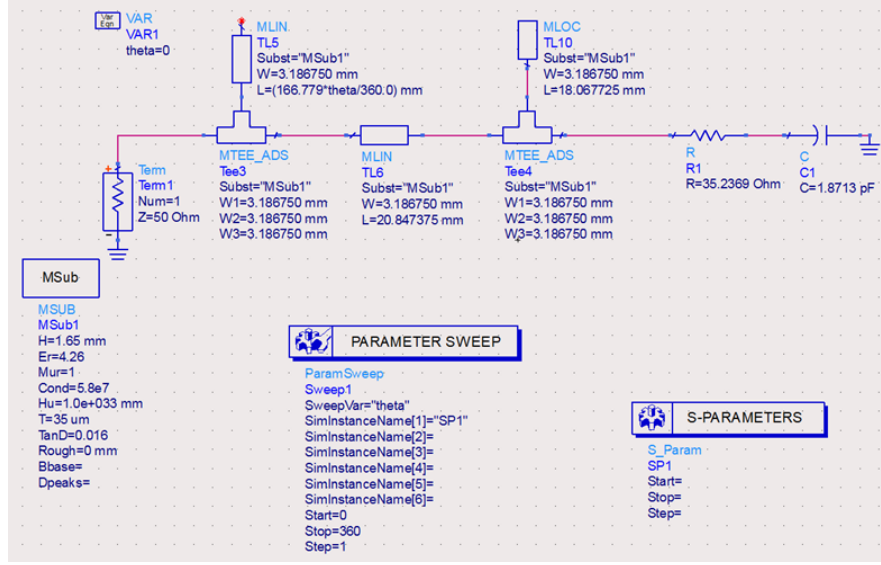


Fig 3.6: We relabelled  $d_3$  as TL5,  $d_4$  as TL10, and the stripline between  $d_3$  and  $d_4$  as TL6.

### 3.3 Stub Length Tuning with FR-4

We also simulated the network with lossy FR-4 microstrip lines on ADS following the same procedures in 3.2. The results are shown in the following plots:

For input network matching:

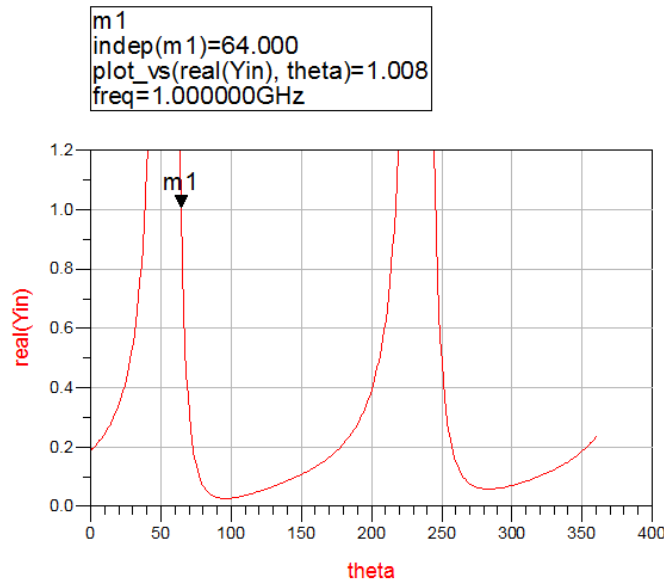


Fig 3.7: Sweeping  $d_2$  while  $d_1$  disabled. The second shortest  $d_2 = 64^\circ$  when  $\text{Re}\{Y_{in}\}=1$ .

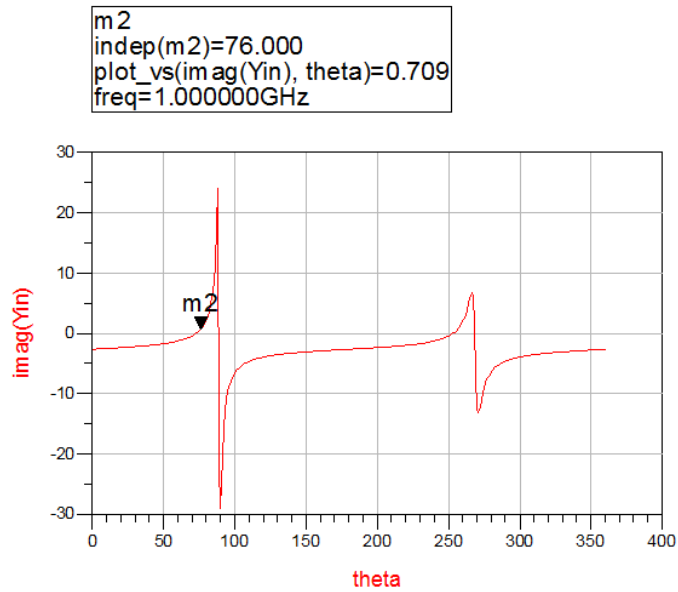


Fig 3.8: Sweeping  $d_1$  while  $d_2 = 64^\circ$ . Imaginary part of  $Y_{in}$  is 0 when  $d_1 = 76^\circ$

For output network matching:

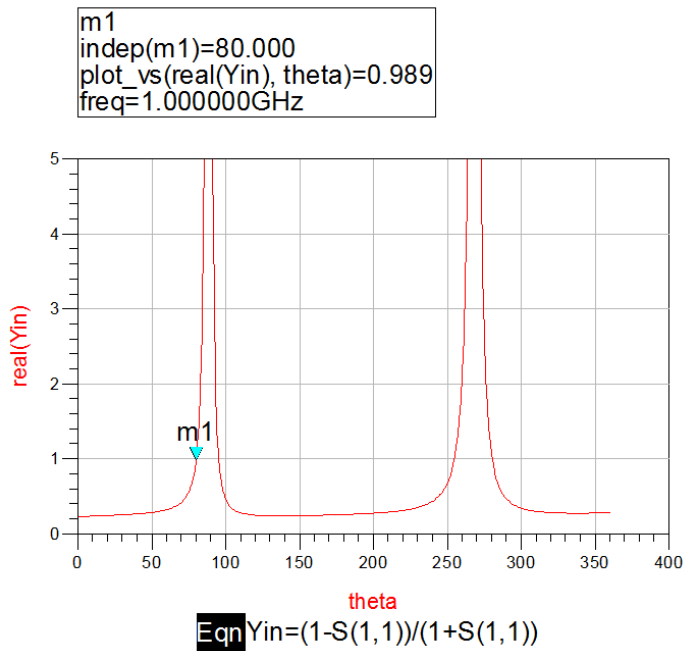


Fig 3.9: Sweeping  $d_3$  while  $d_4$  disabled. The shortest  $d_3 = 80^\circ$  when  $\text{Re}\{Y_{in}\}=1$ .

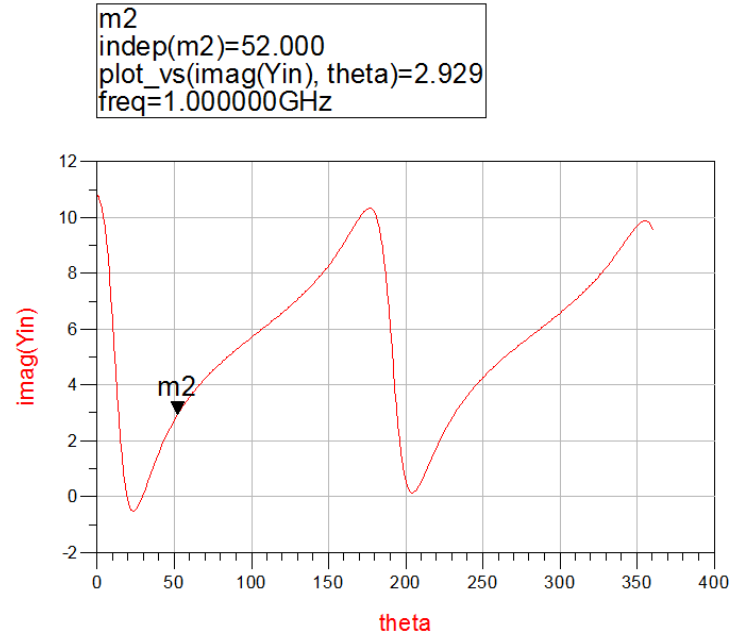


Fig 3.10: Sweeping  $d_4$  while  $d_3 = 80^\circ$ . Imaginary part of  $Y_{out}$  is 0 when  $d_4 = 52^\circ$

The resultant stub lengths are  $d_1=28.5\text{mm}$ ,  $d_2=35.2\text{mm}$ ,  $d_3=35.2\text{mm}$  and  $d_4=18.1\text{mm}$ .

The following is the final schematic for the amplifier network using optimized stub lengths:

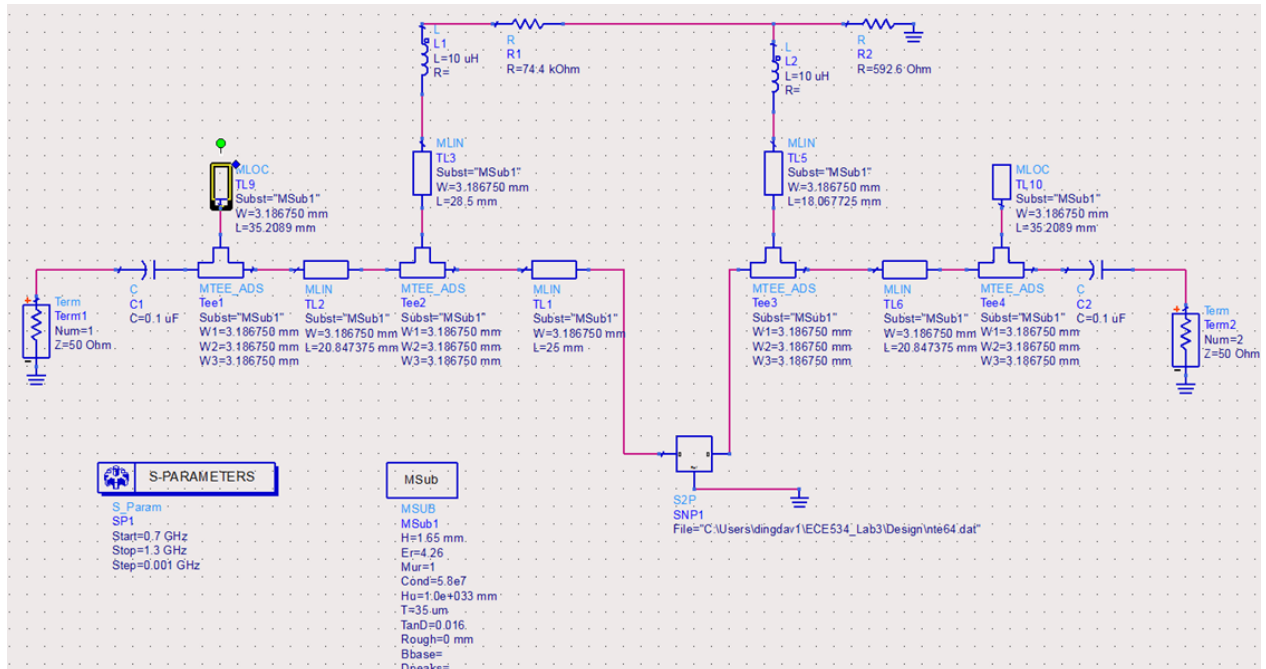


Fig 3.11: Final schematic for the amplifier network



The simulations for S-parameters are as follows:

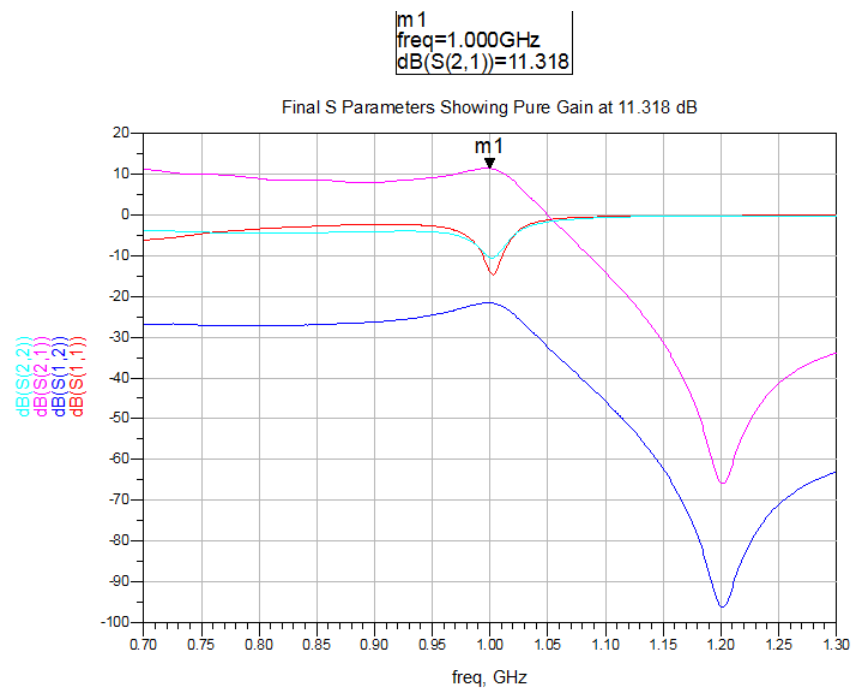


Fig 3.12: S-parameters on FR-4

## 4. Experimental Plots

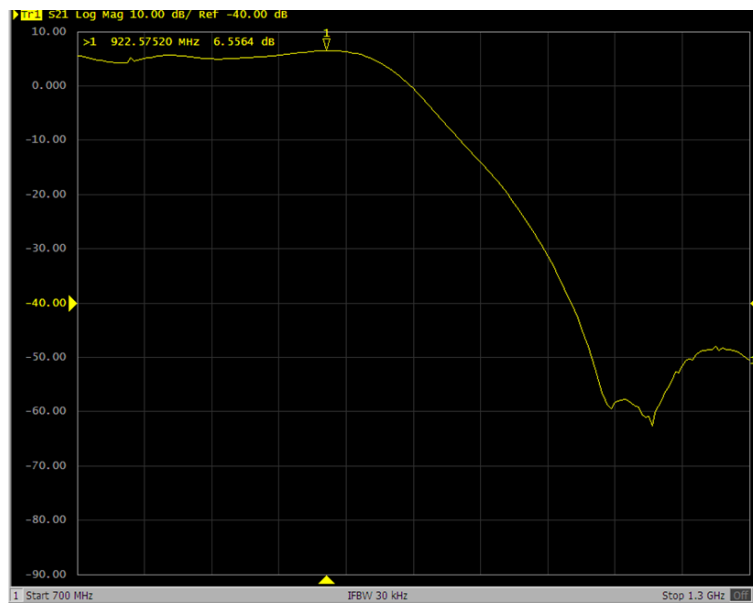


Fig 4.1: S21

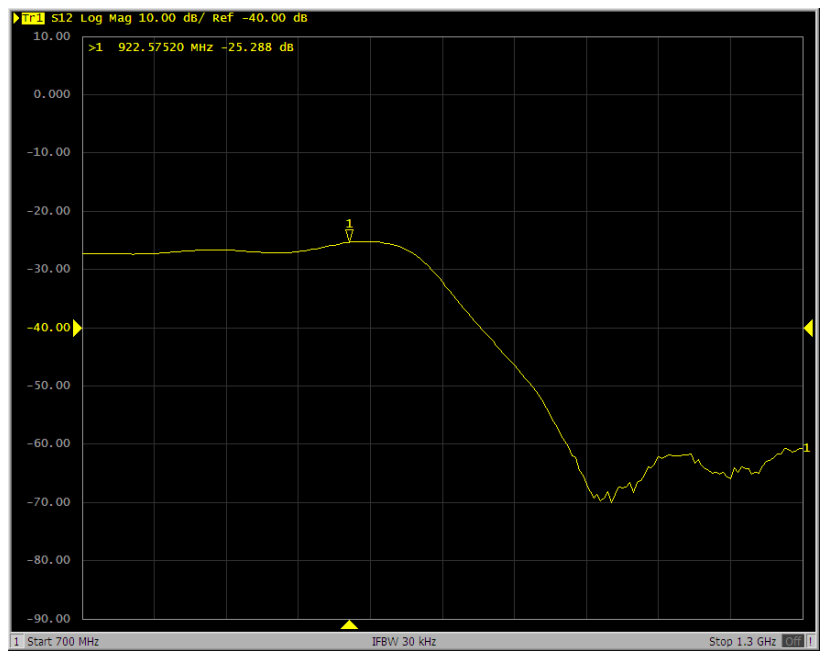


Fig 4.2: S12

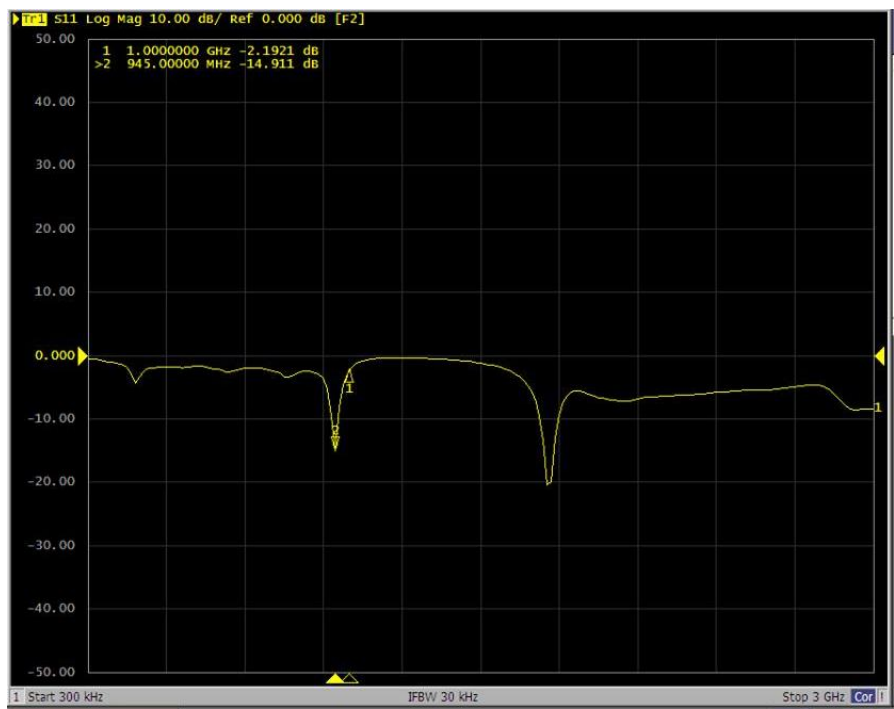


Fig 4.3: S11

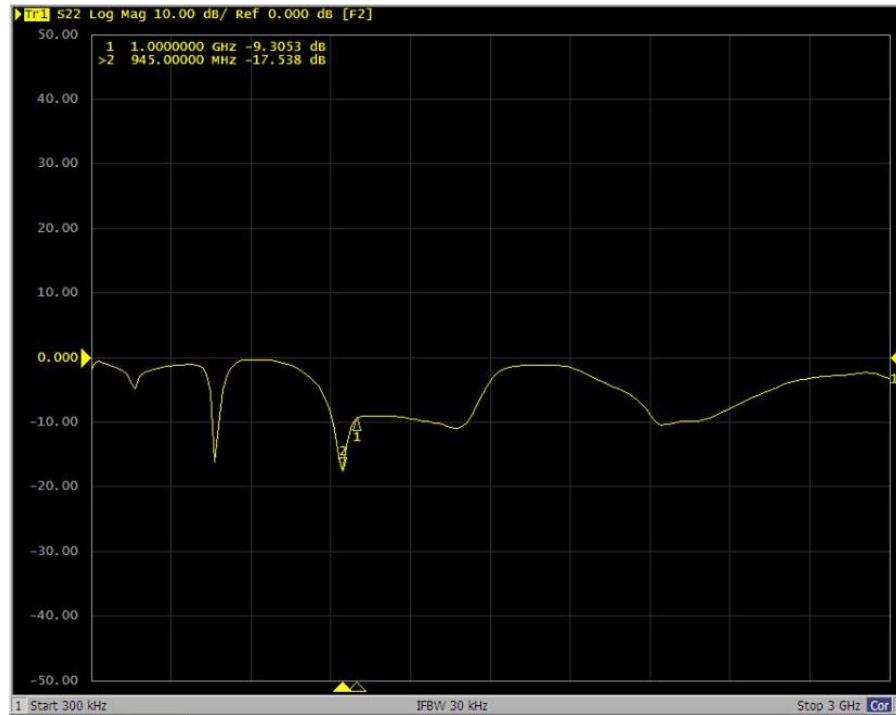


Fig 4.4: S22

## 5. Discussions

1. Biasing resistors  $R_1$  and  $R_2$  for an operating point of  $I_0=10\text{mA}$ ,  $V_0=10\text{V}$  at  $V_S = 16\text{V}$  and  $h_{FE}= 80$ .

The current into the base of BJT is  $i_b = I_0/h_{FE}=10\text{mA}/80=0.125\text{mA}$ .

$$V_x = V_0 + I_0 Z_0 = 10.5\text{V}$$

$$R_1 + 2Z_0 = (V_x - V_{BE})/i_b \Rightarrow R_1 = 78.3\text{k}\Omega$$

$$R_2 = (V_S - V_x)/(I_0 + i_b) = 543.21\Omega$$

2. Stability factors  $K$  and  $\Delta$  at 1 GHz

From the data sheet, at 1 GHz,  $S_{11}=0.4454\angle 161.638^\circ$ ,  $S_{21}=3.6707\angle 53.358^\circ$ ,  
 $S_{12}=0.08264\angle 46.371^\circ$ ,  $S_{22}=0.37975\angle -51.66^\circ$

$$|\Delta| = |S_{11}S_{22} - S_{12}S_{21}| = 0.1402 < 1$$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} = 1.116 > 1$$

So the network is unconditionally stable at 1GHz.

3. Theoretical maximum transducer gain of the amplifier at 1 GHz

At 1GHz,

$$B_1 = 1 + |S_{11}|^2 - |S_{11}|^2 - |\Delta|^2 = 1.0345$$

$$B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 = 0.9262$$

$$C_1 = S_{11} - \Delta S_{22}^* = 0.49495 \angle 159.265^\circ$$

$$C_2 = S_{22} - \Delta S_{11}^* = 0.43803 \angle -54.806^\circ$$

For stability, we only choose  $|\Gamma_{in}| < 1$  and  $|\Gamma_{out}| < 1$ , or equivalently  $|\Gamma_S| < 1$  and  $|\Gamma_L| < 1$ :

$$\Gamma_S = \frac{B_1 - \sqrt{B_1^2 - 4|C_1|^2}}{2C_1} = 0.74151 \angle -159.265^\circ$$

$$\Gamma_L = \frac{B_2 - \sqrt{B_2^2 - 4|C_2|^2}}{2C_2} = 0.7141 \angle 54.806^\circ$$

$$G_{Tmax} = \frac{1}{1 - |\Gamma_S|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_S|^2} = 27.57 \text{ or } 14.4\text{dB}$$

4. Input and output impedances of the transistor

$$\Gamma_{in} = \frac{Z_{in} - Z_0}{Z_{in} + Z_0} = \Gamma_S^* \Rightarrow Z_{in} = 7.66 + j8.94 \Omega$$

$$\Gamma_{out} = \frac{Z_{out} - Z_0}{Z_{out} + Z_0} = \Gamma_L^* \Rightarrow Z_{out} = 35.68 - j84.97 \Omega$$

5. For choosing the stub lengths, why are there four options and are there benefits to one over the others?

When finding the length of one stub using double stub tuning on admittance Smith chart, there are two options, which one of the solution is closer to the BJT than the other. For instance, the  $g = \text{Re}\{Z_{in}'\}$  circle intersects the rotated (by  $\lambda/8$ )  $g=1$  circle at two different points. And also the full circle of the Smith chart represents  $180^\circ$  or  $\lambda/2$ , by sweeping from  $0^\circ$  to  $360^\circ$ , we traversed through the full Smith chart twice, thus it creates two more options, where the second pair of solutions differ the first pair by  $\lambda/2$ .

The longer than stubs are, the more conductor loss there are in the network. However, shorter stubs may be more susceptible to parasitic capacitance.

6. What will be the reactance of the capacitance  $C=0.1 \mu\text{F}$  at 1 GHz? Would this act as a good decoupling capacitor at this frequency?

$$Z_c = \frac{1}{j\omega C} = -j1.592 \times 10^{-3} \Omega$$

Since  $|Z_c/Z_0| \ll 1\%$ , it acts as a short and is a good decoupling capacitor at 1GHz.

7. What will be the reactance of the inductance,  $L = 10 \text{ nH}$  at  $1 \text{ GHz}$ ? Would this act as a good RF-choke at  $1 \text{ GHz}$ ?

$Z_c = j\omega L = j62.83 \Omega$  which is not very large compare with  $R_1$  or  $R_2$ .

So it is not a good RF-choke at  $1 \text{ GHz}$ , an inductor with higher inductance is preferred to create high impedance.

## 6. Differences between Simulation and Measurement

The experimental plots and simulated plots agree with each other in general, however a few differences have been observed. The simulated plots have lower return loss and higher insertion loss around  $1 \text{ GHz}$ . The most significant difference is in  $S_{21}$  such that the experimental plot has its maximum value  $6.56 \text{ dB}$  at  $922.6 \text{ MHz}$  comparing with the simulated plot which has maximum value  $11.3 \text{ dB}$  at  $1 \text{ GHz}$ . The maximum value of the simulated  $S_{21}$  is much closer to the theoretical maximum transducer gain  $G_{T\max} = 14.4 \text{ dB}$ .

The observed difference between the measured and simulated central frequency could be accounted by assuming that the two stubs are actually longer than what their physical length is. This is because each open-circuited stub induces a fringing field at its open end. This field can be modeled as a shunt fringing capacitance  $C_f$  attached to the open end. Equivalently,  $C_f$  can be accounted for by assuming that the open stub is actually longer than its physical length, since a short section of an open-circuited line behaves capacitively.

The discrepancy for the maximum value of  $S_{21}$  could be due to the non-ideal components used for constructing the circuit network. Each physical component has limited quality factor. The original inductor we used as RF-choke gave us negative dB values in  $S_{21}$ , but after replacing the inductor, we were able to achieve  $6.56 \text{ dB}$  in  $S_{21}$ , and the gain is significantly improved. To achieve a higher gain, an inductor with higher inductance is needed, but it will also require the inductor to have larger size and it may also create some other undesired effects. Another source of the discrepancy may be caused by soldering and wiring. In the lab, we observed that the S-parameter values fluctuate when we touch or press the wires. Repositioning the wires could introduce parasitic capacitance that diminishes the effect of inductors.

## 7. Conclusion

In this lab, we designed, simulated, and tested a BJT amplifier network at 1GHz on microstrip. By examining the S-parameters, the amplifier network is determined to be unconditionally stable at 1GHz. There are some discrepancies between the simulated results and experimental results mainly due to the non-ideal components used to construct the network. By replacing the original inductor with a new one, we improved the transducer gain to 6.56dB, which is still lower than the simulated value of 11.4dB. However, it is possible to further improve the gain by using components with higher quality factors.